# Industry Heterogeneity and Wage Inequality

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August 29, 2022

- Wage Inequality has risen since the 1980s.
- The distribution of wages inside firms does not follow the same trend as the entire economy.
- Song, Price, Guvenen, Bloom, and Von Wachter (2019), show that a substantial part of the rise in dispersion has occurred between firms instead of within firms.
- At the same time there has been an increase in occupational and educational, segregation of employees.

- I want to focus on the relationship between the composition of the workforce (Labor Input Ratio)
  - Skilled workers vs Unskilled workers
- and wage inequality between those groups (the Skill Premium).
- I will use the model proposed by Krusell, Ohanian, Ríos-Rull, and Violante (2000) (KORV) to isolate two effects influencing the growth of the skill premium:

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  - the effect of the relative input of skilled vs. unskilled workers.
  - the effect of skill-biased technological change. (Capital-skill complementarity hypothesis)
- I will analyze these effects have evolved industry level.

## **Objectives**

This work has two primary objectives:

- Extend the analysis from KORV beyond the original period.
- Evaluate the capital-skill complementarity hypothesis at the industry level.

### Motivation

- In a recent work Haltiwanger, Hyatt and Spletzer (2022), shows that the rise in wage inequality is concentrated in a small number of industries (about 10%).
  - This work analyzes industries at the 4-digit NAICS level.
  - I work with more aggregated data.
- There is a fact that holds at a higher level:
  - High-wage industries are more likely to exhibit larger skill-premium.

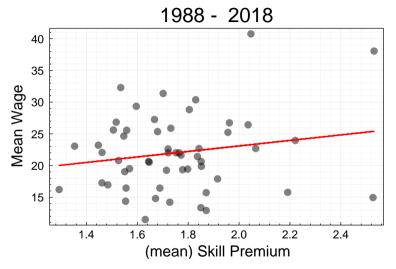


Figure: Relationship between skill premium and mean wage.

### Data

- I constructed data series for wages, labor input, and capital input from 1963 to 2018.
  - The original data from KORV covers the period from 1963 to 1992.
- I followed the methodology of Ohanian, Orak and Shen (2021).
- Re-create the same series for 56 industry groups for the period from 1998 to 2018.

## Capital Data

- I obtained investment series in equipment  $(I_e)$  and structures  $(I_s)$  from NIPA.
- Equipment  $(K_e)$  and structure  $(K_s)$  capital series were constructed using the perpetual inventory method:

$$K_{i_{t+1}} = (1 - \delta_{i_t})K_{i_t} + I_{i_t} \qquad i \in \{e, s\}$$

- For capital data at the industry level I used the BEA Fixed Assets dataset that groups industries into 76 groups.
- To construct a series of the labor share of output by industry, I used the BEA-BLS Integrated Industry-level Production Accounts (KLEMS),
- KLEMS data consists of 56 industry groups some of which are aggregations of industries on the BEA dataset.

#### **Labor Data**

- Labor input and wages are estimated using the march supplement of the Current Population Survey (CPS).
- Again, I follow the methodology of Ohanian, Orak and Shen (2021) to clean and aggregate the data.
- To obtain labor series I segmented the labor data into the 56 industry groups for which capital data is available and then aggregated the labor data repeating the same procedure as before.
- The classification of a worker being a skilled or an unskilled worker is based on the latest year of education completed.

## **Industry Groups**

- I used the crosswalk between the KLEMS, BEA, and CPS industry codes provided by Acemoglu, and Restrepo (2020) to map the industry codes.
- KLEMS codes are often the combination of the several BEA and CPS codes:
  - Oil and gas extraction: KLEMS-211, BEA-2110, CPS-42
  - Hospitals and nursing and residential care facilities: KLEMS-622HO, BEA-622h, 6230, CPS-831,832 and 870.
  - The largest KLEMS code (Retail trade) consists of 131 CPS codes.

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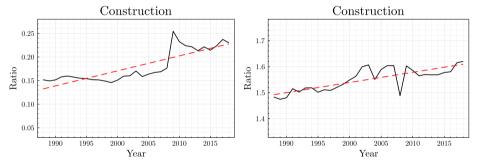


Figure: Trends: Construction

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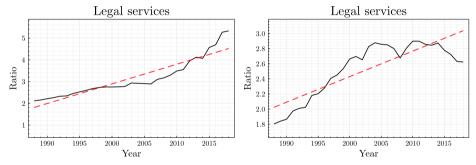


Figure: Trends: Legal Services

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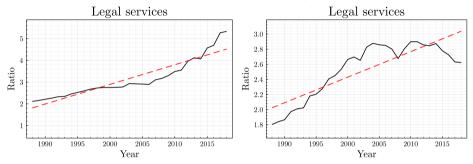


Figure: Trends: Legal Services

- For 49 industries (87.5%)the skill premium increased in the period and the input ratio showed the same pattern for 52 (92.8%) industries.

### Industry Level Trends PBack

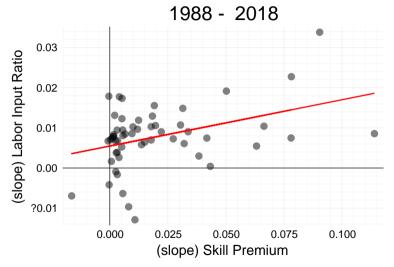


Figure: Realtionship between the trends of Labor Input and Skill Premium. 84% of the industries are increasing in both.

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### **KORV**

- Two types of capital
  - $k_s$ , structures.
    - Buildings.
  - $k_e$ , equipment, with a relative price equal to 1/q
    - Machines, computers, intellectual property.
- Two types of labor
  - u low-skilled labor.
    - $u = \psi^u h_u$  where  $h_u$  is hours (observed) and  $\psi^u$  is the quality of low-skilled labor (unobserved).
  - s high-skilled labor.
    - $s=\psi^S h_S$  where  $h_S$  is hours (observed) and  $\psi^S$  is the quality of high-skilled labor (unobserved).

### **KORV**

- There are three final goods:
  - Consumption c
  - Structure investment is
  - Equipment investment i<sub>e</sub>.
- Aggregate production:

$$c_t + i_{e_t} + i_{s_t} = Y_t = A_t G(k_{s_t}, k_{e_t}, u_t, s_t)$$
 (1)

### Production function

- The production function is:

$$G(k_{s_t}, k_{e_t}, u_t, s_t) = k_{s_t}^{\alpha} \left( \mu u_t^{\sigma} + (1 - \mu) \left( \lambda k_{s_t}^{\rho} (1 - \lambda) s_t^{\rho} \right)^{\frac{\sigma}{\rho}} \right)^{\frac{1 - \alpha}{\sigma}}$$
(2)

- $\sigma_H = 1/(1-\rho)$  is the elasticity between equipment and high-skilled.
- $\sigma_L = 1/(1-\sigma)$  is the elasticity between low-skilled and equipment + high-skilled.
- Firms solve the following profit maximization problem

$$\max_{k_{s_t}, k_{e_t}, u_t, s_t} G(k_{s_t}, k_{e_t}, u_t, s_t) - r_{s_t} k_{s_t} - r_{e_t} k_{e_t} - w_{u_t} h_{u_t} - w_{s_t} h_{s_t}$$
 (3)

#### **Production Function**

- My objective is to use this model to test whether the evolution of the change in the wage premium for skilled labor in different industries can be explained using the capital-skill complementarity hypothesis.
- I can observe,  $w_u$ ,  $w_{s_t}$ ,  $k_{s_t}$ ,  $k_{e_t}$ ,  $h_{u_t}$ ,  $h_{s_t}$

### Skill Premium in the Model

 Assuming competitive markets, workers are paid their marginal products per unit, of work:

$$\omega_{t} = \frac{w_{s_{t}}}{w_{u_{t}}} = \frac{G_{h_{s}}(k_{s_{t}}, k_{e_{t}}, u_{t}, s_{t})}{G_{h_{u}}(k_{s_{t}}, k_{e_{t}}, u_{t}, s_{t})}$$

- We can obtain the following (log-linearized) expression for  $\omega_t$ :

$$\ln \omega_t \simeq \lambda \frac{\sigma - \rho}{\rho} \left( \frac{k_{e_t}}{s_t} \right)^{\rho} + (1 - \sigma) \ln \left( \frac{h_{u_t}}{h_{s_t}} \right) + \sigma \ln \left( \frac{\psi_t^s}{\psi_t^u} \right) \tag{4}$$

- Which in turn can be written in terms of growth rates  $(g_x)$ :

$$g_{\omega t} \simeq (1 - \sigma) \left( g_{h_{u_t}} - g_{h_{s_t}} \right) + \sigma \left( g_{\psi_t^s} - g_{\psi_t^u} \right)$$

$$+ (\sigma - \rho) \lambda \left( \frac{k_{e_t}}{s_t} \right)^{\rho} \left( g_{k_{e_t}} - g_{h_{s_t}} - g_{\psi_t^s} \right)$$

$$(5)$$

## Skill Premnium Decomposition

We have decomposed the skill premium into three parts:

- $(1-\sigma)(g_{h_{u_t}}-g_{h_{s_t}})$  depends on the difference of the growth rates of skilled and unskilled and labor.
  - If both types of labor are substitutes i.e  $\sigma_u < 0 \implies (1 \sigma) < 0$
  - If skilled labor grows at a faster rate than unskilled labor, then the skill premium decreases.

## Skill Premnium Decomposition

We have decomposed the skill premium into three parts:

- $\sigma\left(g_{\psi_t^s}-g_{\psi_t^u}\right)$  depends on the growth rate of the productivity of skilled and unskilled and labor.
  - I follow KORV in making the following stochastic assumptions about labor productivity:

$$\psi_t^i = \psi_0^i + \epsilon \qquad \epsilon \sim N(0, \eta_\omega^2) \qquad i \in \{s, u\}$$
 (6)

- On average  $\sigma(g_{\psi^s_t}-g_{\psi^u_t})$  is constant over time and does not affect the growth rate of the skill premium.

## Skill Premnium Decomposition

We have decomposed the skill premium into three parts:

- 
$$(\sigma-\rho)\lambda\left(rac{k_{e_t}}{s_t}
ight)^{
ho}\left(g_{k_{e_t}}-(g_{h_{s_t}}+g_{\psi_{s_t}})\right)$$
. This component depends on two factors:

- 1. The growth rate of equipment relative to the growth rates of skilled labor input.
  - Characterize the capital-skill complementarity hypothesis as  $\sigma > \rho$ .
  - If equipment capital grows faster than skilled labor, the skill-premium will increase.
- 2. The ratio of capital equipment to skilled labor
  - The effect will get larger (smaller) over time if  $ho > 0 \ (
    ho < 0)$ .

### **Estimation**

- I follow the same methodology as KORV to estimate the model parameters.
- To simplify notation:

$$\begin{split} \psi_t &= \{ \psi_t^u, \psi_t^s \} \\ X_t &= \{ k_{s_t}, k_{e_t}, h_{s_t}, h_{u_t} \} \\ \Phi &= \{ \alpha, \sigma, \rho, \mu, \lambda, \psi_0^u, \psi_0^s, \eta_\omega \} \end{split}$$

- Any  $\{\mu, \lambda, \psi_0^u, \mu, \lambda, \psi_0^u, \psi_0^s\}$  act as scaling parameters thus, one can be fixed.
- There are 7 parameters to be estimated.

### **Estimation**

- I follow the same methodology as KORV to estimate the model parameters.
- The parameters are estimated using the following structural equations:

$$\begin{split} A_{t+1}G_{k_{s}}(X_{t+1},\psi_{t+1}\mid\Phi) &= q_{t}A_{t+1}G_{k_{s}}(X_{t+1},\psi_{t+1}\mid\Phi) + (1-\delta_{e})\left(\frac{q_{t}}{q_{t+1}}\right) + \nu_{t} \\ &\frac{w_{s_{t}}h_{s_{t}} + w_{u_{t}}h_{u_{t}}}{Y_{t}} &= lsh(X_{t},\psi_{t}\mid\Phi) \\ &\frac{w_{s_{t}}h_{s_{t}}}{w_{u_{t}}h_{u_{t}}} &= wbr(X_{t},\psi_{t}\mid\Phi) \end{split}$$

### **Estimation**

- I follow the same methodology as KORV to estimate the model parameters.
- The estimation method is a two-stage simulated pseudo-maximum likelihood estimation (SPMLE).
- In the first stage labor input is considered to be endogenous and is instrumented using: both capital series, lagged capital series, lagged prices, and indicators of the business cycle.
- In the second stage:
  - Taking the variance  $\eta_{\omega}$  as given, for each date t, generate S realizations of the model.
  - For each date *t* calculate the mean and variance of the realizations.
  - Minimize the distance between the first moments of the model and the data, using the second moment as a weighting matrix.

### Results

- First, I will show the results of the replication of the model using updated data.
- Second, I will show the results of applying the model to each industry.

|                 | <b>KORV Estimation</b> | Replication | <b>Updated Data</b> | <b>Updated Data</b> |
|-----------------|------------------------|-------------|---------------------|---------------------|
|                 | 1963 - 1992            | 1963 - 1992 | 1963 - 2018         | 1988 - 2018         |
| $\alpha$        | 0.117                  | 0.113       | 0.118               | 0.08                |
| $\sigma$        | 0.401                  | 0.464       | 0.503               | 0.313               |
| $\rho$          | -0.495                 | -0.56       | -0.343              | -0.154              |
| $\eta_{\omega}$ | 0.043                  | 0.043       | 0.083               | 0.043               |

Table: Parameter estimates KORV model.

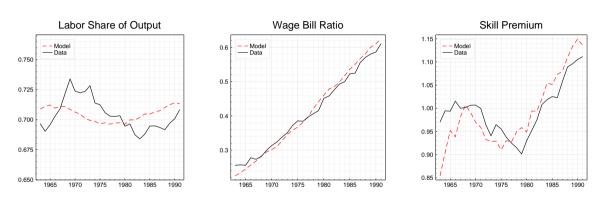


Figure: Fit for the 1963 - 1992 period with KORV Data.

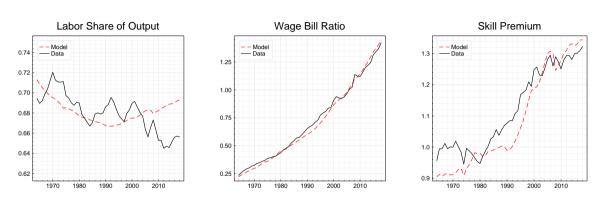


Figure: Fit for the 1963 - 2018 period with Updated Data.

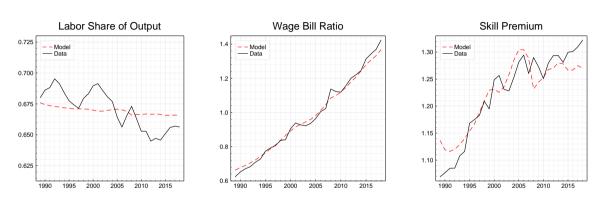


Figure: Fit for the 1988 - 2018 period with Updated Data.

### Caveats

- Convergence is highly sensitive to the initial conditions.
  - Not a problem when estimating KORV.
  - But when estimating the model for each industry, the initial conditions are not well defined.
- Initially I tried to sweep the parameter space to find the best initial conditions, I tried a 10 values for each parameter (total of 700 points), it took me more than a day to run the code.
- I settled on the trying 10 initial conditions.

# **Industry Level Results**

|                 | <b>Updated Data</b> | Industry Level | Industry Level |
|-----------------|---------------------|----------------|----------------|
|                 | 1988 - 2018         | (mean)         | (std)          |
| $\alpha$        | 0.08                | 0.241          | 0.206          |
| $\sigma$        | 0.313               | 0.483          | 0.710          |
| ρ               | -0.154              | -0.289         | 0.816          |
| $\eta_{\omega}$ | 0.043               | 0.131          | 0.195          |

Table: Industry Level Estimates.

## **Industry Level Results**

- On averegage the Capital-skill complementarity hypothesis  $(\sigma>\rho)$  is holds at the industry level.
- Specifically, the hypothesis holds for for 44 of 56 (78.8%) industries.

#### **Future Work**

- Improve the estimation using an altertive methodology, e.g.
  - Polgreen, and Silos(2008) discuss the sentitivity of KORV to variations in the data and propose a methodology to estimate the parameters that avoid the instabilities that can arise in maximizing a multidimensional function numerically
- Incorporate alternative sources of data. Specifically, Quarterly Workforce Indicators (QWI) published as part of the Longitudinal Employer-Household Dynamics. This will allow me to avoid having to segment the CPS data to estimate the labor input and wage series at the industry level.

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