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Abstract

We examine [X]

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This paper

1 Introduction

2 Industry Specific Skill Premium

3 Model

This section presents the model which is the same as (Krusell et al., 2000). There are four inputs for production in this economy: two types of capital, equipment (k_e) and structures (k_s) and two types of labor, skilled (s) and unskilled (u). Inputs are combined through a production function $G(\cdot)$ to produce three final goods: consumption (c), investment in equipment (i_e) and investment in structures (i_s). Assuming an Hicks-neutral technological shocks A , the aggregate production is given by

$$c_t + i_{e_t} + i_{s_t} = A_t G(k_{s_t}, k_{e_t}, u_t, s_t) \quad (1)$$

The production function is assumed to be Cobb-Douglas in structures and a nested CES in all other inputs:

$$G(k_{s_t}, k_{e_t}, u_t, s_t) = k_{s_t}^\alpha \left(\mu u_t^\sigma + (1 - \mu) (\lambda k_{s_t}^\rho (1 - \lambda) s_t^\rho)^\frac{\sigma}{\rho} \right)^\frac{1-\alpha}{\sigma} \quad (2)$$

where α is the share of capital structures in output, μ and λ are income shares, ρ and σ govern the elasticity of substitution between capital equipment and labor:

- $\sigma_H = 1/(1 - \rho)$ is the elasticity of substitution between equipment and high-skilled.
- $\sigma_L = 1/(1 - \sigma)$ is the elasticity of substitution between low-skilled and equipment + high skill labor.

Labor input is defined as

$$\begin{aligned} u &= \psi_t^u h_t^u \\ s &= \psi_t^s h_t^s \end{aligned}$$

where ψ_t^i is the (unobserved) efficiency of each type of labor and h_t^i is the number of labor hours.

3.1 Skill Premium

Firms solve the following profit maximization problem

$$\max_{k_{s_t}, k_{e_t}, u_t, s_t} G(k_{s_t}, k_{e_t}, u_t, s_t) - r_{s_t} k_{s_t} - r_{e_t} k_{e_t} - w_{u_t} h_{u_t} - w_{s_t} h_{s_t} \quad (3)$$

Remember to show that capital-skill complementarity requires $\sigma > \rho$

4 Data

I estimate the model following the approach outlined in KORV Krusell et al. (2000). I constructed data series for wages, labor input, and capital input from 1963 to FINAL YEAR to replicate KORV with updated data following Ohanian et al. (2021). I then collect the same series at the industry level to re-estimate the model, due to data availability industry series cover the period from INITIAL YEAR-FINAL YEAR.

Labor input and wages are estimated using CPS data downloaded from IPUMS, see Flood et al. (2015),

4.1 Capital Data

To extend both capital series to replicate KORV I obtained investment series in equipment (I_e) and structures (I_s) from NIPA Table 5.2.5. Then the equipment (K_e) and structure (K_s) capital series were constructed using the perpetual inventory method:

$$K_{i,t+1} = (1 - \delta_{i,t})K_{i,t} + I_{i,t} \quad i \in \{e, s\} \quad (4)$$

I departed from KORV by using time-varying depreciation rates $\delta_{i,t}$, instead of constant depreciation rates for each series. As in (Ohanian et al., 2021) I deflate structures using the implicit price deflator of GDP ¹, and equipment using the product of the consumption deflator² and the relative price of equipment ³.

To obtain capital data at the industry level I used the BEA Fixed Assets dataset to obtain investment and capital consumption series by industry and type, details of which tables were used are included in Appendix A.1. Fixed Assets dataset groups industries into 76 groups. To construct a series of the labor share of output by industry, I used the BEA-BLS Integrated

¹Available <https://fred.stlouisfed.org/series/GDPDEF>

²Available at <https://fred.stlouisfed.org/series/CONSDEF>

³Available at <https://fred.stlouisfed.org/series/PERIC>

Industry-level Production Accounts (KLEMS)⁴. KLEMS data consists on 57 industry groups some of which are aggregations of industries on the BEA dataset. Table presents the crosswalk between BEA, KLEMS, and Census industry codes. I used the crosswalk provided by (Acemoglu and Restrepo, 2020). A description of the codes is in **INSERT TABLE AND REFERENCE IT**.

4.2 Labor Data

5 Results

⁴Available at <https://www.bls.gov/productivity/articles-and-research/industry-production-account-capital.xlsx>

References

- Acemoglu, D. and P. Restrepo (2020). Unpacking skill bias: Automation and new tasks. In *aea Papers and Proceedings*, Volume 110, pp. 356–61.
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- Krusell, P., L. E. Ohanian, J.-V. Ríos-Rull, and G. L. Violante (2000). Capital-skill complementarity and inequality: A macroeconomic analysis. *Econometrica* 68(5), 1029–1053.
- Ohanian, L. E., M. Orak, and S. Shen (2021). Revisiting capital-skill complementarity, inequality, and labor share. Technical report, National Bureau of Economic Research.

A Data Construction

A.1 Capital Inputs and Labor Share

OUTLINE

- Mention why are those delators used.
- How is the depreciation rate contructed?

A.2 Labor Inputs and Wage Rates