

Sets

B Buildings $\{0, \dots\}$
 A Activities $\{0, \dots\}$
 A_{rCA} recurring activities
 A_{oCA} once-off activities
 T time periods, T_{bus} = time periods in business hours
 $T_{off} = T \setminus T_{bus}$

D^r set of weekdays $\{0, \dots, 4\}$
 D^o set of days in month $\{0, \dots, 29\}$

Data

n_b^{small} # small rooms in building $b \in B$
 n_b^{large} # large rooms in building $b \in B$
 cap_b Battery capacity of building $b \in B$ ($0 \neq \infty$ battery)
 eff_b Battery efficiency of building $b \in B$
 p_b^{max} Max battery power of building $b \in B$
 d_a duration of activity $a \in A$
 p_a power draw of activity $a \in A$
 $prec_a$ Precedent activities for activity $a \in A$
 $demand_{bt}^{base}$ Demand @ building $b \in B$ in period $t \in T$
 p_{bt}^{solar} Solar power @ building $b \in B$ in period $t \in T$
 $price_t$ Grid price in period $t \in T$
 $r2t(t)$, For a time period $t \in T$, returns the relevant (d, t) times used

for scheduling recurring classes

$o2t(t)$. . .

r_a^{small}

small rooms required by activity a

r_a^{large} . . .

Variables

$x_{abd}^r \in \{0,1\}$ 1 if activity $a \in A_r$ is scheduled in building b during the t^{th} period of day $d \in \bar{D}$

$y_{abd}^r \in \{0,1\}$ start activity $a \in A_r$

$x_{abd}^o \in \{0,1\}$. . . $d \in \bar{D}^o$

$y_{abd}^o \in \{0,1\}$. . . $d \in \bar{D}^o$

ignore battery for now

p_t^{grid} grid power @ time $t \in T$

demand _{b} ^{class}

$Z = \max p_t^{grid}$

Objective

$$\min \sum_{t \in T} \frac{0.25}{1000} p_t^{\text{grid}} \cdot \text{price}_t + 0.05 \left(\max_t p_t \right)^2$$

$$+ \sum_{a \in A^0} \left(\sum_{\substack{(d', t') \in O2t(T_{\text{bus}}) \\ b \in B}} \text{Value}_a^{\text{bus}} y_{abd't'}^0 + \sum_{\substack{(d', t') \in O2t(T_{\text{off}}) \\ b \in B}} \text{Value}_a^{\text{off}} y_{abd't'}^0 \right)$$

Constraints

Run each recurring activity once per week

$$\sum_{\substack{b \in B \\ d \in D^r \\ t \in T_0}} y_{abdt}^r = 1$$

$$\forall a \in A^r$$

Run each one-off activity at most once

$$\sum_{\substack{b \in B \\ d \in D^0 \\ t \in T}} y_{abdt}^0 \leq 1 \quad \forall a \in A^0$$

Supply matches demand

$$p_t^{\text{grid}} + \sum_{b \in B} \left(p_{bt}^{\text{solar}} - \text{demand}_{bt}^{\text{base}} - \text{demand}_{bt}^{\text{class}} \right) = 0 \quad \forall t \in T$$

Enough classrooms available

$$\sum_{a \in A^0} \sum_{(d,t') \in \text{O2T}(t)} x_{ad't'}^0 \cdot r_a^{\text{small}} + \sum_{a \in A^r} x_{ad't'}^r \cdot r_a^{\text{small}} \leq n_b^{\text{small}} \quad \forall b \in B, t \in T$$

$(d,t') = r2t(t)$

same for large rooms

link x & y variables, must end before

$$\sum_{t'=t}^{t+da-1} x_{abdt'}^r \geq y_{abdt}^r \cdot dnr_a \quad \text{COB} \quad \forall a \in A^r, t \in \{0, \dots, 36-da\}$$

in code

$$\sum_{t'=t}^{t+da-1} x_{abdt'}^0 \geq y_{abdt}^0 \cdot dnr_a \quad \forall a \in A^0, b \in B, d \in D^0, t \in \{0, \dots, 96-da\}$$

also set $y_{abdt} = 0$ for periods before end (or do in code)

Precedence

$$|prec_a| \sum_{\substack{b \in B \\ t \in T}} y_{abdt}^r \leq \sum_{\substack{a' \in prec_a \\ b \in B \\ d' < d \\ t \in T}} y_{a'bdt'}^r \quad \forall a \in A^r, d \in D^r$$

Exact same for one-off