# Higher-order readings of wh-questions

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**Abstract** In most cases, a wh-question expects an answer that names an entity in the set denoted by the extension of the wh-complement. However, evidence from questions with necessity modals and questions with collective predicates argues that sometimes a wh-question must be interpreted with a higher-order reading, in which this question expects an answer naming a generalized quantifier.

This paper investigates the distribution and compositional derivation of higher-order readings of wh-questions. First, I argue that the generalized quantifiers that can serve as semantic answers to wh-questions must be homogeneously positive. Next, on the distribution of higher-order readings, I observe that questions in which the wh-complement is singular-marked or numeral-modified can be responded by elided disjunctions but not by conjunctions. I further present two ways to account for this disjunction-conjunction asymmetry. In the uniform account, these questions admit disjunctions because disjunctions (but not conjunctions) may satisfy the atomicity requirement of singular-marking and the cardinality requirement of numeral-modification. In the reconstruction account, the wh-complement is syntactically reconstructed, which gives rise to local uniqueness and yields a contradiction for conjunctive answers.

**Keywords:** wh-words, questions, higher-order readings, quantifiers, Boolean coordinations, number-marking, uniqueness, collectivity, reconstruction

### 1. Introduction

A wh-question (with who, what, or which-NP) expects an answer that names either an entity in the set denoted by the wh-complement or a generalized quantifier (GQ) ranging over of a subset of this set. This requirement is especially robustly seen with short answers to questions. For example in (1), the speaker uttering the short answer (1a) is committed to that the mentioned individual is a math professor (Jacobson 2016). Moreover, this inference projects over quantification: the most prominent reading of the disjunction (1b) yields that both mentioned individuals are math professors.<sup>1</sup>

(1) Which math professor left the party at midnight?

a. Andy.  $\rightsquigarrow$  Andy is a math professor.

b. Andy or Billy.  $\rightsquigarrow$  Andy and Billy are math professors.

To capture this question-answer relation, it is commonly assumed that wh-phrases are functions (e.g., existential  $(\exists$ -)quantifiers or function domain restrictors) over first-order predicates, and that the domain for quantification or abstraction is the set denoted by the extension of the wh-complement. An LF schema for wh-questions is given in (2): the wh-phrase combines with a first-order function denoted by the scope and binds an e-type variable

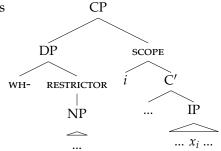
<sup>&</sup>lt;sup>1</sup>Elided disjunctions are scopally ambiguous relative to this commitment, as described in (i). This paper considers only the reading (ia). The other reading can be derived by accommodating the presupposition locally.

<sup>(</sup>i) a. Andy and Billy are math professors, and one of them left the party at midnight.

b. Either Andy or Billy is math professor who left the party at midnight.

inside the question nucleus (viz., the IP).

(2) LF schema of wn-questions



In this view, the root denotation of a wH-question is either a one-place function defined for values in the extension of the NP-complement, as assumed in categorial approaches and structured meaning approaches, or a set of propositions naming such values, as assumed in propositional approaches (such as Hamblin-Karttunen Semantics, Partition Semantics, and Inquisitive Semantics). For convenience in describing the relation between wH-phrases and wH-questions in meaning, the following presentation follows categorial approaches (Hausser and Zaefferer 1979; Hausser 1983; among others). The core ideas of this paper, however, are independent from the assumptions of categorial approaches on defining and composing questions.

Categorial approaches define questions as functions and wH-phrases as function domain restrictors. In (3), for example, in forming the question *which student came?*, the wH-phrase *which student* applies to a first-order function defined for any individuals and returns a more restrictive first-order function that is only defined for atomic students. I henceforth call this functional denotation of a question a "Q-function" and the domain of a Q-function a "Q-domain".

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(3) a. [which student] = \lambda P_{\langle e,t \rangle} \lambda x_e: student(x).P(x)
b. [which student came?] = [which student](\lambda x_e.came(x))
= \lambda x_e: student(x).came(x)
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Treating short answers as bare nominals, categorial approaches regard the relation between matrix questions and short answers as a simple function-argument relation — the Q-function serves as a function for an entity-denoting answer and an argument for a GQ-denoting answer. For example, in (4a), applying the Q-function denoted by the question to an individual denoted by the short answer yields that this individual came and the presupposition that this individual is a student. In (4b), in contrast, since the disjunctive answer has a complex type  $\langle et,t\rangle$ , the question-answer relation is flip-flopped into an argument-function relation. Applying the Boolean disjunction  $a^{\uparrow} \cup b^{\uparrow}$  (i.e., the union of two Montagovian individuals<sup>2</sup>)

The conjunctive *and* is commonly treated ambiguously as either an **intersection** operator ' $\cap$ ' (for combining sets, in analogy to the union meaning of *or*) or a **summation** operator ' $\oplus$ ' (for combining entities) (Link 1983; Hoeksema 1988). Another view is to interpret *and* uniformly and attribute the ambiguity to covert operations. For example, Winter (2001) and Champollion (2016b) treat *and* unambiguously an intersection operator and use covert type-shifting operations to derive the summation-like reading.

<sup>&</sup>lt;sup>2</sup> Disjunctions over set-denoting expressions are standardly treated as **unions** ' $\cup$ '. This idea follows a more general schema defined in Partee and Rooth 1983. Since entities are not sets, to be disjoined, they have to be first type-shifted into GQs of a conjoinable type  $\langle et, t \rangle$  via Montague-lift. Hence, in a disjunction of two referential DPs, or combines with two Montagovian individuals and returns their union (Keenan and Faltz 1985: Part 1A).

<sup>(</sup>i) For any meaning  $\alpha$  of type  $\tau$ , the Montague-lifted meaning is  $\alpha^{\uparrow}$  (of type  $\langle \tau t, t \rangle$ ) such that  $\alpha^{\uparrow} =_{\mathrm{df}} \lambda m_{\langle \tau, t \rangle}.m(\alpha)$ .

to the Q-function yields the presupposition that both of the disjoined individuals a and b are students.

The above discussion considers **first-order readings** of wH-questions. If a question has a first-order reading, the Q-function denoted by this question is a first-order function. However, as first observed by Spector (2007, 2008), in some cases a wH-question can only be properly addressed by an answer that specifies a GQ. For example in (5), the elided disjunction in the answer is interpreted under the scope of the necessity modal *have to*. Spector argues that to obtain this narrow scope reading, *which books* should bind a higher-order trace (of type  $\langle et, t \rangle$ ) across the necessity modal, so that a disjunction can be semantically reconstructed to a scopal position under the modal.

(5) Which books does John have to read? The French novels or the Russian novels. The choice is up to him.  $(\Box \gg or)$ 

Examples like (5) show that questions can also have **higher-order readings**, in which the yielded Q-functions take GQs as arguments. This paper investigates into those higher-order readings.

The rest of this paper is organized as follows. Section 2 discusses cases where a question must be interpreted with a higher-order reading, drawn on evidence from questions with modals and/or collective predicates. Section 3 examines what higher-order meanings can be members of a Q-domain and be used as semantic answers to higher-order questions. I argue that the higher-order meanings involved in a Q-domain must be "homogeneously positive". Sections 4 and 5 investigate the derivation and distributional constraints of higher-order readings. These two sections focus on a puzzling conjunction-disjunction asymmetry — questions with a singular-marked or numeral-modified wh-phrase reject conjunctive answers but admit disjunctive answers. I present two ways to account for this asymmetry, including a uniform account and a reconstruction account. Section 6 concludes.

# 2. Evidence for higher-order readings

Saying that a question has a first-order reading yields two predictions regarding to its GQ-naming answers. First, the named GQ must be interpreted with wide scope relative to any scopal expressions in the question nucleus. Second, the answer space (viz., the Hamblin set) of this question consists of only propositions denoted by the entity-naming answers. If an answer names a GQ, the proposition denoted by this answer is not in the answer space of this question, and the named GQ is not in the Q-domain; instead, those answers are derived by applying additional Boolean operations to propositions in the answer space.

This section presents counterexamples to both predictions, showing that first-order readings are insufficient. First, evidence from questions with necessity modals (e.g., which books does John have to read?) argues that sometime the Q-domain of a question must contain

Boolean disjunctions and existential quantifiers (Sect. 2.1). Second, evidence from questions with collective predicates (e.g., *which children formed one team?*) shows that sometimes the Q-domain of a question must contain Boolean conjunctions and universal quantifiers (Sect. 2.2). Finally, combinations of these two diagnostics rule in the Boolean coordinations of the aforementioned GQs (Sect. 2.3).

## 2.1. Non-reducibility: Evidence for disjunctions and existential quantifiers

In general, to completely address a question, one needs to provide the strongest true answer to this question (Dayal 1996). Hence, for an answer to be possibly complete, there must be a world in which this answer is the strongest true answer. As seen in (6), in responding to a basic wh-question, a disjunctive answer is always partial/incomplete — whenever the disjunctive answer is true, it is asymmetrically entailed by another true answer, namely, a/the true disjunct.

- (6) a. Which books did John read?
  - b. The French novels or the Russian novels.

Spector (2007, 2008) observes that, however, disjunctions can completely address wh-questions in which the nucleus contains a necessity modal (called "□-questions" henceforth). For example in (7), the elided disjunction is scopally ambiguous. If the disjunction takes scope over the necessity modal *have to*, the disjunctive answer has a partial answer reading. Alternatively, if interpreted under the scope of the modal, the elided disjunction can be regarded as a complete specification of John's reading obligations — there is not any specific book that John has to read, his only reading obligation is to choose between the French novels and the Russian novels. This narrow scope complete answer reading is also observed with existential quantifiers, as seen in (8).

- (7) a. Which books does John have to read?
  - b. The French novels or the Russian novels.
    - i. 'John has to read the French novels or the Russian novels. I don't know which exactly.' (Partial:  $or \gg \Box$ )
    - ii. 'John has to read the French novels or the Russian novels. The choice is up to him.' (Complete:  $\square \gg or$ )
- (8) a. Which books does John have to read?
  - b. At least two books by Balzac.
    - i. 'There are at least two books by Balzac that John has to read. I don't know what they are.' (Partial:  $\exists \gg \Box$ )
    - ii. 'John has to read at least two books by Balzac, which two (or more) to read is up to his own choice.' (Complete:  $\square \gg \exists$ )

To obtain the complete answer reading (7b-ii), the elided disjunctive answer must be treated as a GQ (i.e., the Boolean disjunction  $f^{\uparrow} \cup r^{\uparrow}$ ) and be reconstructed to a position under the scope of the necessity modal. Thus, Spector (2007) concludes that the  $\Box$ -question (7a) is ambiguous between a high reading and a low reading where "high" and "low" mean that the scope of the disjunction is wide and narrow relative to the modal, respectively. To highlight the contrast between these two readings with respect to the types of the yielded

Q-functions, I instead call the two readings the **first-order reading** and the **higher-order reading**, respectively. As paraphrased in (9), the first-order reading expects answers that specify an entity, while the higher-order reading expects answers that specify a GQ.

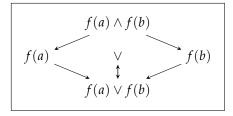
- (9) Which books does John have to read?
  - a. First-order reading:'For which book(s) *x* is such that John has to read *x*?'
  - b. Higher-order reading: 'For which a GQ  $\pi$  over books is such that John has to read  $\pi$ ?'

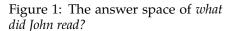
Spector assumes that the derivation of the higher-order reading involves **semantic reconstruction** (Cresti 1995; Rullmann 1995): the WH-phrase binds a higher-order trace  $\pi$  (of type  $\langle et,t\rangle$ ) across the necessity modal. Adapting this analysis to the categorial approach, I propose the LFs and Q-functions for the two readings as follows. (Subject-movement is ignored. '@' stands for the actual world, and 'smlo( $\pi$ )' stands for the smallest live-on set of  $\pi$ . The assumed Q-domain for the higher-order reading is subject to revision. For now, I just assume that this Q-domain is the set of GQs ranging over a set of books.<sup>3</sup> See Sect. 3 for refinements.) Observe that, for the higher-order reading, the GQ-denoting answer is interpreted at whatever scopal position that the higher-order wh-trace  $\pi$  takes.

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(10) First-order reading
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 $\Box$ -questions are useful in validating the existence of Boolean disjunctions in a Q-domain because the answer space of a  $\Box$ -question is not closed under disjunction. A proposition set Q is closed under disjunction if and only if for any two propositions p and q, if both p and q are members of Q, then the disjunction  $p \lor q$  is also a member of Q. The following figures illustrate the answer space of a plain episodic question and that of a  $\Box$ -question. f(x) abbreviates for the proposition  $\lambda w.read_w(j,x)$ . Arrows indicate entailments. The middle disjunctive symbol ' $\lor$ ' stands for the disjunction of the two atomic sentences; in specific, it stands for  $f(a) \lor f(b)$  in Figure 1 and  $\Box f(a) \lor \Box f(b)$  in Figure 2.

<sup>&</sup>lt;sup>3</sup>For any  $\pi$  of type  $\langle \tau t, t \rangle$  and set A of type  $\langle \tau, t \rangle$ , we say that  $\pi$  **lives on** A if and only if for every set B:  $\pi(B) \Leftrightarrow \pi(B \cap A)$  (Barwise and Cooper 1981), and that  $\pi$  **ranges over** A if and only if A is the **smallest live-on set** (SMLO) of  $\pi$  (Szabolcsi 1997). For example, the smallest live-on set of *some/every/no student* is the set of atomic students. These notions will be crucial for discussions on constraining what types of GQs should and should not be ruled into a Q-domain (see Sect. 3).





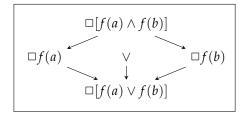


Figure 2: The answer space of *what does John have to read?* 

In Figure 1, the disjunctive answer  $f(a) \vee f(b)$  is semantically equivalent to the disjunction of the two individual answers f(a) and f(b). Hence, the disjunctive answer can never be the strongest true answer to the question — whenever the disjunctive answer is true, there will be another true answer, f(a) or f(b), asymmetrically entailing it. In contrast, in Figure 2, the disjunctive answer  $\Box[f(a) \vee f(b)]$  can be the strongest true answer since it is semantically weaker than the disjunction of the two individual answers  $\Box f(a)$  and  $\Box f(b)$ . For example, if John's only reading obligation is to read either a or b, the individual answers are false, and the disjunctive answer is the unique true answer and hence the strongest true answer.

The diagnostic given by Spector can be generalized to the following:  $\Box$ -questions may yield Q-functions that are "non-reducible" relative to disjunctions and existential quantifiers. The following defines reducibility, where '•' stands for the combinatory operation between the function  $\theta$  and a GQ:<sup>4</sup>

(12) A function  $\theta$  is **reducible** relative to a GQ  $\pi$  (of type  $\langle \tau t, t \rangle$ ) if and only if  $\theta \bullet \pi \Leftrightarrow \pi(\lambda x_{\tau}.\theta \bullet x^{\uparrow})$ .

The same as  $\Box$ -questions, the following questions, with a word expressing universal quantification, also have readings where the Q-function is not reducible relative to disjunctions or to existential quantifiers. ((13) and (14) are taken from Spector (2007).)

- (13) Attitude verbs
  - a. Which books did John demand that we read?
  - b. Which books is John certain that Mary read?
  - c. Which books does John **expect** Mary to read?
- (14) Modals
  - a. Which books is it **sufficient** to read?
  - b. Which books is John **required** to read?
- (15) Quantifiers
  - a. Which books did all of the students read?
  - b. Which books does John always/usually read?

<sup>&</sup>lt;sup>4</sup>The definition of the combinatory operation '•' varies by the semantic type of the function  $\theta$ . Let the GQ  $\pi$  be of type  $\langle \tau t, t \rangle$  where  $\tau$  is an arbitrary type, we have the following: (i) if  $\theta$  is of type  $\langle \tau tt, t \rangle$ , '•' stands for Forward Functional Application; (ii) if  $\theta$  is of type  $\langle \tau, t \rangle$ , '•' stands for Backward Functional Application; (iii) if  $\theta$  cannot compose with a GQ directly, then either '•' involves a type-shifting operation or  $\theta$  •  $\pi$  is undefined.

### 2.2. Stubborn collectivity: Evidence for conjunctions and universal quantifiers

Spector (2007, 2008) and Fox (2013) have assumed that a Q-domain may contain Boolean conjunctions, but they have not provided empirical evidence for this assumption. Clearly, the non-reducibility diagnostic generalized in (12) does not extend to Boolean conjunctions: the Q-functions of  $\Box$ -questions as well as those discussed in (13) to (15) are reducible relative to Boolean conjunctions.

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(16) a. [\lambda \pi. J \text{ has to read } \pi](f^{\uparrow} \cup r^{\uparrow}) \neq J \text{ has to read } f \vee J \text{ has to read } r
b. [\lambda \pi. J \text{ has to read } \pi](f^{\uparrow} \cap r^{\uparrow}) = J \text{ has to read } f \wedge J \text{ has to read } r
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This section introduces a new diagnostic for ruling in Boolean conjunctions. This diagnostic draws on the fact that questions with a stubbornly collective predicate (e.g., *formed a team*, *co-authored two papers*) may have answers naming Boolean conjunctions, and especially that stubborn collectivity in these questions does not trigger uniqueness.

First, to see what is stubborn collectivity, observe that the phrasal predicate *formed a/one team* admits a collective reading but not a covered/ (non-atomic) distributive reading. The sentence (17a) cannot be truthfully uttered in the given context, because it admits only a collective reading and this reading is false in the given scenario. In contrast, the plural counterpart *formed teams* admits a covered/ non-atomic distributive (or cumulative/ semi-distributive) reading and thus (17b) can be truthfully uttered.

- (17) (w: The four relevant children abcd formed exactly two teams in total: a + b formed one, and c + d formed one.)
  - a. #The children formed a/one team.
  - b.  $\sqrt{\text{The children formed teams}}$ .

The falsehood of (17a) is not improved even if the context has explicitly separated the four children into two pairs, as seen in (18).

(18) [Yesterday, the pair of children a + b competed against the pair of children c + d.] Today, the children (all) formed a/one team. (OK collective, #covered/distributive)

Hence, I call the predicate *formed a/one team* "stubbornly collective", in contrast to predicates like *lifted the piano* which admits both collective and covered/distributive readings. Stubborn collectivity is widely observed with quantized phrasal predicates of the form "V + counting noun", such as *formed one committee* and *co-authored two papers*.<sup>5</sup>

Second, for the absence of uniqueness effects, compare the sentences in (19a-b) in the same discourse. The declarative-embedding sentence (19a) suffers a presupposition failure, because the factive verb *know* embeds a false collective declarative. However, the sentence (19b), where *know* embeds the interrogative counterpart of this collective declarative, does not suffer a presupposition failure. Moreover, intuitively, (19b) implies that John knows precisely the component members of each team formed by the considered children, which is a conjunctive inference.

(19) (w: The four relevant children abcd formed exactly two teams in total: a + b formed one, and c + d formed one.)

 $<sup>^5</sup>$ A predicate P is **quantized** if and only if whenever P holds for x, P does not hold for any proper subpart of x (Krifka 1997). Formally:  $\forall x \forall y [P(x) \land P(y) \rightarrow [x \leq y \rightarrow x = y]]$ . Defining predicates as sets of events, Champollion (2016a) argues that distributive readings are not available with quantized phrasal predicates because the extension of a quantized verbal phrase is not closed under summation formation.

- a. # John knows [that the children formed a team].
- b.  $\sqrt{\text{John knows [which children formed a team]}}$ .
- c.  $\rightsquigarrow$  John knows that a + b formed a team and c + d formed a team.

The conjunctive inference in (19c) is quite surprising — where does the conjunctive closure come from? Clearly, no matter how we analyze collectivity, this conjunctive closure cannot come from the predicate *formed a team* or anywhere within the question nucleus, otherwise the embedded clause in (19a) would admit a covered/distributive reading and (19a) would be felicitous, contra fact. In contrast, I argue that this conjunctive closure is provided by the wh-phrase: the wh-phrase quantifies over a set of higher-order meanings including the Boolean conjunction  $(a \oplus b)^{\uparrow} \cap (c \oplus d)^{\uparrow}$ .

(20) Which children formed a team?

Higher-order reading: 'For which GQ  $\pi$  over children is such that  $\pi$  formed a team?'

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a. [CP which-children \lambda \pi_{\langle et, t \rangle} [PP \pi \lambda x_e [VP x formed a team ]]]
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\text{b. } \llbracket \text{wh-Q} \rrbracket = \lambda \pi_{\langle \textit{et}, \textit{t} \rangle} \colon \text{smlo}(\pi) \subseteq \textit{children}_@.\lambda w [\pi(\lambda \textit{x}_\textit{e}.\textit{f.a.team}_w(\textit{x}))]
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c. \llbracket \text{wh-Q} \rrbracket ((a \oplus b)^{\uparrow} \cap (c \oplus d)^{\uparrow})
= \{a \oplus b, c \oplus d\} \subseteq \text{children}_@.\lambda w [\text{f.a.team}_w (a \oplus b) \land \text{f.a.team}_w (c \oplus d)]
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One might suggest to ascribe the conjunctive closure to an operator outside the question denotation, such as Heim's (1994) answerhood-operator Ans-H. As schematized in (21), Ans-H contains a  $\cap$ -closure. It applies to an evaluation world w and a Hamblin set Q and returns the conjunction of all the propositions in Q that are true in w.

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(21) a. Ans-H(w)(Q) = \bigcap \{p \mid w \in p \in Q\}
b. \bigcap \{\lambda w. f.a. team_w(a \oplus b), \lambda w. f.a. team_w(c \oplus d)\}
= \lambda w. f.a. team_w(a \oplus b) \land f.a. team_w(c \oplus d)
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However, Ans-H is insufficient as it cannot capture the contrast with respect to uniqueness in (22). The question-embedding sentence (22b) is infelicitous because the embedded numeral-modified question (viz., the embedded question in which the wh-complement is numeral-modified) has a uniqueness presupposition which contradicts the context.

- (22) (w: The four relevant children abcd formed exactly two teams in total: a + b formed one, and c + d formed one.)
  - a.  $\sqrt{\text{John knows }}$  [which children formed a team].
  - b. # John knows [which two children formed a team].
    - *→ Only two of the children formed any team.*

Uniqueness presuppositions in wh-questions are standardly explained by "Dayal's presupposition" — a question is defined only if it has a strongest true answer (Dayal 1996). For a question with a Hamblin set Q, its strongest true answer is the true proposition in Q entailing all the true propositions in Q. In the rest of this subsection, I argue that the contrast between (22a-b) is due to the following: in (22a), the embedded simple plural-marked question has a strongest true answer in the given discourse, while in (22b), the embedded numeral-modified question does not.

Dayal's presupposition is originally motivated to explain the uniqueness requirement of singular-marked wн-questions (i.e., questions in which the wн-complement is singular-marked). In Srivastav 1991, she observes that a singular-marked wн-question cannot have

multiple true answers. For illustration, compare the examples in (23). The continuation in (23a) is infelicitous because the preceding singular-marked wh-question has a uniqueness presupposition that only one of the children came. In contrast, this inconsistency disappears if the singular wh-phrase *which child* is replaced with the plural wh-phrase *which children* or the bare wh-word *who*, as seen in (23b-c).

- (23) a. "Which child came? # I heard that many children came."
  - b. "Which children came? I heard that many children came."
  - c. "[Among the children,] who came? I heard that many children came."

To capture the uniqueness presuppositions of singular-marked wh-questions, Dayal (1996) defines a presuppositional answerhood-operator Ans-D which checks the existence of the strongest true answer. Applying Ans-D to a world w and the Hamblin set Q returns the unique strongest of the propositions in Q true in w and presupposes the existence of this strongest true proposition.

(24) Ans-D(w)(Q) = 
$$\exists p[w \in p \in Q \land \forall q[w \in q \in Q \rightarrow p \subseteq q]].$$
  
 $\iota p[w \in p \in Q \land \forall q[w \in q \in Q \rightarrow p \subseteq q]]$ 

Adopting the ontology of individuals by Sharvy (1980) and Link (1983), Dayal assumes that the Hamblin set of a singular-marked wh-question is smaller than that of its plural-marked counterpart. The ontology of individuals assumes that both singular and plural nouns denote sets of entities. In particular, a singular noun denotes a set of atomic entities, while a plural noun denotes a set consisting of both atomic and sum entities.<sup>6</sup> If sums are defined in terms of part-hood relation, this ontology can be represented as in Figure 3. Letters abc each denote an atomic child. Lines indicate part of relations from bottom to top. For example, atomic entities a and b are parts of their sum  $a \oplus b$ .

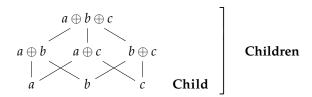


Figure 3: Ontology of individuals (Sharvy 1980; Link 1983)

Accordingly, as illustrated in (25), the Hamblin set of the singular-marked wh-question includes only propositions naming an atomic child, while the Hamblin set of the corresponding plural-marked wh-question includes also propositions naming a sum of children.  $Q_w$  stands for the set of propositions in Q that are true in w, namely, the Karttunen set in w. As a result, in a discourse where both Andy and Bill came, (25b) has a strongest true answer  $\lambda w.came_w(a \oplus b)$  while (25a) does not, and then employing Ans-D in (25a) gives rise to a presupposition failure. To avoid this presupposition failure, the singular-marked wh-question (25a) can only be felicitously uttered in a world where only one of the children came, which therefore explains its uniqueness requirement.

<sup>&</sup>lt;sup>6</sup>The view of treating plurals as sets ranging over not only sums but also atomic elements is called the "inclusive" theory of plurality (Sauerland et al. 2005, among others), as opposed to the "exclusive" theory which defines plurals as denoting sets consisting of only non-atomic elements. Whether plurals are treated inclusive or exclusive is not crucial in this paper. The following presentation follows the inclusive theory.

- (25) (w: Among the considered children, only Andy and Billy came.)
  - a. Which child came?

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i. Q = \{\lambda w. \mathit{came}_w(x) \mid x \in \mathit{child}\}
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- ii.  $Q_w = \{\lambda w.\mathsf{came}_w(a), \lambda w.\mathsf{came}_w(b)\}$
- iii. Ans-D(w)(Q) is undefined
- b. Which children came?

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i. Q = \{\lambda w. came_w(x) \mid x \in children\}
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- ii.  $Q_w = \{\lambda w.\mathsf{came}_w(a), \lambda w.\mathsf{came}_w(b), \lambda w.\mathsf{came}_w(a \oplus b)\}$
- iii. Ans-D(w)(Q) =  $\lambda w$ .came<sub>w</sub>( $a \oplus b$ )

It is also straightforward that, to account for the uniqueness presupposition, the Q-domain yielded by a singular-marked wh-phrase must exclude Boolean conjunctions such as  $a^{\uparrow} \cap b^{\uparrow}$ . Otherwise, the singular-marked wh-question (25a) would admit conjunctive answers like  $\lambda w.came_w(a) \wedge came_w(b)$  and would not be subject to uniqueness, contra fact.<sup>7</sup>

Numeral-modified wh-questions also have a uniqueness presupposition. For example, the numeral-modified question in (26a) implies that only two of the children came, and the one in (26b) implies that only two or three of the children came. Both inferences contradict their continuations.

- (26) a. "Which two children came? # I heard that three children did."
  - b. "Which two or three children came? # I heard that five children did."

Dayal's account of uniqueness easily extends to numeral-modified wн-questions. As seen in (27), for a question of the form "which N-children came?" where N is a cardinal numeral read as 'exactly N', Dayal's presupposition is satisfied only if exactly N of the children came. If the number of children who came is smaller than N, this question has no true answer (viz.,  $Q_w = \emptyset$ ); if the number of children who came is larger than N, the question does not have a strongest true answer.

(27) (w: Among the considered children, only Andy, Billy, and Clark came.) Which two children came?

```
a. Q = \{\lambda w. came_w(x) \mid x \in 2\text{-children}_{@}\}
```

b. 
$$Q_w = \{\lambda w. \mathsf{came}_w(a \oplus b), \lambda w. \mathsf{came}_w(a \oplus c), \lambda w. \mathsf{came}_w(b \oplus c)\}$$

(i) Quién formó un grupo? who.sg formed.sg a group 'Who formed a group?'

a. Los estudiantes. b. Los estudiantes y los profesores. the students the students and the professors.

The answer (ib) has a conjunction reading that the students formed a group and the professor formed a group. The felicity of this answer shows that the  $qui\acute{e}n$ -question admits answers naming Boolean conjunctions over non-atomic elements. Alonso-Ovalle & Rouillard thus conclude that  $qui\acute{e}n$  is number-neutral in meaning and is semantically ambiguous — it ranges over either a set of atomic and non-atomic individuals or a set of Boolean conjunctions and disjunctions.

<sup>&</sup>lt;sup>7</sup>Drawing on facts from Spanish *quién* 'who.sc' which is singular-marked but does not trigger uniqueness (Maldonado 2020), Elliott et al. (2020) by contrast propose that *quién*-questions admit also higher-order readings, in which the yielded Q-domain ranges over a set of Boolean conjunctions over atomic elements. Alonso-Ovalle and Rouillard (2019) argue against this view: as seen in (i), *quién* 'who.sc' can be used to combine with a stubbornly collective predicate *formó un grupo* 'formed.sc a group', and the formed question expects to specify the component members of one or more groups.

c. Ans-D(w)(Q) is undefined

The same as in a singular-marked wh-question, the uniqueness effect shows that the Q-domain of a numeral-modified wh-question does not contain Boolean conjunctions; otherwise, (27) would have a strongest true answer based on  $(a \oplus b)^{\uparrow} \cap (a \oplus c)^{\uparrow} \cap (b \oplus c)^{\uparrow}$ .

Return to the contrast of question-embeddings in (22), repeated below:

- (28) (w: The children abcd formed two teams in total: a + b formed one, and c + d formed one.)
  - a.  $\sqrt{\text{John knows }}$  [which children formed a team].
  - b. # John knows [which two children formed a team].
    - *→ Only two of the children formed any team.*

The contrast is explained if we assume that the Q-domain of a basic plural-marked wh-question contains Boolean conjunctions, while that of a numeral-modified wh-question does not. More specifically, in (28a), the Q-domain yielded by which children includes Boolean conjunctions and hence the embedded question which children formed a team admits conjunctive answers. In the given scenario, the Boolean conjunction  $(a \oplus b)^{\uparrow} \cap (c \oplus d)^{\uparrow}$  yields the strongest true answer. In contrast, in (28b), the Q-domain yielded by which two children consists of only pluralities denoting sums of two children (e.g.,  $a \oplus b$  and  $c \oplus d$ ), and hence the embedded question in (28b) has two true answers including  $\lambda w.f.a.team_w(a \oplus b)$  and  $\lambda w.f.a.team_w(c \oplus d)$ , but neither of them counts as the strongest true answer. In conclusion, (28b) is infelicitous because the embedded question does not satisfy Dayal's presupposition, and this presupposition failure projects over the factive predicate know.<sup>8</sup>

It is worthy noting that the argumentation for ruling in Boolean conjunctions is not totally dependent on whether using Dayal's presupposition to explain the uniqueness effects in singular-marked and numeral-modified wн-questions — any account of uniqueness has to explain the contrast between *which children* and *which two children* in admitting Boolean conjunctions. Recent literature has found evidence for other ways to encode or derive uniqueness (Uegaki 2018, 2020; Hirsch and Schwarz 2020; Fox 2018, 2020). For example, to account for the projection of uniqueness presuppositions and existential presuppositions in question-embeddings, Uegaki (2018, 2020) argues to encode the uniqueness inference within the question nucleus (details of the arguments omitted). Moreover, as we will see in section 5.1, Hirsch and Schwarz (2020) observe that in questions with a possibility modal, the uniqueness inference triggered by a singular-marked wн-phrase can be interpreted under the scope of the possibility modal. In line with Rullmann and Beck (1998), Uegaki and

The QPM principle, however, predicts that the wh-phrase in any non-modalized question cannot range over GQs. For example, if the question *who left* admits a higher-order reading, its Hamblin set should contain plain disjunctions such as  $\lambda w.left_w(a) \lor left_w(b)$ , which cannot be paired with any partition cell by exhaustification, violating QPM. To account for the absence of uniqueness in *which children formed a team*, Fox assumes that here *which children* ranges over a set of higher-order pluralities, not over a set of GQs. For example, in Fox's account, the conjunctive answer a+b and c+d is interpreted as  $\{\{a,b\},\{c,d\}\}$ , not as  $(a\oplus b)^{\uparrow}\cap (c\oplus d)^{\uparrow}$ .

<sup>&</sup>lt;sup>8</sup>In contrast to my analysis, Fox (2020) assumes higher-order pluralities to account for the data in (22)/(28). He proposes to get rid of Dayal's presupposition and accounts for the uniqueness effects based on the Question Partition Matching (QPM) Principle. According to this principle, a singular-marked wн-question is only acceptable in context sets where its uniqueness presupposition is satisfied. Moreover, Fox argues that QPM can better account for the unavailability of higher-order readings in questions with a negative island as well as the modal obviation effects of higher-order readings in those questions (details of the arguments are omitted).

 <sup>(</sup>i) Question Partition Matching (Fox 2018, 2020)
 For any question with a Hamblin set Q, if it induces a partition P in a context set A, this question is acceptable in A if and only if: (i) every cell in P is identical to the exhaustification of a proposition in Q; and conversely (ii) every proposition p in Q is such that the exhaustification of p is identical to a cell in P.

Hirsch and Schwarz propose that uniqueness is introduced by the lexicon of a copy of the which-determiner that appears within the nucleus. For this account to explain the contrast between *which children* and *which two children*, it still has to assume that *which children* may range over Boolean conjunctions, while *which two children* cannot. In section 5.3, I will present a way to account for the unavailability of Boolean conjunctions in singular-marked and numeral-modified wh-questions while encoding uniqueness locally.

### 2.3. Evidence for complex GQ-coordinations

Previous sections have provided two diagnostics for simplex GQs. The diagnostic based on non-reducibility validates the existence of Boolean disjunctions and existential quantifiers in a Q-domain. The diagnostic based on stubbornly collectivity provides evidence for ruling in Boolean conjunctions and universal quantifiers. Combining these two diagnostics, the following shows that a Q-domain also contains complex GQ-coordinations:

Context: The eight students enrolled in a class are separated into four pairs by year and major. As part of the course requirement, each pair of students has to co-present one paper this or next week. Moreover, the instructor requires the presentations in each week to be given by students having the same major.

junior linguists: 
$$\{a_1, b_1\}$$
 junior philosophers:  $\{a_2, b_2\}$  senior linguists:  $\{c_1, d_1\}$  senior philosophers:  $\{c_2, d_2\}$ 

- (29) a. Guest: "[In your class,] which students have to present a paper together this week?"
  - b. Instructor: "The two junior linguists and the two senior linguists, OR, the two junior philosophers and the two senior philosophers."

The question raised by the guest involves a necessity modal *have to* as well as a stubbornly collective predicate *present a paper together* (abbreviated as 'p.a.p.t.'). The answer provided by the instructor can be unpacked as follows: the disjunctive answer conveys overall the free choice inference (30a), and the choices are specified as in (30b-c).

- (30) a. The presentations this week have to be given by either the linguists or the philosophers. They can be given by the linguists, and they can be given by the philosophers.
  - b. If the presentations are given by the linguists,  $a_1 \oplus b_1$  will p.a.p.t., and  $c_1 \oplus d_1$  will p.a.p.t..
  - c. If the presentations are given by the philosophers,  $a_2 \oplus b_2$  will p.a.p.t., and  $c_2 \oplus d_2$  will p.a.p.t..

To derive the free choice inference (30a), the disjunction must be interpreted under the scope of the necessity modal. Further, since the predicate *present a paper together* is stubbornly collective, to derive the conjunctive inferences in (30b-c), each disjunct/choice must be understood as naming a Boolean conjunction over two pairs of students. In sum, the answer should be interpreted with the following scopal pattern:  $\Box \gg or \gg and \gg a$  *paper*. To derive this scopal pattern, the nucleus of this question should contain a higher-order wh-trace between the necessity modal and the stubbornly collective predicate, as in (31). The answer of the instructor should be interpreted as a Boolean disjunction over two Boolean conjunctions, namely,  $((a_1 \oplus b_1)^{\uparrow} \cap (c_1 \oplus d_1)^{\uparrow}) \cup ((a_2 \oplus b_2)^{\uparrow} \cap (c_2 \oplus d_2)^{\uparrow})$ .

(31) [CP which-students  $\lambda \pi_{\langle et, t \rangle}$  [PP have-to [ $\pi \lambda x_e$  [VP x present a paper together]]]]

### 2.4. Interim summary

To sum up, this section discusses cases where a wh-question must be interpreted with a higher-order reading and provides two diagnostics to rule in higher-order meanings into a Q-domain. The first diagnostic is based on narrow scope readings of GQ-naming answers to questions in which the Q-function is non-reducible relative to the named GQs. Results of this diagnostic rule in Boolean disjunctions and a class of existential quantifiers. The second diagnostic is based on the absence of uniqueness effects in questions with a stubbornly collective predicate. This diagnostic rules in Boolean conjunctions and universal quantifiers. In addition, combining these two diagnostics, I further show that a Q-domain contains also complex GQ-coordinations.

## 3. Constraints on the Q-domain

The previous section has shown that the Q-domain of a wh-question may contain Boolean disjunctions, conjunctions, a class of existential quantifiers, universal quantifiers, as well as their Boolean coordinations. One might wonder whether we can make the following generalization:

In a higher-order reading, the Q-domain yielded by a wh-phrase consists of all the GQs ranging over a subset of the set denoted by the extension of the wh-complement as well as the Boolean combinations of these GQs.

In this section, I will show that this generalization is too strong. Spector (2007, 2008) provides some counterexamples to this generalization and argues that the GQs included in a Q-domain must be **increasing**. Extending Spector's diagnostic to a broad range of non-monotonic GQs(-coordinations), I show that the increasing-ness requirement is too strong: in some higher-order readings, the Q-domain of a wH-questions includes not only increasing GQs but also some non-monotonic GQs. I also find that not all non-monotonic GQs can serve as semantic answers. To capture these observations, I argue that whether a higher-order meaning can be ruled into a Q-domain and be used as a semantic answer to a higher-order wH-question is determined by its **positiveness** (roughly, the property of ensuring existence with respect to certain quantification domain, see Sect. 3.2): the higher-order meanings involved in a Q-domain must be homogeneously positive. <sup>10</sup>

# 3.1. Completeness Tests and The Increasing-ness Constraint

Whether a meaning is included in the Q-domain of a question can be examined by the **Completeness Test** generalized in (32). This test draws on a deductive relation between attitudes held towards a question and attitudes held towards the answers to this question: the

- (i) For any  $\pi$  of type  $\langle et, t \rangle$ :
  - a.  $\pi$  is **increasing** if and only if  $\pi(A) \Rightarrow \pi(B)$  for any sets of entities A and B:  $A \subseteq B$ ;
  - b.  $\pi$  is **decreasing** if and only if  $\pi(A) \leftarrow \pi(B)$  for any sets of entities A and B:  $A \subseteq B$ ;
  - c.  $\pi$  is **non-monotonic** if and only if  $\pi$  is neither increasing nor decreasing.

<sup>&</sup>lt;sup>9</sup>Monotonicity of GQs is defined as follows:

 $<sup>^{10}</sup>$ The issues and proposals in sections 4 and 5 are independent from the findings in this section. Leisure readers may jump to the interim summary in section 3.4.

question-embedding sentence x knows Q implies that x knows the complete true answer to the embedded question Q. The complete answer to a question is the strongest true proposition in the Hamblin set of this question (Dayal 1996); hence, if a proposition p is true but is not entailed by the complete true answer to Q, p is not in the Hamblin set of Q.

(32) The Completeness Test (generalized from Spector 2008)

For any proposition p that names a short answer  $\alpha$  to a question Q: if there is a world in which both p and x *knows* Q are true but x *knows* p is not true, then p is not in the Hamblin set of Q, and  $\alpha$  is not in the Q-domain of Q.

For simple illustration, consider the truth conditions of the question-embedding sentence (33b) under the context described in (33a). Strikingly, there is a reading of (33b) in which this sentence implies that Sue knows John's reading obligation (a-i), but not that she knows (a-ii); Sue can be ignorant about whether John has to read any Russian novels. (Note that Sue cannot have a false belief that John has to read some Russian novels, due to a separate "False-answer Sensitivity" condition. See details in footnote 12.)

- (33) a. Context: John's summer reading obligations include the following:(i) he has to read at least two French novels; (ii) he must read no Russian novel
  - (since he has already read too many Russian novels).

    b. Sue knows which books John has to read this summer.
    - $\rightsquigarrow$  Sue knows (a-i).

Given this contrast, Spector (2008) proposes that the GQs used as direct semantic answers to higher-order questions must be **increasing**. 'x knows Q' implies that x knows the complete/strongest true answer to Q; therefore, that Sue can be ignorant about John's reading obligation (a-ii) excludes the decreasing GQ *no Russian novel* and the non-monotonic

- (i) 'x knows Q' is true if and only if
  - a. *x* knows a/the complete true answer of Q.

(Completeness)

b. *x* does not have any false belief relevant to Q.

(False-Answer Sensitivity)

Second, the Completeness Test can only be used to determine what meanings should be <u>excluded</u> from a Q-domain, not what meanings should be <u>included</u> in a Q-domain. A bi-conditional characterization, namely, ruling in all the short answers that are not filtered out by the Completeness Test, could yield conflicting predictions. As I will show in Sect. 3.3, the Completeness Test shows that the higher-order Q-domain of the question *what does John have to read* contains the non-monotonic quantifier *exactly three books* but not the decreasing quantifier *less than four books*, even though the propositional answer yielded by the former (i.e., *John has to read exactly three books*) asymmetrically entails the propositional answer yielded by latter (i.e., *John has to read less than four books*).

<sup>13</sup>Strikingly, in contrast to (33b), the following two sentences with a concealed question or a definite description do imply that Sue knows both of John's summer reading obligations list in (33a).

- (i) a. Sue knows what John's summer reading obligations are.
  - b. Sue knows John's summer reading obligations.

<sup>&</sup>lt;sup>11</sup>The Completeness Test here considers only questions with at most one complete true answer, which is the strongest true answer. For mention-some questions which can have multiple complete true answers, see Fox (2013, 2018) and Xiang (2016b: chapter 2).

<sup>&</sup>lt;sup>12</sup>The Completeness Test does not aim to fully characterize the truth conditions of a question-embedding sentence or to exhaustively determine what can and cannot be included in a Q-domain. First, this test is only concerned about one aspect of the truth conditions of question-embedding sentences, namely, the Completeness condition. In addition to Completeness, question-embeddings are also subject to a False-Answer Sensitivity condition. (Klinedinst and Rothschild 2011; George 2013; Cremers and Chemla 2016; Uegaki 2015; Xiang 2016a,b; Theiler et al. 2018; among others) For example, for the sentence (33b) being true, Sue can be ignorant about whether John should read any Russian novels, but she cannot have the false belief that John should read some Russian novel(s).

GQ-coordination at least two French novels and no Russian novel from the Q-domain. <sup>14</sup> The higher-order reading of the question which books John has to read is then paraphrased as follows: 'for which increasing GQ  $\pi$  over books, it is the case that John has to read  $\pi$ ?'

## 3.2. The Positiveness Constraint

The following example makes a minimal change to the context of the Completeness Test in (33): John also has to read exactly two Chinese novels. With this added reading obligation, the embedding sentence (33'b) implies that Sue knows that John has to read exactly two Chinese novels, not just that Sue knows that John has to read at least two Chinese novels.

- (33') a. Context: John's summer reading obligations include the following:
  - (i) he has to read at least two French novels; (ii) he must read no Russian novel;
  - (iii) he has to read exactly two Chinese novels.
  - b. Sue knows which books John has to read.
    - → Sue knows (a-i) and (a-iii).

The example (34) applies the Completeness Test to a broader range of GQs. The game requirements listed in (34a) each name a GQ ranging over a set of cards. Among those GQs, (i-ii) are increasing, (iii-iv) are decreasing, and (v) is non-monotonic. These GQs are all interpreted with narrow scope relative to the necessity modal *require to*. The two exceptives are also read with narrow scope: (ii) implies that John is allowed not to play the largest black club in his hand, and (iv) implies that he is allowed to play the largest red heart in his hand. These exceptions leave the player the flexibility to determine which two Kings to play to fulfill the requirement (v). Intuitively, the question-embedding sentence (34b) implies that Sue knows about not only the game requirements (i-ii) but also (v). In particular, for the condition regarding to her knowledge towards (v), it is insufficient if Sue knows that John has to play at least two Kings but does not know that he cannot play more than two Kings.<sup>15</sup>

- (34) a. Context: John is playing a board game. This game requires him to play ...
  - i. least three black spades;

- ii. every black club except the largest black club in his hand;
- .

iii. at most three red diamonds;

•

- iv. no red heart except the largest red heart in his hand;

v. exactly two Kings;

- (i) a. Context: John's summer reading obligations consist of the following:
  - i. he has to read <u>no leisure book or more than two math books</u>. (In other words, John has to read more than two math books if he reads any leisure book.)
  - ii. he has to read none or all of the Harry Potter books, (because Harry Potter books must be rented in a bundle, and it would be a waste of money if he rents the entire series but only reads part of them.)

 $<sup>^{14}</sup>$ The Completeness Test in (i) considers two more cases that involve GQ-disjunctions (underlined). This test further confirms that Boolean disjunctions involving a decreasing GQ-disjunct must be excluded from a Q-domain.

<sup>&</sup>lt;sup>15</sup>The embedded question *which cards John has to play* also has a reading in which it admits all of the listed GQs, regardless of whether they are increasing, non-monotonic, or even decreasing. This reading is similar to what I observe with concealed questions and definite descriptions, as witnessed in footnote 13.

- b. Sue knows which cards John has to play.
  - $\rightsquigarrow$  Sue knows that John has to play (a-i), (a-ii), (a-v).
  - $\not \rightarrow$  Sue knows that John has to play (a-iii)/(a-iv).

In the above two tests, Spector's Increasing-ness Constraint overly rules out the non-monotonic GQs *exactly two Chinese novels* and *exactly two Kings*; thus, it fails to predict that (33'b) implies that Sue knows the reading obligation (33'a-iii), and that (34b) implies that Sue knows the game requirement (34a-v).

More generally, any monotonicity-based constraint faces a dilemma — we need a characterization that rules out non-monotonic GQ-coordinations such as *at least two French novels and no Russian novel* while not excluding simplex non-monotonic GQs like *exactly two Chinese novels*. <sup>16</sup> Moreover, note that it is also not just a matter of differentiating between complex and simplex non-monotonic GQs. For example, extending the Completeness Test (33) to other GQs, we can find that the Q-domain of the embedded question *which books John has to read* includes a few complex non-monotonic GQs such as the disjunction *exactly three French novels or exactly four Russian novels* and the conjunction *at least three French novels but no more than 20 (any kind of) novels*, but not the simplex non-monotonic GQ *less than three or more than ten novels*.

In contrast to Spector (2008), I propose that whether a GQ should be ruled into a Q-domain is determined by its "positiveness", not its monotonicity.

(35) The Positiveness Constraint (To be revised in (37)) GQs in the Q-domain of a wH-question must be positive.

A GQ being positive means that the meaning of this GQ ensures existence with respect to the set it ranges over (i.e., its smallest live-on set (smlo), see definitions in footnote 3). For example, at least two books and exactly two books, while having different monotonicity patterns, both entail some books and are thus positive. By contrast, the decreasing GQ at most two books and the non-monotonic GQ less than three or more than ten books do not entail some books and are thus not positive. A formal definition of positiveness is as follows, where  $\mathbb E$  stands for the existential quantifier (i.e.,  $\mathbb E =_{\mathrm{df}} \lambda Q \lambda P.Q \cap P \neq \emptyset$ ):

(36) For any  $\pi$  of type  $\langle et, t \rangle$ ,  $\pi$  is **positive** if and only if  $\pi \subseteq \mathbb{E}(\text{SMLO}(\pi))$ .

Table 1 compares monotonicity and positiveness for a list of coordinations over Montagovian individuals and simplex GQs that range over a set of books. a and b are two distinct atomic books. Observe that increasing ( $\uparrow_{MON}$ ) GQs are all positive, decreasing ( $\downarrow_{MON}$ ) GQs are all non-positive, while non-monotonic (N.M.) GQs can be either positive or non-positive.

<sup>&</sup>lt;sup>16</sup>I call a GQ "simplex" if it can be expressed as a single 'D+NP' phrase and "complex" otherwise. For example, the GQ-coordination *at least two books but no more than five books* is simplex because it can be equivalently expressed as *two to five books*.

Generalized quantifier $\pi$	$smlo(\pi)$	Increasing?	Positive?
$a^{\uparrow}$	{a}	Yes (↑ <sub>MON</sub> )	Yes
$a^{\Uparrow}\cap b^{\Uparrow}$ , $a^{\Uparrow}\cup b^{\Uparrow}$	$\{a,b\}$	Yes $(\uparrow_{MON})$	Yes
{at least, more than} two books	books	Yes $(\uparrow_{MON})$	Yes
every book except a	$book - \{a\}$	Yes $(\uparrow_{MON})$	Yes
{at most, less than, no more than} two books	books	No $(\downarrow_{MON})$	No
no book except <i>a</i>	$book - \{a\}$	No $(\downarrow_{MON})$	No
less than three or more than ten books	books	No (n.m.)	No
every or no book	book	No (n.m.)	No
exactly two books	books	No (n.м.)	Yes
two to four books	books	No (n.m.)	Yes
some but not all books	books	No (n.m.)	Yes
(exactly) two or four books	books	No (n.m.)	Yes
an even number of books	books	No (n.m.)	Yes

Table 1: Increasing-ness/monotonicity versus positiveness

#### 3.3. The Homo-Positiveness Constraint

Table 1 considers only coordinations over Montagovian individuals and simplex GQs. Benjamin Spector (pers. comm.) points out that, however, the Positiveness Constraint does not exclude many unwanted non-monotonic GQ-coordinations such as *every article and no book* and *some article and no book*: letting  $\pi = [every \ article \ and \ no \ book]$  and representing  $\pi$  as  $\{X \mid A \subseteq X \land B \cap X = \emptyset\}$ , we have  $\text{SMLO}(\pi) = A \cup B$  and  $\pi \subseteq \mathbb{E}(A \cup B)$ .

More generally, to determine whether a non-monotonic GQ can be included in a Q-domain, it is insufficient to examine existence with respect to the set that the entire GQ ranges over. Instead, thinking of a non-monotonic GQ as a Boolean coordination of increasing GQs and decreasing GQs (for example, every article and no book is the conjunction of every article and no book, and exactly two books is the conjunction of at least two books and no more than two books), we need to examine whether existence is ensured homogeneously with respect to both the following (A) and (B) sets:

- (A) the set that the coordinated increasing GQs range over;
- (B) the set that the coordinated decreasing GQs range over.

For example, the GQ-coordination *every article but no book* is excluded because it ensures existence with respect to articles but not to books. Intuitively, when existence is ensured with respect to set (A) but not to set (B), the exclusions expressed by the coordinated decreasing GQs would be irrelevant to the inclusions expressed by the coordinated increasing GQs. For

$$\text{(i)} \quad \left\{ X \; \left| \begin{array}{l} [A \subseteq (X \cap (A \cup B))] \wedge \\ [B \cap (X \cap (A \cup B)) = \varnothing] \end{array} \right\} \Leftrightarrow \left\{ X \; \left| \begin{array}{l} [A \subseteq X \wedge A \subseteq (A \cup B)] \wedge \\ [(B \cap (A \cup B)) \cap X = \varnothing] \end{array} \right\} \Leftrightarrow \pi$$

Next, the equivalence in (ii) shows that  $A \cup B$  is the smallest live-on set: for any a, replacing X with  $X \cap (A \cup B - \{a\})$  in the set description makes no change to the set being defined if and only if  $a \notin A \cup B$ .

(ii) 
$$\left\{ X \; \middle| \; \begin{array}{l} [A \subseteq (X \cap ((A \cup B) - \{a\}))] \land \\ [B \cap (X \cap ((A \cup B) - \{a\})) = \varnothing] \end{array} \right\} \Leftrightarrow \left\{ X \; \middle| \; \begin{array}{l} [A \subseteq X \land A \subseteq (A \cup B - \{a\})] \land \\ [(B \cap ((A \cup B) - \{a\})) \cap X = \varnothing] \end{array} \right\} \\ \Leftrightarrow \left\{ X \; \middle| \; \begin{array}{l} [A \subseteq X \land A \subseteq (A \cup B) \land a \notin A] \land \\ [(B - \{a\}) \cap X = \varnothing] \end{array} \right\} \\ \Leftrightarrow \pi \text{ if and only if } a \notin A \text{ and } a \notin B$$

<sup>&</sup>lt;sup>17</sup>The following explains why  $A \cup B$  is the smallest live-on set of  $\pi$ , where  $\pi = \{X \mid A \subseteq X \land B \cap X = \emptyset\}$ . First, the equivalence in (i) shows that  $A \cup B$  is a live-on set of  $\pi$ : replacing X with  $X \cap (A \cup B)$  in the set description does not change the set.

example, in the sentence *John has to read every article but no book*, how many books John has to read is irrelevant to how many articles he has to read. Hence, I strengthen the Positiveness Constraint (35) to (37). The definition of "homogeneously (homo-)positive" is given in (39).

# (37) The Homo-Positiveness Constraint (Final)

GQs in the Q-domain of a wH-question must be homogeneously positive.

In most GQ-coordinations, the GQs being coordinated cannot be semantically retrieved from their coordination. First, some GQs cannot be decomposed into a simple coordination of monotonic GQs. For example, the decomposition in (38a) has to involve at least disjunctions over conjunctions of monotonic GQs. Second, even for a GQ that can be decomposed into a simple coordination, there are multiple ways to decompose it, as seen in (38b-c).

Despite of this challenge, to determine whether a GQ-coordination is homo-positive, we just need to find out the involved strongest increasing and decreasing GQs which determine the lower and upper bounds of this GQ-coordination. I define homo-positiveness as in (39).  $\pi^+$  is the logically strongest increasing GQ entailed by  $\pi$  which determines the lower bound of  $\pi$ , and  $\pi^-$  is the logically strongest decreasing GQ entailed by  $\pi$  which determines the upper bound of  $\pi$ .<sup>18</sup>

```
(39) For any \pi of type \langle et, t \rangle, \pi is homogeneously positive if and only if a. \pi \subseteq \mathbb{E}(\mathsf{smlo}(\pi^+)), where \pi^+ =_{\mathsf{df}} \{P \mid \exists P' \subseteq P[\pi(P')]\}; b. \pi \subseteq \mathbb{E}(\mathsf{smlo}(\pi^-)), where \pi^- =_{\mathsf{df}} \{P \mid \exists P' \supseteq P[\pi(P')]\}.
```

Table 2 compares the three parameters (i.e., monotonicity, positiveness, and homopositiveness) for a broader range of GQs. The GQs are divided into three groups depending on whether they are simplex or have to be expressed as a GQ-disjunction or a GQ-conjunction. ABC are three sets of entities; C is a superset of A, and B is not. (The conjunction 'every A but no C' is ignored since it denotes an empty set.) Observe that whether a GQ  $\pi$  is homo-positive is independent from whether  $\pi$  is simplex/complex, disjoined/conjoined, (non-)increasing, (non-)monotonic, and upper (un-)bound.<sup>19</sup>

 $<sup>^{18}</sup>$ In an earlier version (Xiang 2019), treating positiveness and homogeneity as two separate conditions, I incorrectly claimed that any  $\pi$  of type  $\langle et,t\rangle$  can be decomposed into a conjunction  $\pi^+ \cap \pi^-$  and proposed that  $\pi$  is homogenous if  $\pi$  is monotonic or if  $\pi^+$  and  $\pi^-$  range over the same set. However, as pointed out by Lucas Champollion (pers. comm.), the equation  $\pi = \pi^+ \cap \pi^-$  does not hold for disjoined GQs such as an even number of cards and two or four cards.

 $<sup>^{19}</sup>$ If a GQ  $\pi$  is unbound, then one or both of the strongest GQs retrieved from  $\pi$  are trivial (viz., equivalent to  $D_{(e,t)}$ ), ranging over the discourse domain  $D_e$ . In specific, increasing GQs are upper-unbound, and decreasing GQs are lower-unbound.

<sup>(</sup>i) a. If  $\pi$  is upper-unbound, namely,  $\forall P[P \in \pi \to \exists P' \in \pi[P' \supseteq P]]$ , then  $\pi^- = D_{\langle e,t \rangle}$ . Example: at least two books, an even number of books, less than two or more than four books

b. If  $\pi$  is lower-unbound, namely,  $\forall P[P \in \pi \to \exists P' \in \pi[P' \subseteq P]]$ , then  $\pi^+ = D_{\langle e,t \rangle}$ . Example: less than two or more than four books, at most four books.

Generalized quantifier $\pi$	$\pi^+$	$\pi^-$	Mon?	Pos?	Homo-Pos?
at least 2 A	at least 2 A	$D_{\langle e,t \rangle}$	↑ <sub>MON</sub>	Yes	Yes
an even number of A	at least 2 A	$D_{\langle e,t\rangle}$	N.M.	Yes	Yes
exactly 2 A	at least 2 A	no more than 2 A	N.M.	Yes	Yes
exactly 2 to 4 A	at least 2 A	no more than 4 A	N.M.	Yes	Yes
exactly 2 or 4 A	at least 2 A	no more than 4 A	N.M.	Yes	Yes
no more than 4 A	$D_{\langle e,t \rangle}$	no more than 4 A	↓mon	No	No
less than 2 or more than 5 A	$D_{\langle e,t\rangle}$	$D_{\langle e,t \rangle}$	N.M.	No	No
every or no A	every A	no A	N.M.	No	No
every A or no B	every A	no B	N.M.	No	No
every A or no C	every A	no C	N.M.	No	No
every A but no B	every A	no B	N.M.	Yes	No
every A but no C					
at least 2 A but no more than 4 B	at least 2 A	no more than 4 B	N.M.	Yes	No
at least 2 A but no more than 4 C	at least 2 A	no more than 4 C	N.M.	Yes	Yes

Table 2: Monotonicity (Mon) versus Positiveness (Pos) versus Homo-positiveness

The generalizations from Table 1 still hold here. First, every GQ that is not positive is also not homo-positive. Second, for any increasing  $\pi$ , the retrieved  $\pi^-$  is trivial (viz.,  $\pi^- = D_{\langle e,t\rangle}$ , see fn. 19), and thus this increasing  $\pi$  being positive ensures  $\pi$  being homo-positive.

For non-monotonic GQs, however, the Homo-Positiveness Constraint yields a different prediction. The simplex non-monotonic GQ *exactly two books* is positive as well as homopositive: *exactly two books* entails *some books*, and the retrieved  $\pi^+$  *at least two books* and  $\pi^-$  *no more than two books* both range over the set of books. In contrast, the complex non-monotonic GQ-coordination *every article and no book* is positive but not homo-positive: the retrieved  $\pi^-$  *no book* ranges over the set of books, but *every article and no book* does not entail *some book*.<sup>20</sup>

### 3.4. Interim summary

To sum up, not all GQs can be used as semantic answers to wh-questions. In general, increasing GQs are qualified answers while decreasing GQs are not; however, there is a prominent higher-order reading of wh-questions in which some of the non-monotonic GQs are also qualified answers. Homo-positiveness captures the subtle difference among the non-monotonic GQs: the GQs that are homo-positive are more readily available to be used as

- (i) (Context: John has to read a book, but he is not allowed to read any leisure books.)Sue will tell John what he has to read.
  - a. Sue will tell John that he has to read a book.
  - b. Sue will tell John that he cannot read any leisure books.

I argue that the Homo-Positiveness Constraint still holds here. In the given scenario, the Completeness condition of the embedding sentence (i) should be (ic), which is stronger than (ia) and weaker than the conjunction of (ia-b). The complete true short answer to *what John has to read* is *some non-leisure book*, which is homo-positive.

(i) c. Sue will tell John that he has to read a non-leisure book.

<sup>&</sup>lt;sup>20</sup>A puzzle arises with non-monotonic GQ-coordinations such as *some book but no leisure book*, where the set that the coordinated decreasing GQ ranges over (viz., *leisure book*) is a proper subset of the set that the coordinated increasing GQ ranges over (viz., *book*). In (i), telling John that he has to read a book is clearly insufficient — John might incorrectly think that reading a leisure book suffices for his reading requirement. It is appealing to say that the question-embedding sentence (i) entails both (ia) and (ib), and that the complete answer to the embedded question names the GQ-coordination *some book but no leisure book*. However, this GQ-coordination is not homo-positive — it does not entail existence with respect to the set of leisure books.

semantic answers than GQs that are non-decreasing but not homo-positive. In this reading, the Q-domain yielded by the wh-phrase 'wh-A' is the set consisting of the homo-positive GQs ranging over a subset of A. I write this set as  ${}^{\text{H}}\!A$ .

(40) For a set of entities A, we have:  ${}^{\mathsf{H}}\!A = \{\pi_{\langle et, t \rangle} \mid \mathsf{sMLO}(\pi) \subseteq A \land \pi \text{ is homogeneously positive} \}, \text{ where } \pi \text{ is homogeneously positive if and only if } \pi \subseteq \mathbb{E}(\mathsf{SMLO}(\pi^+)) \text{ and } \pi \subseteq \mathbb{E}(\mathsf{SMLO}(\pi^-)).$ 

It is yet unclear where the Homo-Positiveness Constraint comes from. It could be in the lexicon of a type-shifting operator, presupposed by the higher-order *wh*-trace, a constraint on semantic reconstruction, or even just a matter of pragmatics. For now, I treat the H-shifter as a type-lifting operator syntactically presented within the wH-phrase and assume that it asserts homo-positiveness. If compelling evidence suggests that homo-positiveness does not come from the wH-phrase, the meaning of the H-shifter can be altered accordingly.

With the above assumptions, I attribute the first-order/higher-order ambiguity of a warquestion to the absence/presence of the H-shifter within the wh-phrase. (For distributional constraints of the H-shifter and where this operator is placed within a noun phrase, see Sect. 4.) As exemplified in (41), in the LF for the higher-order reading, a H-shifter is applied to the wh-complement, shifting the restrictor of the wh-determiner from a set of entities to a set of homo-positive GQs, and then the wh-phrase binds a higher-order trace  $\pi$  across the modal.

- (41) Which books does John have to read?
  - a. First-order reading

```
[cp which-books \lambda x_e [ip have-to [vp John read x ]]] [wh-Q] = \lambda x_e: x \in books_@.\Box[\lambda w.read_w(j,x)]
```

b. **Higher-order reading** ( $\square \gg \pi$ ) (Revised from (11)) [CP which-Hooks  $\lambda \pi_{\langle et,t \rangle}$  [PP have-to [ $\pi \lambda x_{\ell}$  [VP John read x ]]]] [WH-Q] =  $\lambda \pi_{\langle et,t \rangle}$ :  $\pi \in \text{Hooks}_@.\square[\lambda w.\pi(\lambda x_{\ell}.read_w(j,x))]$ 

# 4. Distributing the 'conjunction-admitting' higher-order reading

As discussed in Sect. 2.2, uniqueness effects in wh-questions show that higher-order readings are unavailable in questions where the wh-complement is singular-marked or numeral-modified. Aforementioned examples are collected in the following:

- - b. Which child came?
    - *→ Only one of the children came.*
  - c. Which two children came?→ Only two of the children came.
- - b. Which two children formed a team? 

    → Only one pair/group of children formed any team.

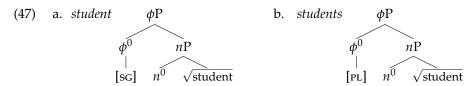
According to Dayal (1996), the singular-marked wH-question (42a) presupposes uniqueness because its strongest true answer exists only when it has exactly one true answer. This analysis

also extends to the numeral-modified wH-questions (42b-c), as argued in section 2.2. Adopting this analysis of uniqueness, I have concluded that these questions cannot take answers that name Boolean conjunctions, and further that these questions do not have a higher-order reading. Since the uniqueness effect is only associated with the diagnostic for ruling in Boolean conjunctions, I call the higher-order reading in which a wH-question admits conjunctive answers the 'conjunction-admitting' higher-order reading. In the above examples, this reading is available in (42a) and (43a) but not in the rest singular-marked/numeral-modified wH-questions. Section 5 will discuss another reading that rejects conjunctive answers but admits disjunctive answers, which I will the 'conjunction-rejecting' higher-order reading.

Strikingly, in contrast to a numeral-modifier, a PP-modifier does not block higher-order readings. Compare (45) and (46) for example. Although *students* (*who are*) in a group of two is semantically similar to *two students*, the embedded question in (46) does not presuppose uniqueness, and the question-embedding sentence can be naturally followed by an answer sentence that names a Boolean conjunction. This contrast suggests that the availability of higher-order readings is sensitive to the internal structure of the wh-complement.

- (44) I know  $\left\{\begin{array}{l} \textbf{who} \\ \text{which } \textbf{students} \end{array}\right\}$  presented a paper together,
  - a. ... the two boys.
  - b. ... the two boys and the two girls.
- (45) I know which two students presented a paper together,
  - a. ... the two boys.
  - b. # ... the two boys and the two girls.
- (46) I know which **students (who are) in a group of two** presented a paper together,
  - a. ... the two boys.
  - b. ... the two boys and the two girls.

To account for the above distributional constraints, I assume that the H-shifter (viz., the operator that turns a set of entities into a set of GQs) must be applied locally to the nP within the wH-complement. In what follows, I argue that the application of H is blocked in singular nouns and numeral-modified nouns due to conflicts in meaning and type. First, I assume the following structure for a singular/plural bare noun:

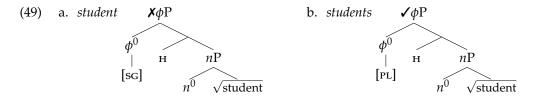


At the right bottom of each tree,  $n^0$  combines with the root  $\sqrt{\text{student}}$  and returns a projection nP which denotes a set with a complete join semi-lattice structure (Harbour 2014). For example, with three atomic students abc, [nP] =  $\{a, b, c, a \oplus b, a \oplus c, b \oplus c, a \oplus b \oplus c\}$ . The number feature [sg]/[PL] is evaluated at  $\phi^0$ . Following Sauerland (2003), I treat [PL] semantically vacuous while [sg] a predicate modifier asserting (or presupposing) atomicity.

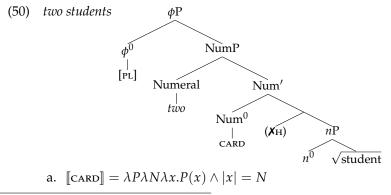
(48) a. 
$$[[PL]] = \lambda P_{\langle e,t \rangle} \lambda x_e. P(x)$$
  
b.  $[[SG]] = \lambda P_{\langle e,t \rangle} \lambda x_e. Atom(x) \wedge P(x)$   
(or:  $[[SG]] = \lambda P_{\langle e,t \rangle} \lambda x_e : Atom(x). P(x))$ 

c. 
$$[[PL](nP)] = [nP] = \{a, b, c, a \oplus b, a \oplus c, b \oplus c, a \oplus b \oplus c\}$$
  
d.  $[[sg](nP)] = \{a, b, c\}$ 

The above assumptions straightforwardly explain why the H-shifter cannot be used in singular nouns. In (49a), applying the H-shifter to nP returns a set of GQs, which are non-atomic and conflict with the atomicity requirement of [sG]. (See a possible amendment of this view in Sect. 5.2.) Hence, the H-shifter cannot be applied in a singular-marked wH-question because it would yield an empty Q-domain. In contrast, the H-shifter can be freely used in simple plural-marked and number-neutral wH-questions because in these questions the [PL] feature carried by  $\phi^0$  is semantically vacuous.<sup>21</sup>



Next, consider numeral-modified nouns. Following Scontras (2014), I place cardinal numeral-modifiers at [Spec, NumP] and assume that Num<sup>0</sup> is located between  $n^0$  and  $\phi^0$  and is occupied by a cardinality predicate CARD. As defined in (50a), CARD combines with a predicate P and a numeral N and returns the set of individuals x such that P holds for x and x is constituted of exactly-N atoms. These assumptions easily explain why the H-shifter cannot be used in a numeral-modified noun: the CARD-predicate at Num<sup>0</sup> checks the cardinality of the elements in the set it combines with and hence it cannot combine with a set of GQs. (See a possible amendment of this generalization in Sect. 5.2.)



<sup>&</sup>lt;sup>21</sup>This claim holds regardless of whether plurals are treated inclusively or exclusively. I also assume that the bare wh-words who and what have a structure similar to which people/things. Alternatively, one can treat [PL] as a predicate restrictor that asserts/presupposes non-atomicity or anti-presupposes atomicity (see also footnote 6). The latter option is more suited for languages in which plural-marking is not vacuous. For example, Spanish bare wh-words can be singular-marked or plural-marked. Interestingly, as seen in (i), while the singular form admits both atomic and non-atomic answers (see also footnote 7), the plural form admits only non-atomic answers (Maldonado 2020). For languages as such, it is plausible to assume that the the singular morpheme is semantically neutral, while the plural morpheme asserts/presupposes non-atomicity (Alonso-Ovalle and Rouillard 2019; cf. Elliott et al. 2020).

b. Quiénes se fue? who.pl refl left 'Who.pl left' '#John.'/'<sup>OK</sup>John and Billy.'

b. Without the н-shifter

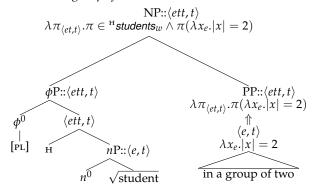
$$[Num'] = \lambda N \lambda x. students_w(x) \wedge |x| = N 
 [NumP] = \lambda x. students_w(x) \wedge |x| = 2 
 = \{a \oplus b, b \oplus c, a \oplus c\}$$

с. With the н-shifter

<code>『Num'</code> is undefined (or Num' has type-mismatch)

In contrast to numeral-modifiers, PP-modifiers are adjoined to the entire NP/ $\phi$ P. Hence, the H-shifter can be used within the modified NP without causing a type-mismatch. As illustrated in (51), all we need is to apply argument-lifting to the PP-modifier (indicated by ' $\uparrow$ ') and shift it into a set of GQs. The lifted PP composes with the higher-order  $\phi$ P standardly via Predicate Modification. This analysis also extends to NPs modified by a relative clause.

## (51) students in a group of two



# 5. The 'conjunction-rejecting' higher-order reading

### 5.1. The puzzles

In Sect. 2.2, based on stubborn collectivity and uniqueness effects, I showed that singular-marked and numeral-modified wh-questions do not admit answers naming Boolean conjunctions. I further concluded in Sect. 4 that these questions do not have higher-order readings and explained this distributional constraint. The explanation attributed the unavailability of higher-order readings to that applying the h-shifter yields semantic consequences that conflict with the atomicity requirement of singular nouns and the cardinality requirement of numerals.

Surprisingly, I find that narrow scope disjunctions are not as bad as conjunctions when used as direct answers to a  $\Box$ -question that has a singular-marked or numeral-modified wH-phrase. This contrast is seen clearly in (52) and marginally in (53).

(52) I know which book John has to read,

a. # ... Book A and Book B.

b. ? ... Book A or Book B. 
$$(\#or \gg \Box, ?\Box \gg or)$$

<sup>&</sup>lt;sup>22</sup>The conjunctive continuation in (53a) is intuitively more acceptable than the conjunctive continuation in (52a), as pointed out by Gennaro Chierchia (pers. comm.). A reviewer of *Natural Language Semantics* also reported that they found no clear contrast between (53a-b). One possibility for the improvement in (53a) is that the numeral modifier *two* alone can be reconstructed to the nucleus, which yields a simple plural-marked question roughly read as 'which books are two books that John have to read?'

- (53) I know which two books John has to read ...
  - a. ?? ... the two French novels and the two Russian novels.
  - b. ? ... the two French novels or the two Russian novels.  $(\#or \gg \Box, ?\Box \gg or)$

Narrow scope readings of disjunctive answers are even more readily available in discourse. In (54), the disjunction in the answer is interpreted under the scope of *should*, conveying a free choice inference that the questioner is free to use any one of the two mentioned textbooks. By the diagnostic of non-reducibility given in Sect. 2.1, that the disjunctive answer admits a narrow scope reading suggests that here the  $\Box$ -question admits higher-order answers, which conflicts with the aforementioned generalization that singular-marked questions do not have a higher-order reading.

(54) Which textbook should I use for this class? *Heim & Kratzer* or *Meaning & Grammar*. The choice is up to you.

Moreover, I observe the same contrast between conjunctive and disjunctive answers in questions with a possibility modal (called " $\diamond$ -questions" henceforth). In what follows, I will first introduce the general facts with  $\diamond$ -questions and their answers, and then discuss specifically the answers to singular-marked and numeral-modified  $\diamond$ -questions.

 $\diamond$ -questions are known to be ambiguous between mention-some (MS-)readings and mention-all (MA-)readings (Groenendijk and Stokhof 1984; for a discussion on what is MS, see Xiang 2016b: chapter 2). As exemplified in (55), if interpreted with a MS-reading, the  $\diamond$ -question can be naturally addressed by an answer that specifies only one feasible option; while in MA-readings, the  $\diamond$ -question requires the addressee to exhaustively list out all the feasible options. Crucially, MA-answers of  $\diamond$ -questions can have either an elided conjunctive form, as in (55b), or an elided disjunctive form read as free choice, as in (55c). While having different forms, both of the MA-answers convey the same conjunctive inference that we can use *Heim & Kratzer* for this class <u>and</u> we can use *Meaning & Grammar* for this class.

(55) What can we use [as a textbook] for this class?

a. Heim & Kratzer. (MS)

b. Heim & Kratzer and Meaning & Grammar. (Conjunctive MA)

c. Heim & Kratzer or Meaning & Grammar. (Disjunctive MA)

Xiang (2016b: chapter 2) proposes that MS-readings are higher-order readings: in the LF of a  $\diamond$ -question with a MS-reading, the wh-phrase binds a higher-order trace across the possibility modal. MA-readings of  $\diamond$ -questions arise as long as one of the following two conditions is met: (i) the higher-order wh-trace takes wide scope, or (ii) this trace is associated with an operator with a meaning akin to the Mandarin free choice licensing particle *dou*. In particular, condition (i) yields conjunctive MA, and condition (ii) yields disjunctive MA. I will give more details of this analysis in Sect. 5.3.2.

It is commonly believed that MS-readings and multi-choice readings are unavailable in singular-marked  $\diamond$ -questions because these questions presuppose uniqueness (Fox 2013; Xiang 2016b: chapter 3). The infelicity of the continuations in (56) supports this view: the continuations name multiple choices of textbooks, while the preceding question-embedding sentence implies that there is only one feasible choice.

- (56) I know which textbook we can use for this class, ...
  - a. # ... Heim & Kratzer and Meaning & Grammar.

b. ? ... Heim & Kratzer or Meaning & Grammar.

However, Hirsch and Schwarz (2019) novelly observe that the matrix singular-marked  $\diamond$ -question in (57) does admit a multi-choice reading. They argue that the singular wh-phrase triggers uniqueness but this uniqueness presupposition can be accommodated under the scope of the modal verb *could*. The question can be read as 'for which x, it is the case that x is the unique letter missing in  $fo_m?'$ .

(57) Which letter could be missing in *fo\_m*?

(Hirsch and Schwarz 2019)

- a. (The missing letter could be) *a*.
- b. The missing letter could be a and the missing letter could be r.

Note that in Hirsch and Schwarz's original example (57), the multi-choice answer (57b) is not a direct answer. As seen in (58a-b), in the form congruent with the question or in the form of a short answer, the conjunctive answers are greatly degraded. In contrast, the multi-choice inference can be felicitously expressed in the form of an elided free choice disjunction, as in (58c). The same pattern is seen with numeral-modified wh-questions, as shown in (59). (For reasons why the conjunctive answer (59a) is marginally acceptable, see footnote 22.)

- (58) Which letter could be missing in *fo\_m*?
  - a. ?? a could be missing in  $fo_m$  and r could be missing in  $fo_m$ .
  - b. # a and r.
  - c. *a* or *r*. (Both are possible.)
- (59) [Hearing a rhotic back vowel] Which two letters could be missing in  $f_{-}m$ ?
  - a. ?? or and ar.
  - b. or or ar.

To directly compare with the number-neutral  $\diamond$ -question (55), I re-illustrate Hirsch and Schwarz's idea in (60). According to Hirsch and Schwarz, the uniqueness presupposition triggered by the singular-marked wh-phrase which textbook can be interpreted either globally or locally. The global uniqueness reading says: there is only one textbook that we can use for this class, and the questioner asks to specify this book. The local uniqueness reading says: we will only use one textbook for this class, and the questioner asks to specify one feasible option, as in a MS-reading, or all the feasible options, as in a MA-reading. In contrast to the numeral-neutral  $\diamond$ -question (55) to which an elided MA-answer can be either a conjunction or a disjunction, here an elided MA-answer must be a disjunction, as seen in (60a-b). The disjunction-conjunction contrast is also seen with the universal free choice item any book, which is argued to be existential in lexicon (Chierchia 2006, 2013), and the basic universal quantifier every book, as in (60c-d).

- (60) Which textbook can I use for this class?
  - a. Heim&Kratzer or Meaning and Grammar.

Disjunctive MA

b. # Heim&Kratzer and Meaning and Grammar.

Conjunctive MA

- c. Any book that teaches compositionality.
- d. # Every book that teaches compositionality.

 $<sup>^{23}</sup>$ This example is cited from the original SALT 29 poster presentation of Hirsch and Schwarz (2019). In the recently published proceedings paper Hirsch and Schwarz 2020, they instead use a short answer "a or r", not a full sentence.

In sum, singular-marked and numeral-modified  $\diamond$ -questions admit multi-choice readings if uniqueness is interpreted locally. In multi-choice readings, their MA-answers must be expressed in the form of a free choice disjunction, not a conjunction.

Other than wh-questions, Gentile and Schwarz (2018) observe similar local uniqueness readings with *how many*-questions. The same as singular-marked and numeral-modified wh-phrases, *how many* presuppose uniqueness. For example, the question in (61) cannot be felicitously responded by a multi-choice answer expressed by the conjunction of two cardinal numerals. Given that the predicate *solved this problem together* is stubbornly collective, Gentile and Schwarz conjecture from the uniqueness effect that the Q-domain of this question does not include Boolean conjunctions over numerals.<sup>24</sup>

(61) How many students solved this problem together?
# Two and three.

(Intended: 'Two students solved this problem together, and (another) three students solved this problem together.')

Further, Gentile and Schwarz (2018) observe that possibility modals can obviate violations of uniqueness in *how many*-questions: the question in (62) admits multi-choice answers like (62a-b). In analogy to the examples in (58-60), I add that the multi-choice answer cannot be expressed by an elided conjunction, as seen in (62c).

- (62) How many students are allowed to solve this problem together?
  - a. Two are OK and three are OK.
  - b. Two or three.
  - c. # Two and three.

I call the higher-order reading in which a question admits a Boolean conjunctive answer the 'conjunction-admitting' reading and the higher-order reading in which a question rejects Boolean conjunctive answers the 'conjunction-rejecting' reading. Two puzzles arise from the above observations. First, why singular-marked and numeral-modified wн-questions can be directly responded by elided disjunctions but not by elided conjunctions? Second, why this 'conjunction-rejecting' reading is available despite that the wн-phrase is singular-marked or numeral-modified, in contrast to the 'conjunction-admitting' reading discussed in Sect. 4?

The following subsections provide two approaches to derive the 'conjunction-rejecting' reading and explain its distributional constraints. One approach treats the 'conjunction-

I don't think the above example can knock down Gentile and Schwarz's conjecture. The information conveyed by the above conjunctive answer can and even more preferably be expressed as a narrow scope disjunction, namely, below 50 meters or above 2000 meters ( $\neg \gg \diamond \gg or$ ). To argue against Gentile and Schwarz (2018), one would have to find a case where the strongest true answer can and can only be expressed as a higher-order conjunction over degrees/intervals. For example, in a context where the only group work constraint is that we cannot have two students work together while simultaneously another three students work together, the strongest true answer to the following negative  $\diamond$ -question, if available, would have to be a narrow scope conjunction. However, as seen in (ii), this conjunction does not appear felicitous.

(ii) How many students are not allowed solve this problem together?

# Two and three. (Intended: "It is not allowed that [two students solve the problem together and simultaneously (another) three students solve this problem together].")

<sup>&</sup>lt;sup>24</sup> Fox (2020) disagrees with Gentile and Schwarz's conjecture. He argues that *how many*-phrases can range over higher-order conjunctions of degrees/intervals, in light of the following data:

<sup>(</sup>i) How fast are we not allowed to fly?Below 50 meters (too low) and above 2000 meters (too high). (and ≫ ¬ ≫ ◊)

rejecting' reading the very same reading as the 'conjunction-admitting' reading but gives a weaker semantics to singular and numeral-modified nouns (Sect. 5.2). The other approach considers the 'conjunction-rejecting' reading a special higher-order reading: the derivation of this reading involves reconstructing the wh-complement to the question nucleus and interpreting uniqueness locally (Sect. 5.3). Both approaches can well explain the two puzzles.

### 5.2. A uniform approach

The uniform approach treats the 'conjunction-rejecting' reading the very same reading as the 'conjunction-admitting' reading. The core idea of this approach comes from a personal communication with Manuel Križ. To unify these two readings, all we need is to allow some of the Boolean disjunctions to be atomic or cardinal, just like entities.

In the following definitions, the (a)-condition on minimal witness sets ensures the atomic/cardinal GQ to be a disjunction, an existential quantifier, or a Montagovian individual. In comparison, if  $\pi$  is a universal quantifier or a Boolean conjunction, its minimal witness set is not singleton. For example, the Boolean conjunction  $a^{\uparrow} \cap b^{\uparrow}$  is ruled out because its only minimal witness set  $\{a,b\}$  is not singleton. The (b)-condition applies the original singularity/cardinality-requirement to each element in the smallest live-on set of  $\pi$ . For example, the Montagovian individual  $(a \oplus b)^{\uparrow}$  and the Boolean disjunction  $(a \oplus b)^{\uparrow} \cup c^{\uparrow}$  are ruled out by (63b) because their smallest live-on sets (viz.,  $\{a \oplus b\}$  and  $\{a \oplus b,c\}$ , respectively) include a non-atomic element  $a \oplus b$ .

- (63) A GQ  $\pi$  is atomic if and only if
  - a. the minimal witness sets of  $\pi$  are all singleton sets;
  - b. every member in the smallest live-on set of  $\pi$  is atomic.
- (64) A GQ  $\pi$  has the cardinality N if and only if
  - a. the minimal witness sets of  $\pi$  are all singleton sets;
  - b. every member in the smallest live-on set of  $\pi$  has the cardinality N.

Incorporating the above assumptions to the semantics of the singular feature [sg] and the cardinality predicate CARD yields the revised definitions in (66). 'Mws(A, x)' is read as 'A is a minimal witness set (Mws) of x'. Both [sg] and CARD are now treated as polymorphic restrictors which can combine with either predicates of entities or predicates of higher-order meanings.

(65) Old definitions

a. 
$$\llbracket [sg] \rrbracket = \lambda P_{\langle e,t \rangle} \lambda x_e. P(x) \wedge \text{Atom}(x)$$
  
b.  $\llbracket \text{Card} \rrbracket = \lambda P_{\langle e,t \rangle} \lambda N \lambda x_e. P(x) \wedge |x| = N$ 

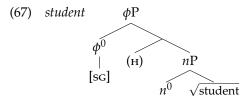
(66) New definitions

$$\text{a. } \llbracket [\mathtt{SG}] \rrbracket = \lambda P \lambda x. \left\{ \begin{array}{ll} P(x) \wedge \mathrm{Atom}(x) & \text{if } P \subseteq D_{\ell} \\ P(x) \wedge \forall A [\mathtt{Mws}(A,x) \to |A| = 1] \wedge \\ \forall y \in \mathtt{SMLO}(x) [\mathrm{Atom}(y)] & \text{if } P \subseteq D_{\langle \ell t, t \rangle} \end{array} \right.$$

 $<sup>^{25}</sup>$ Witness sets are defined in terms of the living-on property as follows (Barwise and Cooper 1981): if a GQ  $\pi$  lives on a set B, then A is a **witness set** of  $\pi$  if and only if  $A \subseteq B$  and  $\pi(A)$ . For example, given a discourse domain including three students abc, the universal quantifier every student has a unique minimal witness set  $\{a,b,c\}$ , while the singular existential quantifier some student has three minimal witness sets  $\{a\}$ ,  $\{b\}$ , and  $\{c\}$ , each of which consists of one atomic student.

$$\text{b. } \llbracket \texttt{CARD} \rrbracket = \lambda P \lambda N \lambda x. \begin{cases} P(x) \wedge |x| = N & \text{if } P \subseteq D_e \\ P(x) \wedge \forall A [\texttt{MWS}(A, x) \to |A| = 1] \wedge \\ \forall y \in \texttt{SMLO}(x) [|y| = N] & \text{if } P \subseteq D_{\langle et, t \rangle} \end{cases}$$

With the revised definitions, the H-shifter can be used regularly in singular nouns and numeral-modified nouns. In a discourse with three students abc, the singular noun student and the numeral-modified noun two students are interpreted as follows. Again, nP denotes a set of entities closed under summation formation:  $[nP] = \{a, b, c, a \oplus b, a \oplus c, b \oplus c, a \oplus b \oplus c\}$ .



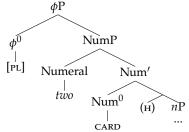
a. Without н:

$$\llbracket \phi \mathbf{P} \rrbracket = \{a, b, c\}$$

b. With н:

$$\llbracket \phi \mathbf{P} \rrbracket = \{ a^{\uparrow}, b^{\uparrow}, c^{\uparrow}, a^{\uparrow} \cup b^{\uparrow}, a^{\uparrow} \cup c^{\uparrow}, b^{\uparrow} \cup c^{\uparrow}, a^{\uparrow} \cup b^{\uparrow} \cup c^{\uparrow} \}$$
$$= \{ \bigcup A \mid A \subseteq \{ x^{\uparrow} \mid x \in \{a, b, c\} \}$$

(68) two students



a. Without н:

$$\llbracket \phi \mathbf{P} \rrbracket = \llbracket \mathbf{NumP} \rrbracket = \{ a \oplus b, b \oplus c, a \oplus c \}$$

b. With н:

In sum, in the uniform approach, higher-order readings of wh-questions are uniformly derived as follows. <sup>26</sup> **First**, applying an h-shifter to the nP within the wh-complement yields a higher-order domain. (In the following examples, BOOK/CHILD abbreviates for the nP within the noun book(s)/child(ren).) In particular, if the wh-phrase is number-neutral or

<sup>&</sup>lt;sup>26</sup>Given that it is possible to account for the uniqueness effects with singular-marked and numeral-modified wh-phrases while assuming a higher-order reading, one might wonder whether wh-questions have first-order readings at all. I so far do not see any direct evidence to object to this claim. However, assuming no first-order reading would lead to a prediction that the application of the H-shifter is mandatory, which is conceptually problematic. The presence of the H-shifter should be independent from the wh-determiner since it is applied locally to the root *n*P; thus, if the H-shifter were mandatory, we would expect that any NP has only a higher-order reading. However, in *the student* for example, the complement of *the* has to be interpreted as a set of entities, not as a set of GQs.

bare plural as in (69), the yielded domain is the set of homo-positive GQs ranging over a subset of [nP]. If the wh-phrase is singular-marked as in (70), the yielded domain is a set of disjunctions of Montagovian individuals  $x^{\uparrow}$  where x is an atomic element in [nP]. If the wh-complement is modified by a numeral N as in (72), the yielded domain is a set of disjunctions of  $x^{\uparrow}$  where x is an entity in [nP] with N-many atomic subparts. **Second**, the shifted wh-phrase binds a higher-order trace in the nucleus, yielding a higher-order Q-function as the root denotation of the question. This uniform analysis easily explains the availability of narrow scope disjunctive answers in (69) and (70) while accounting for the unavailability of conjunctive answers in (70) and (72) (cf. (69) and (71)).

(69) {What, Which books} does John have to read?

[CP [DP which [PL]-HBOOK]  $\lambda \pi_{\langle et,t \rangle}$  [IP have-to [ $\pi \lambda x_e$  [VP John read x]]]]

- a. The French novels.
- b. The French novels or the Russian novels. The choice is up to him.
- c. The French novels and the Russian novels.
- (70) Which book does John have to read?

[CP [DP which [SG]-HBOOK]  $\lambda \pi_{\langle et,t \rangle}$  [IP have-to [ $\pi \lambda x_e$  [VP John read x]]]]

- a. Book A
- b. Book A or Book B. The choice is up to him.
- c. # Book A and Book B.
- (71) Which children formed a team?

[CP [DP which [PL]-HCHILD]  $\lambda \pi_{\langle et,t \rangle}$  [IP  $\pi \lambda x_e$  [VP x formed a team]]]

- a. The two girls.
- b. The two girls and the two boys.
- (72) Which two children formed a team?

[CP [DP which [PL]-two-HCHILD]  $\lambda \pi_{\langle et,t \rangle}$  [PP  $\pi \lambda x_e$  [VP x formed a team]]]

- a. The two girls.
- b. # The two girls and the two boys.

# 5.3. A reconstruction approach

In contrast to the uniform approach, the reconstruction approach assumes that the derivation of the 'conjunction-rejecting' reading requires additional machinery — the wh-complement is syntactically reconstructed to the question nucleus. In what follows, I will present the derivation and explain the consequences of employing reconstruction, especially why it enables singular-marked  $\Box$ -questions to have narrow scope disjunctive answers (Sect. 5.3.1). Then I will extend this analysis to  $\Diamond$ -questions and show how this analysis accounts for the contrast between disjunctive and conjunctive MA-answers (Sect. 5.3.2).

### 5.3.1. $\Box$ -questions

Let me start with a singular-marked  $\Box$ -question. (73) provides the rough LF structures and the yielded Q-functions for first-order and higher-order readings with local uniqueness. In both LF structures, the singular-marked wh-complement *book* is syntactically reconstructed to a position in the nucleus c-commanded by the necessity modal. This reconstruction

has two consequences. First, it leaves a semantically unmarked variable D as the restrictor of the wh-determiner, which can be type-lifted freely by the h-shifter without causing a type-mismatch or a violation to atomicity. Thus, a higher-order reading arises if the h-shifter is applied to the D variable and if the wh-phrase binds a higher-order trace, as in (73b). Second, uniqueness is evaluated at whichever scopal position that the reconstructed noun adjoins to. In both (73a-b), uniqueness takes scope below the necessity modal.<sup>27</sup>

- (73) Which book does John have to read?
  - a. First-order reading ( $\square \gg \iota$ )

'For which entity  $x_e$ , it has to be the case that x is the book that John read?'

- i. [CP which  $\lambda x_{\ell}$  [PP have-to [VP x is the book John read ]]]
- ii.  $\llbracket \mathsf{wH}\text{-}\mathsf{Q} \rrbracket = \lambda x_e : x \in D. \Box [\lambda w. x = \iota y [\mathsf{book}_w(y) \land \mathsf{read}_w(y)] \rrbracket$
- b. Higher-order reading ( $\square \gg \pi \gg \iota$ )

'For which (homo-positive)  $\pi_{\langle et,t\rangle}$ , it has to be the case that for  $\pi$  x, x is the book that John read?'

- i. [CP which  $\lambda \pi_{\langle et,t \rangle}$  [PP have-to [  $\pi \lambda x_e$  [VP x is the book John read ]]]]
- $\text{ii.} \quad \llbracket \mathsf{wH-Q} \rrbracket = \lambda \pi_{\langle et, t \rangle} : \pi \in {}^{\mathsf{H}} D. \Box [\lambda w. \pi(\lambda x_e. x = \iota y [\mathit{book}_w(y) \wedge \mathit{read}_w(j, y)])]$

The following trees illustrate the two LF structures in more details. The reconstruction of the wh-complement is realized in three steps. First, a copy of which book is interpreted within the nucleus. As assumed in categorial approaches, which book John read denotes a one-place predicate. Second and third, the-insertion introduces uniqueness, and variable insertion introduces a variable bound by the wh-phrase. In particular, in the LF (75) for the higher-order reading, the same as what is assumed for conjunction-admitting readings, here the wh-restrictor (viz., the domain variable D) is type-raised by a h-shifter, and the wh-phrase binds a higher-order trace  $\pi$  across the necessity modal.  $^{29}$ 

(i) Which two cards do you need to win the game? The two red aces or the two black aces.

I argue that the local uniqueness inference in (i) is assessed dynamically relative to an updated context, namely, the context where the player has a bunch of cards in hand and only needs two more cards to close the game.

<sup>28</sup>One might have concerns with the assumed syntax for reconstruction. The assumed THE-insertion and variable insertion, on the one hand, are similar to the operations of determiner replacement and variable insertion used in trace conversion (Fox 2002) especially backward trace conversion (Erlewine 2014). On the other hand, in trace conversion, THE-insertion and determiner replacement are locally applied to the moved DP *which book*, while in my proposal, THE-insertion and variable insertion apply to a larger constituent DP+VP *which book John read*. I admit that the assumed syntax for reconstruction is unconventional, but this is not necessarily a problem for considering (75) as the structure that derives the 'conjunction-rejecting' reading. As seen in section 5.1, this reading itself is a bit unnatural. It is much harder to obtain than the conjunction-admitting reading, especially in question-embeddings (see (52-53) and (56)). Thus, it is likely that the derivation of this reading requires abnormal operations, and it is possible that the structure used for deriving this reading is not the real LF of the considered question.

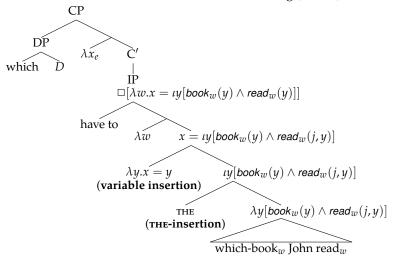
 $^{29}$ I assume a locality constraint that the variable introduced by variable insertion has to be directly bound by the wh-phrase. With this assumption, in the LF for the higher-order reading, variable insertion introduces a higher-order variable  $\pi$ ; it cannot be as follows where variable insertion (underlined) introduces an individual variable x bound by the higher-order wh-trace:

(i) \* [ whP 
$$\lambda \pi_{(et,t)}$$
 [ have-to [  $\pi \lambda x_e$  [  $\lambda y.x = y$  [ THE [ which book John read ]]]]]

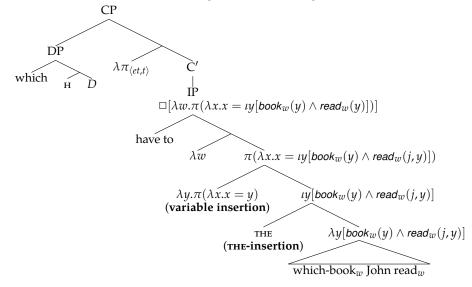
This constraint avoids unattested split scope readings of conjunctive answers to questions with an existential quantifier. Observe that the singular-marked question in (ii) cannot be felicitously responded by a conjunction. The infelicity of the conjunctive answer suggests that this answer cannot be interpreted with a split scope reading as follows: 'for a math problem  $x_1$ , Andy is the unique student who solved  $x_1$ , and for a math problem  $x_2$ , Billy is the

 $<sup>^{27}</sup>$ Luis Alonso-Ovalle (pers. comm.) points out that the assumed local uniqueness inference might be too strong for  $\Box$ -questions. For example, the question-answer pair in (i) can be felicitously uttered in a context where it is taken for granted that to win the game, one needs a group of two cards and also other cards.

(74) LF with reconstruction for the first-order reading ( $\square \gg \iota$ )



(75) LF with reconstruction for the higher-order reading ( $\square \gg \pi \gg \iota$ )



The above derivation predicts that the higher-order trace  $\pi$  immediately scopes over uniqueness. This prediction explains why a question in this reading rejects conjunctive answers: if  $\pi$  is a Boolean conjunction, combining  $\pi$  with a predicate of uniqueness yields a contradiction. As shown in (76b), unless Book A and B are the same book, combining the Q-function with the conjunction  $a^{\uparrow} \cap b^{\uparrow}$  yields a contradiction.

(76) Which book does John have to read? 
$$[\![\text{wH-Q}]\!] = \lambda \pi_{\langle et,t \rangle} \colon \pi \in {}^{\text{H}}D. \Box [\lambda w. \pi(\lambda x_e. x = \iota y [\textit{book}_w(y) \land \textit{read}_w(j,y)])]$$

unique student who solved  $x_2'$  (and  $\gg \exists \gg \iota$ ). The unavailability of this reading requests to rule out the LF in (iib) where the existential quantifier a math problem takes scope between the higher-order trace  $\pi$  and the inserted THE.

- (ii) Which student solved a math problem? # Andy and Billy. (and  $\gg \iota \gg \exists$ )
  - a. [  $whP \lambda \pi_{\langle et,t \rangle}$  [  $\lambda y.\pi(\lambda x.x = y)$  [ The [ which student solved a math problem ]]]]
  - b. \* [ whP  $\lambda \pi_{\langle et,t \rangle}$  [  $\pi \lambda x_e$  [ a-math-problem  $\lambda z$  [  $\lambda y.x = y$  [ the [ which student solved z ]]]]]]

a. Book A or Book B.

$$\llbracket \mathsf{wH-Q} \rrbracket (a^{\pitchfork} \cup b^{\pitchfork}) = \Box [\lambda w. [a = \iota y [\mathsf{book}_w(y) \land \mathsf{read}_w(j,y)]] \lor \\ [b = \iota y [\mathsf{book}_w(y) \land \mathsf{read}_w(j,y)]]$$

(It has to be the case that the unique book that John read is Book A or that the unique book that John read is Book B.)

b. # Book A and Book B.

$$\llbracket \mathsf{WH-Q} \rrbracket (a^{\pitchfork} \cap b^{\pitchfork}) = \Box [\lambda w. [a = \iota y [\mathsf{book}_w(y) \wedge \mathsf{read}_w(j,y)]] \wedge \\ [b = \iota y [\mathsf{book}_w(y) \wedge \mathsf{read}_w(j,y)]]$$

(#It has to be the case that the unique book that John read is Book A and that the unique book that John read is Book B.)

### **5.3.2. ♦-questions**

The MA-answer to a question is the true answer that entails all the true answers to this question. As seen in Sect. 5.1, in responding to a  $\diamond$ -question, the MA-answer can be expressed in the form of an elided conjunction or a free choice disjunction. However, if the wh-phrase in the  $\diamond$ -question is singular-marked or numeral-modified, the MA-answer can only be expressed in the form of a free choice disjunction. In Xiang 2016b: chapter 2, I argue that the MA-reading expecting a conjunctive answer and the MA-reading expecting a disjunctive answer are derived via different LF structures. With the assumed reconstruction, the contrast in LF between these two MA-readings naturally predicts the conjunction-disjunction asymmetry in singular-marked and numeral-modified  $\diamond$ -questions.

In the conjunctive MA-reading, the wh-phrase binds a higher-order trace which takes scope above the possibility modal. The following considers the interpretations of a number-neutral  $\diamond$ -question in cases where the higher-order wh-trace  $\pi$  takes scope below and above the possibility modal can. For these two cases, the structure of the question nucleus and the yielded Q-function and answer space are illustrated in (77a-b). 'f(x)' abbreviates for the proposition we use x for this class. For example,  $\diamond Of(a)$  is read as 'it can be the case that we use only Book A [as a textbook] for this class.' The illustrations of the answer space consider only the propositions derived by applying the Q-function to the following four GQs: the conjunction  $a^{\uparrow} \cap b^{\uparrow}$ , the Montagovian individuals  $a^{\uparrow}$  and  $b^{\uparrow}$ , and the disjunction  $a^{\uparrow} \cup b^{\uparrow}$ . Arrows indicate entailments among the propositions, and shading marks the propositions that are true in the considered world.

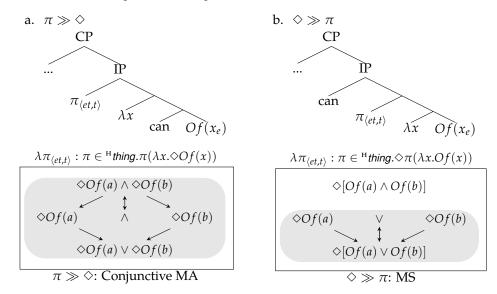
(i) 
$$O_C(p) = \lambda w.p(w) = 1 \land \forall q \in C[p \not\subseteq q \rightarrow p(w) = 0]$$
 (Chierchia et al. 2012)

Xiang (2016b: chapter 2) argues that MS-reading arises if the higher-order wh-trace  $\pi$  scopes below the possibility modal, and the local O-operator is assumed for predicting the facts that MS-answers are always mention-one answers, and that any answer that names one feasible option is a possible MS-answer. These issues are beyond the scope of this paper.

 $<sup>^{30}</sup>$ In both structures, an exhaustivity operator 'O' ( $\approx$  only) is inserted under the possibility modal and is associated with the individual wh-trace x.

(77) (w: Book A and Book B each can be used as the only textbook for this class; no other book can be used as a textbook for this class.)

What can we use [as a textbook] for this class? Book A and Book B.



In (77a) where the wh-trace  $\pi$  scopes above the possibility modal, the conjunctive answer derived by combining the Q-function with the Boolean conjunction  $a^{\uparrow} \cap b^{\uparrow}$  entails all the true answers, and thus it is the complete/MA- answer to the  $\diamondsuit$ -question. This conjunctive answer is read as 'it can be the case that we only use Book A for this class, and it can be the case that we only use Book B for this class.' In contrast, in (77b) where  $\pi$  scopes under the possibility modal, the inference derived based on  $a^{\uparrow} \cap b^{\uparrow}$  is a contradiction (and therefore is not shaded), read as '# it can be the case that we only use Book A for this class and only use Book B for this class.' In short, the take-away point is that conjunctive MA-answers are available only if the higher-order wh-trace  $\pi$  scopes above the possibility modal ( $\pi \gg \diamondsuit$ ).

Next, consider the corresponding singular-marked  $\diamond$ -question in (78). Again, the puzzle is that multi-choice answers to this question cannot have an elided conjunctive form. As assumed in section 5.3.1, the derivation of the higher-order reading of a singular-marked wh-question involves syntactically reconstructing the wh-complement. Reconstructing the singular noun *book* and letting the higher-order wh-trace  $\pi$  take scope above the possibility modal yield the following scopal pattern:  $\pi \gg \iota \gg \diamond$ . As shown in (78b), unless A and B are the same book, combining the derived Q-function with the Boolean conjunction  $a^{\uparrow} \cap b^{\uparrow}$  yields a contradiction.

(78) Which book can we use [as a textbook] for this class? # Book A and Book B.

a. 
$$\llbracket \mathsf{wh} - \mathsf{Q} \rrbracket = \lambda \pi_{\langle et, t \rangle} : \pi \in {}^{\mathsf{H}} D.[\lambda w. \pi(\lambda x_e. x = \iota y [\mathsf{book}_w(y) \land \Diamond_w f(y)])]$$

b. 
$$\llbracket \text{wh-Q} \rrbracket (a^{\uparrow} \cap b^{\uparrow}) = \lambda w. [a = \iota y [book_w(y) \land \diamondsuit_w Of(y)]] \land [b = \iota y [book_w(y) \land \diamondsuit_w Of(y)]]$$

(#a is the unique book that we can use as the only textbook for this class, and b is the unique book that we can use as the only textbook for this class.)

In contrast to conjunctive MA, disjunctive MA arises only if the higher-order wh-trace is associated with an DOU-operator, regardless of whether this trace takes scope below or above the possibility modal. The DOU-operator is the covert counterpart of the Mandarin particle

dou. Despite of many different uses of dou, the most important uses for understanding the semantics of  $\diamondsuit$ -questions are the following: in  $\diamondsuit$ -questions, associating dou with a wn-phrase blocks the MS-reading, as seen in (79a); in  $\diamondsuit$ -declaratives, associating dou with a pre-verbal disjunction yields a free choice inference, as shown in (79b). (For other uses of dou and a unified analysis, see Xiang 2020.) It is thus appealing to unify the derivation of free choice disjunction in  $\diamondsuit$ -declaratives and the derivation of disjunctive MA-readings of  $\diamondsuit$ -questions.<sup>31</sup>

- (79) a. **Dou** [shei] keyi jiao jichu hanyu?

  DOU who can teach Intro Chinese

  'Who can teach Intro Chinese?' (MA only)
  - b. [Yuehan huozhe Mali] dou keyi jiao jichu hanyu John or Mary dou can teach intro Chinese
     Intended: 'Both John and Mary can teach Intro Chinese.'

Xiang (2016b, 2020) defines dou as a pre-exhaustification exhaustifier over sub-alternatives: dou affirms its propositional argument and negates the exhaustification of each of the sub-alternatives of its propositional argument. The alternations in function of dou come from minimal variations with the semantics of sub-alternatives (details omitted). In particular, for a disjunctive sentence of the form  $\diamondsuit(\phi \lor \psi)$  or the form  $\diamondsuit\phi \lor \diamondsuit\psi$ , the sub-alternatives are  $\diamondsuit\phi$  and  $\diamondsuit\psi$ . The covert dou is semantically identical to dou except that it does not presuppose non-vacuity. With this semantics, applying dou/dou to a disjunctive sentence yields a universal free choice inference.

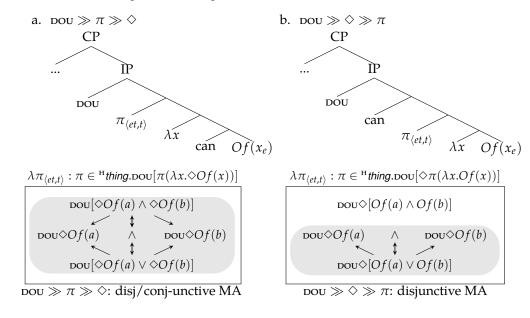
- [80)  $\llbracket dou_C \rrbracket = \lambda p \lambda w : \exists q \in \operatorname{Sub}(p,C).p(w) = 1 \land \forall q \in \operatorname{Sub}(p,C)[O_C(q)(w) = 0]$  (For any proposition p and world w,  $\llbracket dou_C \rrbracket(p)(w)$  is defined only if C contains a sub-alternative of p. When defined,  $\llbracket dou_C \rrbracket(p)(w)$  asserts that p is true in w, and that for any q that is a sub-alternative of p, the exhaustification of q is false in w.)
- (81)  $[DOU_C] = \lambda p \lambda w : p(w) = 1 \land \forall q \in Sub(p, C)[O_C(q)(w) = 0]$

The following illustrates two possible structures of the question nucleus for the disjunctive MA-reading as well as the Q-function and answer space yielded by each structure. In both structures, a covert dou-operator is presented at the left edge of the question nucleus and is associated with the higher-order trace  $\pi$ . The two structures differ only with respect to the scopal pattern between the trace  $\pi$  and the possibility modal  $\mathit{can}$ . As computed in (83), no matter whether  $\pi$  scopes above or below  $\mathit{can}$ , dou strengthens the disjunctive answer into a free choice statement that is semantically equivalent to the conjunction of the two individual answers.

<sup>&</sup>lt;sup>31</sup>There is a rich literature on the semantics of *dou*, but very few analyses can account for the widely discussed distributor use and the *even*-like use of *dou* while also explaining its FC-triggering effect in declarative sentences. Other than the adopted account of Xiang (2016b, 2020), another possible candidate is Liu 2016. Although Liu (2016) does not discuss FC disjunctions in specific, his analysis predicts the mandatory use of pre/recursive-exhaustifications in the presence of *dou*. See Xiang 2020 for a review.

(82) (w: Book A and Book B each can be used as the only textbook for this class; no other book can be used as a textbook for this class.)

What can we use [as a textbook] for this class? Book A or Book B.



(83) a. For  $\mathtt{DOU} \gg \pi \gg \diamondsuit$ :  $\mathtt{DOU}[\diamondsuit Of(a) \lor \diamondsuit Of(b)]$   $= [\diamondsuit Of(a) \lor \diamondsuit Of(b)] \land \neg O\diamondsuit Of(a) \land \neg O\diamondsuit Of(b)$   $= [\diamondsuit Of(a) \lor \diamondsuit Of(b)] \land [\diamondsuit Of(a) \to \diamondsuit Of(b)] \land [\diamondsuit Of(b) \to \diamondsuit Of(a)]$   $= [\diamondsuit Of(a) \lor \diamondsuit Of(b)] \land [\diamondsuit Of(a) \leftrightarrow \diamondsuit Of(b)]$   $= \diamondsuit Of(a) \land \diamondsuit Of(b)$ b. For  $\mathtt{DOU} \gg \diamondsuit \gg \pi$ :  $\mathtt{DOU} \diamondsuit [Of(a) \lor Of(b)]$   $= \diamondsuit [Of(a) \lor Of(b)] \land \neg O\diamondsuit Of(a) \land \neg O\diamondsuit Of(b)$   $= \diamondsuit [Of(a) \lor Of(b)] \land [\diamondsuit Of(a) \to \diamondsuit Of(b)] \land [\diamondsuit Of(b) \to \diamondsuit Of(a)]$   $= \diamondsuit [Of(a) \lor Of(b)] \land [\diamondsuit Of(a) \leftrightarrow \diamondsuit Of(b)]$   $= \diamondsuit Of(a) \land \diamondsuit Of(b)$ 

Next, return to singular-marked  $\diamond$ -questions. Recall that, while rejecting conjunctive answers, singular-marked  $\diamond$ -questions admit elided disjunctions as their MA-answers. The following considers the two discussed possibilities where a covert dou-operator is presented in the nucleus and is associated with a higher-order wh-trace. For the numeral-neutral  $\diamond$ -question in (82), the Q-functions yielded by the two possible LFs have the same output when combining with a Boolean disjunction — they both yield a free choice inference. In the corresponding singular-marked  $\diamond$ -question, however, whether  $\pi$  takes scope above or below the possibility modal yields a crucial difference with free choice disjunctive answers. If  $\pi$  takes a wide scope, as seen in (84a), the derived free choice inference is a contradiction, just like the case of the wide scope conjunctive answer in (78). In contrast, as seen in (84b), if  $\pi$  takes a narrow scope relative to the possibility modal, the derived free choice inference is not contradictory and is a desired MA-answer.

(84) Which book can we use [as a textbook] for this class? Book A or Book B.

(#a is the unique book that we can use as the only textbook for this class, and b is the unique book that we can use as the only textbook for this class.)

b. If  $\text{dou} \gg \diamondsuit \gg \pi \gg \iota$ :  $[\![\text{wh-Q}]\!] = \lambda \pi_{\langle et,t \rangle} : \pi \in {}^{\text{H}}D.\text{dou} \diamondsuit [\lambda w.\pi(\lambda x_e.x = \iota y[book_w(y) \land Of_w(y)])]$  $[\![\text{wh-Q}]\!] (a^{\uparrow} \cup b^{\uparrow}) = \text{dou} \diamondsuit [\lambda w.(a^{\uparrow} \cup b^{\uparrow})(\lambda x_e.x = \iota y[book_w(y) \land Of_w(y)])]$  $= [\diamondsuit \lambda w.a = \iota y[book_w(y) \land Of_w(y)]] \cap \\[\lozenge \lambda w.b = \iota y[book_w(y) \land Of_w(y)]]$ 

(a can be the unique book that we use as the only textbook for this class, and b can be the unique book that we use as the only textbook for this class.)

To sum up, number-neutral  $\diamondsuit$ -questions admit three types of MA-answers, including wide scope conjunctions, wide scope free choice disjunctions, and narrow scope free choice disjunctions. As for a singular-marked  $\diamondsuit$ -question, however, the MA-answer can only be a narrow scope disjunction: due to the uniqueness inference associated with the individual variable bound by the higher-order wh-trace, wide scope conjunctions and wide scope free choice disjunctions yield contradictory inferences. This analysis also applies to numeral-modified  $\diamondsuit$ -questions.

## 5.4. Comparing the two approaches

Both the uniform approach and the reconstruction approach can properly derive and account for the distributional constraints of the 'conjunction-rejecting' higher-order reading.

First, both approaches explain why singular-marked and numeral-modified wh-questions admit higher-order disjunctive answers. In the uniform approach, assuming that disjunctions can be singular/cardinal, the atomicity/cardinality restrictor in the wh-complement does not block the application of the h-shifter, this approach allows the Q-domain of a singular-marked/numeral-modified wh-question to range over a set of Boolean disjunctions (and Montagovian individuals). In the reconstruction approach, the atomicity/cardinality restrictor in the wh-complement can block the application of the h-shifter, but this blocking effect disappears once the wh-complement is syntactically reconstructed to the question nucleus.

Second, both approaches explain why these questions reject conjunctive answers. In the uniform approach, Boolean conjunctions are not atomic or cardinal, and hence are ruled out immediately by the atomicity/cardinality restrictor in the wh-complement. In the reconstruction approach, conjunctive answers are not acceptable because the individual variable immediately bound by the higher-order wh-trace triggers uniqueness, and conjoining two uniqueness inferences yields a contradiction.

Last, both approaches capture the local uniqueness effects. In the uniform approach, disjunctions that are considered singular range over a set of atomic entities, and likewise, disjunctions having the cardinality N range over a set of entities each of which has the

cardinality N. In the reconstruction approach, reconstruction involves the assertion which introduces uniqueness.

These two approaches, however, are not notational equivalence of each other. First, they attribute the deviance of conjunctive answers to different reasons and thus can make different predictions in certain cases. In the reconstruction approach, disjunctive answers are acceptable because disjoining two uniqueness inference does not yield a contradiction. However, the computation in (84a) shows an exception: if disjunctions are interpreted as wide scope free choice, they would yield contradictions the same as conjunctions. In contrast, the uniform approach does not predict disjunctions to be deviant in any case. Unfortunately, it is hard to check the predictions with real data. Second, the uniform approach derives the 'conjunction-rejecting' reading in the very same way as the 'conjunction-admitting' reading, while the reconstruction approach uses a salvaging strategy. Therefore, on the one hand, the uniform approach is technically neater, and on the other hand, the reconstruction approach predicts the general difficulty in interpreting singular-marked and numeral-modified questions with higher-order readings.

#### 6. Conclusion

This paper investigates the higher-order readings of wH-questions. First, drawing on evidence from questions with necessity modals or collective predicates, I showed that sometimes a wH-question can only be completely addressed by a GQ and must be interpreted with a higher-order reading. Next, I argued that the GQs that can serve as possible semantic answers to questions must be homogeneously positive. Incorporating this constraint into the meaning of a H-shifter, I proposed that higher-order readings arise if the H-shifter converts the wH-restrictor into a set of higher-order meanings and if the wH-phrase binds a higher-order trace. Accordingly, higher-order readings are unavailable if the application of the H-shifter is blocked, either by the atomicity constraint of the singular feature [sG] in singular nouns, or by the cardinality constraint of numerals in numeral-modified nouns.

Further, a puzzle arose that singular-marked and numeral-modified questions admit disjunctive answers but not conjunctive answers. I provided two explanations to this asymmetry. In the uniform approach, these questions admit disjunctions because some disjunctions (but no conjunction) may satisfy the atomicity/cardinality requirement. In the reconstruction approach, the wh-complement is reconstructed, which gives rise to local uniqueness and yields contradictions for conjunctive answers.

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