

Sets

A Activities $\{1, \dots, |A|\}$

$A^r \subseteq A$ Recurring activities

$A^o \subseteq A$ one-off activities

T Time periods in month $\{1, \dots, 2880\}$

T^{bus} Time periods which fall in business hours

$T^{off} = T \setminus T^{bus}$

T^r Time periods for recurring activities $\{1, \dots, 32\}$

T^o Time periods for one-off activities $\{1, \dots, 96\}$

D^r Days of week $\{1, \dots, 5\}$

D^o Days of month $\{1, \dots, 30\}$

Data

n^{small}
 n^{large}

} # small/large rooms available

p_t^{base}

base load @ time $t \in T$

p_t^{solar}

solar supply @ time $t \in T$

$price_t$

grid price @ time $t \in T$

$dura$ Duration of activity $a \in A$
 p_a power consumption (per room) of activity $a \in A$

r_a^{small}
 r_a^{large} } small / large rooms needed for activity $a \in A$

T_a^{start} Valid start times for activity $a \in A$
 (indexes come from T^r if $a \in A^r$, T^o if $a \in A^o$)

$value_a$ Value of activity $a \in A^o$

$penalty_a$ Penalty if activity $a \in A^o$ is scheduled outside of business hours

Functions

$T2Tr(T)$ Map a subset of T to the corresponding
 $(d, t) \in D^r \times T^r$ pairs used to index
 recurring activities

$T2To(T)$ " where $(d, t) \in D^o \times T^o$

Variables

$y_{adt}^{r/o} \in \{0,1\} = 1$ if activity $a \in A^{r/o}$ starts on day $d \in D^{r/o}$ at time $t \in T_a^{\text{start}}$

$x_{adt}^{r/o} \in \{0,1\} = 1$ if activity $a \in A^{r/o}$ is running on day $d \in D^{r/o}$ at time $t \in T_a^{\text{start}}$

p_t^{grid} grid power used @ time $t \in T$

p_t^{class} power demand from classed @ $t \in T$

Objective

$$\min \sum_{t \in T} \frac{0.25}{1000} p_t^{\text{grid}} \cdot \text{price}_t + 0.05 \left(\max_t p_t^{\text{grid}} \right)^2 - \sum_{a \in A^o} \left(\sum_{(d,t) \in T_2 T_o(T^{\text{bus}})} \text{Value}_a \cdot y_{adt}^o + \sum_{(d,t) \in T_2 T_o(T^{\text{off}})} (\text{Value}_a - \text{penalty}_a) y_{adt}^o \right)$$

Constraints

Recurring once per week

$$\sum_{\substack{d \in D^r \\ t \in T^r}} y_{adt}^r = 1 \quad \forall a \in A^r$$

One-off at most once

$$\sum_{\substack{d \in D^o \\ t \in T^o}} y_{adt}^o \leq 1 \quad \forall a \in A^o$$

Link x and y variables

$$\sum_{t'=t}^{t+dura} x_{adt'}^r \geq dura \cdot y_{adt}^r \quad \forall a \in A^r, d \in D^r, t \in T_a^{start}$$

$$\sum_{t'=t}^{t+dura} x_{adt}^o \geq dura \cdot y_{adt}^o \quad \forall a \in A^o, d \in D^o, t \in T_a^{start}$$

Precedence

$$|prec_a| \sum_{t \in T_a^{start}} y_{adt}^r \leq \sum_{\substack{d' \in prec_a \\ d' < d \\ t \in T_{a'}^{start}}} y_{a'd't}^r \quad \forall a \in A^r, d \in D^r$$

$$|prec_a| \sum_{t \in T_a^{start}} y_{adt}^o \leq \sum_{\substack{d' \in prec_a \\ d' < d \\ t \in T_{a'}^{start}}} y_{a'd't}^o \quad \forall a \in A^o, d \in D^o$$

Enough rooms to run classes

$$\sum_{a \in A^r} r_a^{\text{small}} x_{adr,t^r}^r + \sum_{a \in A^o} r_a^{\text{small}} x_{ado,t^o}^o \leq n^{\text{small}} \quad \forall t \in T$$

if $(d^r, t^r) \in D^r \times T^r$

$$\sum_{a \in A^r} r_a^{\text{large}} x_{adr,t^r}^r + \sum_{a \in A^o} r_a^{\text{large}} x_{ado,t^o}^o \leq n^{\text{large}} \quad \forall t \in T$$

if $(d^r, t^r) \in D^r \times T^r$

Demand from classes

$$\sum_{a \in A^r} (r_a^{\text{small}} + r_a^{\text{large}}) x_{adr,t^r}^r \cdot P_a + \sum_{a \in A^o} (r_a^{\text{small}} + r_a^{\text{large}}) x_{ado,t^o}^o \cdot P_a$$

if $(d^r, t^r) \in D^r \times T^r$

$$= p_t^{\text{class}}$$

$$\forall t \in T \begin{pmatrix} (d^r, t^r) = T2Tr(t) \\ (d^o, t^o) = T2To(t) \end{pmatrix}$$

Match supply and demand

$$p_t^{\text{grid}} + p_t^{\text{solar}} = p_t^{\text{class}} + p_t^{\text{base}}$$

$$\forall t \in T$$