The nature of the semantic stimulus: the acquisition of *every* as a case study*

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Abstract

We evaluate the richness of the child's input in semantics, and our case study is the acquisition of the universal quantifier *every*. We report two main findings on the basis of a corpus study of child-directed and child-ambient speech. Our first finding is that the input in semantics (as opposed to the input in syntax or phonology) is rich enough to systematically eliminate instances of the subset problem of language acquisition: overly general hypotheses about the meaning of *every* can violate pragmatic constraints, making such hypotheses inconsistent with the child's input. Our second finding is that the semantic input is too poor to eliminate instances of the superset problem, the mirror image of the subset problem. We use a quantificational analog of Goodman's *grue* predicate to claim that at least some overly specific hypotheses about the meaning of *every* are consistent with the child's input, suggesting either that those hypotheses are not made available by UG or that non-trivial inductive biases are involved in children's acquisition of *every*.

1 Introduction

As part of language acquisition, the child needs to make sense of unanalyzed input: she brings to the task a space of possible grammars, and she chooses a

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grammar in that space that can generate the input. If two conceivable grammars G, G' are compatible with the input and the child ends up selecting G, we can draw interesting conclusions regarding learning. It could be, for example, that G' is outside of the child's hypothesis space, or that the child is biased towards choosing G over G'. The literature on acquisition in syntax and phonology has identified cases where multiple grammars are compatible with the input, suggesting that learning in those domains is non-trivial.

Consider, for example, the so-called *that-trace effects* in English discovered by Perlmutter (1971) and discussed in the context of acquisition by Chomsky and Lasnik (1977). A *wh*-question in English can be formed by extracting an object out of an embedded clause regardless of whether the complementizer *that* is pronounced (1), while subject extraction is only possible without a pronounced complementizer (2).

- (1) Object extraction is possible with or without an overt complementizer
 - a. Who do you think Michelle met _?
 - b. Who do you think **that** Michelle met _?
- (2) Subject extraction is only possible without an overt complementizer
 - a. Who do you think _ met Michelle?
 - b. *Who do you think **that** _ met Michelle?

Negative evidence directly informing the English-learning child that (2b) is not part of the language is unavailable. Nevertheless, the child prefers a grammar that does not generate (2b) over a more permissive grammar G' that does generate it, given in (3), an instance of the so-called *subset problem* of language acquisition.

- (3) a. G =the grammar of English
 - b. G' = generates (2b) in addition to whatever G generates

This instance of the subset problem could suggest, for example, that G' is not part of the hypothesis space (at least before we consider the behavior of that-trace effects in other languages). Alternatively, if both G and G' are in the child's hypothesis space, this instance of the subset problem would teach us that the null theory of language acquisition, according to which learning is trivial and involves no induction – is incorrect. A version of this null theory is given in (4). It presupposes that there is exactly one grammar in the hypothesis space that is consistent with the child's input, and it states that the child simply selects that grammar.

(4) Null theory of language acquisition (to be updated below in (16)) The child selects the (only) hypothesis compatible with the input

If both G and G' are in the child's hypothesis space, the null theory would not be able to explain why the child selects G over G' (more generally, the null theory fails whenever two grammars in the hypothesis space are compatible with the input). Instead, the fact that the child selects G in the face of an available alternative would support a more complex theory of language acquisition where some bias guides the learner towards G over the more permissive G'. Since (4) is a simple – in fact, trivial – theory of language acquisition, rejecting it in favor of a more complex theory is an interesting discovery about language acquisition. Other instances of the subset problem have been discussed by Dell (1981), Berwick (1985), Wexler and Manzini (1987), Crain et al. (1994), and Prince and Tesar (2004), among others.

Here is another syntactic example from English, which presents the mirror image of the subset problem. English *wh*-questions can be formed by extracting direct objects out of unboundedly many embedded clauses, as illustrated in (5a)-(5b). The child never hears questions like (5b), in which an object has been extracted out of multiple embedded clauses (at least not beyond a certain degree of embedding, which for the sake of discussion we will assume is two). Nevertheless, adult speakers judge sentences like (5b) as grammatical.

- (5) Object extraction is possible out of unboundedly many embedded clauses
 - a. Who do you think **that** Michelle met _?
 - b. Who do you think **that** Michelle said **that** Bill believes **that** John met _?

In this case, the English-learning child draws a generalization and converges on a grammar that is more permissive than a conceivable alternative: a grammar G' that only allows extraction out of a limited number of embedded clauses, given in (6). This state of affairs could teach us that G' is not part of the hypothesis space or that the null theory of language acquisition in (4) is incorrect; instead, the correct theory of acquisition includes a learning bias in favor of the grammar of English over the grammar G' which generates fewer sentences. We will refer to the problem of converging on a more permissive grammar as the *superset problem* of acquisition, to highlight the symmetry between this problem and the more familiar subset problem.

¹Its simplicity can be measured, for example, by the amount of characters required to implement it as a Python program.

- (6) a. G =The grammar of English
 - b. G' = Can generate whatever G generates except for sentences with object extraction out of more than two embedded clauses.

In this paper we will construct and evaluate candidates for similar learning problems in semantics and discuss their implications for the hypothesis space in semantics and for the null theory of acquisition in (4) as a potential theory of semantic acquisition. Our case study is the acquisition of the universal quantifier *every*. As we will see, acquiring the meaning of *every* faces a version of the subset problem whenever alternative meanings that are logically weaker than the universal quantifier would be consistent with the input, whereas alternative, logically-stronger meanings pose a version of the superset problem.

Consider first a simple candidate for a subset problem in the acquisition of *every*, introduced by Piantadosi et al. (2012). To simplify the discussion, we will assume that the adult's meaning of *every* is the one in (7): a function that takes two sets as arguments and presupposes its first argument to be non-empty. [[every]] returns True if the first argument (the restrictor) is a subset of the second argument (the scope). Consider also the alternative denotation for *every* in (8) – the set representation of the existential quantifier – which takes two sets and returns True if their intersection is non-empty. We will refer to this alternative as [[every]].

- (7) $\|every\| = \lambda P : |P| > 0.\lambda O.P \subseteq O$
- (8) $\llbracket every_{\exists} \rrbracket = \lambda P.\lambda Q.P \cap Q \neq \emptyset$ (= $\llbracket some \rrbracket$)

The desired universal [[every]] asymmetrically entails the existential [[every]]. This means that in many contexts, the usage of the universal quantifier by a caregiver would be consistent with the existential meaning, but not the other way around, as illustrated by (9)-(10).

- (9) Context: five out of five girls ran
 - a. Every girl ran (True)
 - b. Some girl ran (True)
- (10) Context: three out of five girls ran
 - a. Some girl ran (True)
 - b. Every girl ran (False)

For the child acquiring the meaning of the English word *every*, the challenge would be to converge on a meaning whose extension is a subset of that of an alternative meaning:

(11) A potential subset problem in the acquisition of every:² $[[every]] \subset [[every]]$

If $\llbracket every_{\exists} \rrbracket$ is consistent with the input available to the English-learning child, the fact that the child converges on $\llbracket every \rrbracket$ could suggest that the null theory of acquisition in (4) is not the right theory of quantifier learning and that the child is instead biased in favor of the grammar of English which includes $\llbracket every_{\exists} \rrbracket$ (along-side *some*) over a grammar G' that includes $\llbracket every_{\exists} \rrbracket$:

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(12) a. G = \text{The grammar of English:}

• \llbracket some \rrbracket = \lambda P.\lambda Q.P \cap Q \neq \emptyset

• \llbracket every \rrbracket = \lambda P : P \neq \emptyset.\lambda Q.P \subseteq Q

• \cdots

b. G' =

• \llbracket some \rrbracket = \lambda P.\lambda Q.P \cap Q \neq \emptyset

• \llbracket every_{\exists} \rrbracket = \lambda P.\lambda Q.P \cap Q \neq \emptyset
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Learning biases that could push the child towards G (and towards [[every]] over [[every]]) have been previously proposed in the literature. They include the principle of contrast (Clark 1987), the Semantic Subset Principle (Crain et al. 1994), and the likelihood component of Bayesian inference (Piantadosi et al. 2012). If it turns out that [[every]] is not consistent with the child's input, the subset problem would not arise in this case and the null theory of acquisition in (4) could be maintained as a theory of quantifier learning without the complication of additional learning biases.³

Does the subset problem indeed arise in this case and supports the rejection of (4) in favor of a theory with additional learning biases? The answer depends on whether $[[every_3]]$ is in fact consistent with usages of every in the child's input. In our discussion above of the subset problem in syntax, we mentioned that parents do not tend to correct their children for grammaticality, making both the English grammar and a more permissive alternative consistent with the input. It has already been pointed out, however, that the input in semantics is quite different

²Here and below we use $[Q_1] \subset [Q_2]$ as shorthand for: $\forall P$. $[Q_1](P) \subset [Q_2](P)$.

³Certain biases have been proposed for other learning problems in semantics – see, for example, Markman (1990), Landau et al. (1988), Markman et al. (2003), and Xu and Tenenbaum (2007). In this paper we focus on the problem of quantifier learning and leave aside other learning problems and their consequences for theories of learning.

from the input in syntax. For example, while parents do not tend to correct their children for grammaticality, they do object to false statements made by children (Brown and Hanlon 1970). Direct objections are one kind of input that can provide the child with direct evidence against [[every]], but it remains an open question whether relevant objections or other kinds of informative input are systematically available to the child.

We address this question in section 2, where we examine whether the semantic input is rich enough to rule out [[every]]] as an alternative to [[every]] and eliminate this instance of the subset problem. We will first consider truth-conditional evidence that can rule out [every] – i.e., caregiver utterances that would be false if the intended [[every]] were replaced with [[every]] – and conclude that such evidence is not systematically present in the child's input. Importantly, however, we will show that pragmatic input changes the picture. Our main finding reported in section 2 is that the child is systematically exposed to utterances that would violate some pragmatic constraint on the assumption that every has the existential meaning but not on the assumption that it has the universal meaning. An example is the question in (13a), uttered in a context where a variant of the question with an existential quantifier would be odd (this example and others will be discussed in more detail in section 2). If the child is able to use such input to conclude that $\llbracket every_{\exists} \rrbracket$ is an inappropriate meaning for every, no special learning biases would be needed to push the child away from [[every]] towards [[every]] and the null theory of acquisition in (4) would be sufficient in this case.

- (13) Context: somebody has arrived
 - a. Is everybody here?
 - b. #Is anybody here?

After discussing the subset problem in section 2, we turn to the superset problem in section 3. An example of a potential superset problem in the acquisition of *every* is provided by the quantifier in (14). This quantifier is a variant of the universal quantifier with a stronger presupposition that requires its restrictor to have a cardinality greater than 2 (rather than just be non-empty).

(14)
$$\|[every_{>2}]\| = \lambda P : |P| > 2.\lambda Q.P \subseteq Q$$

[[every>2]] is logically stronger than [[every]], meaning that the extension of [[every]] is a superset of the extension of [[every>2]]. If [[every>2]] is consistent with the child's input, we have an instance of the superset problem of acquisition, since the English-learning child ends up selecting the superset meaning [[every]]:

(15) A potential superset problem in the acquisition of *every*: $[every_{>2}] \subset [every]$

In section 3 we draw a connection between quantifiers like (14) and Goodman's (1955) *grue* predicate, which he used to illustrate what he referred to as the "New Riddle of Induction". By examining the English-learning child's input, our main finding reported in section 3 is that there is no systematic evidence against quantifiers like $[every_{>2}]$ as a meaning for *every*, posing a superset problem of induction for the English-learning child.

1.1 General methodology

To investigate whether the child's input contains negative evidence against competing hypotheses about the meaning of *every*, we used the Manchester corpus in CHILDES (Theakston et al. 2001, MacWhinney 2000). The Manchester corpus consists of transcripts of audio recordings from 12 British-English-speaking children, collected over a period of one year. Children were roughly two years old at the beginning of the study and three years old at the end. The transcripts record conversations during normal play activities between the children and their mothers.

We extracted all tokens of *every* in child-directed and child-ambient speech as well as child speech and examined each utterance with *every* in context (up to 50 lines of preceding discourse and 5 following).⁴ We included occurrences of *every* as parts of other words, such as *everything*, *everyone*, and *everybody*, on the assumption that these are complex words which contain the lexical item *every*, and we excluded occurrences of quantifiers like *all* and *each*, on the assumption that these are distinct lexical items whose denotation needs to be learned separately. We coded each child utterance with *every* for whether the use of *every* elicited explicit negative feedback from the caregiver. We coded each caregiver utterance with *every* for whether it contributes negative evidence of two types – truth-conditional evidence and pragmatic evidence – according to specific criteria that will be described in more detail in the following sections. All utterances were coded independently by the two authors, with 90% inter-coder reliability.

Figures 1 and 2 show the frequency of *every* relative to the total number of words produced by each speaker per corpus. The y-axes show relative frequency

⁴As is standard, we exclude from the counts full or partial repetitions and clearly rote or formulaic expressions.

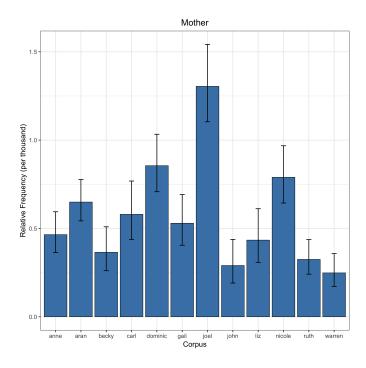


Figure 1: The relative frequency of *every* in the speech of mothers. 95% binomial proportion confidence intervals calculated using Agresti-Coull's approximate method

per thousand words. As the figures make plain, across corpora, *every* was infrequent in both caregiver speech (746 out of 339,713 utterances overall) and child speech (72 out of 224,795 utterances overall). Given that the spontaneous speech samples in the corpus represent only around 1-2% of the language the child hears and produces during the sampling period, the question arises whether the findings from the sample are in fact true to the child's actual experience (see Tomasello and Stahl 2004 for discussion). Throughout the paper we will assume that the sample size for parent speech is big enough to make the corpus representative in terms of the frequency of occurrences. We provide binomial-proportion confidence intervals along with our reported frequencies to support this assumption.⁵ The conclusions to be drawn from child speech are more limited as the relevant occurrences are extremely sparse.

Our starting point for evaluating of the availability of negative evidence against

⁵Unless otherwise specified, these are 95% confidence intervals calculated using Agresti-Coull's approximate method.

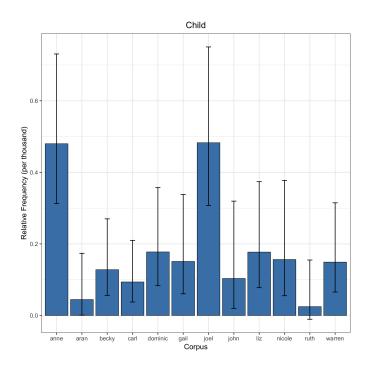


Figure 2: The relative frequency of *every* in the speech of children. 95% binomial proportion confidence intervals calculated using Agresti-Coull's approximate method

competing meanings for *every* was the null theory of learning in (4). This theory is an idealization which ignores issues like the presence of noise in the input, i.e., ungrammatical utterances made by the caregivers. As noted by Marcus (1993), if the input includes some amount of noise, the learner must be able to select grammars that are inconsistent with a small percentage of the input, so in order for negative evidence to be informative for the child it has to be *systematically available*. Suppose, for example, that the learner can simply ignore 2% of the input as noise. Then a slight modification of the null theory which deals with noise will be as follows:

(16) Null theory of language acquisition (updated from (4))The child selects the (only) hypothesis compatible with at least X% of the input.X = 98.

The theory of language acquisition in (16) remains a simple, idealized and trivial theory that says that language acquisition involves no real induction but rather simply a selection of the single hypothesis compatible with the evidence, up to some noise. Evidence against this theory, as has been found in syntax and phonology, would constitute meaningful progress in our understanding of language acquisition in the domain of quantifier learning. Exactly how much noise the child can ignore and exactly what percentage of the evidence counts as systematic is an open and interesting question that we will have nothing to say about in this paper. Instead, our goal will be to evaluate the null theory of language acquisition in (16) as a theory of acquisition in the domain of quantifier learning, assuming the number 98% as a rough approximation, i.e., assuming that negative evidence for ruling out an hypothesis must constitute at least 2% of the input. In the remainder of this paper, whenever we discuss the systematicity of negative evidence and its ability to rule out competing hypotheses about the meaning of every, we will be assuming the theory in (16). The conclusions that we draw in the following sections do not rely on the precise number 2%. In particular, the one case of negative evidence we considered to be systematic concerned 17.5% (131/746) informative utterances with negative evidence, and the three cases of negative evidence we considered to be non-systematic concerned 1.75% (13/746) or less of the utterances (we will discuss these numbers again in the respective sections in the context of our specific findings). Of course, the significance of our conclusions will be low if future research discovers that children require different amounts of negative evidence to rule out the alternative hypotheses about the meaning of every that we will consider.

1.2 Related work

To our knowledge, there has been little work on the nature of the stimulus in formal semantics, and the work that does exist has focused on learning problems that are quite different from the ones we are interested in here. In particular, we know of no prior work on the relationship between the semantic stimulus and the hypothesis space for quantifier meanings. Crain et al. (1994) and Gualmini and Schwarz (2009) discuss the evidence available to the child in the process of deciding between multiple interpretations of ambiguous quantificational statements (rather than the process of acquiring lexical entries for quantifiers). The literature on syntactic bootstrapping (Gleitman 1990 *et seq.*) has focused on word-learning problems in which syntactic context can provide helpful evidence for the child when deciding between competing hypotheses. The learning problems we discuss in this paper are meaningfully different in that they all involve choices between competitors for which the syntax is fixed (for example, syntactic context cannot help decide between [[every]]] and [[every>2]] since the two would have an identical syntactic distribution).

More closely related to our goals in this paper, Hacquard and Lidz (2019) discuss the evidence available to the child when acquiring the meaning of attitude predicates like *think* and *want*. They propose that in addition to syntactic context, the child's ability to understand speakers' intended speech acts (e.g., identify a request) can help the child to learn the meaning of attitude predicates. Differently from the problems discussed by Hacquard and Lidz, such abilities will not help the child in the cases we consider. Similarly to Hacquard and Lidz, however, we will conclude that pragmatic evidence can play an important role in semantic acquisition (specifically, general pragmatic reasoning can help eliminate certain instances of the subset problem given the child's input).

2 Logically-weaker alternatives and the subset problem

In this section we address the question of whether an existential meaning for the English word *every* is systematically incompatible with usages of *every* in the child's input. We start, in 2.1, by asking whether caregivers provide explicit negative feedback to children's incorrect uses of *every*. Having shown that such cases are vanishingly rare, in 2.2, we focus on the truth-conditional content of caregiver utterances, leaving pragmatic reasoning aside. We consider several potential

sources of truth-conditional evidence that could provide the child with evidence against the existential meaning, including downward-entailing environments, nonmonotonic environments, and various environments where the existential quantifier cannot be used. In each case, we ask whether replacing the universal meaning of every with an existential meaning in a given utterance results in a false utterance or in a violation of some semantic constraint. If it does, we consider the utterance to be informative, i.e., we consider it to provide the child with direct evidence against the existential meaning. Our conclusion in 2.2 will be that while some of these sources do exist in the input, they do not provide systematic evidence against the existential meaning. We then proceed to examine the contribution of pragmatics in section 2.3. We show that once familiar pragmatic principles are taken into consideration, a meaningful portion of the usages of every in the child's input would have been odd if every had an existential meaning. If the child is able to reason pragmatically about such input before having acquired the meaning of every, she can eliminate the existential hypothesis for every without special learning biases, in accordance with the null theory of language acquisition in (16).

2.1 Explicit negative feedback

On the basis of an analysis of child-parent interactions, Brown and Hanlon (1970) reported that parents object to around 25% of false statements made by children. A direct objection to a child's utterance could provide explicit evidence against weaker meaning candidates for a quantifier. Consider the hypothetical exchange in (17). In this exchange, the child makes a statement that is false under a universal meaning for *every* but not under the weaker existential meaning. On the assumption that interlocutors speak truthfully, the parent's objection would be nonsensical if *every* were an existential. Given such an exchange, the child could conclude that *every* does not have an existential meaning.

- (17) Scenario: a family expects three guests for dinner: Michelle, John, and Sue. Michelle has arrived in time, but John and Sue are late
 - a. Child: every guest is here.
 - b. Parent: no. Only Michelle is here. John and Sue are not here.

The potential informativeness of direct objection with respect to the subset problem is general. Since stronger quantifier meanings can lead to stronger statements, a child using a word with a stronger meaning than a conceivable alternative might make statements that are too strong to be true. If parents systematically object to children's false utterances, as reported by Brown and Hanlon, direct objection is a possible source of explicit negative evidence that can serve as a solution to the subset problem in the acquisition of *every*.

2.1.1 Coding

To assess the availability and generality of objections to children's statements with *every*, we manually examined all children's utterances that included *every* (a total of 72 utterances). Direct objection from caregivers to *every*-statements by the child within 5 lines of subsequent discourse was coded as a correction.

2.1.2 Results

Only one example with an objection was found, given in (18). In this example, the parent's response would have been false if *every* had an existential meaning.

- (18) Context: Pretend play with a train. Child pretends to get on the train with sister and dad, but states that "Mommy left behind"
 - a. Child: that one Nina [sister]
 Child: and that one Daddy

Child: and Mummy left behind

Mother: oh

Child: Look

Child: Everybody's on the train

b. Mother: Not everybody

Dominic, Age 2;7

2.1.3 Summary: explicit negative feedback

The extreme low frequency of *every* in our sample of child speech makes it difficult to estimate the availability of explicit negative feedback in general. At the same time, there is an independent reason to be unsurprised by the observed scarcity of direct objections to children's utterances with *every*, which is that there is evidence that children acquire the correct meaning of *every* by the time they start using it (Philip 2011 and references cited therein). We will tentatively conclude that direct objections do not provide systematic evidence against the existential

meaning, with the caveat that the sample size in this case was small and potentially unrepresentative of child speech.

2.2 Informative truth-conditional evidence

The input may contain truth-conditional evidence against a weaker meaning for *every* besides explicit negative feedback. The subset problem arises because in many situations a universal claim is compatible with a weaker, existential claim, but there are situations where this is not the case, either because the entailment patterns are different or because the existential claim violates some semantic constraint. We counted as potentially useful truth-conditional evidence downward-entailing and non-monotonic environments, as well as "existential-rejecting" environments — environments where the existential quantifier cannot be used for semantic reasons, including exceptive phrases, NPIs, and the adverbials *almost* and *nearly*. If caregivers systematically produce *every* in such environments and children know enough about the properties of such environments to exploit the evidence, then truth-conditional evidence alone may allow the child to solve this particular instantiation of the subset problem.

2.2.1 Coding

To evaluate the availability and systematicity of truth-conditional evidence against the existential meaning for *every*, we inspected caregiver utterances for uses of *every* (*i*) in the scope of negation (*not*, *no*, *never*), with and without other intervening operators, and in the scope of *fewer than n* (downward-entailing environments) and (*ii*) in the scope of *exactly* and *between m and n* (non-monotonic environments). We also considered three types of existential-rejecting environments: exceptive phrases involving *but*, NPIs like *any* and *ever* in the restrictor of *every*, and the scalar modifiers *almost* and *nearly*. We discuss each of these candidates in detail below, before presenting the corpus results.

2.2.2 Downward-entailing environments

Gualmini and Schwarz (2009) observed that input with downward-entailing environments may provide a general solution to the subset problem in semantics. Since downward-entailing environments reverse entailment relations, replacing the universal meaning of *every* with an existential meaning results in a stronger statement, and stronger statements may be too strong to be consistent with usages

of *every* in the input. Consider the example in (19), where the downward-entailing operator is the propositional negation *it's not the case that*. Under negation, the statement with the existential quantifier (here pronounced as *any*) entails the statement with the universal quantifier.

- $(19) \quad (a) \to (b)$
 - a. It's not the case that any girl ran
 - b. It's not the case that every girl ran

Since replacing the universal quantifier with the existential results in a stronger meaning, we can construct scenarios in which (19b) is true but (19a) is false. An example of a relevant scenario is given in (20). In this scenario, assigning an existential meaning to *every* results in falsity. If such scenarios are available in the child's input, they could provide the child with direct evidence against the existential hypothesis for *every*.

(20) Context: Three out of five girls ran It's not the case that every girl ran

Of course, propositional negation of the form *it's not the case that* is typically not available in child-language corpora. The more common form is *not*, which makes the picture more complicated. We now turn to *not* as our first example of a potentially-informative downward-entailing operator.

2.2.2.1 Negation Consider the following scenario, where *every* is interpreted in the scope of *not*:

- (21) Context: the child is asking to put more Mercurochrome (an antiseptic) on her cut, even though some had been used in a previous day. The mother rejects the request because Mercurochrome should not be used on a daily basis.
 - a. Child: Mercurochrome on it.
 - b. Mother: you got Mercurochrome on it. You only put a little bit. You **don't** put it on **every** day, you know. It'll go away.

If the quantifier pronounced as *every* takes scope under negation, it cannot have the existential meaning. Given the existential meaning, the mother's utterance would mean that Mercurochrome should *never* be used, which is too strong in this context given that Mercurochrome has been used recently. But *every* could

have the existential meaning if it scopes over negation, in which case the resulting meaning would be equivalent to a universal under negation. This equivalence can be illustrated using the following unambiguous paraphrases:

- (22) a. It's not the case that one puts Mercurochrome every day.
 - b. Some day is such that one doesn't put Mercurochrome then.

If mechanisms for inverse scope are available to the child, and in particular mechanisms that allow an existential to take inverse scope over negation, examples like (21) provide no definitive basis for the child to rule out the existential meaning for *every*.⁶ The mother's utterance is compatible with a grammar in which *every* has the existential meaning if this grammar allows the existential to scope over negation. To be able to rule out the existential meaning using downward-entailing environments, we need to consider other downward-entailing environments where no scope possibility for the existential would be equivalent to the intended meaning. We turn to such environments next.

2.2.2.2 Downward-entailing environments that break equivalence Consider another downward-entailing operator, the determiner *no*:

(23) No girl read every book

In this case, both surface and inverse scopes with the existential meaning are logically stronger than surface scope with the universal meaning. The two scopes for the existential can be unambiguously paraphrased as follows:

- (24) No girl read any book (surface scope)
- (25) Some book is such that no girl read it (inverse scope)

We can construct hypothetical scenarios in which the existential meaning would be too strong under either scope, while the surface-universal scope would be true. For example, suppose that there are three books and three girls, and the relation between girls and books they have read is as in (26).

(26) Context:

a. books =
$$\{b_1, b_2, b_3\}$$

⁶It has been claimed that children have a preference for surface-scope readings for sentences containing a quantifier and negation (Musolino 1998, Musolino and Lidz 2003), but also that children are indeed able to access inverse scope readings at the same ages (Musolino and Lidz 2006, Gualmini et al. 2008).

- b. girls = $\{g_1, g_2, g_3\}$
- c. g_1 only read b_1 , g_2 only read b_2 , g_3 only read b_3

In this context, the utterance in (23) would only be true under the universal meaning for *every* but not under the existential meaning (i.e., both (24) and (25) would be false). This means that usages of *every* alongside *no* in such contexts would constitute informative input for the child.

Equivalence could also break down when another operator intervenes between negation and the quantifier. A modal is such an operator. Consider the following utterance:

- (27) Context: Two parents and their child are ready to have dessert. There is a cookie, a cake, and a pudding on the table.
 - a. Child: Which dessert is for me?
 - b. Mother: You can eat the cookie, the cake, or the pudding, but **you** can't eat everything.

The mother's utterance in bold is multiply ambiguous. To see why, let us represent its three operators as follows: $not = \neg$, $can = \diamond$, $every = \forall$. Let us also assume that the relative scope between negation and can is fixed such that \neg out-scopes \diamond ($\neg > \diamond$), as is the case in English. This leaves three potential meanings, where (a) is the intended meaning:

(28) a. $\neg > \diamond > \forall$

It is not allowed that you eat everything.

b. $\neg > \forall > \diamond$

There is a thing that you are not allowed to eat.

c. $\forall > \neg > \diamond$

Everything is such that you are not allowed to eat it (i.e., you cannot eat anything)

Meanings (b) and (c) are stronger than (a) and are incompatible with the context, since the mother explicitly states that the child can pick any of the desserts to eat. If the universal meaning is replaced with the existential, we get the following three corresponding interpretations:

(29) a. $\neg > \diamond > \exists$

Everything is such that you are not allowed to eat it (i.e., you cannot eat anything)

b. $\neg > \exists > \diamond$

Everything is such that you are not allowed to eat it (i.e., you cannot eat anything)

c. $\exists > \neg > \diamond$

There is a thing that you are not allowed to eat.

Given the existential meaning for *every*, none of the three interpretations are compatible with the mother's utterance in (27). If children are exposed to utterances with negation, a modal, and *every* in a context that rules out all stronger interpretations given the existential meaning, then children could use such utterances to rule out the existential as a meaning for *every*. We therefore further coded all negative environments for the presence or absence of an intervening modal, including existential as well as universal modals.

2.2.3 Non-monotonic environments

Non-monotonic environments are environments that are neither downward-entailing nor upward-entailing. For non-monotonic environments, it is possible to construct scenarios in which every scope for the existential quantifier would be false. Consider the non-monotonic operator *exactly* and a context in which there are three books, four girls, and the relation between girls and books that they read is as in (30).

(30) Context:

- a. books = $\{b_1, b_2, b_3\}$
- b. girls = $\{g_1, g_2, g_3, g_4\}$
- c. g_1 and g_2 each read b_1 , b_2 , and b_3 ; g_3 read b_1 and b_2 ; g_4 read b_2 and b_3

In this context, the utterance in (31) is true under the universal meaning for *every* but, as we will now see, not under the existential meaning.

(31) Exactly two girls read every book

The two scopes for the existential relative to *exactly* can be unambiguously paraphrased as follows:

- (32) Exactly two girls are such that they read some book (surface scope)
- (33) Some book is such that exactly two girls read it (inverse scope)

Surface existential scope is false in the context in (30) because more than two girls read books and inverse scope is false because each book was read by at least three girls.

Like downward-entailing environments, non-monotonic environments have the property that they can provide a general solution to the subset problem.

2.2.4 Existential-rejecting environments

There are several environments where *every* can be used but an existential quantifier cannot. Here we consider such environments as further potential kinds of informative input.

- **2.2.4.1 NPI-licensing.** The first environment involves negative-polarity items (NPI) like *any* and *ever*, which are licensed in the restrictor of *every*. In contrast to *every*, existential quantifiers do not license NPIs in their restrictor:
 - (34) a. Every movie that I have *ever* watched was good.
 - b. *Some movie that I have *ever* watched was good.

Theories of NPI-licensing typically attribute this contrast to a semantic difference between *every* and the existential quantifier (Ladusaw, 1980). Namely, *every* is downward-entailing in its restrictor but the existential quantifier is not. If these theories are correct, then inputs with an NPI in the restrictor of *every* could provide the child with direct evidence against the existential meaning for *every*, if the child already has knowledge of NPI-licensing.⁷

- **2.2.4.2** Almost and nearly. The words almost and nearly are scalar modifiers whose semantics make them incompatible with existential arguments, as illustrated in (35).⁸ Since these words are incompatible with an existential argument, they can provide informative input for the child when used with every. This would be true if the child has knowledge of the universal requirement of almost and nearly before acquiring the meaning of every.
- (35) a. Almost/nearly every student arrived.
 - b. *Almost/*nearly some student arrived.

⁷There is evidence that children as young as 2 treat *any* as an NPI and seem to understand where it is licensed (Tieu 2015, Gualmini 2004), and that 4-year-olds are sensitive to the fact that *every* is downward-entailing in its restrictor (Gualmini et al. 2003, Crain et al. 2004).

⁸For theories of the difference between universal and existential complements to *almost* and *nearly*, see Sadock (1981), Sevi (1998), Penka (2006), Amaral and Del Prete (2010).

- **2.2.4.3** The exceptive *but*. The distribution of the exceptive *but* obeys a universality restriction (von Fintel, 1993), illustrated in (36). If the child has knowledge of this restriction before having acquired the meaning of *every*, then utterances like (36a) would be informative.
- (36) a. Every girl but Michelle read a book.
 - b. *Some girl but Michelle read a book.

2.2.5 Results

2.2.5.1 Downward-entailing environments *Every* occurred in the scope of *not* a total of 77 times (11.7% CIs[5.2%-23.9%]) in caregiver utterances in the Manchester corpus. Figure 3 displays the proportion of DE-environments in caregiver utterances by corpus.

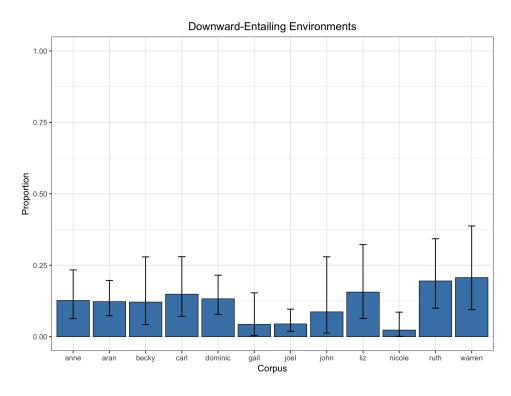


Figure 3: Proportions and 95% binomial confidence intervals of DE-environments in caregiver utterances

Though DE-environments are reliably present in caregiver speech, we saw

above that usages of *every* in the scope of *not* are unhelpful for rejecting the existential hypothesis for *every*, because inverse scope with the existential is logically equivalent to surface scope with the universal. We therefore looked for cases where this equivalence is broken: cases where *every* is in the scope of *no* or and cases where a modal operator intervenes between negation and *every*. There were no occurrences of *every* scoping under *no* in the corpora. The same result of 0 occurrences was obtained for *fewer than n*, which has a similar behavior to *no*. There were 16 (2.14%) occurrences of *every* with negation and an intervening modal, but none appeared in an informative context that rules out the existential meaning. An example is the following occurrence:

- (37) Context: Playtime; the child is refusing to share his toys with his mother. Whenever she asks if she can play with a certain toy, the child says that he will play with that toy.
 - a. Mother: So if I play with this yellow car that's alright then?
 - b. Child: I play yellow car
 - c. Mother: You can't play with everything.

Dominic, Age 2;3

If *every* has an existential meaning and it takes widest scope over negation and the modal, the resulting interpretation is the one in (38). This interpretation can be true in the context: it could be that there is a certain car that the child is not allowed to play with, and this car is the yellow car (this utterance would not be a cooperative utterance, but recall that in this section we are only considering the possibility that utterances with the existential are true. The contribution of pragmatics will be discussed separately in section 2.3).

$$(38)$$
 $\exists > \neg > \diamond$

There is a thing that you are not allowed to play with.

Our conclusion is that, considering truth conditions alone, downward-entailing environments did not provide unambiguous evidence against the existential meaning for *every*.

2.2.5.2 Non-monotonic environments To asses the availability of informative non-monotonic environments in the input, we searched the corpora for occurrences of the non-monotonic operators *exactly* and *between m and n*. There

were no occurrences of these operators (0/746), indicating that informative non-monotonic environments with these operators do not in fact provide the child with a solution to the subset problem for *every*.

2.2.5.3 Existential-rejecting environments We examined the corpus for occurrences of the three types of existential-rejecting environments discussed above. This included the NPIs *any* and *ever* in the restrictor of *every*, occurrences of the expressions *nearly* and *almost* modifying *every* and exceptives of the form *every A but x.* We found 13 such cases overall, distributed among 5 of the 12 corpora examined.

We found two informative examines of the NPIs *any* and *ever* in the restrictor of *every*, one of which is given below.

(39) Mummy's fallen off **every** single horse she's **ever** got on. *Joel, Age 2;6*

There were 5 occurrences in the corpus of *almost every* or *nearly every*.

(40) We've tried playing with **almost everything** today, haven't we? *Aran, Age 2;5*

Finally, there were 6 examples like (41) in the corpus with *but* and *every*, 4 of which were made by the same parent.

(41) I think that's everything but the dolly. *Nicole, Age 2;3*

Overall, 1.75% (CIs[0-11.4%]) of caregiver utterances in the corpus comprised of *every* in potentially informative existential-rejecting environments.

2.2.6 Summary: truth-conditional evidence

We have seen that different sources of truth-conditional evidence that could provide the child with evidence against the existential meaning for *every* were either infrequent or consistent with weaker meanings. Considering downward-entailing environments, non-monotonic environments, NPI-licensing, *almost*, *nearly*, and the exceptive *but*, there were a total of 13 informative utterances (1.75%) overall. On the basis of this result, and assuming the null theory of acquisition in (16), we

⁹In addition, these 13 informative utterances came from a subset of 5 corpora, meaning that the remaining 7 children were not exposed to any informative utterances of this sort.

conclude that the input is not rich enough to systematically rule out the existential meaning using truth-conditional evidence alone.

2.3 Informative pragmatic evidence

In this section we consider sources of pragmatic input that could provide the child with evidence against the existential meaning. In the previous section, we asked whether replacing the universal meaning of every with an existential meaning resulted in a false utterance or in a violation of some semantic constraint. Here we ask a different question: whether replacing the universal with an existential results in an *odd* utterance that violates some pragmatic constraint. We first consider utterances where replacement with an existential results in oddness due to a violation of Grice's (1967/1975) Maxim of Quantity. We will see that such utterances are commonly available in the input. However, we will point out that the child's ability to use such utterances to eliminate the existential hypothesis for every depends on certain open questions concerning implicature computation and alternatives that are actively debated in the literature. We then turn to oddness due to violations of two different pragmatic constraints: a constraint on the non-redundancy of assertions and a constraint on the non-vacuity of questions. Both are constraints against triviality: that one must not proffer information that is already common ground and that one must not ask a question whose answer is already common ground. In both cases, the input is abundant with utterances that become odd under an existential meaning for every. If the child is able to use these constraints, she could infer that every does not have the existential meaning and thus avoid this instance of the subset problem in the acquisition of every. This, in turn, would mean that the null theory of acquisition in (16) could be maintained and that adding learning biases to the theory is not needed.

2.3.1 Coding

To assess the availability of pragmatic evidence ruling out the existential hypothesis for *every*, we manually examined each caregiver utterance with *every* in context. 50 lines of the preceding discourse and 5 lines of the following dialogue were examined in order to establish a discourse context against which the utterance was evaluated. All utterances were coded independently by the two authors and later checked for inter-coder agreement ($\kappa = .90$). For each utterance for which there was disagreement, agreement was later established after considering a greater portion of the preceding discourse.

We coded each utterance for whether or not it would violate one of three pragmatic principles if the universal meaning of *every* were replaced with an existential one: Maxim of Quantity, Non-redundancy of Assertions, and Non-vacuity of Questions. In each case, we asked whether, given the context, the child has grounds to believe that a weaker, existential meaning would render an utterance with *every* uncooperative in the relevant sense (the three principles and our coding criteria for each principle are discussed in the following sections). If so, we coded the utterance as potentially informative on the basis of one of the three constraints.

We discuss each candidate in detail below, before presenting our results.

2.3.2 Maxim of Quantity

Consider the following hypothetical exchange:

- (42) Context: The parent encourages the child to eat as many cookies as possible. There are three cookies in the jar.
 - a. Parent: Let's see if you can finish eating the cookies in the jar.
 - b. (The child eats all three cookies.)
 - c. Parent: Good job, you ate every cookie.

Given the context, the parent's utterance in (c) would be odd under an existential meaning for *every*:

(43) Parent: #Good job, you ate some cookie.

In addition – though our focus in this paper is on the existential alternative to *every* – any replacement of *every* with a weaker quantifier would be odd in this context:

(44) Parent: #Good job, you ate most cookies.

Can the child reason pragmatically about scenarios like (42) to eliminate the existential hypothesis for *every*? To answer this question, we need to look more closely into theories of the oddness of (43). Here we discuss a theory that relies on the Neo-Gricean Maxim of Quantity (NGMQ; Horn 1972, Horn and Ward 2004, Sauerland 2004, Spector 2006, among others):

(45) NGMQ: a speaker shouldn't utter ϕ if there is a stronger alternative ψ that the speaker believes is true

In order for the child to use NGMQ to infer that (43) would be odd, at least three conditions must be met:

- (46) a. The child can use NGMQ.
 - b. The child must believe that her parent believes that the universal statement is correct (i.e., that she ate all the cookies).
 - c. The set of alternatives for (43) must include an utterance in which the existential is replaced with an element that leads to a stronger meaning.

Condition (a) can be met if the child is at a stage where she can use NGMQ. Condition (b) can be easily met if the child is at a stage where she can hold beliefs regarding other people's beliefs. In the scenario in (42), for example, the child sees directly that her parents sees that she ate all the cookies. Condition (c), however, depends on the set of alternatives for the existential that are available to the child before she has acquired the meaning of every. The literature on implicatures has offered two competing theories regarding the set of available alternatives, and the difference between the two theories matters. 10 On one theory, alternatives are available to a speaker regardless of whether she has lexicalized them (Deal 2011, Buccola et al. 2018). For example, the universal quantifier would be an alternative to the existential even in languages that do not have a word for the universal. If this theory is correct, the English-learning child should have access to the universal quantifier as an alternative to other quantifiers even before acquiring the meaning of every, and condition (c) could be satisfied. In other words, if alternatives like the universal quantifier are available to the child before lexicalization, the child could use scenarios like (42) to rule out the existential hypothesis for every, and this instance of the subset problem could disappear. 11 On other theories, however, morphemes cannot serve as alternatives unless they have been lexicalized (Katzir 2007, Fox and Katzir 2011). If this is the case, then in order for condition (c) to be satisfied, the child should have already lexicalized a meaning that is stronger

¹⁰Here we make the simplifying assumption that the alternatives used for the computation of oddness are the same alternatives used for the computation of implicatures. This need not be the case, but as far as we can tell, our conclusions will not change if the two sets turn out to be distinct: our discussion could remain the same except that "alternatives" would refer only to alternatives used for the computation of oddness, as long as there is no evidence regarding those alternatives that conflicts with our claims.

¹¹Previous acquisition research suggests that children are more accepting of sentences that violate the Maxim of Quantity in comprehension tasks (Noveck 2001 and many others since). More recently, it has been proposed that children's difficulties stem from their inabilities to retrieve the relevant lexical alternatives (Barner et al. 2011). If this proposal is on the right track, then scenarios like (42) may not be helpful for the child even if the requisite alternatives are in principle available without lexicalization.

than the existential quantifier, and acquiring any such meaning should have posed a version of the subset problem. In other words, on the assumption that alternatives are not accessible before they have been lexicalized, scenarios like (42) are uninformative unless the child had already solved an instance of the subset problem and correctly rejected the existential meaning in favor of some stronger meaning. Since this is the very learning problem that we are interested in here, it would be unreasonable to assume that the child had already independently solved an instance of the subset problem. We are left to conclude that oddness due to NGMQ provides a general strategy for rejecting the weaker existential meaning if the following conditions are met:

- (47) Conditions for using NGMQ as a solution to the subset problem:
 - 1. The child can use NGMQ.
 - 2. The child can hold beliefs regarding other speakers' beliefs.
 - 3. Stronger alternatives to the existential quantifier (e.g., the universal quantifier) are available regardless of lexicalization.

2.3.3 Assertions and non-redundancy

Sentences asserted in a conversation are meant to contribute new information; redundant assertions are to be avoided. An influential theory of what counts as redundant comes from Stalnaker (1974, 1978, 1999, 2002). On this view, the basic role assertive speech acts play in language use is to update the body of shared beliefs of the interlocutors – the *common ground* – by adding the content of what is asserted to what was already shared information (see also von Fintel 2008). Stalnaker (1978) introduces a pragmatic principle stating that assertion of sentence S with respect to context c is felicitous only if it results in a non-trivial update of c. One way for triviality to obtain is if the information is already part of the conversational common ground, i.e. it is redundant. A speaker making a speech act is therefore expected to adhere to the principle in (48).

(48) *Principle of Non-Redundancy:* An assertion is infelicitous if the asserted proposition is already common ground. (paraphrased from Stalnaker 1999, p. 88)

Against this background, consider the hypothetical exchange in (49).

(49) Context: The child's older brother is in the kitchen eating cookies from a jar that contains 10 cookies. Every few minutes, the parent updates the

child (who is in a different room) about the total number of cookies her brother has eaten so far.

- a. Parent: Your brother ate two cookies.
- b. (The parent goes to the kitchen and then returns with another update.)
- c. Parent: Your brother ate every cookie.

In the given context, the parent's assertion in (c) would be odd if *every* were an existential quantifier:

(50) Parent: #Your brother ate some cookie.

Notice that differently from the exchange in (42), here the child does not know whether the statement with *every* is correct, so the Maxim of Quantity is unhelpful in accounting for the oddness of (50). Instead, according to the principle in (48), the utterance in (50) is odd since it repeats information known to both interlocutors (the brother's eating of some cookie) and cannot change the common ground of the conversation. If the child can use this principle before she has acquired the meaning of *every*, she could use scenarios like (49) to rule out the existential meaning for *every*.

2.3.4 Questions

Questions are another possible source of pragmatic evidence against the existential meaning. Consider a context in which somebody has arrived. In this context, the question in (51a) would be natural but the question in (51b) would be odd.

- (51) Context: somebody has arrived
 - a. Is everybody here?
 - b. #Is anybody here?

The oddness of (51b) is presumably due to a pragmatic constraint like the following (different formulations of this constraint are assumed in Groenendijk and Stokhof 1984, Roberts 1996, Büring 2003, Fox 2018, among others):

(52) Do not ask a question whose answer is common ground.

According to this constraint, the question in (51b) is odd in the context assuming that the speaker and the addressee already know that at least one person has arrived. If the child can use (52) before she has acquired the meaning of *every*, she could use scenarios like (51) to reject the existential meaning for *every*. Given

(52), questions are a helpful source for rejecting the weaker existential meaning since the answer to the question with the existential is weak enough to be entailed by the context.

2.3.5 Results

We examine declaratives and questions separately, as they are governed by distinct pragmatic conditions. There were a total of 528 assertions and 161 questions. The proportion of each type of speech act in caregiver utterances with *every* is displayed in Figure 4. The 'Other' category includes imperatives and uncategorizable utterances (e.g., one word utterances).

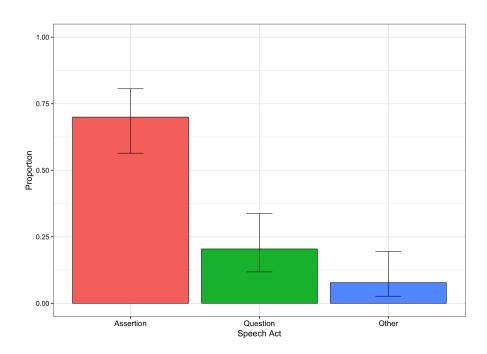


Figure 4: Proportion and 95% CIs of declaratives and questions in caregiver utterances with *every*

2.3.5.1 Declaratives

Maxim of Quantity To address the question of whether the Maxim of Quantity could be helpful in eliminating an existential meaning hypothesis for *every*,

we manually examined all declarative utterances with *every* in context. We were conservative in what we considered to be informative: an utterance with *every* was coded as informative only if the context provided a clear indication that the child has grounds to believe that the speaker/caregiver believes that the universal statement is true. So, given an utterance of the form *Every toy is broken*, if the context makes it likely that the domain of quantification of *every* is a set of toys present and visible to both parent and child in the situation, we counted the sentence as informative; if the domain of quantification was not deducible from the transcripts alone, we did not count the sentence as informative. Our results thus likely under-estimate the amount of informative evidence of this sort that the child is privy to.

Only 26 out of 528 of declarative utterances with *every* were informative in this sense (an example is given in (53)). Of course, as per the discussion in section 2.3.2, whether this is a solution to the subset problem is contingent on what will turn out to be the right theory of alternatives, so we will leave it as a conditional solution that must await further verification.

(53) Mother: shall we put all the food bits back in here?

Child: bread.

Mother: I think that's supposed to be meat.

Child: It looks similar to bread.

Child: Here you go. Mother: Thank you. Child: Here you go. Mother: Thank you.

Mother: Everything (is) in the basket now.

John, Age 2;1

Non-redundancy To assess the availability of scenarios like (49), we searched the corpus for usages of *every* in declaratives, once again examining each usage in context. We considered an assertion to constitute evidence against the existential meaning whenever the context provided a clear indication that the existential variant of the assertion introduces information already known to both the parent and child, as well as a clear indication that the child has grounds to believe that the parent knows that information. There were 94 usages of *every* where the context provided these indications (an example is provided in (54)). This constituted 17.7% of declaratives (CIs[10.1-36.8%]) and 12.6% of the *every* utterances in total (CIs[6.4-26.1%]).

(54) Child: Andy want this? Child: Just that for Andy.

Mother: Make him laugh with all these kisses.

Child: Give me a kiss. Mother: Want to kiss me?

Mother: Oh.

Mother: He's kissing everybody.

Gail, Age 2;6

- **2.3.5.2 Questions** To assess whether non-vacuity conditions on question-asking could systematically provide evidence against an existential meaning for *every*, we manually examined in context all questions in the corpus that included *every* and for each, asked whether the following two conditions were met:
 - 1. There was a clear indication that the context entails the answer to the existential counterpart of the question (i.e., a minimal variant of the question in which *every* is replaced with the existential quantifier).
 - 2. There was a clear indication that the context does not entail the answer to the uttered question (with *every*).¹²

161 of the total caregiver utterances with *every* were questions, and 37 (22.9%, CIs[9.8%-56.2%]) of these were informative according to our criteria (an example is given in (55)). This makes up for a total of 4.9% (CIs[2.08-17.4%)] of the total input informative for rejecting the existential meaning.

(55) Mother: Now what do you need?

Mother: Eggs.

Mother: There we go.

Mother: Have you got everything you want now?

Child: Yeah.

Nicole, Age 2;1

¹²This measure was taken to ensure that the relevant question is in fact information-seeking. Child-directed speech often includes questions that are used by the caregiver for reasons other than eliciting information from the child (e.g., to check that the child is attending to the same things that the caregiver is). The constraint in (52) is inactive in such situations. If the child has grounds to believe that a question is not information-seeking (for example, if the context makes it clear that the caregiver knows the answer to the question), then (52) should play no role in their pragmatic reasoning even if the first condition is met.

2.3.6 Summary: Pragmatic evidence

Figure 5 summarizes the proportions of caregiver utterances that were informative by the three sources of pragmatic evidence discussed in this section.

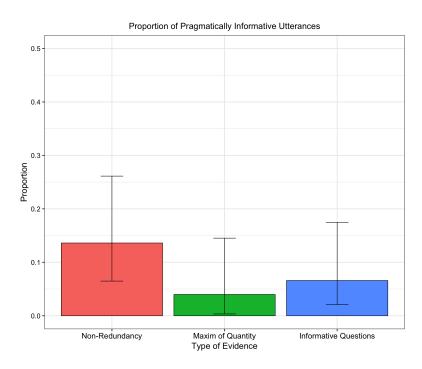


Figure 5: Proportion and 95% CIs of pragmatically informative caregiver utterances with *every*

Informative pragmatic evidence for rejecting the existential meaning for *every* was systematically available in the corpus: considering the non-triviality of assertions and questions (and not counting the Maxim of Quantity), 17.5% of the usages of *every* (133/746) had the property that replacing *every* with the existential quantifier would have led to a violation of a pragmatic constraint. We conclude, assuming the null theory of acquisition in (16), that the pragmatic input is rich enough to provide systematic evidence against the existential meaning for *every*.

3 Logically-stronger alternatives and the superset problem

In this section we discuss potential instances of the supserset problem in the acquisition of *every*, the mirror image of the subset problem. As mentioned in section 1, the superset problem arises whenever logically-stronger meaning candidates for *every* are consistent with the child's input.

Consider the quantifier $[[every_{>2}]]$ in (56) as an alternative to our assumed meaning of every - [[every]] – repeated in (57). Like [[every]], $[[every_{>2}]]$ returns True if its restrictor is a subset of its scope. Unlike [[every]], $[[every_{>2}]]$ presupposes its restrictor to have a cardinality greater than two, a stronger requirement than the presupposition of [[every]]. Given this stronger requirement, the extension of [[every]] is a superset of the extension of $[[every_{>2}]]$, as stated in (58).

- (56) $[[every_{>2}]] = \lambda P : |P| > 2.\lambda Q.P \subseteq Q$
- (57) $\llbracket every \rrbracket = \lambda P : |P| > 0.\lambda Q.P \subseteq Q$
- (58) $\llbracket every_{>2} \rrbracket \subset \llbracket every \rrbracket$

The correct English meaning of *every* in (57) is difficult to distinguish empirically from the alternative in (56). The difficulty arises since usages of English *every* often lead to an inference that its restrictor has more than two elements. The examples in (59) illustrate the oddness of using *every* when the cardinality of the domain is exactly one or two.

- (59) a. #Every nose of Michelle's is runny.
 - b. #Every cheek of Bill's is rosy.
 - c. Every finger of Mary's is long.

According to Sauerland 2003, Sauerland 2008, Percus 2006, and Chemla 2008, among others, the oddness of *every* in (59a) and (59b) arises not because of a lexical presupposition along the lines of [[every>2]], but due to a competition of [[every]] with the presuppositionally-stronger the (which carries a uniqueness presupposition) and the presuppositionally-stronger both (which carries a duality presupposition), respectively. The competition is due to a pragmatic principle, Maximize Presupposition! (Heim 1991), which forces speakers to choose from a set of competitors the sentence that carries the strongest presuppositions satisfied in the context. On the assumption that cooperative speakers adhere to this pragmatic principle, the choice of a competitor with weaker (or no) presuppositions

would be odd. Using (59b) as an example, the speaker's choice of *every* is odd since it only presupposes that Bill has cheeks, while the alternative with *both* carries the stronger presupposition that Bill has exactly two cheeks (which is trivially satisfied given our common knowledge about the duality of human cheeks).

There are two types of evidence that the non-uniqueness and non-duality inferences are not part of the semantics of *every*. The first is that unlike lexically-encoded presuppositions, non-uniqueness and non-duality are easily cancellable. As illustrated by (60a)-(60b), *every* can be used even when the speaker is ignorant about the cardinality of the domain of quantification. The contrast between (60a) and (60b) would be surprising under $[every_{>2}]$, which encodes non-uniqueness and non-duality lexically, but not under [every], which does not encode them.

- (60) a. I don't know if she has more than two cats or not, but I bet that every cat of hers is happy.
 - b. #I don't know if she has any cats or not, but I bet that every cat of hers is happy.

The second type of evidence that non-uniqueness and non-duality are not part of the semantics of *every* is that these inferences behave differently from lexically-encoded presuppositions in embedded contexts. Under various theories of presupposition projection (e.g., Karttunen and Peters 1979, Heim 1983, Schlenker 2008), universally quantified sentences of the form *Every A B* presuppose that every element in the restrictor satisfies the presuppositions in the nuclear scope. The duality presupposition of *both* in the nuclear scope behaves as predicted: in (61a), we take it that every candidate wrote exactly two papers. The non-uniqueness and non-duality inferences of *every* in the nuclear scope do not pattern analogously: (61b) is compatible with situations where some candidates have written exactly one or two papers. The felicity of (61b) in such contexts is surprising if the lower *every* (underlined) means [[*every*>2]], which encodes non-uniqueness and non-duality semantically.

- (61) a. Every candidate submitted both papers of hers.
 - b. Every candidate submitted every paper of hers.

Semanticists have access to utterances like (60a) and (61b) and can use them to reject $[[every_{>2}]]$ in favor of $[[every_{]}]$. Since the predictions of $[[every_{]}]$ and $[[every_{>2}]]$ are so subtly divergent, (60a) and (61b) had to be carefully constructed to properly tease the two meanings apart. For the child, of course, things are different. Informative evidence against the subset meaning $[[every_{>2}]]$ requires

special circumstances (or their combination) for it to occur in the child's input. For evidence like (60a) to occur in the input, the caregiver would need to signal their ignorance about the cardinality of the restrictor of *every*. For evidence like (61b) to occur in the input, *every* needs to be embedded in the scope of another quantifier and in a specific context. For example, the utterance in (61b) would be informative only if the child knows that some candidates have written just one or two papers.

3.1 Coding

To assess the availability of evidence against $[[every_{>2}]]$ in the child's input, we searched the corpora for occurrences of examples like (60a) and (61b). To our knowledge, no other types of evidence have been proposed in the literature to distinguish between the two meanings. For examples like (60a), we examined the usages of *every* in context to determine whether the caregiver's ignorance about the cardinality of the restrictor of *every* was signaled in any way. For examples like (61b), we marked all occurrences of *every* alongside another quantifier which the non-uniqueness and non-duality inferences of *every* do not project out of (*every*, *always*, *usually*, *normally*, *exactly*, *between m and n*, etc.). For each example we found, we evaluated whether the child is provided with the right context to determine that the restrictor of *every* can include exactly one or two elements.

3.2 Results

We found no utterances that are inconsistent with $[[every_{>2}]]$. There were no occurrences of *every* where the caregiver signaled ignorance regarding the size of the restrictor. There were only 6 occurrences of *every* in the scope of another potentially informative quantifier, but none appeared in a context that makes the usage of *every* inconsistent with $[[every_{>2}]]$. One of those 6 examples is given (62). The mother mentions multiple occasions in which the child threw objects on the floor, but there is no indication that one of those occasions involved exactly one or two objects being thrown. Without such indication, it is possible that each occasion involved more than two objects being thrown by the child, which, in turn, would make the utterance in (62) consistent with $[[every_{>2}]]$.

(62) Because you chuck everything on the floor as usual, don't you? *Dominic, Age 2;8*

3.3 Discussion

Our finding suggests that systematic evidence against $[[every_{>2}]]$ is not available in the child's input. This means that the child may as well conclude on the basis of her input that *every* requires its restrictor to have more than two elements. This is the state of affairs discussed in section 1: the child is faced with two competing hypotheses consistent with the input – a grammar with [[every]] and a grammar with $[[every_{>2}]]$ – but ends up selecting one. In this case, the child makes an inductive leap to conclude that [every] allows any non-empty restrictors rather than only restrictors with more than two elements.

The same inductive problem for the child can be repeated using quantifiers other than $[every_{>2}]$. Consider the quantifiers in (63). (63a) is similar to $[every_{>2}]$ but the restriction on its domain is an additional conjunct in the assertive component of the meaning rather than a presupposition. For (63b), assume that the child has been exposed to usages of *every* with restrictors of sizes that do not exceed some finite number n. (63b) adds n as an upper bound on the possible size of the restrictor of *every*. (63c) is even more restrictive, and simply records the sizes of observed restrictors without making any size-based generalization. Each example in (63) adds a pointless complication to the meaning of *every* that makes it more restrictive, in a way that keeps the quantifiers consistent with usages of *every* in the input.

```
(63) a. \lambda P \lambda Q.P \subseteq Q \land |P| > 2
b. \lambda P \lambda Q.P \subseteq Q \land (2 < |P| < n)
c. \lambda P \lambda Q.P \subseteq Q \land (|P| = 3 \lor |P| = 5 \lor |P| = 6 \lor ...)
```

The inductive problem posed by $[[every_{>2}]]$ and by the quantifiers in (63) is similar to an inductive problem that has been discussed in the philosophical literature on induction, albeit in a different context than child language acquisition. Goodman (1955) observed that usages of the English predicate *green*, whose meaning is given in (64), are also consistent with the meaning of the predicate *grue* in (65) (which we have adapted to our notation), assuming that 1/1/2029 is some future time. Goodman's puzzle, which he referred to as the "New Riddle of Induction", concerned the inductive leap from one's past observations of *green* to the meaning in (64), given that the alternative in (65) is also consistent with all past usages of *green*.

- (64) $[green] = \lambda x.x$ is green
- (65) $[grue] = \lambda x.x$ is green if observed before 1/1/2029 or blue if observed later

Similarly, Kripke (1982) proposed the mathematical operator *quus* (\bigoplus) defined in (66) as an alternative to addition. The operator *quus* behaves like the regular addition operator '+' for arguments up to some finite number (57 in Kripke's example) but beyond that number it always returns 5. Kripke's question was what licenses the inference that addition behaves like '+' and not like *quus* (or similar alternatives with a number higher than 57), given that our exposure to addition is consistent with both.

(66)
$$x \bigoplus y = \begin{cases} x + y & \text{if } x, y < 57 \\ 5 & \text{otherwise} \end{cases}$$

In both Goodman's and Kripke's examples, the challenge is to generalize beyond the observed data. Our result that the child's input does not provide evidence against $[[every_{>2}]]$ as an alternative meaning to every indicates that the child faces a version of Goodman's and Kripke's problem in the acquisition of every. Assuming that $[[every_{>2}]]$ is consistent with the child's input, the challenge is to generalize the meaning of every to restrictors of any positive size. Of course, differently from Goodman and Kripke, our goal is to understand the consequences of this inductive problem for child language acquisition. In what follows, we discuss a few possible conclusions that we find interesting that arise from our result, though we will leave a definitive conclusion for future research.

The first possible conclusion is that the child selects [[every]] because Universal Grammar (UG) does not make the quantifiers in (56) and (63) available. Stated differently, the child's hypothesis space is restricted so as to exclude (56) and (63) as possible quantifiers, as well as any other quantifiers with the same extensions. This possibility, while correctly addressing the inductive problem, would require very specific constraints on the child's hypothesis space. The quantifiers in (56) and (63) obey familiar universal constraints on quantifiers, such as Conservativity, Isomorphy, and Extension (Barwise and Cooper 1981, Keenan and Stavi 1986, van Benthem 1986, Peters et al. 2006), and their denotation is similar to other lexicalized meanings. For example, the denotation in (56) is almost identical to the denotation of both, given in (67). Constraints on the child's hypothesis space that exclude (56) would have to be stated specifically enough so as not to also exclude the attested (67). Of course, whether quantifiers like (56) and (63) are in the child's hypothesis space is an empirical question, which could be tested experimentally (see Hunter and Lidz 2012 for a concrete experimental paradigm, though see de Villiers and Spenader 2019 for a criticism of that paradigm).

(67)
$$[both] = \lambda P : |P| = 2.\lambda Q.P \subseteq Q$$

An alternative conclusion to draw from the inductive problem is that the quantifiers in (56) and (63) are part of the child's hypothesis space but the null theory of acquisition in (16) is insufficient, because it says nothing about learning when more than one hypothesis is consistent with the input (up to noise). An alternative to (16) could be a more complex theory of learning according to which the child is biased in favor of [every] over the quantifiers in (56) and (63). Here, a bias such as the Semantic Subset Principle (Crain et al. 1994) which pushes the child towards subset meanings would lead the child astray if used by itself, since the child generalizes to a superset meaning (see Musolino et al. 2019 for other critique of the Semantic Subset Principle). As noted by Goodman (1955), pressure for generalization can come from a bias for simplicity. Intuitively, the meaning of green in (64) is simpler than the meaning of grue in (65), and the definition of quus in (66) is simpler than x + y, the expression for ordinary addition. In generative linguistics, the idea that simplicity could be used as a learning criterion for the child was explored in Halle (1962), Chomsky (1965), and Chomsky and Halle (1968) for both phonology and syntax. Simplicity-based learning criteria have been later proposed for a variety of language-learning tasks by Berwick (1982), de Marcken (1996), Goldsmith (2001), Chater and Vitányi (2007), Rasin and Katzir (2016), and many others.

Can a simplicity bias address the superset problem in the acquisition of *every*? Since simplicity-based comparisons depend on the language of description, the answer depends on how UG allows meaning representations of quantifiers to be written. To illustrate this dependency, consider again the two competing meanings for *every*, repeated in (68). In this case, simplicity will be of little help: the two meanings are roughly equivalent in their complexity, so a child equipped with a bias for simplicity (say, a bias for representations with fewer symbols) will have no incentive to choose one meaning over the other. In other words, if both meaning representations in (68) are in the child's hypothesis space, and assuming that both are consistent with the child's input, then the simplicity-guided child may as well select the incorrect meaning $[every_{>2}]$.

(68) a.
$$\llbracket every \rrbracket = \lambda P : P \neq \emptyset.\lambda Q.P \subseteq Q$$

b. $\llbracket every_{>2} \rrbracket = \lambda P : |P| > 2.\lambda Q.P \subseteq Q$

Suppose, alternatively, that UG does not allow $[[every_{>2}]]$ to be written as in (68) – for example, because of a property like the following:

(69) Property of UG: The symbol '>' is not a primitive that can be used in meaning representations of quantifiers.

If the symbol '>' cannot be used, the competition is no longer between [[every]] and the representation in $[[every_{>2}]]$, but between [[every]] and any remaining representations in the child's hypothesis space that are extentsionally equivalent to $[[every_{>2}]]$. Another way of writing the same quantifier without the symbol '>' is using a sequence of conjunctions, given in (70), again alongside [[every]].

(70) a.
$$\llbracket every \rrbracket = \lambda P : P \neq \emptyset. \lambda Q.P \subseteq Q$$

b. $\llbracket every'_{>2} \rrbracket = \lambda P : P \neq \emptyset \land |P| \neq 1 \land |P| \neq 2.\lambda Q.P \subseteq Q$

The representation in (70b) is extensionally equivalent to the representation of $\llbracket every_{>2} \rrbracket$ in (68), but the two representations differ in their complexity. Assuming the property of UG in (69), a child guided by a preference for simpler representations (e.g., representations with fewer symbols) will now correctly choose $\llbracket every \rrbracket$ over $\llbracket every_{>2} \rrbracket$ and solve the superset problem.

In sum, a theory of UG with the property in (69) can correctly account for children's choice of [[every]] over the alternative when combined with a learning bias for simplicity. Under theories of UG without the property in (69), children's acquisition of every over the alternative in (68) remains a mystery. This discussion shows a way in which our finding regarding the superset problem in the acquisition of every can be used to draw inferences regarding UG, and specifically regarding how representations of quantifier meanings can be written.

As mentioned above, our brief discussion is not meant to provide a definitive conclusion regarding the consequences of the inductive problem presented in this section for language acquisition. Instead, we aimed to illustrate how the inductive problem we presented can lead to concrete conclusions regarding acquisition that we find interesting, such as possible restrictions on the child's hypothesis space, choices regarding the primitives available for the child in constructing meaning representations, or inductive biases such as simplicity. We leave a more systematic exploration of these possibilities for future research.

4 Conclusion

Our findings suggest an asymmetry between the subset problem and the superset problem in the acquisition of *every*. We first discussed the subset problem and showed that the input for semantic learning is rich enough to eliminate overlygeneral hypotheses about the meaning of *every*. Specifically, we saw that if *every* had an existential meaning instead of a universal, a significant percentage of utterances with *every* in the child's input (17.5%) would have been too weak to be

cooperative utterances and would have violated pragmatic constraints on assertions and questions. This finding means that the input in semantics is qualitatively different from the input in syntax and phonology, domains in which systematic negative evidence against overly-general hypotheses is unavailable, and in which the null theory of language acquisition (according to which no induction is involved in learning acquisition) has been rejected. We then discussed some instances of the superset problem in the acquisition of *every*. We showed that as opposed to overly-general hypotheses, usages of *every* in the child's input contain no evidence against some overly-specific hypotheses about the meaning of *every* such as [[every>2]]. Nevertheless, the child induces the English meaning of every. We suggested directions for future research that can use this inductive problem to draw conclusions regarding the hypothesis space of quantifier meanings and the primitive symbols that can be used in writing quantifier representations.

While this paper has focused on the acquisition of *every*, our findings are relevant for semantic acquisition beyond every. Our finding regarding the role of pragmatic constraints in addressing the subset problem is general: weaker hypotheses about word meanings can be too weak to be cooperative, which could make such hypotheses inconsistent with the child's input. Our discussion suggests a general recipe for examining this question in cases other than every by considering weaker alternative meanings and examining the systematicity of evidence against them in the input. Our exploration of the superset problem can also be repeated in cases other than *every*, as highlighted by the comparison between our [every>2] and Goodman's grue: strictly more complex representations can result in stronger meanings that overfit the observed data. If such meanings are not too strong to be systematically inconsistent with the data, the result is a case of non-trivial induction to the more general meaning performed by the child. We hope that further exploration of the relationship between the semantic hypothesis space and the child's input will help advance our understanding of semantic acquisition in general, and of UG in particular.

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