

CS289A_HW03_Prob3

February 27, 2017

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In [121]: import random
import numpy as np
from matplotlib import pyplot as plt

In [122]: def PlotWithArrows(X,Y,arrowwidth,xmin,xmax,ymin,ymax,figname=None):
    # Generate scatter plot of points (X,Y), with arrows representing the eig
    # of the covariance matrix, with lengths of the corresponding eigenvalues

    mu = np.array([np.mean(X),np.mean(Y)])
    Sigma = np.cov(X,Y)
    eigvals, eigvecs = np.linalg.eig(Sigma)

    # Adjust eigenvector arrows to have length of eigenvalue
    arrow1lenx,arrow1leny = eigvals[0]*eigvecs[0,0],eigvals[0]*eigvecs[0,1]
    arrow2lenx,arrow2leny = eigvals[1]*eigvecs[1,0],eigvals[1]*eigvecs[1,1]

    fig1 = plt.figure(figsize=(10,10))
    plt.scatter(X,Y)
    plt.arrow(mu[0],mu[1],arrow1lenx,arrow1leny,width=arrowwidth)
    plt.arrow(mu[0],mu[1],arrow2lenx,arrow2leny,width=arrowwidth)
    plt.xlim(xmin,xmax)
    plt.ylim(ymin,ymax)
    if figname:
        plt.savefig(figname)
    plt.show()

In [123]: # Draw N 2-dimensional points from X1 and X2 given:
    #      X1 ~ N(3,9)    and    X2 ~ N(4,4)
    # *here, N(u,s) is a normal distribution with mean u and variance s

    N = 100
    points = np.empty((100,2))
    for i in range(N):
        x1 = random.gauss(3,3)
        x2 = 0.5*x1+random.gauss(4,2)
        points[i] = [x1,x2]
    X1 = points[:,0]
    X2 = points[:,1]
```

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In [124]: # (3a) Calculate the mean of the sample
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mu = np.mean(points,axis=0)
print(mu)
```

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[ 3.18273256  5.09248548]
```

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In [125]: # (3b) Compute the 2x2 covariance matrix
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Sigma = np.cov(X1,X2)
print(Sigma)
```

```
[[ 8.4943665  4.52103804]
 [ 4.52103804  7.18995243]]
```

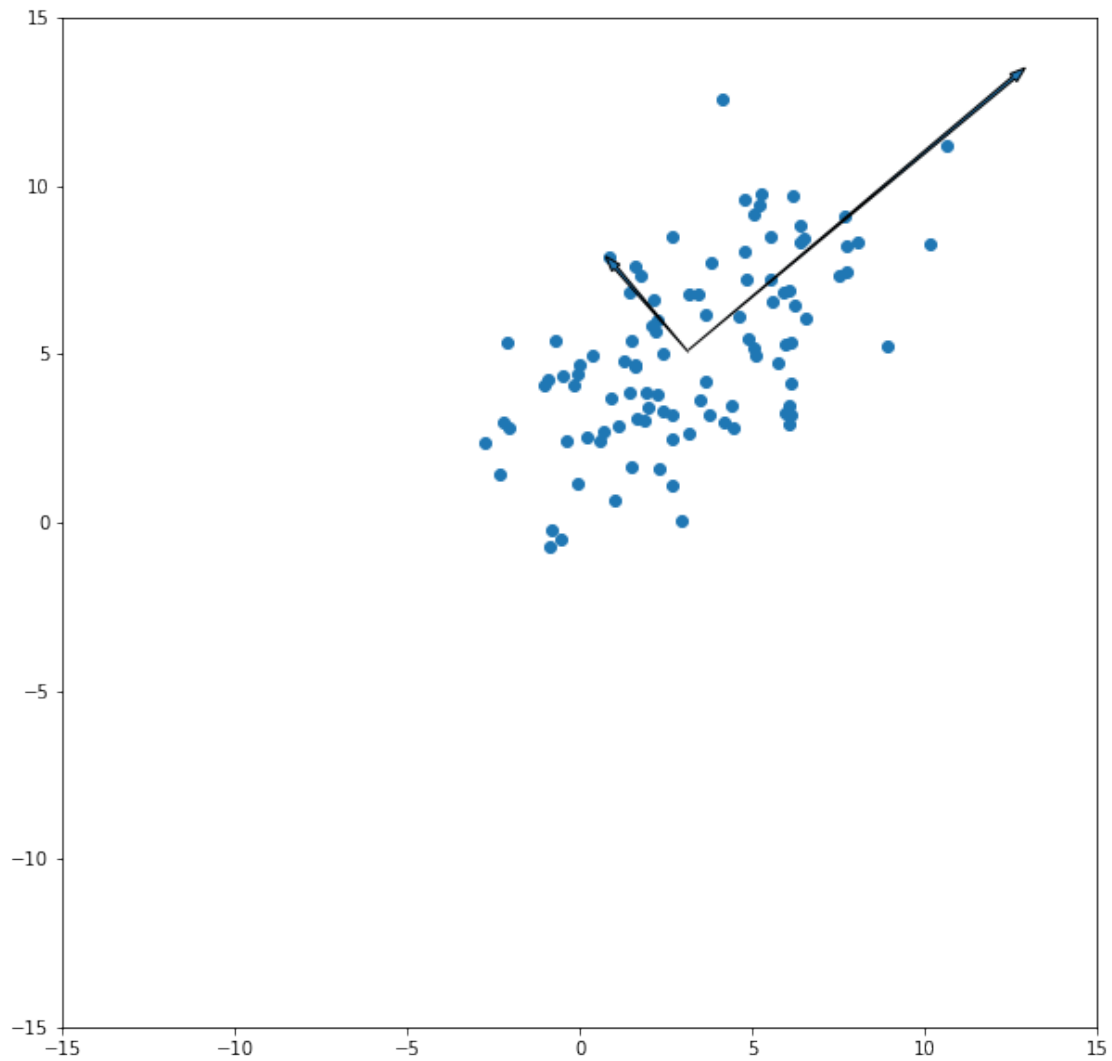
```
In [126]: # (3c) Compute the eigenvectors and eigenvalues of this covariance matrix
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eigvals, eigvecs = np.linalg.eig(Sigma)
print(eigvals)
print(eigvecs)
```

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[ 12.4099991  3.27431983]
[[ 0.75590422 -0.65468222]
 [ 0.65468222  0.75590422]]
```

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In [127]: # (3d) Plot data points on grid, with arrows representing covariance eigen
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```
PlotWithArrows(X1,X2,0.1,-15,15,-15,15,"HW03_prob3d.jpg")
```



In [128]: # (3e) Plot data points on grid, with arrows representing covariance eigen

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if eigvals[0] >= eigvals[1]:
    U = eigvecs
else:
    U = eigvecs[:,::-1]
centeredpoints = points - mu*np.ones_like(points)
rotatedpoints = np.empty_like(centeredpoints)
for i in range(len(rotatedpoints)):
    rotatedpoints[i] = np.dot(U.T,centeredpoints[i])
Y1 = rotatedpoints[:,0]
Y2 = rotatedpoints[:,1]

PlotWithArrows(Y1,Y2,0.1,-15,15,-15,15,"HW03_prob3e.jpg")

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