

\*Note: Code was worked on independently

## Problem 1

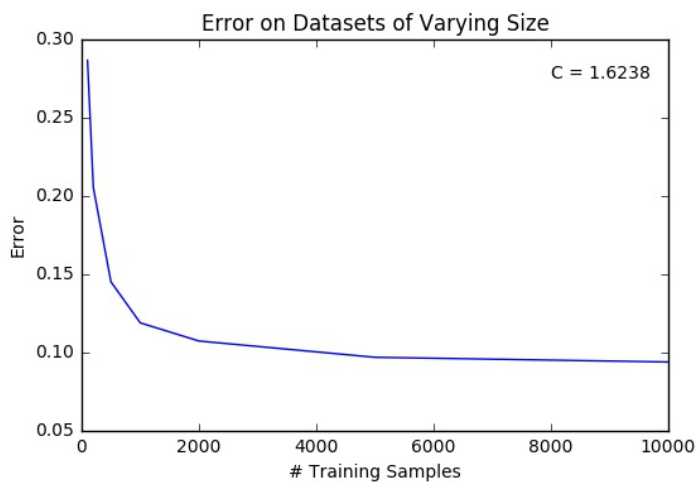
Data was partitioned as specified (10,000 validation images for MNIST, 20% as validation samples for spam, and 5,000 validation images for CIFAR-10). See code, provided in the appendix, for evidence. Partitioning was accomplished by calling the partition function defined in HW01\_utils.py module.

## Problem 2

The linear SVM was trained on all three datasets. The score (accuracy) of the method was calculated for a range of samples. For each data set—MNIST, spam, and CIFAR-10—the error (error = 1-accuracy) is plotted as a function of  $N$  samples used for training.

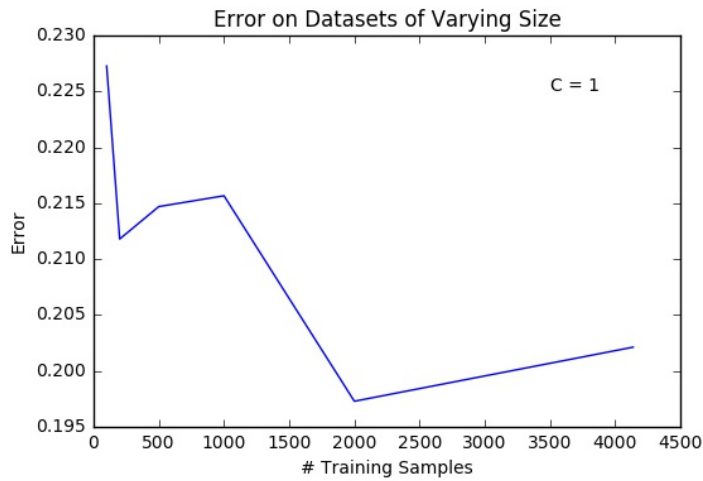
### MNIST

Accuracy of MNIST training for 100, 200, 500, 1,000, 2,000, 5,000, and 10,000 training samples.



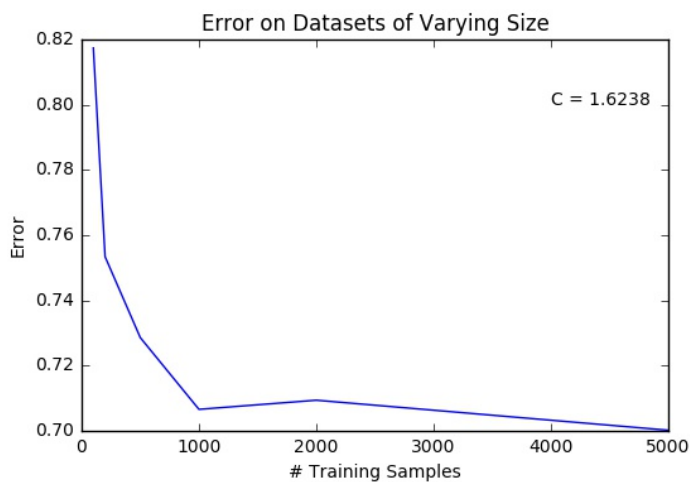
## Spam

Accuracy of spam/ham training for 100, 200, 500, 1,000, 2,000, and all (4,132) training samples.



## CIFAR-10

Accuracy of CIFAR-10 training for 100, 200, 500, 1,000, 2,000, and 5,000 training samples.



## Problem 3

For the MNIST data set, the best value of  $C$  was found to be  $7.84759970351 \times 10^{-7}$ , giving an accuracy of 92.98%. All accuracies for a range of  $C$  values (all trained on 10,000 samples) are given below.

### 10,000 samples

| C                 | Accuracy      |
|-------------------|---------------|
| 1.0000E-08        | 0.8935        |
| 4.2813E-08        | 0.9147        |
| 1.8330E-07        | 0.9255        |
| <b>7.8476E-07</b> | <b>0.9298</b> |
| 3.3598E-06        | 0.9229        |
| 1.4384E-05        | 0.9118        |
| 6.1585E-05        | 0.9071        |

|            |       |
|------------|-------|
| 2.6367E-04 | 0.906 |
| 0.0011288  | 0.906 |
| 0.0048329  | 0.906 |
| 0.0206914  | 0.906 |
| 0.0885867  | 0.906 |
| 0.3792690  | 0.906 |
| 1.6237767  | 0.906 |
| 6.9519280  | 0.906 |
| 29.763514  | 0.906 |
| 127.42750  | 0.906 |
| 545.55948  | 0.906 |
| 2335.7215  | 0.906 |
| 10000.0    | 0.906 |

Full results for all sample counts are provided in the appendix.

## Problem 4

For the spam/ham data sets, best value of  $C$  was found to be 100, giving an accuracy of 80.75%. This value was found using a K-Fold Cross-Validation scheme where  $k = 5$ . Below are all accuracies for a range of  $C$  values when the SVM was trained on 2,000 samples.

### 2,000 samples

| <b>C</b>     | <b>Accuracy</b> |
|--------------|-----------------|
| 1.0000E-08   | 0.710058        |
| 3.3598E-08   | 0.710058        |
| 1.1288E-07   | 0.710058        |
| 3.7927E-07   | 0.710058        |
| 1.2743E-06   | 0.710058        |
| 4.2813E-06   | 0.710058        |
| 1.4384E-05   | 0.710058        |
| 4.8329E-05   | 0.710058        |
| 0.00016238   | 0.717215        |
| 0.00054556   | 0.734429        |
| 0.00183298   | 0.750097        |
| 0.00615848   | 0.768279        |
| 0.02069138   | 0.779304        |
| 0.06951928   | 0.793617        |
| 0.23357215   | 0.8             |
| 0.78475997   | 0.802515        |
| 2.63665090   | 0.804836        |
| 8.85866790   | 0.805029        |
| 29.7635144   | 0.807350        |
| <b>100.0</b> | <b>0.807544</b> |

## Problem 5

My Kaggle Leaderboard name: **mitch**

My Kaggle username: **mnegus**

### Kaggle Scores:

MNIST: 0.93360

Spam: 0.84085

# Appendix

Below are all accuracies tabulated for tested range of hyperparameter C for  $N$  training samples.

Table 1: **MNIST**

| $N \setminus C$ | 1E-08    | 4E-08    | 1.8E-07  | 7.8E-07  | 3.36E-06 | 1.44E-05 | 6.16E-05 | 0.000264 | 0.001129 | 0.004833 |
|-----------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 100             | 0.1119   | 0.2301   | 0.6438   | 0.7169   | 0.7133   | 0.7133   | 0.7133   | 0.7133   | 0.7133   | 0.7133   |
| 200             | 0.0963   | 0.425    | 0.7747   | 0.8005   | 0.7947   | 0.7947   | 0.7947   | 0.7947   | 0.7947   | 0.7947   |
| 500             | 0.3171   | 0.7527   | 0.865    | 0.8635   | 0.8552   | 0.8548   | 0.8548   | 0.8548   | 0.8548   | 0.8548   |
| 1000            | 0.5782   | 0.85     | 0.8867   | 0.8909   | 0.8815   | 0.881    | 0.881    | 0.881    | 0.881    | 0.881    |
| 2000            | 0.7981   | 0.8824   | 0.9043   | 0.9086   | 0.895    | 0.8926   | 0.8926   | 0.8926   | 0.8926   | 0.8926   |
| 5000            | 0.8721   | 0.9038   | 0.9183   | 0.9202   | 0.9135   | 0.9041   | 0.903    | 0.903    | 0.903    | 0.903    |
| 10000           | 0.8935   | 0.9147   | 0.9255   | 0.9298   | 0.9229   | 0.9118   | 0.9071   | 0.906    | 0.906    | 0.906    |
| <hr/>           |          |          |          |          |          |          |          |          |          |          |
| $N \setminus C$ | 0.020691 | 0.088587 | 0.379269 | 1.623777 | 6.951928 | 29.76351 | 127.4275 | 545.5595 | 2335.721 | 10000    |
| 100             | 0.7133   | 0.7133   | 0.7133   | 0.7133   | 0.7133   | 0.7133   | 0.7133   | 0.7133   | 0.7133   | 0.7133   |
| 200             | 0.7947   | 0.7947   | 0.7947   | 0.7947   | 0.7947   | 0.7947   | 0.7947   | 0.7947   | 0.7947   | 0.7947   |
| 500             | 0.8548   | 0.8548   | 0.8548   | 0.8548   | 0.8548   | 0.8548   | 0.8548   | 0.8548   | 0.8548   | 0.8548   |
| 1000            | 0.881    | 0.881    | 0.881    | 0.881    | 0.881    | 0.881    | 0.881    | 0.881    | 0.881    | 0.881    |
| 2000            | 0.8926   | 0.8926   | 0.8926   | 0.8926   | 0.8926   | 0.8926   | 0.8926   | 0.8926   | 0.8926   | 0.8926   |
| 5000            | 0.903    | 0.903    | 0.903    | 0.903    | 0.903    | 0.903    | 0.903    | 0.903    | 0.903    | 0.903    |
| 10000           | 0.906    | 0.906    | 0.906    | 0.906    | 0.906    | 0.906    | 0.906    | 0.906    | 0.906    | 0.906    |

Table 2: **Spam**

| $N \setminus C$ | 1E-08    | 3E-08    | 1.1E-07  | 3.8E-07  | 1.27E-06 | 4.28E-06 | 1.44E-05 | 4.83E-05 | 0.000162 | 0.000546 |
|-----------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 100             | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.709865 | 0.710445 | 0.710638 |
| 200             | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710251 | 0.711025 |
| 500             | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.713926 |
| 1000            | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.711412 | 0.725725 |
| 2000            | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.717215 | 0.734429 |
| 4138            | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.710058 | 0.712186 | 0.725338 | 0.743327 |
| <hr/>           |          |          |          |          |          |          |          |          |          |          |
| $N \setminus C$ | 0.001833 | 0.006158 | 0.020691 | 0.069519 | 0.233572 | 0.78476  | 2.636651 | 8.858668 | 29.76351 | 100      |
| 100             | 0.711605 | 0.716828 | 0.728433 | 0.74236  | 0.754932 | 0.770406 | 0.777756 | 0.786074 | 0.775629 | 0.781044 |
| 200             | 0.716441 | 0.730174 | 0.745261 | 0.758801 | 0.767892 | 0.782592 | 0.789555 | 0.798066 | 0.792456 | 0.786847 |
| 500             | 0.731141 | 0.745261 | 0.763636 | 0.77176  | 0.783172 | 0.791876 | 0.793424 | 0.793037 | 0.792456 | 0.792456 |
| 1000            | 0.741199 | 0.761896 | 0.7706   | 0.784139 | 0.790135 | 0.792843 | 0.797099 | 0.798646 | 0.79942  | 0.798453 |
| 2000            | 0.750097 | 0.768279 | 0.779304 | 0.793617 | 0.8      | 0.802515 | 0.804836 | 0.805029 | 0.80735  | 0.807544 |
| 4138            | 0.763056 | 0.774855 | 0.789362 | 0.794971 | 0.79942  | 0.801354 | 0.802128 | 0.802901 | 0.802708 | 0.802515 |

Table 3: **CIFAR-10**

| $N \setminus C$ | 1E-08    | 4E-08    | 1.8E-07  | 7.8E-07  | 3.36E-06 | 1.44E-05 | 6.16E-05 | 0.000264 | 0.001129 | 0.004833 |
|-----------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 100             | 0.111    | 0.1658   | 0.1834   | 0.1838   | 0.1826   | 0.1826   | 0.1826   | 0.1826   | 0.1826   | 0.1826   |
| 200             | 0.1026   | 0.2272   | 0.2622   | 0.2466   | 0.2466   | 0.2466   | 0.2466   | 0.2466   | 0.2466   | 0.2466   |
| 500             | 0.2202   | 0.295    | 0.3008   | 0.2842   | 0.2708   | 0.2714   | 0.2714   | 0.2714   | 0.2714   | 0.2714   |
| 1000            | 0.2632   | 0.3164   | 0.3306   | 0.3148   | 0.2934   | 0.2934   | 0.2934   | 0.2934   | 0.2934   | 0.2934   |
| 2000            | 0.3      | 0.3476   | 0.345    | 0.321    | 0.3016   | 0.291    | 0.2906   | 0.2906   | 0.2906   | 0.2906   |
| 5000            | 0.353    | 0.3736   | 0.3752   | 0.3518   | 0.3216   | 0.3066   | 0.2992   | 0.2998   | 0.2998   | 0.2998   |
| $N \setminus C$ | 0.020691 | 0.088587 | 0.379269 | 1.623777 | 6.951928 | 29.76351 | 127.4275 | 545.5595 | 2335.721 | 10000    |
| 100             | 0.1826   | 0.1826   | 0.1826   | 0.1826   | 0.1826   | 0.1826   | 0.1826   | 0.1826   | 0.1826   | 0.1826   |
| 200             | 0.2466   | 0.2466   | 0.2466   | 0.2466   | 0.2466   | 0.2466   | 0.2466   | 0.2466   | 0.2466   | 0.2466   |
| 500             | 0.2714   | 0.2714   | 0.2714   | 0.2714   | 0.2714   | 0.2714   | 0.2714   | 0.2714   | 0.2714   | 0.2714   |
| 1000            | 0.2934   | 0.2934   | 0.2934   | 0.2934   | 0.2934   | 0.2934   | 0.2934   | 0.2934   | 0.2934   | 0.2934   |
| 2000            | 0.2906   | 0.2906   | 0.2906   | 0.2906   | 0.2906   | 0.2906   | 0.2906   | 0.2906   | 0.2906   | 0.2906   |
| 5000            | 0.2998   | 0.2998   | 0.2998   | 0.2998   | 0.2998   | 0.2998   | 0.2998   | 0.2998   | 0.2998   | 0.2998   |

Included on the following pages is the code used for this project: namely the 3 Jupyter notebooks and 2 python modules: