Support Vector Machines

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• Lecture

Pick the one with largest margin.

Separate line: (\vec{w} is perpendicular to this line)

$$\vec{w}^T \vec{x} + b = 0$$

Margin:

$$\gamma = \frac{2a}{||\vec{w}||}$$

Confidence:

$$(\vec{w}^T \vec{x}_i + b) y_i$$

Object function of SVM:

$$\max_{\vec{w},b} \gamma = \frac{2a}{||\vec{w}||}, \quad s.t. \ (\vec{w}^T \vec{x}_i + b) y_i \ge a, \ \forall \ i$$

or

$$\min_{\vec{w}} \vec{w}^T \vec{w}, \quad s.t. \ (\vec{w}\vec{x}_i + b)y_i \ge 1, \ \forall \ i$$

1 Support Vectors

Linear yperplane defined by "support vectors". Only need to store the support vectors to predict labels of new points.

2 Data is ont linearly separable

Not quadratic programming:

$$\min_{\vec{w}} \vec{w}^T \vec{w} + C \# mistakes, \quad s.t. \ (\vec{w}^T \vec{x}_i + b) y_i \ge 1, \ \forall \ i$$

C is a tradeoff parameter. Soft margin approach (QP):

$$\min_{\vec{w}} \vec{w}^T \vec{w} + C \sum_{j} \xi, \quad s.t. \ (\vec{w}^T \vec{x}_i + b) y_i \ge 1 - \xi_i \ \forall \ i$$

- ξ : slack variables = (ξ 1 if x_i misclassified)
- C: tradeoff parameter (chosen by cross-validation)

Hinge loss:

$$\xi_i = (1 - (\vec{w}^T \vec{x}_i + b) y_i)_+$$

Regularized hinge loss:

$$\min_{\vec{w}, b} \vec{w}^T \vec{w} + C \sum_{i} (1 - (\vec{w}^T \vec{x}_i + b) y_i)_{+}$$