How Julia programs are organized

```
In [1]:
          # Functions - All Julia functions are generic
          function f(x,y)
            x + y
          end
Out[1]:
          f (generic function with 1 method)
In [2]:
          # Fast user defined datatypes
          immutable Point{T}
               x::T
              y::T
          end
          p = Point(1,2)
          Point{Int64}(1,2)
Out[2]:
```

In [3]: # Methods - Particular specialization of a function. Picked through multiple dispatch.
methods(+)

Out[3]: 171 methods for generic function +:

- +(x::Bool) at bool.jl:33
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/bool.jl#L33)
- +(x::Bool, y::Bool) at bool.jl:36
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/bool.jl#L36)
- +(y::AbstractFloat, x::Bool) at bool.jl:46
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/bool.jl#L46)
- +(x::Int64, y::Int64) at int.jl:8
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/int.jl#L8)
- +(x::Int8, y::Int8) at int.jl:16
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/int.jl#L16)
- +(x::UInt8, y::UInt8) at int.jl:16
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/int.jl#L16)
- +(x::Int16, y::Int16) at int.jl:16
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/int.jl#L16)
- +(x::UInt16, y::UInt16) at int.jl:16
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/int.jl#L16)
- +(x::Int32, y::Int32) at int.jl:16
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/int.jl#L16)
- +(x::UInt32, y::UInt32) at int.jl:16
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/int.jl#L16)
- +(x::UInt64, y::UInt64) at int.jl:16
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/int.jl#L16)
- +(x::Int128, y::Int128) at int.jl:16
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/int.jl#L16)
- +(x::UInt128, y::UInt128) at int.jl:16
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/int.jl#L16)
- +(x::Integer, y::Ptr{T}) at pointer.jl:77
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/pointer.jl#L77)
- +(x::Float32, y::Float32) at float.jl:207
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/float.jl#L207)
- +(x::Float64, y::Float64) at float.jl:208

- (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/float.jl#L208)
- +(z::Complex{T<:Real}, w::Complex{T<:Real}) at complex.jl:111
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/complex.jl#L111)
- +(x::Bool, z::Complex{Bool}) at complex.jl:118
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/complex.jl#L118)
- +(z::Complex{Bool}, x::Bool) at complex.jl:119
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/complex.jl#L119)
- +(x::Bool, z::Complex{T<:Real}) at complex.jl:125
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/complex.jl#L125)
- +(z::Complex{T<:Real}, x::Bool) at complex.jl:126
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/complex.jl#L126)
- +(x::Real, z::Complex{Bool}) at complex.jl:132
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/complex.jl#L132)
- +(z::Complex{Bool}, x::Real) at complex.jl:133
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/complex.jl#L133)
- +(x::Real, z::Complex{T<:Real}) at complex.jl:144
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/complex.jl#L144)
- +(z::Complex{T<:Real}, x::Real) at complex.jl:145
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/complex.jl#L145)
- +(x::Rational{T<:Integer}, y::Rational{T<:Integer}) at rational.jl:179
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/rational.jl#L179)
- +(x::Bool, A::AbstractArray{Bool,N}) at arraymath.jl:136
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/arraymath.jl#L136)
- +(x::Integer, y::Char) at char.jl:43
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/char.jl#L43)
- +(a::Float16, b::Float16) at float16.jl:136
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/float16.jl#L136)
- +(x::BigInt, y::BigInt) at gmp.jl:256
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/gmp.jl#L256)
- +(a::BigInt, b::BigInt, c::BigInt) at gmp.jl:279
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/gmp.jl#L279)
- +(a::BigInt, b::BigInt, c::BigInt, d::BigInt) at gmp.jl:285
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/gmp.jl#L285)
- +(a::BigInt, b::BigInt, c::BigInt, d::BigInt, e::BigInt) at gmp.jl:292
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/gmp.jl#L292)
- +(x::BigInt, c::Union{UInt16,UInt32,UInt64,UInt8}) at gmp.jl:304
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/gmp.jl#L304)

- +(c::Union{UInt16,UInt32,UInt64,UInt8}, x::BigInt) at gmp.jl:308
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/gmp.jl#L308)
- +(x::BigInt, c::Union{Int16,Int32,Int64,Int8}) at gmp.jl:320
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/gmp.jl#L320)
- +(c::Union{Int16,Int32,Int64,Int8}, x::BigInt) at gmp.jl:321
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/gmp.jl#L321)
- +(x::BigFloat, y::BigFloat) at mpfr.jl:208
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/mpfr.jl#L208)
- +(x::BigFloat, c::Union{UInt16,UInt32,UInt64,UInt8}) at mpfr.jl:215
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/mpfr.jl#L215)
- +(c::Union{UInt16,UInt32,UInt64,UInt8}, x::BigFloat) at mpfr.jl:219
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/mpfr.jl#L219)
- +(x::BigFloat, c::Union{Int16,Int32,Int64,Int8}) at mpfr.jl:223
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/mpfr.jl#L223)
- +(c::Union{Int16,Int32,Int64,Int8}, x::BigFloat) at mpfr.jl:227
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/mpfr.jl#L227)
- +(x::BigFloat, c::Union{Float16,Float32,Float64}) at mpfr.jl:231
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/mpfr.jl#L231)
- +(c::Union{Float16,Float32,Float64}, x::BigFloat) at mpfr.jl:235
 (mpfr.jl#L235
- +(x::BigFloat, c::BigInt) at mpfr.jl:239
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/mpfr.jl#L239)
- +(c::BigInt, x::BigFloat) at mpfr.jl:243
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/mpfr.jl#L243)
- +(a::BigFloat, b::BigFloat, c::BigFloat) at mpfr.jl:379
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/mpfr.jl#L379)
- +(a::BigFloat, b::BigFloat, c::BigFloat, d::BigFloat) at mpfr.jl:385
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/mpfr.jl#L385)
- +(a::BigFloat, b::BigFloat, c::BigFloat, d::BigFloat, e::BigFloat) at mpfr.jl:392
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/mpfr.jl#L392)
- +(x::Irrational{sym}, y::Irrational{sym}) at <u>irrationals.jl:72</u>
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/irrationals.jl#L72)
- +(x::Number) at operators.jl:73
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/operators.jl#L73)
- +{T<:Number}(x::T<:Number, y::T<:Number) at promotion.jl:211
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/promotion.jl#L211)
- +{T<:AbstractFloat}(x::**Bool**, y::**T<:AbstractFloat**) at <u>bool.jl:43</u>

- (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/bool.il#L43)
- +(x::Number, y::Number) at promotion.jl:167
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/promotion.jl#L167)
- +(r1::OrdinalRange{T,S}, r2::OrdinalRange{T,S}) at operators.jl:330
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/operators.jl#L330)
- +{T<:AbstractFloat}(r1::FloatRange{T<:AbstractFloat}) at operators.jl:337
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/operators.jl#L337)
- +{T<:AbstractFloat}(r1::LinSpace{T<:AbstractFloat}) at operators.jl:356
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/operators.jl#L356)
- +(r1::Union{FloatRange{T<:AbstractFloat},LinSpace{T<:AbstractFloat},OrdinalRange{T,S}},
 r2::Union{FloatRange{T<:AbstractFloat},LinSpace{T<:AbstractFloat},OrdinalRange{T,S}}) at operators.jl:369
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/operators.jl#L369)
- +(x::Ptr{T}, y::Integer) at pointer.jl:75
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/pointer.jl#L75)
- +{S,T}(A::Range{S}, B::Range{T}) at <u>arraymath.il:69</u>
 (<u>https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/arraymath.il#L69</u>)
- +{S,T}(A::Range{S}, B::AbstractArray{T,N}) at <u>arraymath.jl:87</u>
 (<u>arraymath.jl:87</u>
 (<u>arraymath.jl:87</u>
- +(A::BitArray{N}, B::BitArray{N}) at bitarray.jl:834
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/bitarray.jl#L834)
- +{T}(B::BitArray{2}, J::UniformScaling{T}) at linalg/uniformscaling.jl:28
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/uniformscaling.jl#L28)
- +(A::Array{T,2}, B::Diagonal{T}) at linalg/special.il:122
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.il#L122)
- +(A::Array{T,2}, B::Bidiagonal{T}) at linalg/special.jl:122
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L122)
- +(A::Array{T,2}, B::Tridiagonal{T}) at linalg/special.jl:122
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L122)
- +(A::Array{T,2}, B::SymTridiagonal{T}) at linalg/special.jl:131
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L131)
- +(A::Array{T,2}, B::Base.LinAlg.AbstractTriangular{T,S<:AbstractArray{T,2}}) at linalg/special.jl:159
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L159)
- +(A::Array{T,N}, B::SparseMatrixCSC{Tv,Ti<:Integer}) at sparse/sparsematrix.jl:1019
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/sparse/sparsematrix.jl#L1019)
- +{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period}}
 (x::Union{DenseArray{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period},N},SubArray{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.CompoundPeriod,Base.Dates.Period}

- (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/periods.il#L202)
- +(A::AbstractArray{Bool,N}, x::Bool) at arraymath.jl:135
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/arraymath.jl#L135)
- +
 - (A::Union{DenseArray{Bool,N},SubArray{Bool,N,A<:DenseArray{T,N},I<:Tuple{Vararg{Union{Colon,Int64,Range{Int64}}}}} B::Union{DenseArray{Bool,N},SubArray{Bool,N,A<:DenseArray{T,N},I<:Tuple{Vararg{Union{Colon,Int64,Range{Int64}}}}, at arraymath.il:166
 - (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/arraymath.jl#L166)
- +(A::SymTridiagonal{T}, B::SymTridiagonal{T}) at linalg/tridiag.jl:84
 (linalg/tridiag.jl#L84)
- +(A::Tridiagonal{T}, B::Tridiagonal{T}) at linalg/tridiag.jl:404
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/tridiag.jl#L404)
- +(A::UpperTriangular{T,S<:AbstractArray{T,2}}), B::UpperTriangular{T,S<:AbstractArray{T,2}}) at linalg/triangular.il:347
 - (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/triangular.jl#L347)
- +(A::LowerTriangular{T,S<:AbstractArray{T,2}}), B::LowerTriangular{T,S<:AbstractArray{T,2}}) at linalg/triangular.jl:348
 - (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/triangular.jl#L348)
- +(A::UpperTriangular{T,S<:AbstractArray{T,2}}), B::Base.LinAlg.UnitUpperTriangular{T,S<:AbstractArray{T,2}}) at linalg/triangular.jl:349
 - (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/triangular.jl#L349)
- +(A::LowerTriangular{T,S<:AbstractArray{T,2}}), B::Base.LinAlg.UnitLowerTriangular{T,S<:AbstractArray{T,2}}) at linalq/triangular.il:350
 - (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/triangular.jl#L350)
- +(A::Base.LinAlg.UnitUpperTriangular{T,S<:AbstractArray{T,2}}), B::UpperTriangular{T,S<:AbstractArray{T,2}}) at linalg/triangular.jl:351
 - (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/triangular.jl#L351)
- +(A::Base.LinAlg.UnitLowerTriangular{T,S<:AbstractArray{T,2}}), B::LowerTriangular{T,S<:AbstractArray{T,2}}) at linalg/triangular.jl:352
 - (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/triangular.jl#L352)
- $\bullet \quad + (A:: \textbf{Base.LinAlg.UnitUpperTriangular} \textbf{\{T,S<:} \textbf{AbstractArray} \textbf{\{T,2\}\}},$
 - B::Base.LinAlg.UnitUpperTriangular{T,S<:AbstractArray{T,2}}) at linalg/triangular.jl:353 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/triangular.jl#L353)
- +(A::Base.LinAlg.UnitLowerTriangular{T,S<:AbstractArray{T,2}},
 - B::Base.LinAlg.UnitLowerTriangular{T,S<:AbstractArray{T,2}}) at linalg/triangular.jl:354
 - (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/triangular.jl#L354)
- +(A::Base.LinAlg.AbstractTriangular{T,S<:AbstractArray{T,2}},

- B::Base.LinAlg.AbstractTriangular{T,S<:AbstractArray{T,2}}) at linalg/triangular.jl:355
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/triangular.jl#L355)
- +(Da::Diagonal{T}, Db::Diagonal{T}) at linalg/diagonal.jl:86
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/diagonal.jl#L86)
- +(A::Bidiagonal{T}, B::Bidiagonal{T}) at linalg/bidiag.jl:176
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/bidiag.jl#L176)
- +(UL::UpperTriangular{T,S<:AbstractArray{T,2}}, J::UniformScaling{T<:Number}) at linalg/uniformscaling.jl:45
 (linalg/uniformscaling.jl:45
- +(UL::Base.LinAlg.UnitUpperTriangular{T,S<:AbstractArray{T,2}}, J::UniformScaling{T<:Number}) at linalg/uniformscaling.jl:48
 /(bttps://github.com/ lulia/arg/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/uniformscaling.il#L
 - (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/uniformscaling.jl#L48)
- +(UL::LowerTriangular{T,S<:AbstractArray{T,2}}, J::UniformScaling{T<:Number}) at linalg/uniformscaling.jl:45
 (linalg/uniformscaling.jl:45
- +(UL::Base.LinAlg.UnitLowerTriangular{T,S<:AbstractArray{T,2}}, J::UniformScaling{T<:Number}) at linalg/uniformscaling.jl:48
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/uniformscaling.il#L48)
- +(A::Diagonal{T}, B::Bidiagonal{T}) at linalg/special.il:121 (linalg/special.il:121
- +(A::Bidiagonal{T}, B::Diagonal{T}) at linalg/special.il:122
 (linalg/special.il#L122
- +(A::Diagonal{T}, B::Tridiagonal{T}) at linalg/special.jl:121
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L121)
- +(A::Tridiagonal{T}, B::Diagonal{T}) at linalg/special.il:122
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L122)
- +(A::Diagonal{T}, B::Array{T,2}) at linalg/special.jl:121
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L121)
- +(A::Bidiagonal{T}, B::Tridiagonal{T}) at linalg/special.jl:121
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L121)
- +(A::Tridiagonal{T}, B::Bidiagonal{T}) at linalg/special.jl:122
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L122)
- +(A::Bidiagonal{T}, B::Array{T,2}) at linalg/special.jl:121
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L121)
- +(A::Tridiagonal{T}, B::Array{T,2}) at linalg/special.jl:121
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L121)
- +(A::SymTridiagonal{T}, B::Tridiagonal{T}) at linalg/special.jl:130
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L130)
- +(A::Tridiagonal{T}, B::SymTridiagonal{T}) at linalg/special.jl:131

- (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.il#L131)
- +(A::SymTridiagonal{T}, B::Array{T,2}) at linalg/special.jl:130
 (linalg/special.jl#L130
- +(A::Diagonal{T}, B::SymTridiagonal{T}) at linalg/special.jl:139
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L139)
- +(A::SymTridiagonal{T}, B::Diagonal{T}) at linalg/special.jl:140
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L140)
- +(A::Bidiagonal{T}, B::SymTridiagonal{T}) at linalg/special.jl:139
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L139)
- +(A::SymTridiagonal{T}, B::Bidiagonal{T}) at linalg/special.jl:140
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L140)
- +(A::Diagonal{T}, B::UpperTriangular{T,S<:AbstractArray{T,2}}) at linalg/special.jl:151
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L151)
- +(A::UpperTriangular{T,S<:AbstractArray{T,2}}, B::Diagonal{T}) at linalg/special.il:152
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L152)
- +(A::Diagonal{T}, B::Base.LinAlg.UnitUpperTriangular{T,S<:AbstractArray{T,2}}) at linalg/special.il:151
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L151)
- +(A::Base.LinAlg.UnitUpperTriangular{T,S<:AbstractArray{T,2}}, B::Diagonal{T}) at linalg/special.il:152
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L152)
- +(A::Diagonal{T}, B::LowerTriangular{T,S<:AbstractArray{T,2}}) at linalg/special.jl:151
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L151)
- +(A::LowerTriangular{T,S<:AbstractArray{T,2}}, B::Diagonal{T}) at linalg/special.jl:152
 (linalg/special.jl#L152
- +(A::Diagonal{T}, B::Base.LinAlg.UnitLowerTriangular{T,S<:AbstractArray{T,2}}) at linalg/special.jl:151
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L151)
- +(A::Base.LinAlg.UnitLowerTriangular{T,S<:AbstractArray{T,2}}, B::Diagonal{T}) at linalg/special.il:152
 (linalg/special.il#L152
- +(A::Base.LinAlg.AbstractTriangular{T,S<:AbstractArray{T,2}}, B::SymTridiagonal{T}) at linalg/special.jl:158
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L158)
- +(A::SymTridiagonal{T}, B::Base.LinAlg.AbstractTriangular{T,S<:AbstractArray{T,2}}) at linalg/special.jl:159
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L159)
- +(A::Base.LinAlg.AbstractTriangular{T,S<:AbstractArray{T,2}}, B::Tridiagonal{T}) at linalg/special.jl:158
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L158)
- +(A::Tridiagonal{T}, B::Base.LinAlg.AbstractTriangular{T,S<:AbstractArray{T,2}}) at linalg/special.jl:159
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L159)
- +(A::Base.LinAlg.AbstractTriangular{T,S<:AbstractArray{T,2}}, B::Bidiagonal{T}) at linalg/special.il:158
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L158)

- +(A::Bidiagonal{T}, B::Base.LinAlg.AbstractTriangular{T,S<:AbstractArray{T,2}}) at linalg/special.jl:159
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L159)
- +(A::Base.LinAlg.AbstractTriangular{T,S<:AbstractArray{T,2}}, B::Array{T,2}) at linalg/special.jl:158
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/special.jl#L158)
- +{Tv1,Ti1,Tv2,Ti2}(A_1::SparseMatrixCSC{Tv1,Ti1}, A_2::SparseMatrixCSC{Tv2,Ti2}) at sparse/sparsematrix.jl:1005
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/sparse/sparsematrix.jl#L1005)
- +(A::SparseMatrixCSC{Tv,Ti<:Integer}, B::Array{T,N}) at sparse/sparsematrix.jl:1017
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/sparse/sparsematrix.jl#L1017)
- +(A::SparseMatrixCSC{Tv,Ti<:Integer}, J::UniformScaling{T<:Number}) at sparse/sparsematrix.jl:2988
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/sparse/sparsematrix.jl#L2988)
- +{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period}}
 (Y::Union{DenseArray{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period},N},SubArray{P<:Union{Base.Dates.Dates.CompoundPeriod,Base.Dates.Period})
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/periods.jl#L216)
- +
 {P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period},Q<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period}}
 (X::Union{DenseArray{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period},N},SubArray{P<:Union{Base.Dates.OmpoundPeriod,Base.Dates.Period},N},SubArray{Q<:Union{Base.Dates.OmpoundPeriod,Base.Dates.Period},N},SubArray{Q<:Union{Base.Dates.OmpoundPeriod,Base.Dates.OmpoundPeriod,Base.Dates.OmpoundPeriod,Base.Dates.OmpoundPeriod,Base.Dates.OmpoundPeriod,N},SubArray{Q<:Union{Base.Dates.OmpoundPeriod,Base.Dates.OmpoundPeriod,Base.Dates.OmpoundPeriod,N},SubArray{Q<:Union{Base.Dates.OmpoundPeriod,Base.Dates.
- +{T<:Base.Dates.TimeType,P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period}}
 (x::Union{DenseArray{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period},N},SubArray{P<:Union{Base.Dates.Oates.CompoundPeriod,Base.Dates.Period},N},SubArray{P<:Union{Base.Dates.Oat
- +{T<:Base.Dates.TimeType}(r::Range{T<:Base.Dates.TimeType}, x::Base.Dates.Period) at <u>dates/ranges.jl:39</u>
 <u>https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/ranges.jl#L39</u>)
- +{T<:Number}(x::AbstractArray{T<:Number,N}) at <u>abstractarraymath.jl:49</u>
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/abstractarraymath.jl#L49)
- +{S,T}(A::AbstractArray{S,N}, B::Range{T}) at arraymath.jl:78
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/arraymath.jl#L78)
- +{S,T}(A::AbstractArray{S,N}, B::AbstractArray{T,N}) at arraymath.jl:96
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/arraymath.jl#L96)
- +(A::AbstractArray{T,N}, x::Number) at arraymath.jl:139
 https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/arraymath.jl#L139)
- +(x::Number, A::AbstractArray{T,N}) at arraymath.jl:140
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/arraymath.jl#L140)
- +(x::Char, y::Integer) at char.jl:42

- (https://github.com/JuliaLang/iulia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/char.il#L42)
- +{N}(index1::CartesianIndex{N}, index2::CartesianIndex{N}) at multidimensional.jl:42
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/multidimensional.jl#L42)
- +(J1::UniformScaling{T<:Number}, J2::UniformScaling{T<:Number}) at linalg/uniformscaling.jl:27
 (linalg/uniformscaling.jl#L27
- +(J::UniformScaling{T<:Number}, B::BitArray{2}) at linalg/uniformscaling.jl:29
 (linalg/uniformscaling.jl#L29)
- +(J::UniformScaling{T<:Number}, A::AbstractArray{T,2}) at linalg/uniformscaling.jl:30
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/uniformscaling.jl#L30)
- +(J::UniformScaling{T<:Number}, x::Number) at linalg/uniformscaling.jl:31
 (linalg/uniformscaling.jl#L31
- +(x::Number, J::UniformScaling{T<:Number}) at <u>linalg/uniformscaling.jl:32</u>
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/uniformscaling.jl#L32)
- +{TA,TJ}(A::AbstractArray{TA,2}, J::UniformScaling{TJ}) at linalg/uniformscaling.jl:92
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/linalg/uniformscaling.jl#L92)
- +{T}(a::Base.Pkg.Resolve.VersionWeights.HierarchicalValue{T},
 b::Base.Pkg.Resolve.VersionWeights.HierarchicalValue{T}) at pkg/resolve/versionweight.jl:23
 (pkg/resolve/versionweight.jl:23
 (pkg/resolve/versionweight.jl#L2
- +(a::Base.Pkg.Resolve.VersionWeights.VWPreBuildItem, b::Base.Pkg.Resolve.VersionWeights.VWPreBuildItem)
 at pkg/resolve/versionweight.jl:85
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/pkg/resolve/versionweight.il#L8
- +(a::Base.Pkg.Resolve.VersionWeights.VWPreBuild) at <u>pkg/resolve/versionweight.jl:131</u>
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/pkg/resolve/versionweight.jl#L1
- +(a::Base.Pkg.Resolve.VersionWeights.VersionWeight, b::Base.Pkg.Resolve.VersionWeights.VersionWeight) at pkg/resolve/versionweight.jl:185
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/pkg/resolve/versionweight.jl#L1
- +(a::Base.Pkg.Resolve.MaxSum.FieldValues.FieldValue, b::Base.Pkg.Resolve.MaxSum.FieldValues.FieldValue) at pkg/resolve/fieldvalue.jl:44
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/pkg/resolve/fieldvalue.jl#L44)
- +{P<:Base.Dates.Period}(x::P<:Base.Dates.Period, y::P<:Base.Dates.Period) at dates/periods.jl:43
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/periods.jl#L43)
- +(x::Base.Dates.Period, y::Base.Dates.Period) at dates/periods.jl:190
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/periods.jl#L190)
- +(x::Base.Dates.CompoundPeriod, y::Base.Dates.Period) at dates/periods.jl:191
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/periods.jl#L191)
- +(y::Base.Dates.Period, x::Base.Dates.CompoundPeriod) at dates/periods.jl:192

- (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/periods.il#L192)
- +(x::Base.Dates.CompoundPeriod, y::Base.Dates.CompoundPeriod) at dates/periods.jl:193
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/periods.jl#L193)
- +(x::Base.Dates.CompoundPeriod, y::Base.Dates.TimeType) at <u>dates/periods.jl:238</u>
 (<u>dates/periods.jl#L238</u>
- +(y::Base.Dates.Period, x::Base.Dates.TimeType) at <u>dates/arithmetic.jl:66</u>
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/arithmetic.jl#L66)
- +{T<:Base.Dates.TimeType}(x::Base.Dates.Period, r::Range{T<:Base.Dates.TimeType}) at dates/ranges.jl:40
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/ranges.jl#L40)
- +(x::Union{Base.Dates.CompoundPeriod,Base.Dates.Period}) at <u>dates/periods.jl:201</u>
 (<u>dates/periods.jl:201</u>
- +{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period}}
 (x::Union{Base.Dates.CompoundPeriod,Base.Dates.Period},
 Y::Union{DenseArray{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period},N},SubArray{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period},N},SubArray{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.CompoundPeriod,Base.Dates.Period},N}
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/periods.jl#L215)
- +(dt::DateTime, y::Base.Dates.Year) at dates/arithmetic.jl:13
 dates/arithmetic.jl:13
 <a href="mailto:(https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/arithmetic.jl#L13)
- +(dt::Date, y::Base.Dates.Year) at dates/arithmetic.jl:17
 dates/arithmetic.jl:17
 dates/arithmetic.jl:17
- +(dt::DateTime, z::Base.Dates.Month) at <u>dates/arithmetic.jl:37</u>
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/arithmetic.jl#L37)
- +(dt::Date, z::Base.Dates.Month) at <u>dates/arithmetic.jl:43</u>
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/arithmetic.jl#L43)
- +(x::Date, y::Base.Dates.Week) at dates/arithmetic.jl:60
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/arithmetic.jl#L60)
- +(x::Date, y::Base.Dates.Day) at dates/arithmetic.jl:62
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/arithmetic.jl#L62)
- +(x::DateTime, y::Base.Dates.Period) at <u>dates/arithmetic.jl:64</u>
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/arithmetic.jl#L64)
- +(x::Base.Dates.TimeType) at <u>dates/arithmetic.jl:8</u>
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/arithmetic.jl#L8)
- +(a::Base.Dates.TimeType, b::Base.Dates.Period, c::Base.Dates.Period) at dates/periods.jl:227
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/periods.jl#L227)
- +(a::Base.Dates.TimeType, b::Base.Dates.Period, c::Base.Dates.Period, d::Base.Dates.Period...) at dates/periods.jl:229
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/periods.jl#L229)

- +(x::Base.Dates.TimeType, y::Base.Dates.CompoundPeriod) at <u>dates/periods.jl:233</u>
 (<u>dates/periods.jl:233</u>
- +(x::Base.Dates.Instant) at <u>dates/arithmetic.jl:4</u>
 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/dates/arithmetic.jl#L4)
- +{T<:Base.Dates.TimeType}(x::AbstractArray{T<:Base.Dates.TimeType,N},
 y::Union{Base.Dates.CompoundPeriod,Base.Dates.Period}) at dates/arithmetic.jl:76
 (dates/arithmetic.jl#L76
- +{T<:Base.Dates.TimeType}(y::Union{Base.Dates.CompoundPeriod,Base.Dates.Period},
 x::AbstractArray{T<:Base.Dates.TimeType,N}) at dates/arithmetic.jl:77
 (dates/arithmetic.jl#L77
- +{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period}}(y::Base.Dates.TimeType,
 x::Union{DenseArray{P<:Union{Base.Dates.CompoundPeriod,Base.Dates.Period},N},SubArray{P<:Union{Base.Dates.C at dates/arithmetic.jl:84
 (https://github.com/JuliaLang/julia/tree/2ac30
 4dfba75fad148d4070ef4f8a2e400c305bb/base/dates/arithmetic.il#L84)
- +(a, b, c, xs...) at operators.jl:103 (https://github.com/JuliaLang/julia/tree/2ac304dfba75fad148d4070ef4f8a2e400c305bb/base/operators.il#L103)

```
In [7]:
          # Why Julia is fast? Pick the right method and do the right amount of work
          # Multiple Dispatch makes it easy to organize programs into different behaviours
          # The compiler can pick the most special behaviour for the fastest execution
          @code native Point(1.0,2.0) + Point(3.0,4.0)
                                   TEXT, text, regular, pure instructions
                   .section
          Filename: In[4]
          Source line: 4
                  pushq
                          %rbp
                  movq
                           %rsp, %rbp
          Source line: 4
                  movsd
                           (%rsi), %xmm0
                           8(%rsi), %xmm1
                  movsd
          Source line: 4
                  addsd
                           (%rdx), %xmm0
                          8(%rdx), %xmm1
                  addsd
                           %xmm1, 8(%rdi)
                  movsd
                           %xmm0, (%rdi)
                  movsd
                           %rdi, %rax
                  movq
                           %rbp
                  popq
                  ret
In [8]:
          # Let's try to get to matrix multiplication
          import Base.*
          *(a::Point, b::Point) = Point(a.x * b.x - a.y * b.y, a.y * b.x + a.x * b.y)
          * (generic function with 139 methods)
Out[8]:
In [17]:
          # Use comprehensions to create a random matrix of Points
          A = [Point(rand(), rand())] for i=1:5, j=1:5]
Out[17]:
          5x5 Array{Point{Float64},2}:
           Point{Float64}(0.47505064620192883,0.8243753962519378)
                                                                     ... Point{Float64}(0.0699303396068014,
           Point{Float64}(0.06240865426863951,0.18262544118915414)
                                                                        Point{Float64}(0.6014849971120297,
           Point{Float64}(0.8882480752997501,0.11428465042726565)
                                                                        Point{Float64}(0.7059614326194741,
           Point{Float64}(0.716421397583451,0.5519208330384608)
                                                                        Point{Float64}(0.7605090145521005,
           Point{Float64}(0.16510560870080115,0.39476729812210865)
                                                                        Point{Float64}(0.7417662869684922,
```

```
In [10]:
          A*A
          LoadError: MethodError: `zero` has no method matching zero(::Type{Point{Float64}})
          while loading In[10], in expression starting on line 1
           in generic matmatmul! at linalg/matmul.jl:470
           in generic matmatmul! at linalg/matmul.jl:445
           in * at linalq/matmul.jl:132
In [15]:
          import Base.zero
          zero{T}(::Type{Point{T}}) = Point(zero(T), zero(T))
          zero (generic function with 14 methods)
Out[15]:
In [138]: A*A
Out[138]: 5x5 Array{Point{Float64},2}:
           Point{Float64}(-0.04554527104409692,2.1030424187840535)
                                                                        Point{Float64}(0.5849986385840079,
           Point{Float64}(0.1593127495484561,1.2743987401102095)
                                                                        Point{Float64}(0.5009620298894122,
           Point{Float64}(1.2021362218237734,2.5417597651682535)
                                                                        Point{Float64}(1.2658478493246834,
           Point{Float64}(0.3157140829497066,2.1223220170116375)
                                                                        Point{Float64}(0.3231820201482104,
           Point{Float64}(0.9316342117048305,1.7572152199453253)
                                                                        Point{Float64}(1.5201068219591227,
```

RLEVectors.jl

Debugger demo

So, we now know that Julia is composable

How do we work with data? - DataFrames.jl

```
In [19]: using DataFrames
```

```
In [21]: v = ["x", "y", "z"][rand(1:3, 10^4)];

df = DataFrame(Any[collect(1:10^4), v, rand(10^4)], [:A, :B, :C])
```

Out[21]:

	Α	В	С
1	1	z	0.05912767123600848
2	2	z	0.19640552861681382
3	3	у	0.46618442164926255
4	4	х	0.3523760931780524
5	5	z	0.45494282834946453
6	6	z	0.5729658272524141
7	7	z	0.23037315722729135
8	8	Z	0.5440549378915875
9	9	у	0.684496070434268
10	10	у	0.32477833691341607
11	11	у	0.20962477013524117
12	12	у	0.23367205624316156
13	13	z	0.4520624164770095
14	14	у	0.9294168945999208
15	15	х	0.4476664091230851
16	16	х	0.6595014831821984
17	17	Z	0.8020623735926138
18	18	у	0.18248116941483694
19	19	z	0.18953972333787417
20	20	z	0.44114340172365085
21	21	Х	0.3101659341634062
22	22	х	0.6752615475302539

```
      23
      23
      x
      0.8322961580194035

      24
      24
      z
      0.9111082092530258

      25
      25
      x
      0.8149112711436584

      26
      26
      x
      0.35353331629536176

      27
      27
      z
      0.804528212681962

      28
      28
      z
      0.8656804700825365

      29
      29
      x
      0.917240076566769

      30
      30
      z
      0.8359959957011656

      :
      :
      :
```

```
In [22]:
          function doloop(df)
               A = df[:A]
               s = 0
               for i=1:length(A)
                   s += A[i]
               end
           end
Out[22]:
          doloop (generic function with 1 method)
In [120]: t1 = @elapsed doloop(df)
Out[120]: 0.002105281
In [48]:
          function dosum(v)
               s = zero(eltype(v))
               for i=1:length(v)
                   s += v[i]
               end
               s
           end
```

Out[48]: dosum (generic function with 1 method)

```
In [122]: t Vector = @elapsed dosum(df[:A])
Out[122]: 1.8258e-5
In [137]:
          doloop dosum(df) = dosum(df[:A])
          @time doloop_dosum(df)
            0.002250 seconds (632 allocations: 29.695 KB)
Out[137]: 50005000
In [53]:
          @code_warntype doloop(df)
          Variables:
             df::DataFrames.DataFrame
            A::ANY
            s::ANY
            #s52::ANY
            i::ANY
            ##selected column#8362::Int64
          Body:
            begin # In[22], line 2:
                ##selected column#8362 = (DataFrames.getindex)((top(getfield))(df::DataFrames.DataFrame,:
                A = (Base.arrayref)((top(getfield))(df::DataFrames.DataFrame,:columns)::Array{Any,1},##se
                s = 0 \# In[22], line 5:
                GenSym(0) = (Main.colon)(1,(Main.length)(A)::ANY)::ANY
                \#s52 = (top(start))(GenSym(0))::ANY
                unless (top(!))((top(done))(GenSym(0), #s52)::ANY)::ANY goto 1
                2:
                GenSym(1) = (top(next))(GenSym(0), #s52)::ANY
                i = (top(getfield))(GenSym(1),1)::ANY
                #s52 = (top(getfield))(GenSym(1),2)::ANY # In[22], line 6:
                s = s + (Main.getindex)(A,i)::ANY::ANY
                 3:
                unless (top(!))((top(!))((top(done))(GenSym(0), #s52)::ANY)::ANY)::ANY goto 2
                1:
                0:
                return
             end::Void
```

```
@code warntype dosum(1:100)
In [56]:
          Variables:
            v::UnitRange{Int64}
            s::Int64
            #s52::Int64
            i::Int64
          Body:
            begin # In[48], line 2:
                s = 0 \# In[48], line 4:
                GenSym(2) = (Base.box)(Int64,(Base.checked_sadd)((Base.box)(Int64,(Base.checked_ssub)((to
                GenSym(0) = $(Expr(:new, UnitRange{Int64}, 1, :(((top(getfield))(Base.Intrinsics,:select_
                #s52 = (top(getfield))(GenSym(0),:start)::Int64
                unless (Base.box)(Base.Bool,(Base.not_int)(#s52::Int64 === (Base.box)(Base.Int,(Base.add_
                2:
                GenSym(4) = #s52::Int64
                GenSym(5) = (Base.box)(Base.Int,(Base.add int)(#s52::Int64,1))
                i = GenSym(4)
                \#s52 = GenSym(5) \# In[48], line 5:
                GenSym(3) = (Main.getindex)(v::UnitRange{Int64},i::Int64)::Int64
                s = (Base.box)(Base.Int,(Base.add int)(s::Int64,GenSym(3)))
                3:
                unless (Base.box)(Base.Bool,(Base.not_int)((Base.box)(Base.Bool,(Base.not_int)(#s52::Int6
                1:
                0: # In[48], line 7:
                return s::Int64
            end::Int64
```

The DataArrays approach - with NA values

```
In [131]: t_DataVector/t_Vector
Out[131]: 20.491455800197173
In [65]:
          @code warntype dosum(n2)
          Variables:
            v::DataArrays.DataArray{Int64,1}
            s::ANY
            #s52::Int64
            i::Int64
          Body:
            begin # In[48], line 2:
                s = 0 \# In[48], line 4:
                GenSym(2) = (top(getfield))(v::DataArrays.DataArray{Int64,1},:data)::Array{Int64,1}
                GenSym(3) = (Base.arraylen)(GenSym(2))::Int64
                GenSym(0) = $(Expr(:new, UnitRange{Int64}, 1, :(((top(getfield))(Base.Intrinsics,:select_
                #s52 = (top(getfield))(GenSym(0),:start)::Int64
                unless (Base.box)(Base.Bool,(Base.not_int)(#s52::Int64 === (Base.box)(Base.Int,(Base.add_
                2:
                GenSym(4) = #s52::Int64
                GenSym(5) = (Base.box)(Base.Int,(Base.add int)(#s52::Int64,1))
                i = GenSym(4)
                \#s52 = GenSym(5) \# In[48], line 5:
                s = s::UNION{DATAARRAYS.NATYPE,INT64} + (Main.getindex)(v::DataArrays.DataArray{Int64,1},
                3:
                unless (Base.box)(Base.Bool, (Base.not int)((Base.box)(Base.Bool, (Base.not int)(#s52::Int6
                1:
                0: # In[48], line 7:
                return s::UNION{DATAARRAYS.NATYPE,INT64}
            end::UNION{DATAARRAYS.NATYPE,INT64}
```

The NullableArrays approach

```
In [95]:
          using NullableArrays
          n = NullableArray(collect(1:10^4))
Out[95]:
          10000-element NullableArrays.NullableArray{Int64,1}:
                2
                3
                4
                6
                7
                8
                9
               10
               11
               12
               13
             9989
             9990
             9991
             9992
             9993
             9994
             9995
             9996
             9997
             9998
             9999
            10000
In [133]: zero(::Type{Nullable{Int64}}) = Nullable(0)
          t_Nullables = @elapsed dosum(n)
Out[133]: 3.0955e-5
In [134]: t_Nullables/t_Vector
Out[134]: 1.6954211852338699
In [ ]:
```