



Time Series Analysis & Forecasting Using R

5. Time series features



Outline

- 1 Notice: Material planned to change
- 2 STL Features
- 3 Lab Session 9
- 4 Dimension reduction for features
- 5 Lab Session 10

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Notice: Material planned to change

This material is planned to be updated to better align with the training needs of the Department of Education.

In particular, this section will be removed to make time for:

- econometric concepts
- multivariate models.

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Strength of seasonality and trend

STL decomposition

$$y_t = T_t + S_t + R_t$$

Seasonal strength

$$\max \left(0, 1 - \frac{\text{Var}(R_t)}{\text{Var}(S_t + R_t)} \right)$$

Trend strength

$$\max \left(0, 1 - \frac{\text{Var}(R_t)}{\text{Var}(T_t + R_t)} \right)$$

Feature extraction and statistics

```
tourism |> features(Trips, feat_stl)
```

```
# A tibble: 304 x 12
```

	Region	State	Purpose	trend_strength	seasonal_strength_year
	<chr>	<chr>	<chr>	<dbl>	<dbl>
1	Adelaide	South Aust~	Busine~	0.464	0.407
2	Adelaide	South Aust~	Holiday	0.554	0.619
3	Adelaide	South Aust~	Other	0.746	0.202
4	Adelaide	South Aust~	Visiti~	0.435	0.452
5	Adelaide Hills	South Aust~	Busine~	0.464	0.179
6	Adelaide Hills	South Aust~	Holiday	0.528	0.296
7	Adelaide Hills	South Aust~	Other	0.593	0.404
8	Adelaide Hills	South Aust~	Visiti~	0.488	0.254
9	Alice Springs	Northern T~	Busine~	0.534	0.251
10	Alice Springs	Northern T~	Holiday	0.381	0.832

```
# i 294 more rows
```

```
# i 7 more variables: seasonal_peak_year <dbl>,
```

```
#   seasonal_trough_year <dbl>, spikiness <dbl>, linearity <dbl>,
```

```
#   curvature <dbl>, stl_e_acf1 <dbl>, stl_e_acf10 <dbl>
```

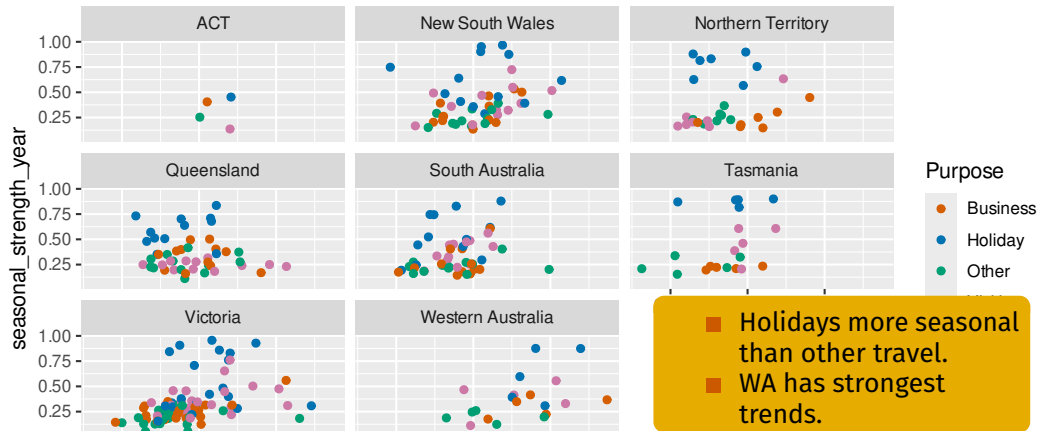
Feature extraction and statistics

```
tourism |>  
  features(Trips, feat_stl) |>  
  ggplot(aes(x = trend_strength, y = seasonal_strength_year, col = Purpose)) +  
  geom_point() + facet_wrap(vars(State))
```



Feature extraction and statistics

```
tourism |>  
  features(Trips, feat_stl) |>  
  ggplot(aes(x = trend_strength, y = seasonal_strength_year, col = Purpose)) +  
  geom_point() + facet_wrap(vars(State))
```



Feature extraction and statistics

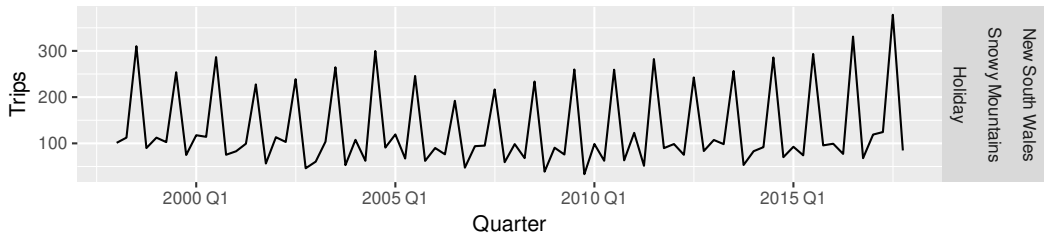
Find the most seasonal time series:

```
most_seasonal <- tourism |>  
  features(Trips, feat_stl) |>  
  filter(seasonal_strength_year == max(seasonal_strength_year))
```

Feature extraction and statistics

Find the most seasonal time series:

```
most_seasonal <- tourism |>
  features(Trips, feat_stl) |>
  filter(seasonal_strength_year == max(seasonal_strength_year))
tourism |>
  right_join(most_seasonal, by = c("State", "Region", "Purpose")) |>
  ggplot(aes(x = Quarter, y = Trips)) +
  geom_line() + facet_grid(vars(State, Region, Purpose))
```



Feature extraction and statistics

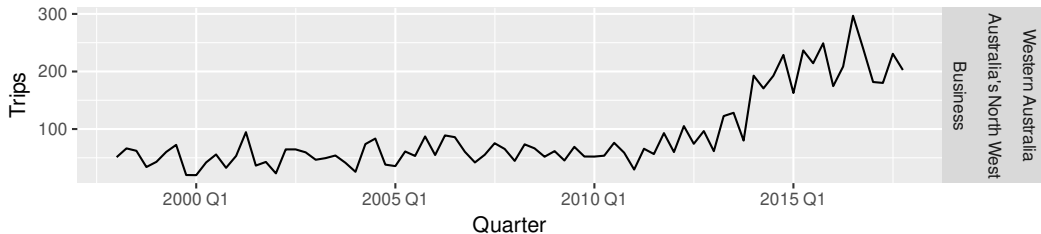
Find the most trended time series:

```
most_trended <- tourism |>  
  features(Trips, feat_stl) |>  
  filter(trend_strength == max(trend_strength))
```

Feature extraction and statistics

Find the most trended time series:

```
most_trended <- tourism |>
  features(Trips, feat_stl) |>
  filter(trend_strength == max(trend_strength))
tourism |>
  right_join(most_trended, by = c("State", "Region", "Purpose")) |>
  ggplot(aes(x = Quarter, y = Trips)) +
  geom_line() + facet_grid(vars(State, Region, Purpose))
```



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Lab Session 9

- Use `GGally::ggpairs()` to look at the relationships between the STL-based features. You might wish to change `seasonal_peak_year` and `seasonal_trough_year` to factors.
- Which is the peak quarter for holidays in each state?

Feature extraction and statistics

```
tourism |> features(Trips, feat_acf)
```

```
# A tibble: 304 x 10
```

	Region	State	Purpose	acf1	acf10	diff1_acf1	diff1_acf10	diff2_acf1
	<chr>	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	Adelaide	Sout~	Busine~	0.0333	0.131	-0.520	0.463	-0.676
2	Adelaide	Sout~	Holiday	0.0456	0.372	-0.343	0.614	-0.487
3	Adelaide	Sout~	Other	0.517	1.15	-0.409	0.383	-0.675
4	Adelaide	Sout~	Visiti~	0.0684	0.294	-0.394	0.452	-0.518
5	Adelaide~	Sout~	Busine~	0.0709	0.134	-0.580	0.415	-0.750
6	Adelaide~	Sout~	Holiday	0.131	0.313	-0.536	0.500	-0.716
7	Adelaide~	Sout~	Other	0.261	0.330	-0.253	0.317	-0.457
8	Adelaide~	Sout~	Visiti~	0.139	0.117	-0.472	0.239	-0.626
9	Alice Sp~	Nort~	Busine~	0.217	0.367	-0.500	0.381	-0.658
10	Alice Sp~	Nort~	Holiday	-0.00660	2.11	-0.153	2.11	-0.274

```
# i 294 more rows
```

```
# i 2 more variables: diff2_acf10 <dbl>, season_acf1 <dbl>
```


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Feature extraction and statistics

All features from the feasts package

```
tourism_features <- tourism |>
  features(Trips, feature_set(pkgs = "feasts"))

# A tibble: 304 x 51
  Region      State      Purpose trend_strength seasonal_strength_year
  <chr>      <chr>      <chr>      <dbl>              <dbl>
1 Adelaide  South Aust~ Busine~      0.464              0.407
2 Adelaide  South Aust~ Holiday    0.554              0.619
3 Adelaide  South Aust~ Other      0.746              0.202
4 Adelaide  South Aust~ Visiti~    0.435              0.452
5 Adelaide Hills South Aust~ Busine~    0.464              0.179
6 Adelaide Hills South Aust~ Holiday    0.528              0.296
7 Adelaide Hills South Aust~ Other      0.593              0.404
8 Adelaide Hills South Aust~ Visiti~    0.488              0.254
9 Alice Springs Northern T~ Busine~    0.534              0.251
10 Alice Springs Northern T~ Holiday    0.381              0.832
# i 294 more rows
# i 46 more variables: seasonal_peak_year <dbl>,
#   seasonal_trough_year <dbl>, spikiness <dbl>, linearity <dbl>,
#   curvature <dbl>, stl_e_acf1 <dbl>, stl_e_acf10 <dbl>, acf1 <dbl>,
#   acf10 <dbl>, diff1_acf1 <dbl>, diff1_acf10 <dbl>, diff2_acf1 <dbl>,
#   diff2_acf10 <dbl>, season_acf1 <dbl>, pacf5 <dbl>, diff1_pacf5 <dbl>,
#   diff2_pacf5 <dbl>, season_pacf <dbl>, zero_run_mean <dbl>, ...
```

Feature extraction and statistics

Principal components based
on all features from the
feasts package

```
pcs <- tourism_features |>
  select(-State, -Region, -Purpose) |>
  prcomp(scale = TRUE) |>
  broom::augment(tourism_features)
```

```
# A tibble: 304 x 100
```

	.rownames	Region	State	Purpose	trend_strength	seasonal_strength_year
	<chr>	<chr>	<chr>	<chr>	<dbl>	<dbl>
1	1	Adelaide	Sout~	Busine~	0.464	0.407
2	2	Adelaide	Sout~	Holiday	0.554	0.619
3	3	Adelaide	Sout~	Other	0.746	0.202
4	4	Adelaide	Sout~	Visiti~	0.435	0.452
5	5	Adelaide ~	Sout~	Busine~	0.464	0.179
6	6	Adelaide ~	Sout~	Holiday	0.528	0.296
7	7	Adelaide ~	Sout~	Other	0.593	0.404
8	8	Adelaide ~	Sout~	Visiti~	0.488	0.254
9	9	Alice Spr~	Nort~	Busine~	0.534	0.251
10	10	Alice Spr~	Nort~	Holiday	0.381	0.832

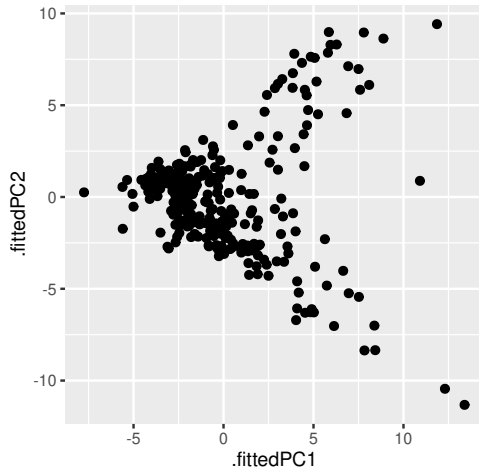
```
# i 294 more rows
```

```
# i 94 more variables: seasonal_peak_year <dbl>,  
# seasonal_trough_year <dbl>, spikiness <dbl>, linearity <dbl>,  
# curvature <dbl>, stl_e_acf1 <dbl>, stl_e_acf10 <dbl>, acf1 <dbl>,  
# acf10 <dbl>, diff1_acf1 <dbl>, diff1_acf10 <dbl>, diff2_acf1 <dbl>,  
# diff2_acf10 <dbl>, season_acf1 <dbl>, pacf5 <dbl>, diff1_pacf5 <dbl>,
```

Feature extraction and statistics

```
pcs |> ggplot(aes(x=.fittedPC1, y=.fittedPC2)) +  
  geom_point() + theme(aspect.ratio=1)
```

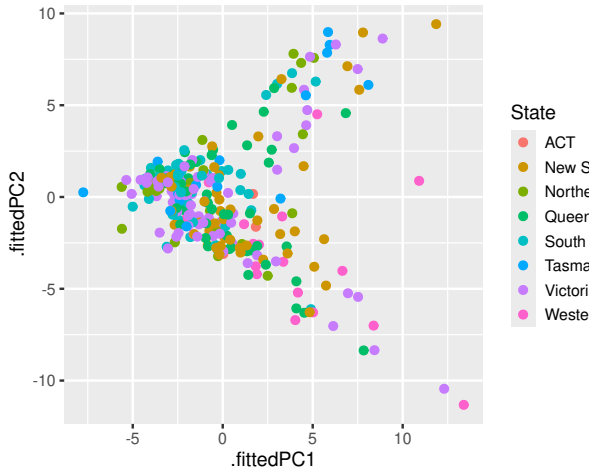
Principal
components based
on all features from
the feasts package



Feature extraction and statistics

```
pcs |> ggplot(aes(x=.fittedPC1, y=.fittedPC2, col=State)) +  
  geom_point() + theme(aspect.ratio=1)
```

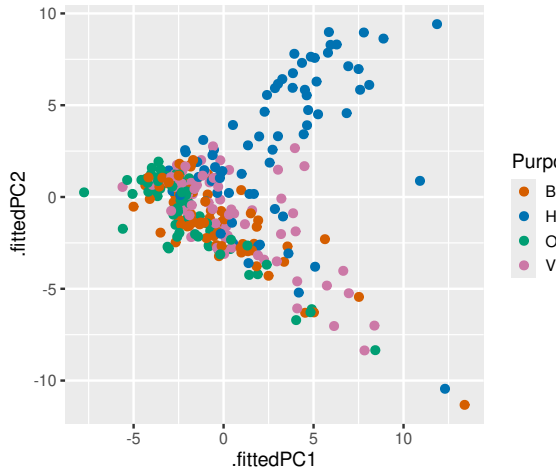
Principal
components based
on all features from
the feasts package



Feature extraction and statistics

```
pcs |> ggplot(aes(x=.fittedPC1, y=.fittedPC2, col=Purpose)) +  
  geom_point() + theme(aspect.ratio=1)
```

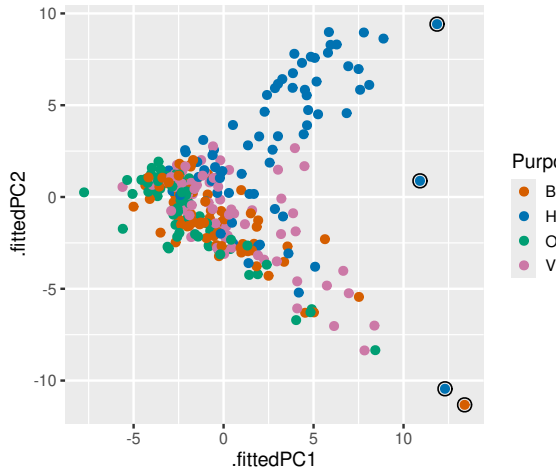
Principal
components based
on all features from
the feasts package



Feature extraction and statistics

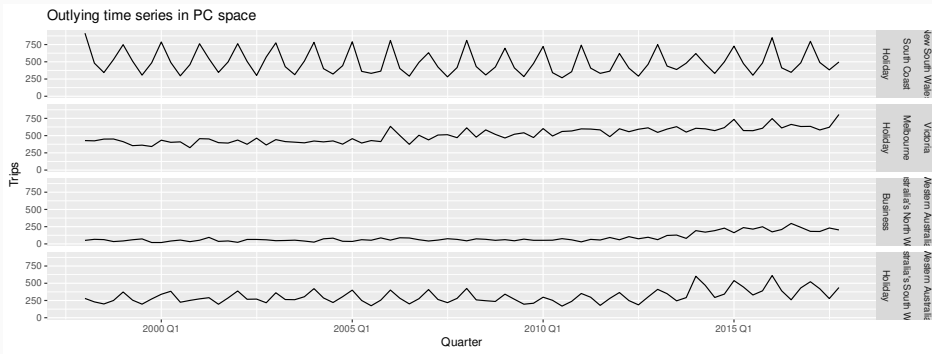
```
pcs |> ggplot(aes(x=.fittedPC1, y=.fittedPC2, col=Purpose)) +  
  geom_point() + theme(aspect.ratio=1)
```

Principal
components based
on all features from
the feasts package



Feature extraction and statistics

```
outliers |>
  left_join(tourism, by = c("State", "Region", "Purpose")) |>
  mutate(Series = glue("{State}", "{Region}", "{Purpose}", .sep = "\n\n")) |>
  ggplot(aes(x = Quarter, y = Trips)) +
  geom_line() + facet_grid(Series ~ .) +
  labs(title = "Outlying time series in PC space")
```



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Lab Session 10

- Use a feature-based approach to look for outlying series in PBS.
- What is unusual about the series you identify as outliers?