

# Nuclear Engineering 150 – Discussion Section

## Team Exercise Solutions #3

### Problem 1

A reactor is operating for a long time at some known power density  $P_0$ . Then, it instantaneously changes power to some power density  $P_1$ . One fission product of interest is  $^{135}\text{Xe}$ , though it has a negligible yield from the initial fission reaction.  $^{135}\text{Xe}$  precursors  $^{135}\text{Te}$  and  $^{135}\text{I}$  are produced with a combined yield of approximately 6%, before decaying via  $\beta^-$  decay to  $^{135}\text{I}$  and  $^{135}\text{Xe}$  respectively. Find the number density of  $^{135}\text{Xe}$  as a function of time after the power change. Let  $Q_f$  be the energy produced per fission, approximately 200 MeV.

Nucleus	Half-life	Thermal $\sigma_a$
$^{135}\text{Te}$	19.0 s	$\sim 0$
$^{135}\text{I}$	6.6 hr	$\sim 0$
$^{135}\text{Xe}$	9.2 hr	$2.6 \times 10^6$ barns

### Problem 1 Solution

We will create the following simple decay chain graphic, built from the information provided in the problem, to visualize the processes described in the problem.

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Starting off, since this is a problem related to decay, we will start from the usual equation for changes in a quantity of radionuclides.

$$\frac{dN}{dt} = \text{production} - \text{losses}$$

First, we find the neutron production. We are told that after the transition, the reactor is now generating with power density  $P_1$ .

The amount of  $^{135}\text{Xe}$  is dependent on its parents,  $^{135}\text{Te}$  and  $^{135}\text{I}$ . Since the half-life of  $^{135}\text{Te}$  (19.0 s) is practically insignificant in comparison to the multi-hour half-lives of its daughters (to be exact,  $T_{1/2, \text{Te}135} = 0.08 T_{1/2, \text{I}135}$  and  $T_{1/2, \text{Te}135} = 0.06 T_{1/2, \text{Xe}135}$ ), we can treat it as instantaneously decaying into iodine.

Now, we can recognize

## Problem 2

*Text of problem 2*

## Problem 2 Solution