



Time Series Analysis & Forecasting Using R

6. Introduction to forecasting



Outline

1 Statistical forecasting

2 Benchmark methods

3 Lab Session 11

Outline

1 Statistical forecasting

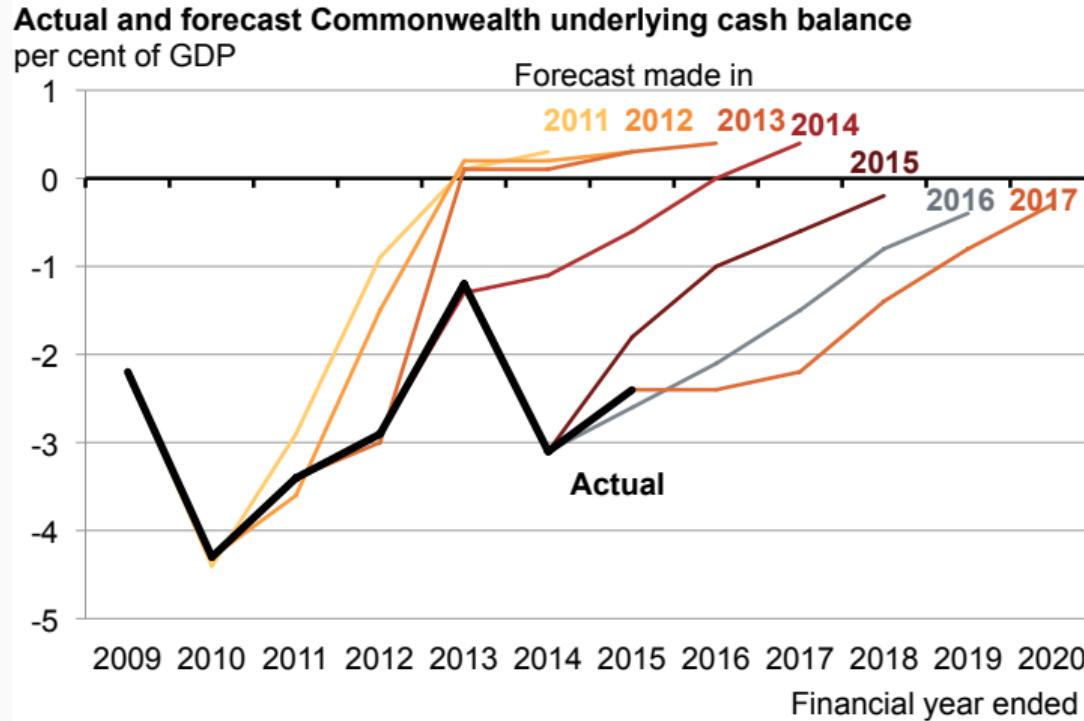
2 Benchmark methods

3 Lab Session 11

Forecasting is difficult

Commonwealth plans to drift back to surplus
show the triumph of experience over hope

GRATTAN
Institute



What can we forecast?



What can we forecast?



What can we forecast?

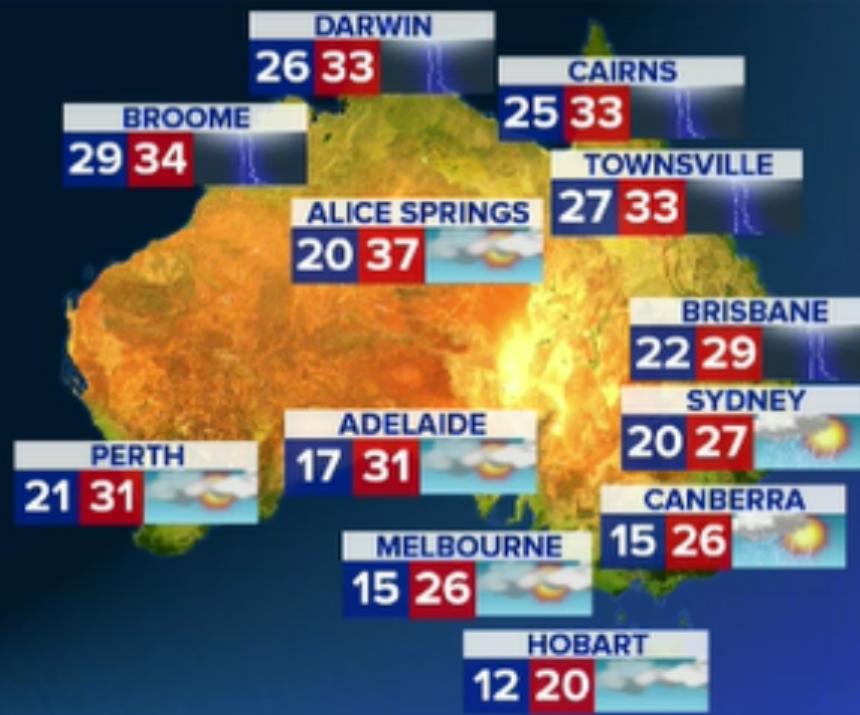


What can we forecast?



What can we forecast?

TOMORROW



What can we forecast?



What can we forecast?



Which is easiest to forecast?

- 1 daily electricity demand in 3 days time
- 2 timing of next Halley's comet appearance
- 3 time of sunrise this day next year
- 4 Google stock price tomorrow
- 5 Google stock price in 6 months time
- 6 maximum temperature tomorrow
- 7 exchange rate of \$US/AUS next week
- 8 total sales of drugs in Australian pharmacies next month

Which is easiest to forecast?

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-
- how do we measure “easiest”?
 - what makes something easy/difficult to forecast?

Factors affecting forecastability

Something is easier to forecast if:

- we have a good understanding of the factors that contribute to it
- there is lots of data available;
- the forecasts cannot affect the thing we are trying to forecast.
- there is relatively low natural/unexplainable random variation.
- the future is somewhat similar to the past

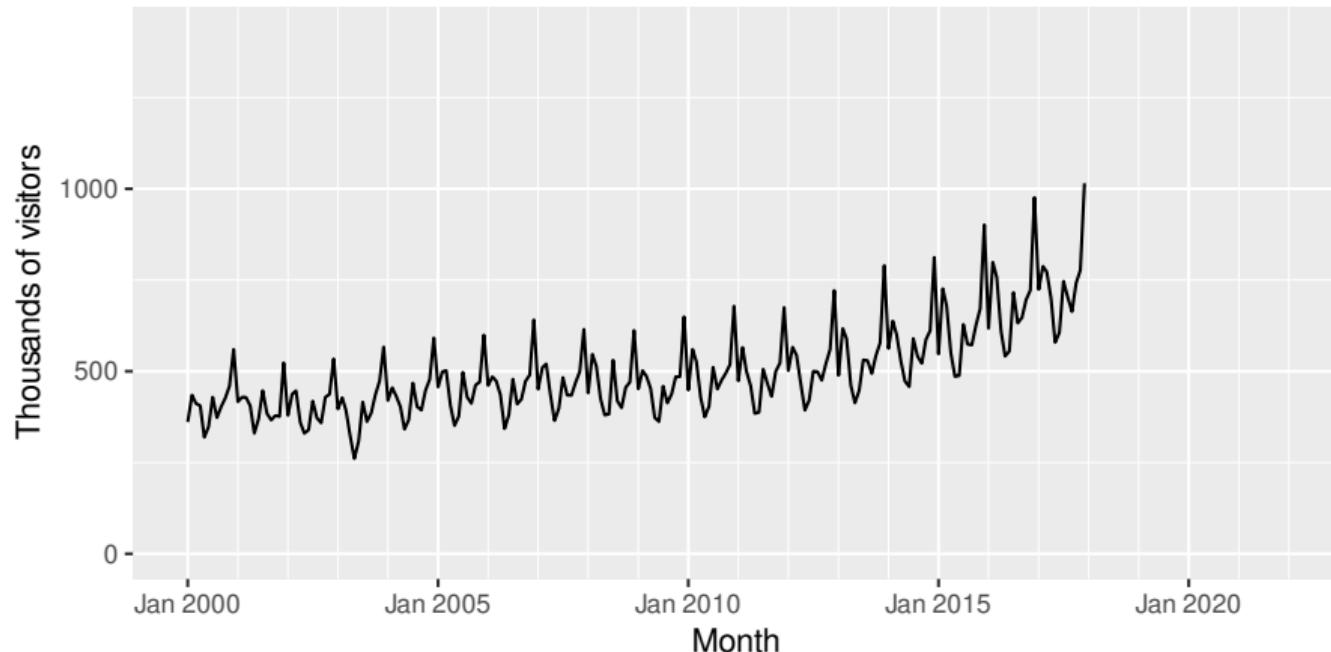
Random futures

A forecast is an estimate of the probabilities of possible futures.

Random futures

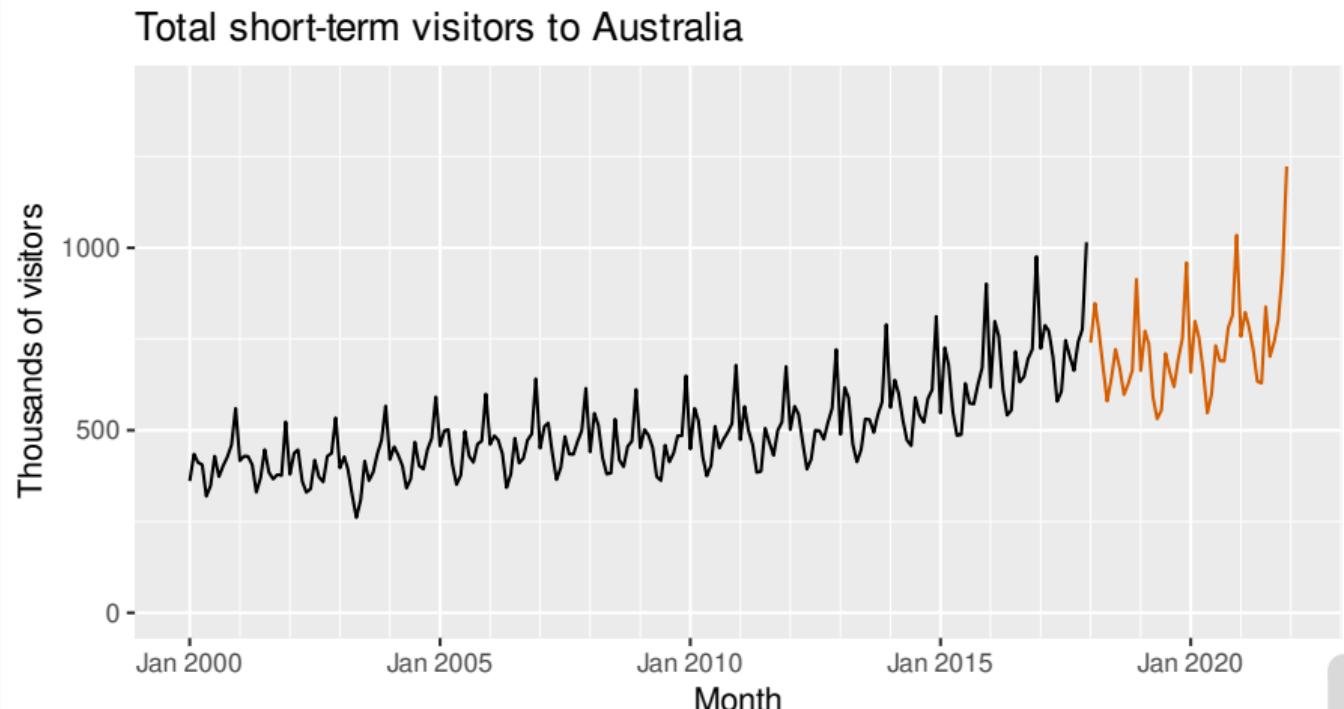
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Total short-term visitors to Australia



Random futures

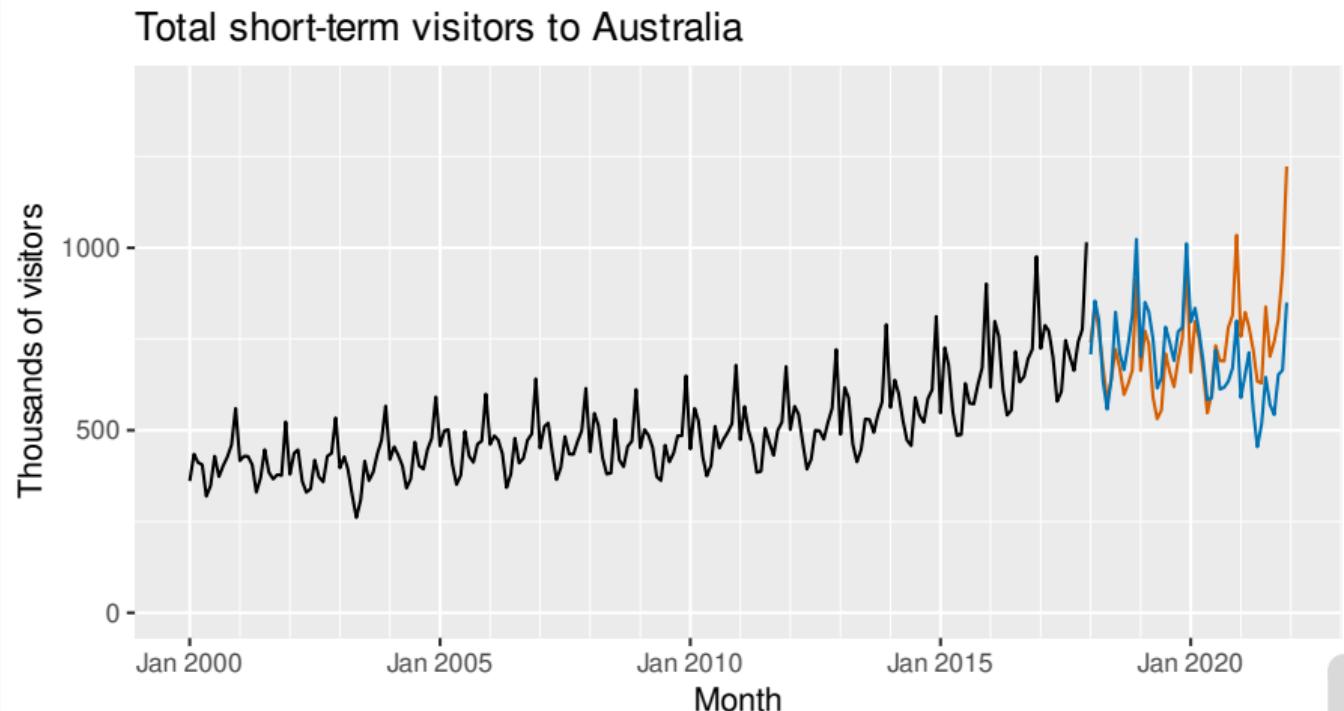
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Simulated futures
from an ETS model

Random futures

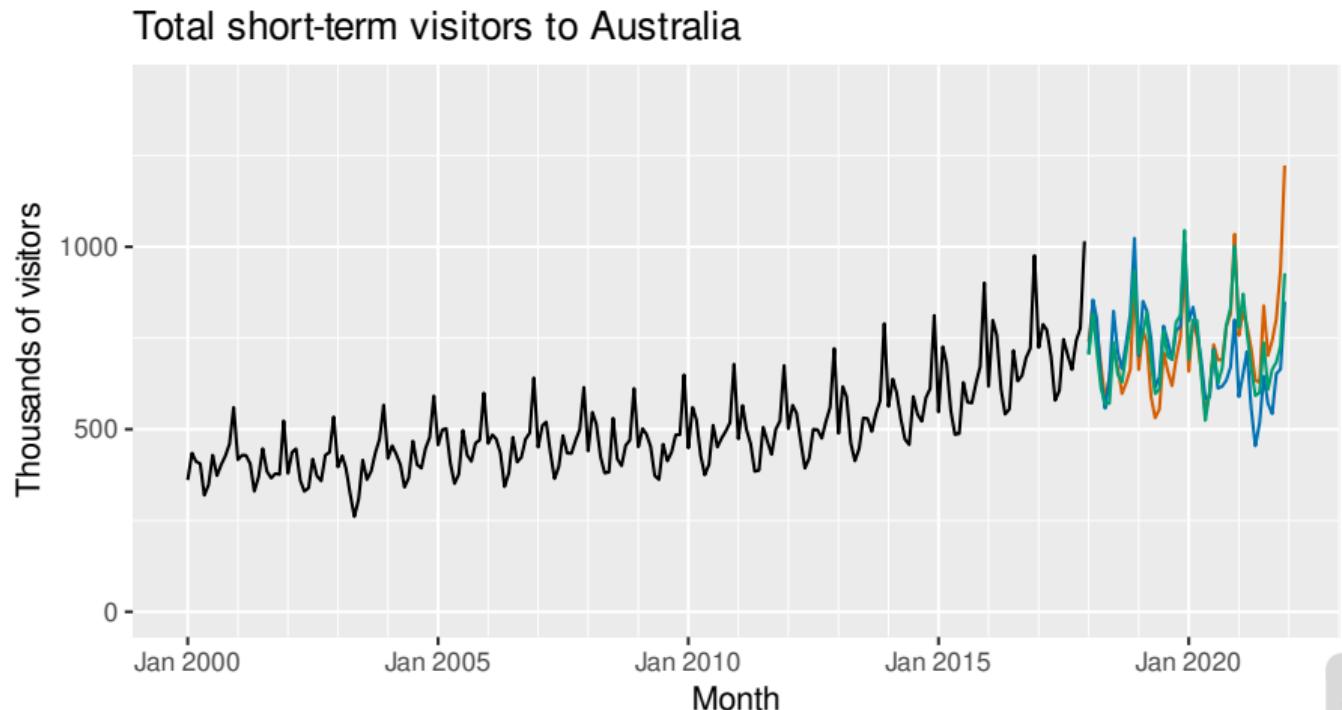
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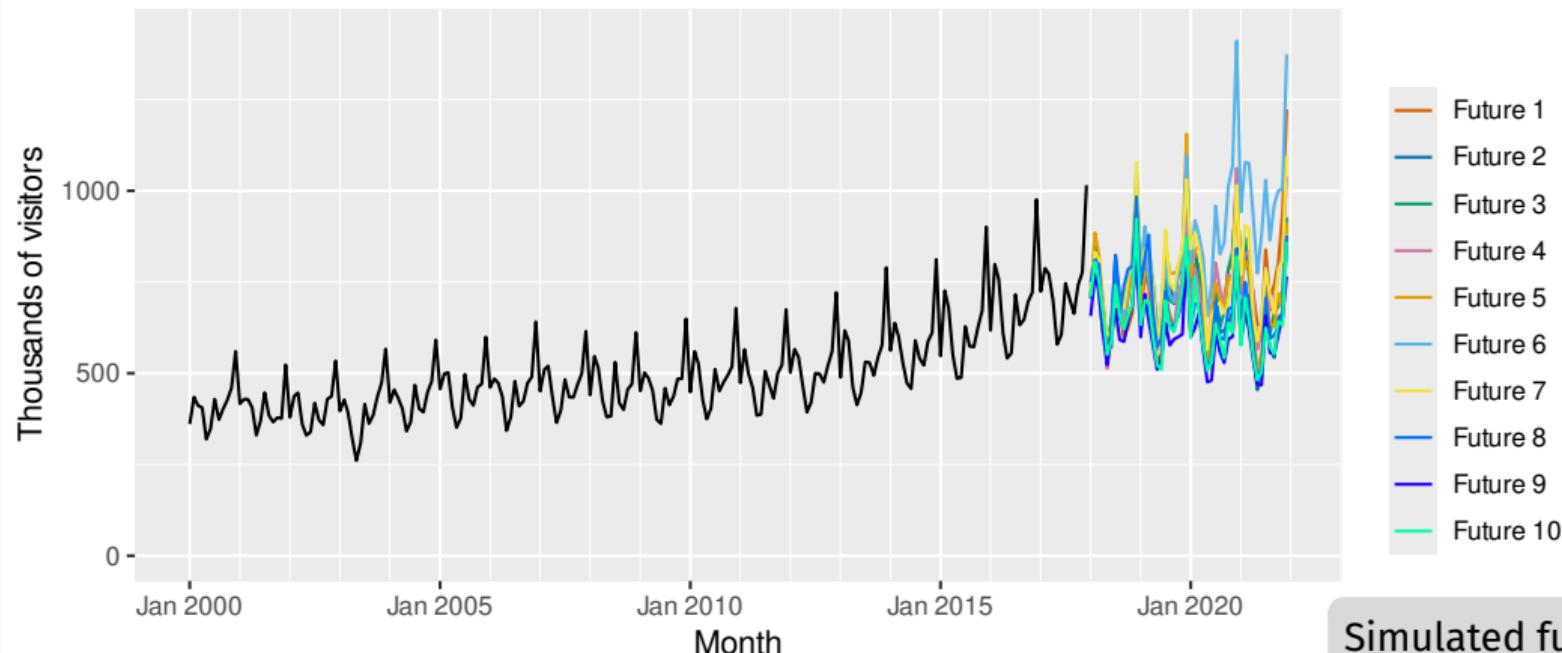


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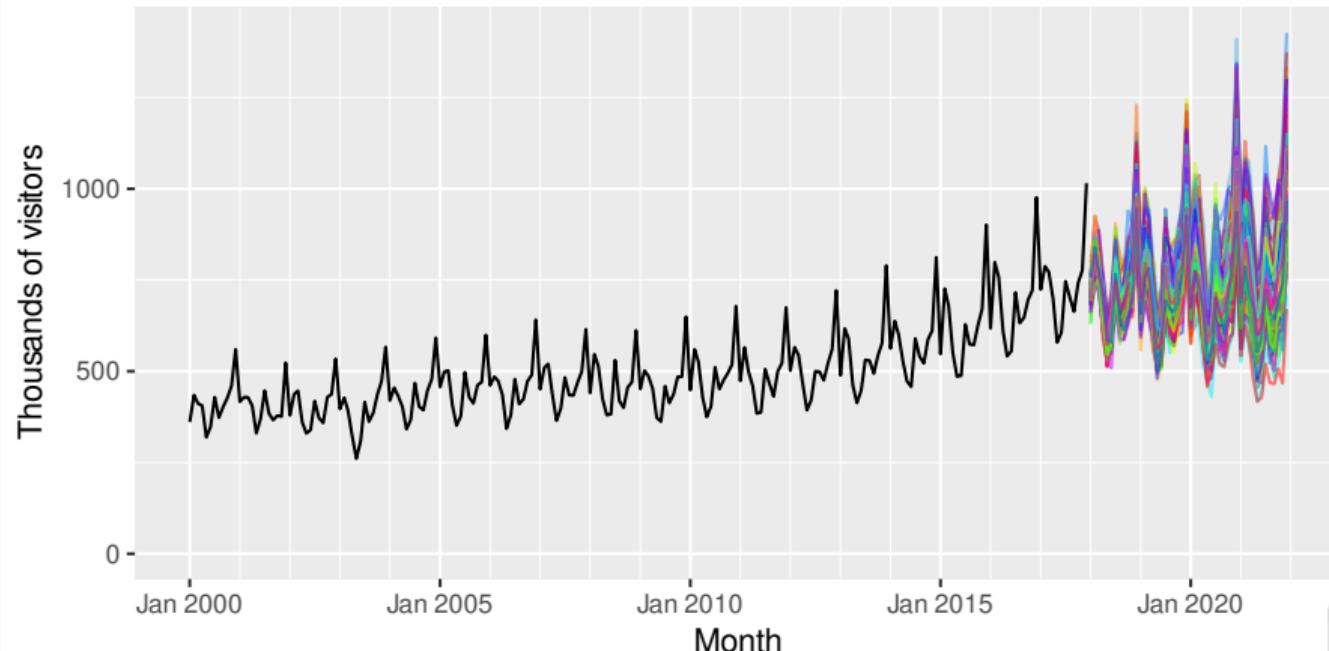


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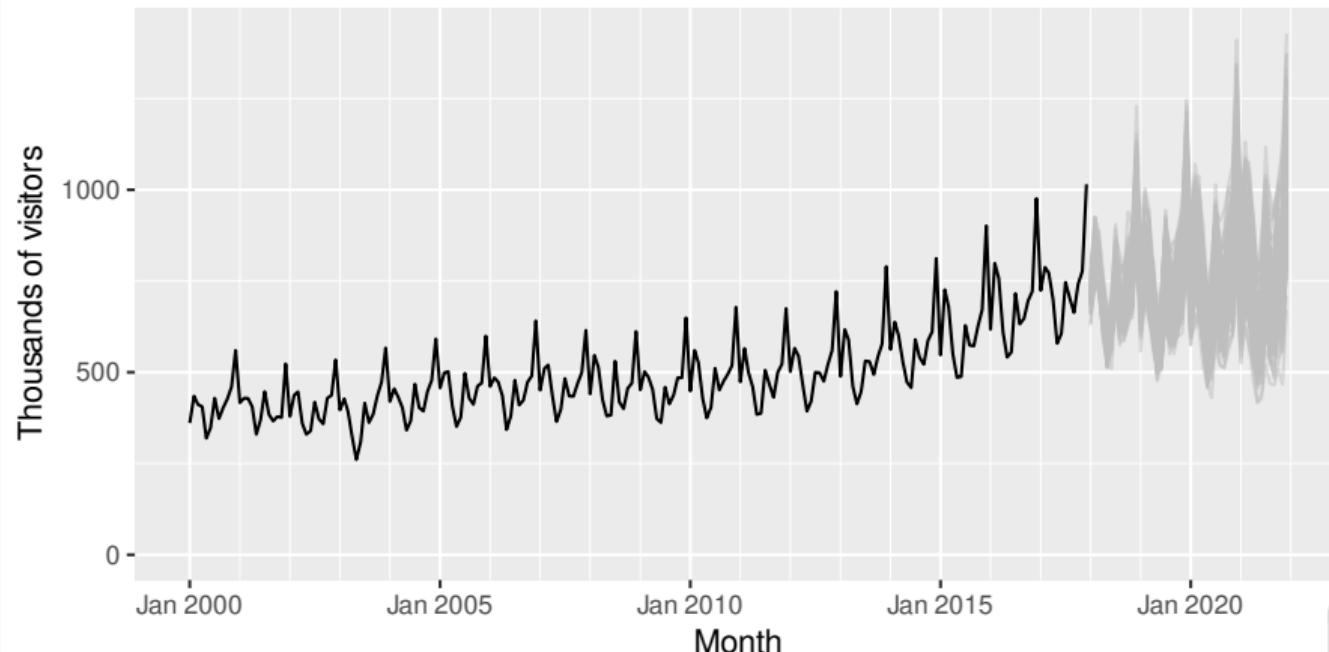


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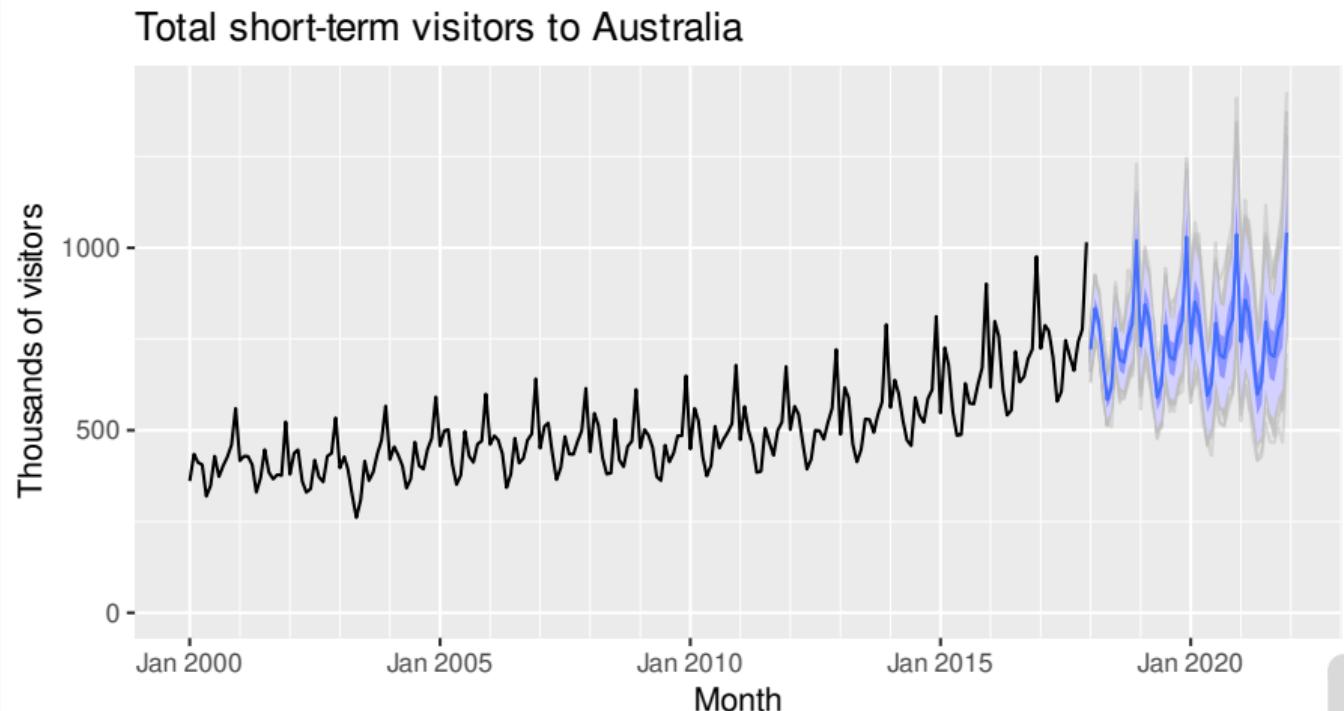
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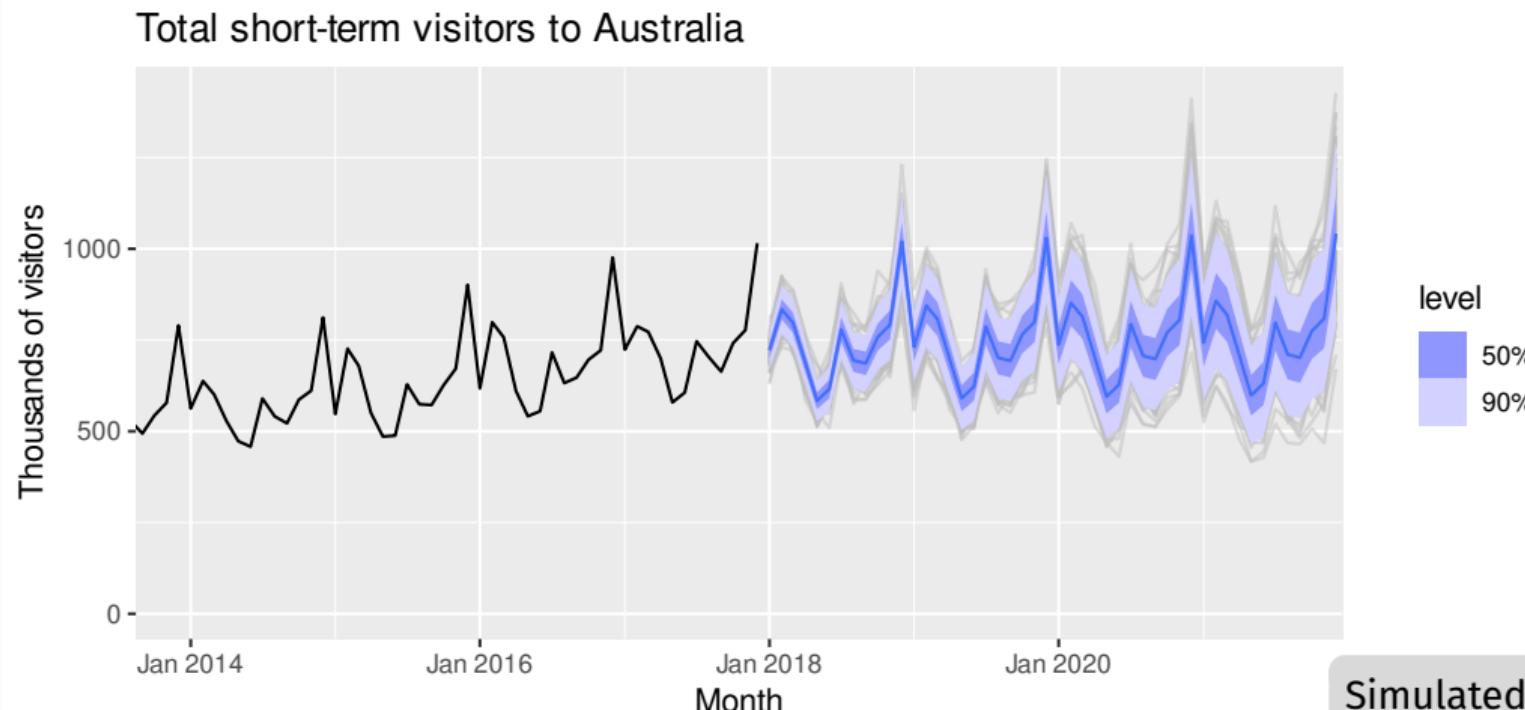
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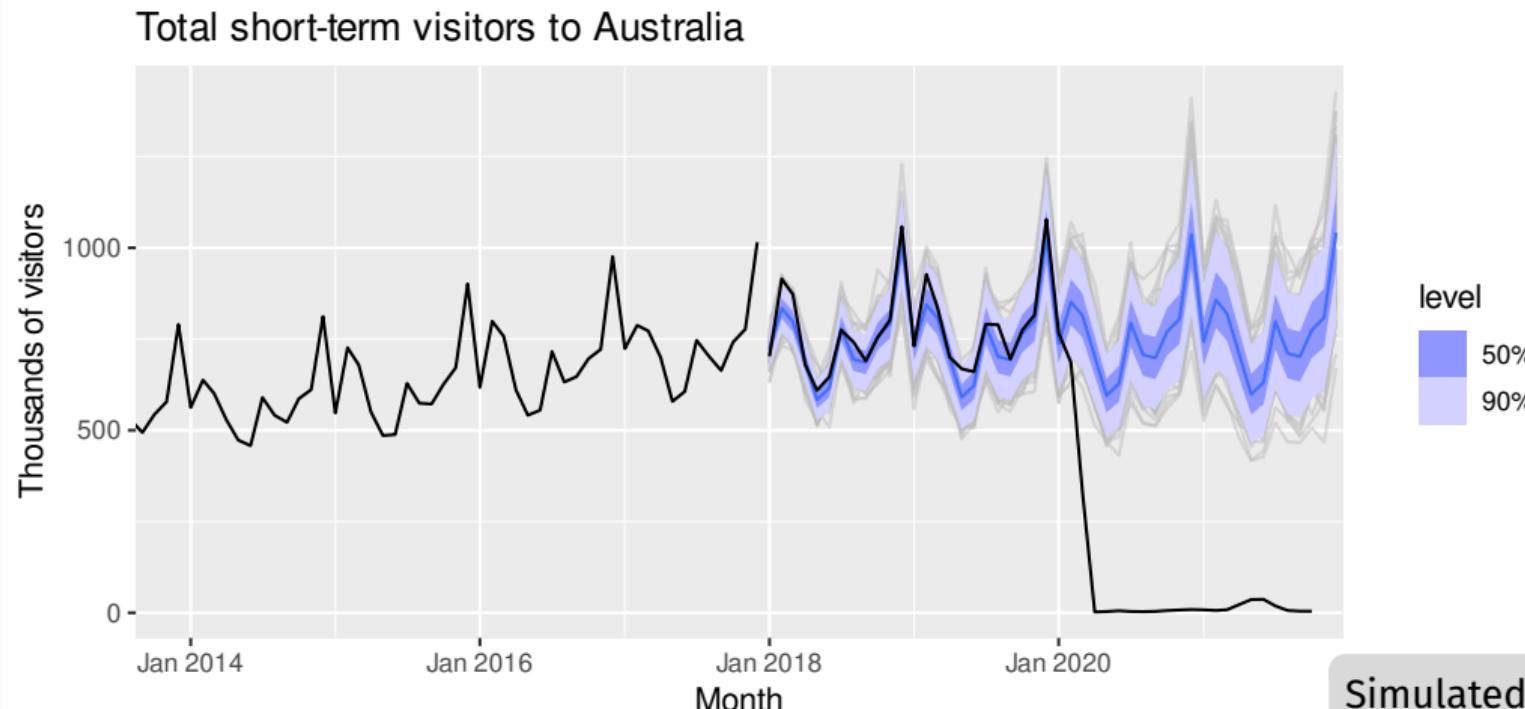


Month

Simulated futures
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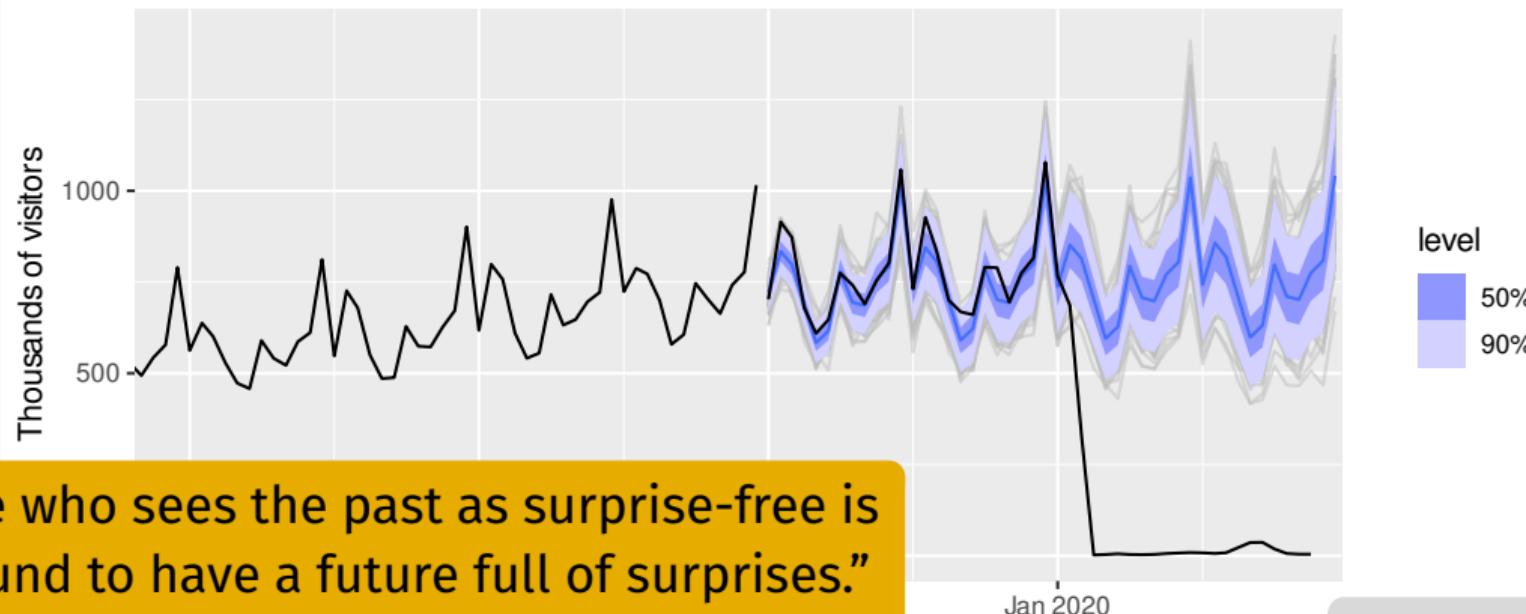
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Random futures

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Total short-term visitors to Australia



“He who sees the past as surprise-free is bound to have a future full of surprises.”

(Amos Tversky)

Simulated futures
from an ETS model

Statistical forecasting

- Thing to be forecast: y_{T+h} .
- What we know: y_1, \dots, y_T .
- Forecast distribution: $y_{T+h|t} = y_{T+h} \mid \{y_1, y_2, \dots, y_T\}$.
- Point forecast: $\hat{y}_{T+h|T} = E[y_{T+h} \mid y_1, \dots, y_T]$.
- Forecast variance: $\text{Var}[y_t \mid y_1, \dots, y_T]$
- Prediction interval is a range of values of y_{T+h} with high probability.

Outline

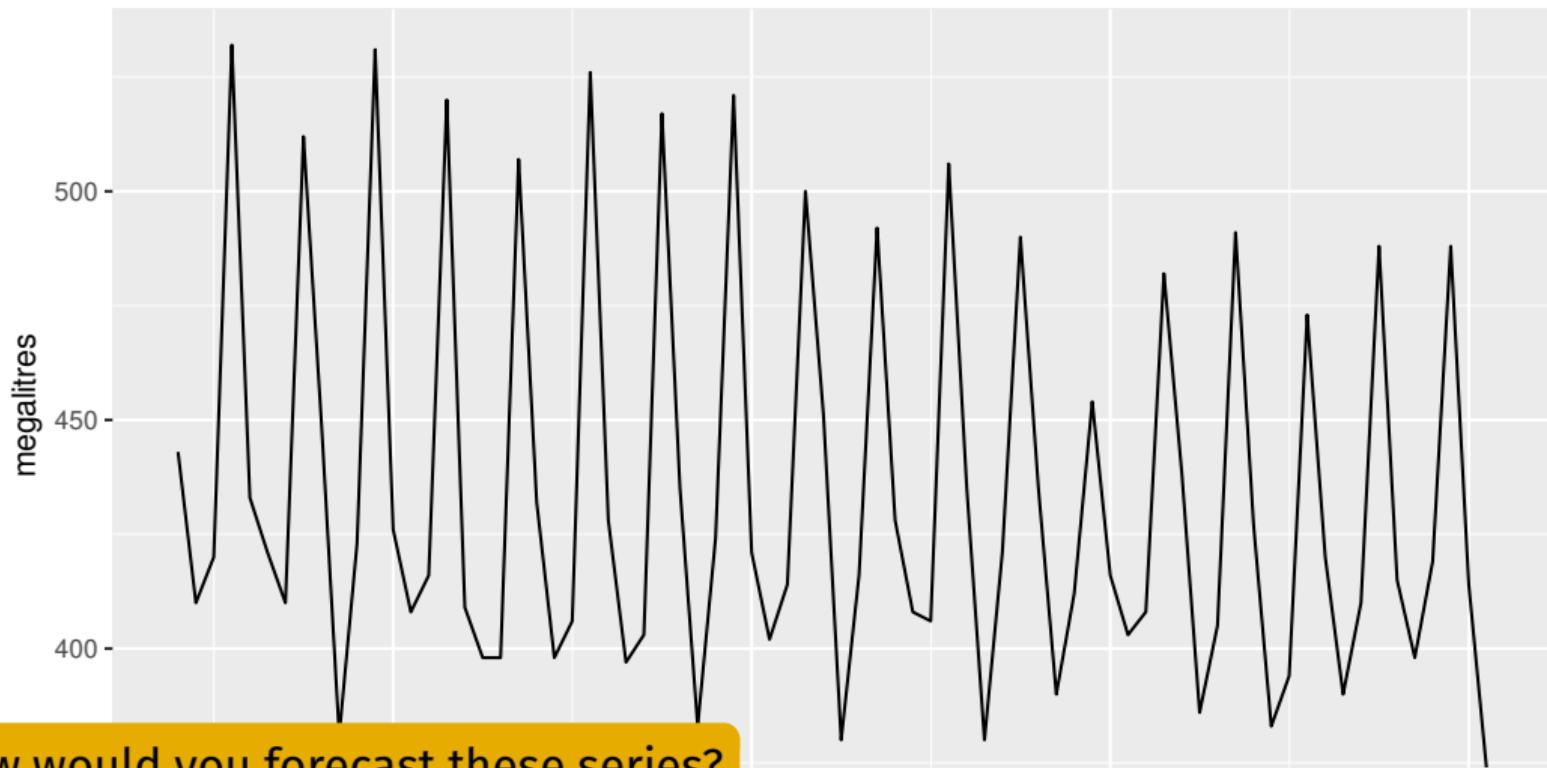
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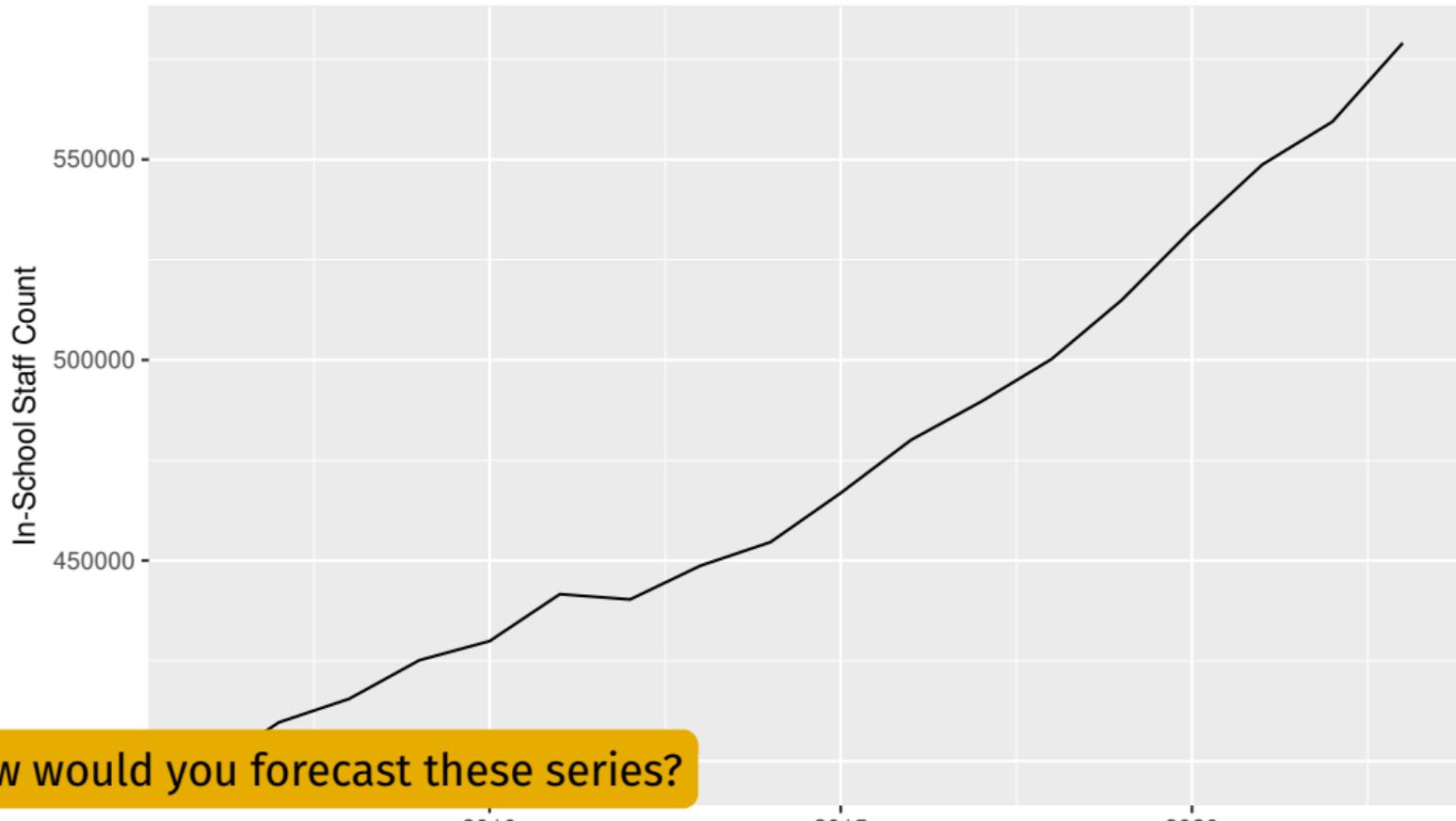
Some simple forecasting methods

Australian quarterly beer production



How would you forecast these series?

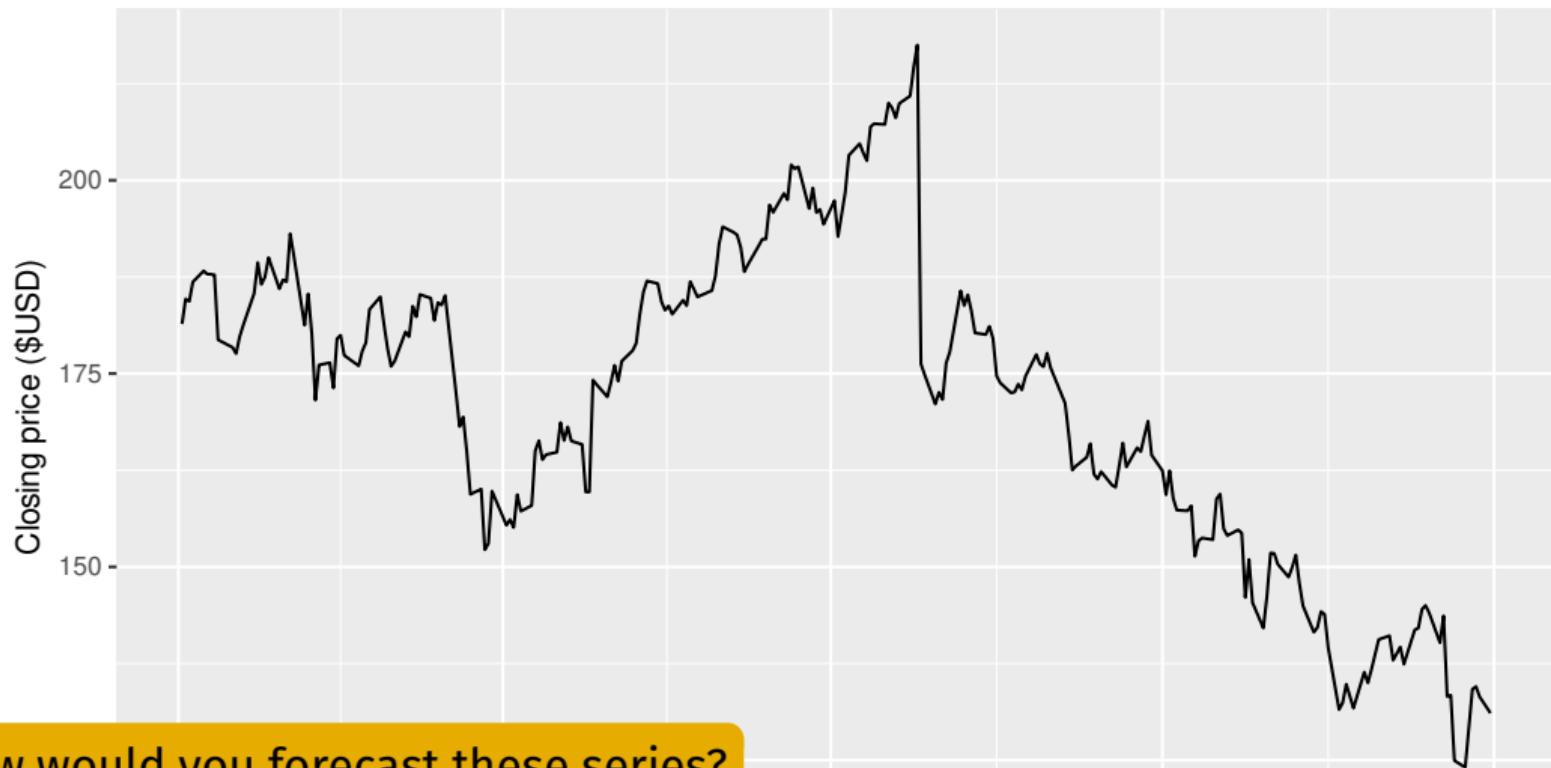
Some simple forecasting methods



How would you forecast these series?

Some simple forecasting methods

Facebook closing stock price in 2018



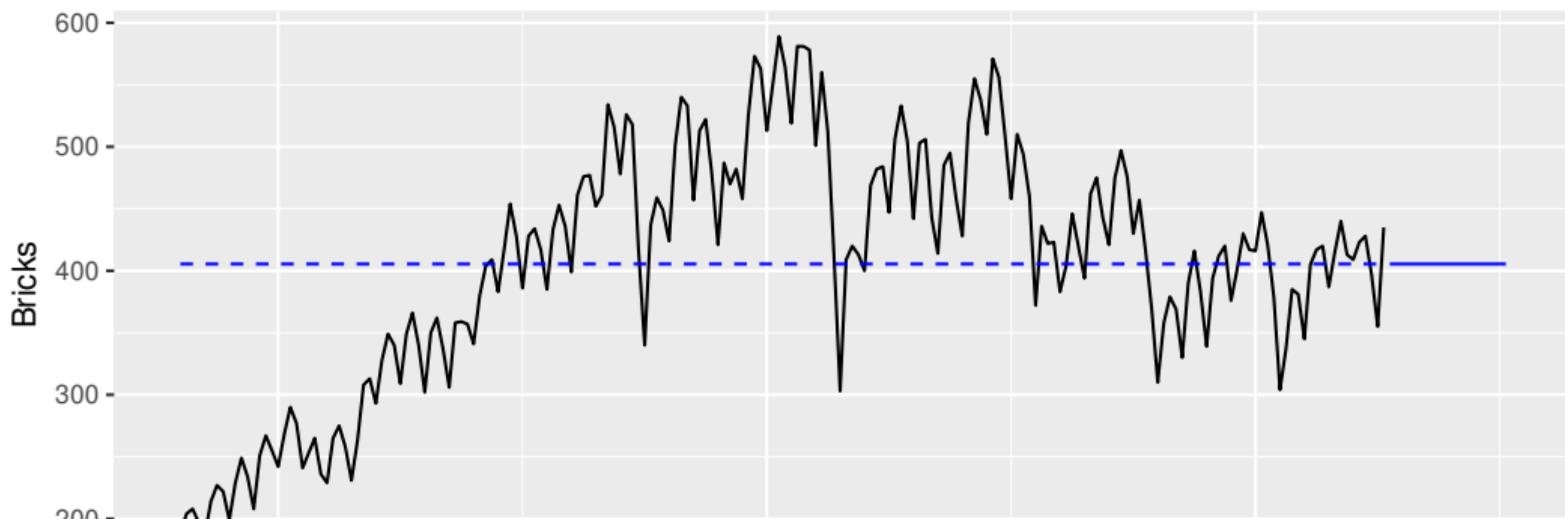
How would you forecast these series?

Some simple forecasting methods

MEAN(y): Average method

- Forecast of all future values is equal to mean of historical data $\{y_1, \dots, y_T\}$.
- Forecasts: $\hat{y}_{T+h|T} = \bar{y} = (y_1 + \dots + y_T)/T$

Clay brick production in Australia

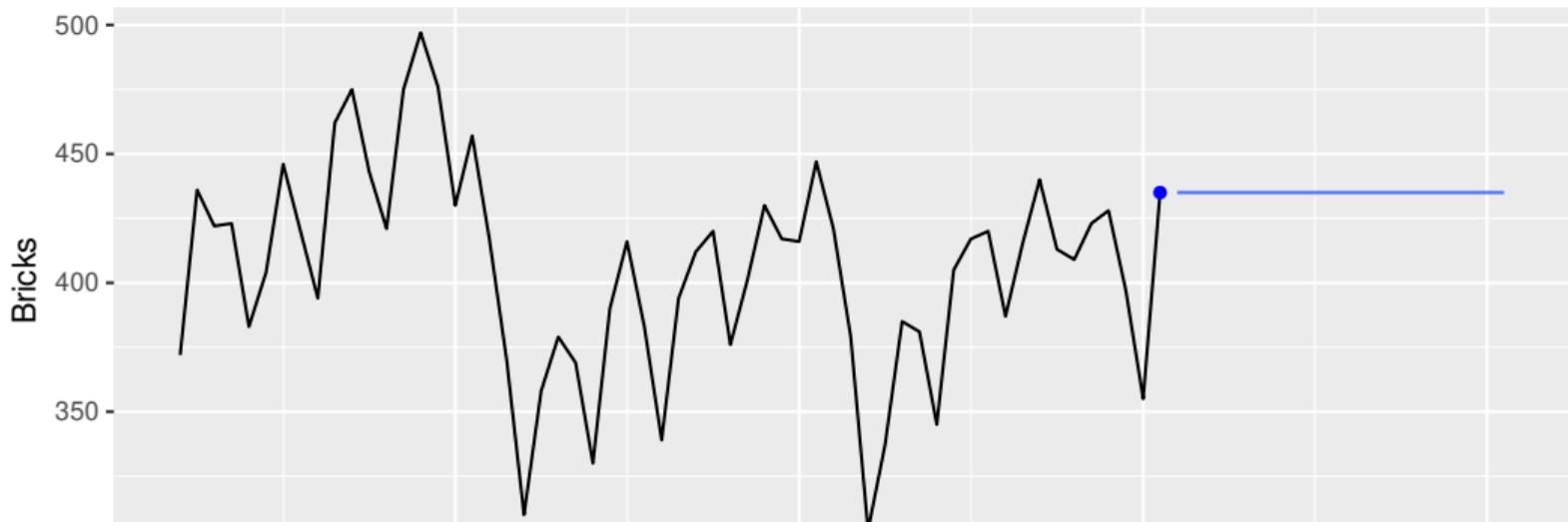


Some simple forecasting methods

NAIVE(y): Naive method

- Forecasts equal to last observed value.
- Forecasts: $\hat{y}_{T+h|T} = y_T$.
- Consequence of efficient market hypothesis.

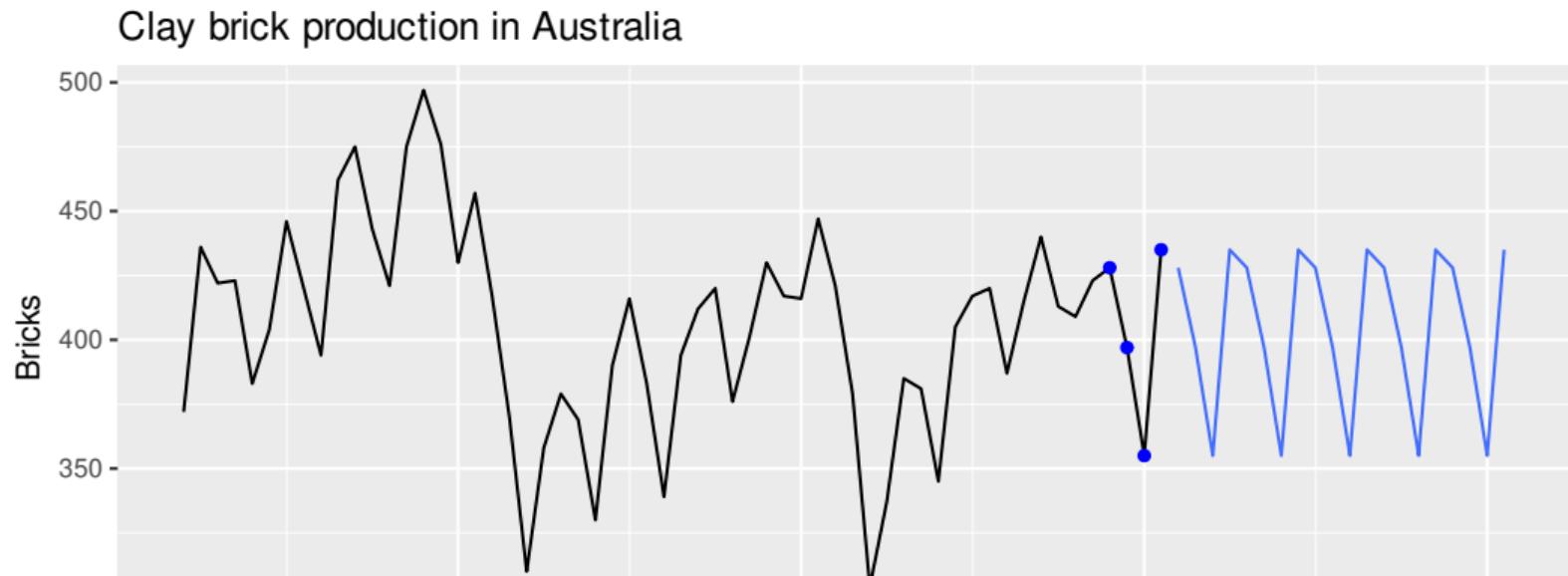
Clay brick production in Australia



Some simple forecasting methods

SNAIVE($y \sim \text{lag}(m)$): Seasonal naive method

- Forecasts equal to last value from same season.
- Forecasts: $\hat{y}_{T+h|T} = y_{T+h-m(k+1)}$, where m = seasonal period and k is the integer part of $(h - 1)/m$.



Some simple forecasting methods

RW(y ~ drift()): Drift method

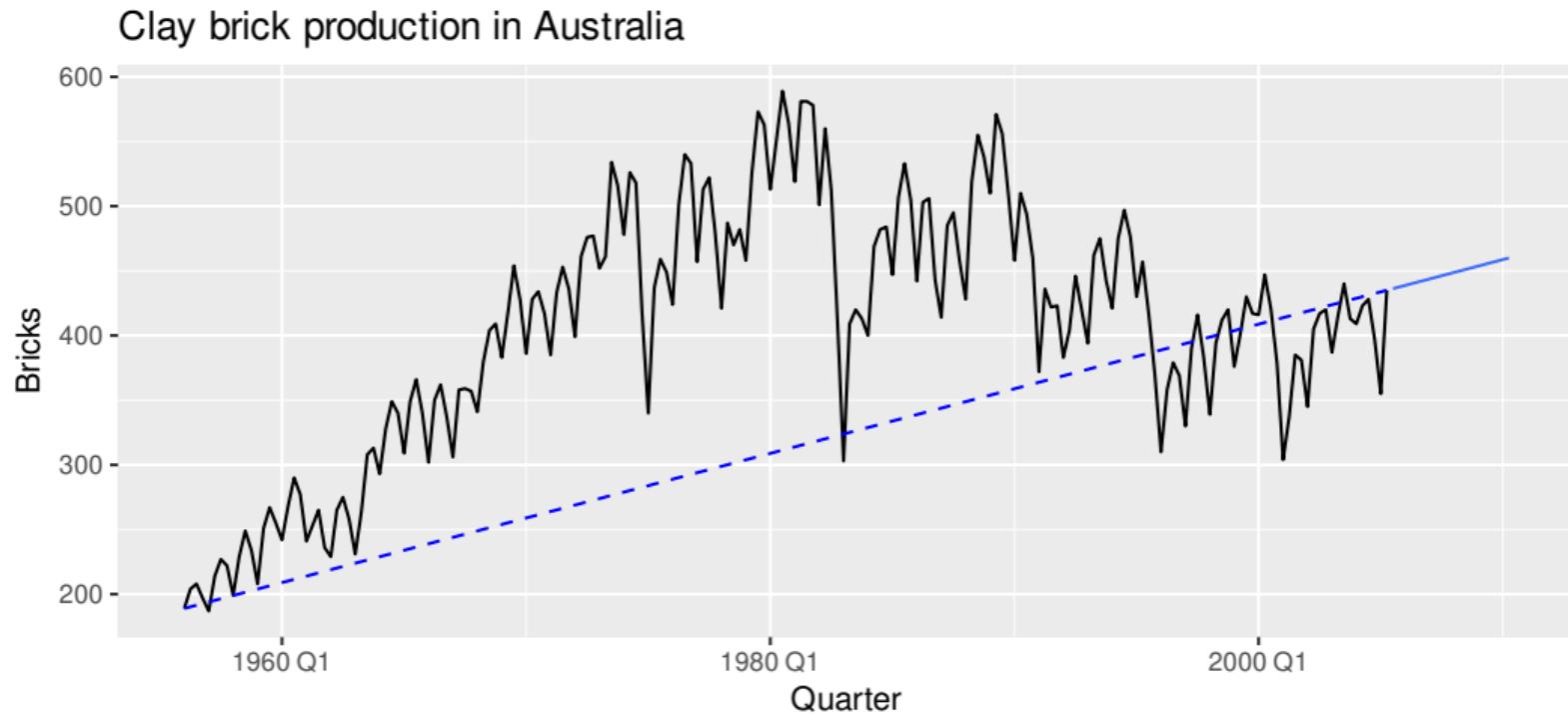
- Forecasts equal to last value plus average change.
- Forecasts:

$$\begin{aligned}\hat{y}_{T+h|T} &= y_T + \frac{h}{T-1} \sum_{t=2}^T (y_t - y_{t-1}) \\ &= y_T + \frac{h}{T-1} (y_T - y_1).\end{aligned}$$

- Equivalent to extrapolating a line drawn between first and last observations.

Some simple forecasting methods

Drift method



Model fitting

The `model()` function trains models to data.

```
brick_fit <- aus_production |>
  filter(!is.na(Bricks)) |>
  model(
    `Seasonal_naive` = SNAIVE(Bricks),
    `Naive` = NAIVE(Bricks),
    Drift = RW(Bricks ~ drift()),
    Mean = MEAN(Bricks)
  )
```

```
# A mable: 1 x 4
  Seasonal_naive     Naive          Drift      Mean
                <model> <model>      <model> <model>
1       <SNAIVE> <NAIVE> <RW w/ drift> <MEAN>
```

A `mable` is a model table, each cell corresponds to a fitted model.

Producing forecasts

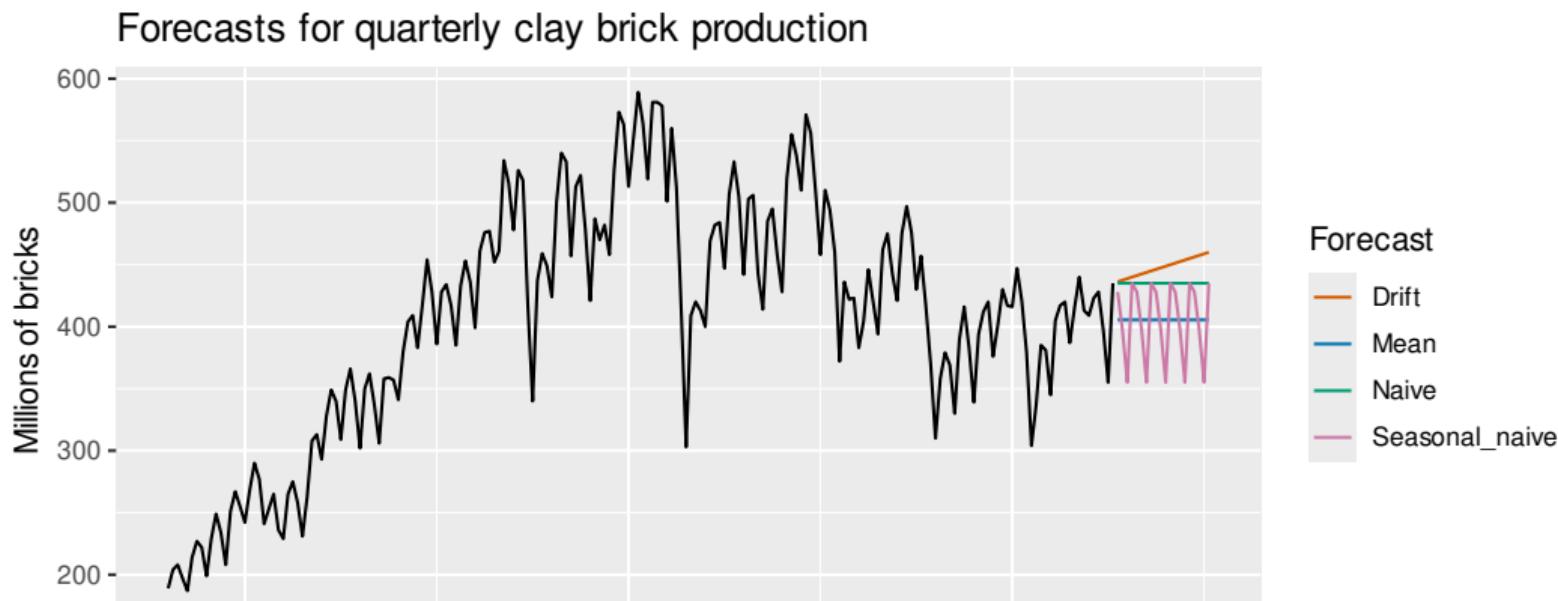
```
brick_fc <- brick_fit |>  
  forecast(h = "5 years")
```

```
# A fable: 80 x 4 [1Q]  
# Key:      .model [4]  
#  
.model          Quarter  
<chr>           <qtr>  
1 Seasonal_naive 2005 Q3  
2 Seasonal_naive 2005 Q4  
3 Seasonal_naive 2006 Q1  
4 Seasonal_naive 2006 Q2  
# i 76 more rows  
# i 2 more variables: Bricks <dist>, .mean <dbl>
```

A fable is a forecast table with point forecasts and distributions.

Visualising forecasts

```
brick_fc |>  
  autoplot(aus_production, level = NULL) +  
  labs(title = "Forecasts for quarterly clay brick production",  
       x = "Year", y = "Millions of bricks") +  
  guides(colour = guide_legend(title = "Forecast"))
```



Prediction intervals

```
brick_fc |>  
  hilo(level = c(50, 75))
```

```
# A tsibble: 80 x 6 [1Q]  
# Key:       .model [4]  
  .model      Quarter  
  <chr>       <qtr>  
1 Seasonal_naive 2005 Q3  
2 Seasonal_naive 2005 Q4  
3 Seasonal_naive 2006 Q1  
4 Seasonal_naive 2006 Q2  
5 Seasonal_naive 2006 Q3  
6 Seasonal_naive 2006 Q4  
7 Seasonal_naive 2007 Q1  
8 Seasonal_naive 2007 Q2  
9 Seasonal_naive 2007 Q3  
10 Seasonal_naive 2007 Q4
```

Prediction intervals

```
brick_fc |>
  hilo(level = c(50, 75)) |>
  mutate(lower = `50%`$lower, upper = `50%`$upper)
```

```
# A tsibble: 80 x 8 [1Q]
# Key:      .model [4]
  .model      Quarter
  <chr>       <qtr>
1 Seasonal_naive 2005 Q3
2 Seasonal_naive 2005 Q4
3 Seasonal_naive 2006 Q1
4 Seasonal_naive 2006 Q2
5 Seasonal_naive 2006 Q3
6 Seasonal_naive 2006 Q4
7 Seasonal_naive 2007 Q1
8 Seasonal_naive 2007 Q2
9 Seasonal_naive 2007 Q3
```

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Lab Session 11

Produce forecasts using an appropriate benchmark method, and plot the results using `autoplot()` for the following time series:

- 1 Total in-school staff in Australia (staff)
- 2 Preschool and School education payroll jobs (payroll_education)
- 3 Total Australian retail turnover (aggregate aus_retail)