

# Title Goes Here!!!\*

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August 28, 2022

## **Abstract**

We examine [X]

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\*Valdes-Bobes: University of Wisconsin. I thank [X] for the helpful comments and discussions.

This paper...

## 1 Introduction

## 2 Literature Review

This work is inserted in several strands of literature.

- Capital-Skill complementarity:
  - [Krusell et al. \(2000\)](#)
  - Replications, [Ohanian et al. \(2021\)](#), [Polgreen and Silos \(2008\)](#), [Maliar et al. \(2020\)](#), [Castex et al. \(2022\)](#).
- Income Shares:
  - [Karabarbounis and Neiman \(2014\)](#)
  - Possible Explanations:
    - \* Occupations [Orak \(2017\)](#)
- Industry Stuff [Haltiwanger et al. \(2022\)](#)
- Job Polarization stuff [Song et al. \(2019\)](#)

### 3 Data

I estimate the model following the approach outlined in KORV [Krusell et al. \(2000\)](#). I constructed data series for wages, labor input, and capital input from 1963 to **FINAL YEAR** to replicate KORV with updated data following [Ohanian et al. \(2021\)](#). I then collect the same series at the industry level to re-estimate the model, due to data availability industry series cover the period from **INITIAL YEAR-FINAL YEAR**.

#### 3.1 Capital Data

To extend both capital series to replicate KORV I obtained investment series in equipment ( $I_e$ ) and structures ( $I_s$ ) from NIPA Table 5.2.5. Then the equipment ( $K_e$ ) and structure ( $K_s$ ) capital series were constructed using the perpetual inventory method:

$$K_{i,t+1} = (1 - \delta_{i,t})K_{i,t} + I_{i,t} \quad i \in \{e, s\} \quad (1)$$

I departed from KORV by using time-varying depreciation rates  $\delta_{i,t}$ , instead of constant depreciation rates for each series. As in ([Ohanian et al., 2021](#)) I deflate structures using the implicit price deflator of GDP <sup>1</sup>, and equipment using the product of the consumption deflator<sup>2</sup> and the relative price of equipment <sup>3</sup>. Figure 1 shows the comparison between the original capital series obtained by ([Krusell et al., 2000](#)) and the updated capital series.

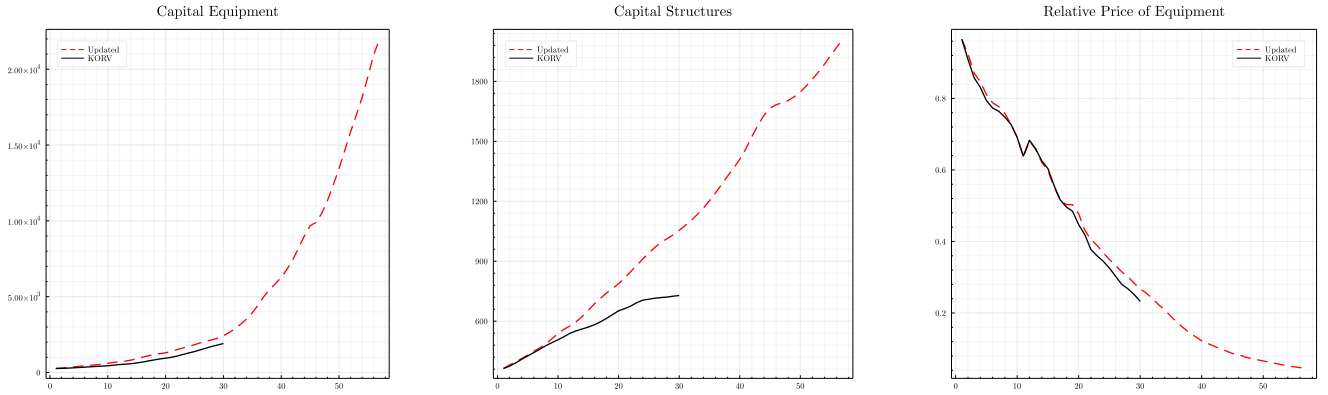


Figure 1: Capital Series

To obtain capital data at the industry level I used the BEA Fixed Assets dataset to obtain investment and capital consumption series by industry and type, details of which tables were used are included in Appendix B.1. Fixed Assets dataset groups industries into 76 groups. To construct a series of the labor share of output by industry, I used the BEA-BLS Integrated

<sup>1</sup>Available <https://fred.stlouisfed.org/series/GDPDEF>

<sup>2</sup>Available at <https://fred.stlouisfed.org/series/CONSDEF>

<sup>3</sup>Available at <https://fred.stlouisfed.org/series/PERIC>

Industry-level Production Accounts (KLEMS)<sup>4</sup>. This dataset contains the data underlying the BEA/BLS Integrated Industry-level Production Account for the United States. The data covers 1987-2020. KLEMS data consists of 57 industry groups some of which are aggregations of industries on the BEA dataset. The table presents the crosswalk between BEA, KLEMS, and Census industry codes. I used the crosswalk provided by (Acemoglu and Restrepo, 2020). A description of the codes is in [INSERT TABLE AND REFERENCEIT](#).

### 3.2 Labor Data

Labor input and wages are estimated using the march supplement of the Current Population Survey (CPS), downloaded from IPUMS<sup>5</sup>, see Flood et al. (2015). Flowing (Krusell et al., 2000) and (Ohanian et al., 2021) I include all observations excluding agents: younger than 16 or older than 70, unpaid family workers, those working in the military, those who report working less than 40 weeks a year and/or 35 hours a week, individuals with allocated income, those with hourly wages below half of the minimum federal wage rate, those did not report their education level and self-employed workers. Appendix B.2 describes in detail the cleaning process undertaken to obtain the labor input and wage series. Figure 2 displays the labor input and wage series for the 1963 - 2018 period compared with the original data.

I used the crosswalk in Table [INSERT TABLE AND REFERENCEIT](#) to group Census code groups for each industry and subdivided the original CPS data. I then repeated the process described in Appendix B.2 to obtain labor input and wage series for each industry.

### 3.3 Labor Income Shares

To construct labor share series at the economy level I follow Krusell et al. (2000), Castex et al. (2022) and Ohanian et al. (2021) in following the Cooley and Prescott (1995). I first generate a series containing capital income ( $CI$ ) consisting of the sum of

- (i) net interest and miscellaneous payments, domestic industries,
- (ii) corporate profits,
- (iii) consumption of fixed capital.

Capital share is defined as the ratio between  $CI$  and gross domestic income (net of proprietors' income)  $Y - PI$ . Labor share is then calculated as

$$LI = 1 - \frac{CI}{Y - PI}$$

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<sup>4</sup>Available at <https://www.bls.gov/productivity/articles-and-research/industry-production-account-capital.xlsx>

<sup>5</sup><https://cps.ipums.org/cps/index.shtml>

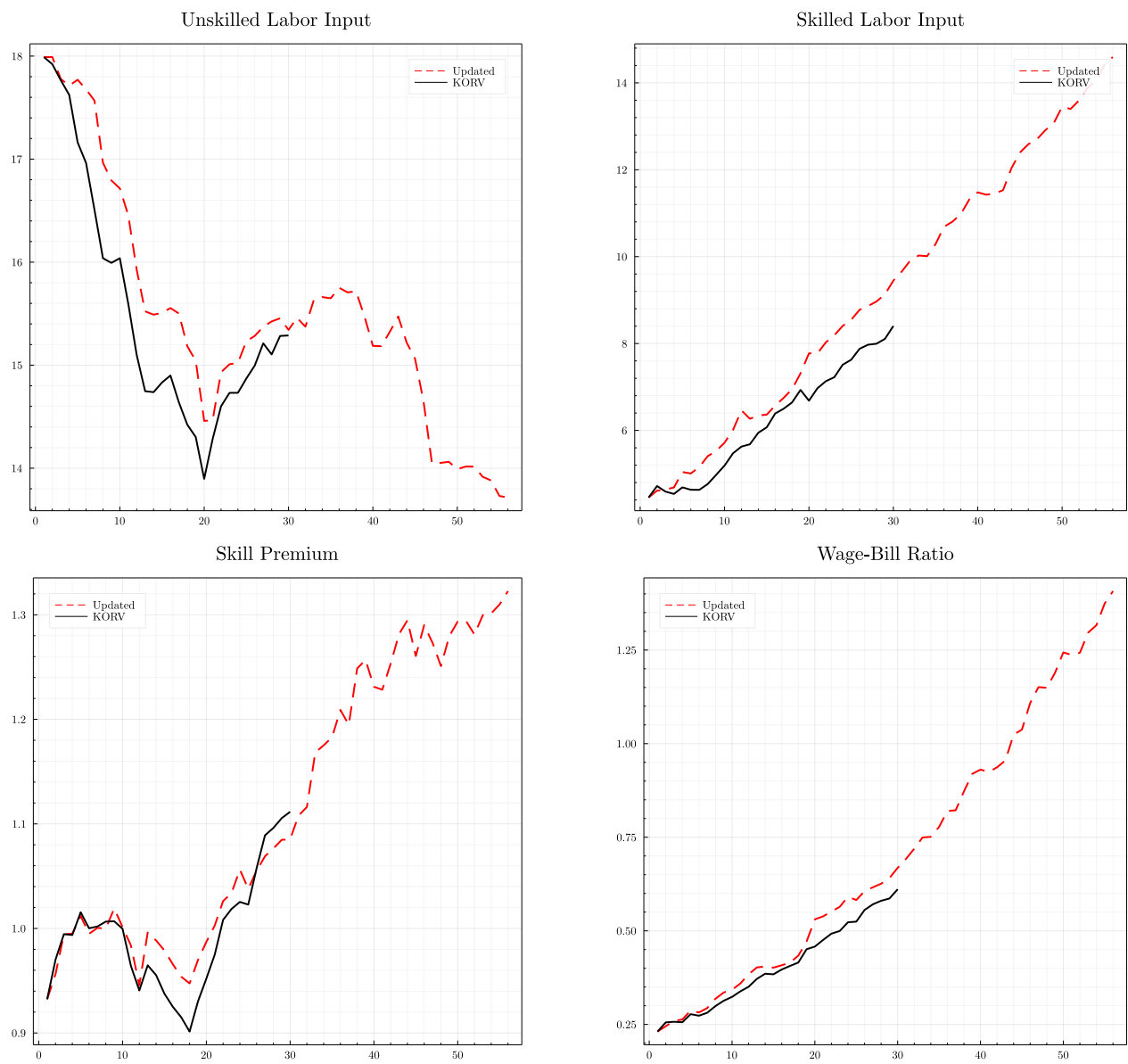
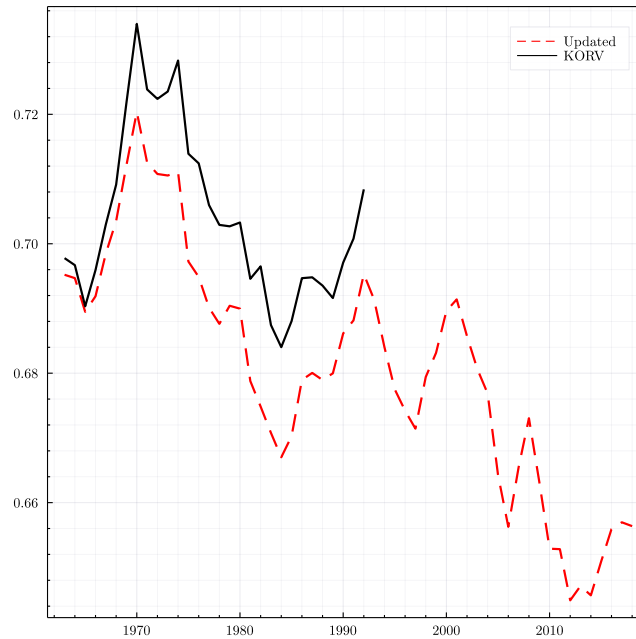


Figure 2: Labor Series

To construct labor share series at the industry level, I used the BEA-BLS Integrated Industry-level Production Accounts (KLEMS). KLEMS dataset contains information on the compensation of employees (with and without a college degree) and the value added by industry, I then follow ([Karabarbounis and Neiman, 2014](#)) and define the labor share as the ratio between the total compensation of employees and the total value added by industry.



Labor Share of Income

## 3.4 Data Description

### 3.4.1 Industry Trends

The trend of the labor share in the industry is the same at the national level Figure 3

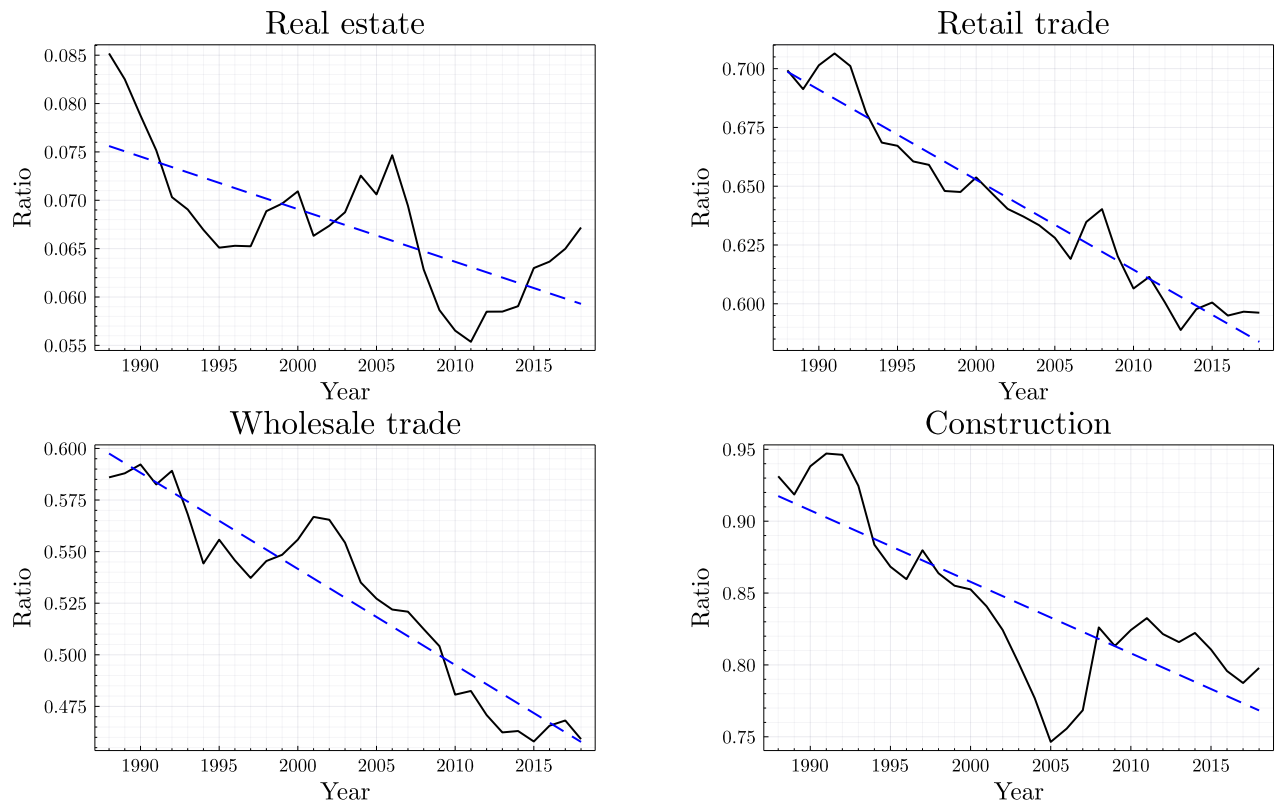


Figure 3: Declining Labor Share four larges industries

To justify exploring the skill-biased technical change I want to show that the feature of increasing labor input ratio holds and also the skill premium increasing holds at the industry level.

I calculate the slope of the labor input and get that **RESULTS**, I then repeat the process for the skill premium and get the **RESULTS**. Figure 4 shows a scatter plot of slopes. The first thing to note is that for almost all industries (**percentage**) there's been an increase in both indicators, furthermore the more that labor input ratio increases the more the skill premium increases.

Figure 4 shows ...

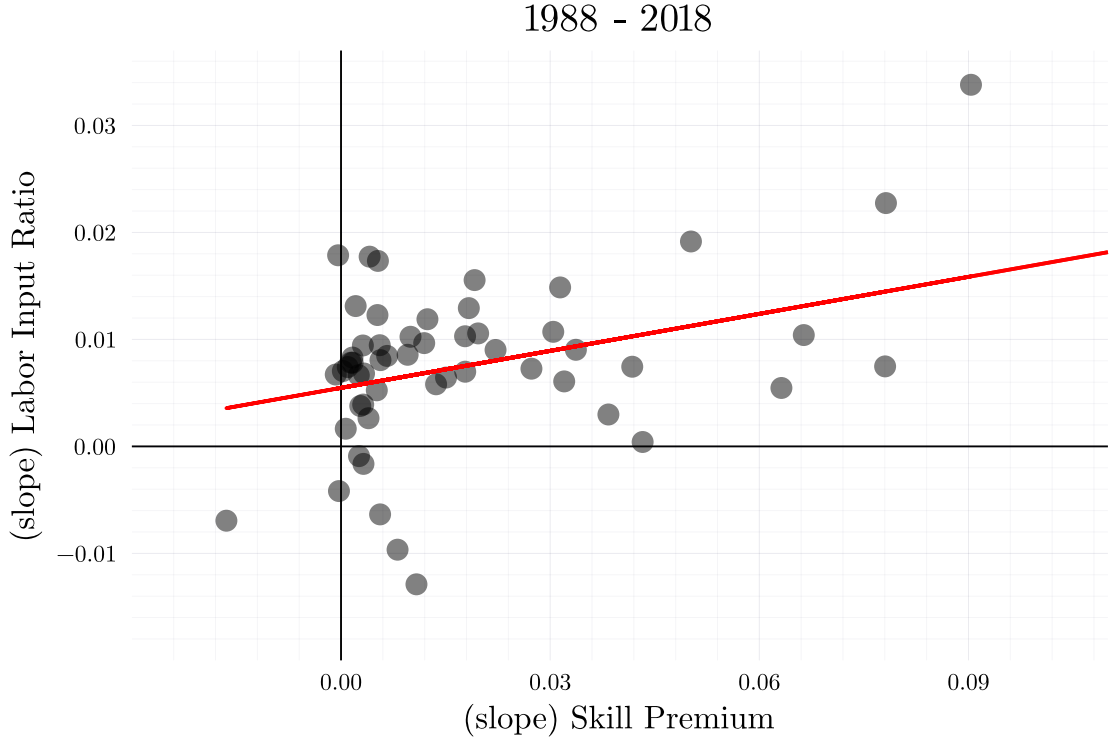


Figure 4: Correlation between the slopes of the Labor Input Ratio and the Skill Premium.

## 4 Model

This section presents the model which is the same as (Krusell et al., 2000). There are four inputs for production in this economy: two types of capital, equipment ( $k_e$ ) and structures ( $k_s$ ) and two types of labor, skilled ( $s$ ) and unskilled ( $u$ ). Inputs are combined through a production function  $G(\cdot)$  to produce three final goods: consumption ( $c$ ), investment in equipment ( $i_e$ ) and investment in structures ( $i_s$ ). Assuming a hicks-neutral technological shock  $A$ , the aggregate production is given by

$$c_t + i_{e,t} + i_{s,t} = Y_t = A_t G(k_{s,t}, k_{e,t}, u_t, s_t) \quad (2)$$

Capital evolves following the law of motion in (1). The production function is assumed to be Cobb-Douglas in structures and a nested CES in all other inputs:

$$G(k_{s,t}, k_{e,t}, u_t, s_t) = k_{s,t}^\alpha \left( \mu u_t^\sigma + (1 - \mu) (\lambda k_{e,t}^\rho (1 - \lambda) s_t^\rho)^{\frac{\sigma}{\rho}} \right)^{\frac{1-\alpha}{\sigma}} \quad (3)$$

where  $\alpha$  is the share of capital structures in output,  $\mu$ , and  $\lambda$  are income shares,  $\rho$  and  $\sigma$  govern the elasticity of substitution between capital equipment and labor:

- $\sigma_s = 1/(1 - \rho)$  is the elasticity of substitution between equipment and high-skilled.
- $\sigma_u = 1/(1 - \sigma)$  is the elasticity of substitution between low-skilled and equipment + high



skill labor.

Labor input is defined as

$$\begin{aligned} u &= \psi_t^u h_t^u \\ s &= \psi_t^s h_t^s \end{aligned}$$

where  $\psi_t^i$  is the (unobserved) efficiency of each type of labor and  $h_t^i$  is the number of labor hours.

## 4.1 Skill Premium

The model can be used to analyze the determinants of the skill premium growth, i.e. growth of the ratio of wages of skilled labor to wages of unskilled labor.

Firms solve the following profit maximization problem

$$\max_{k_{s_t}, k_{e_t}, u_t, s_t} G(k_{s_t}, k_{e_t}, u_t, s_t) - r_{s_t} k_{s_t} - r_{e_t} k_{e_t} - w_{u_t} h_{u_t} - w_{s_t} h_{s_t} \quad (4)$$

$r_{s_t}$  and  $r_{e_t}$  are rental rates of capital and  $w_{u_t}$  and  $w_{s_t}$  are wages of unskilled and skilled workers. Assuming perfect competition, labor is paid its marginal productivity therefore the skill premium at time  $t$ , ( $\omega_t$ ) is given by

$$\omega_t = \frac{w_{s_t}}{w_{u_t}} = \frac{G_{h_s}(k_{s_t}, k_{e_t}, u_t, s_t)}{G_{h_u}(k_{s_t}, k_{e_t}, u_t, s_t)} \quad (5)$$

this gives the following expression for the skill premium:

$$\omega_t = \frac{(1-\mu)(1-\lambda)}{\mu} \left[ \lambda \left( \frac{k_{e_t}}{s_t} \right)^\rho + (1-\lambda) \right]^{(\sigma-\rho)/\rho} \left( \frac{h_{u_t}}{h_{s_t}} \right)^{1-\sigma} \left( \frac{\psi_t^s}{\psi_t^u} \right)^\sigma. \quad (6)$$

Since the object of interest is the steady state growth of  $\omega_t$  (6) can be log-linearized to obtain the following expression:

$$\ln \omega_t \simeq \lambda \frac{\sigma-\rho}{\rho} \left( \frac{k_{e_t}}{s_t} \right)^\rho + (1-\sigma) \ln \left( \frac{h_{u_t}}{h_{s_t}} \right) + \sigma \ln \left( \frac{\psi_t^s}{\psi_t^u} \right) \quad (7)$$

Which in turn can be written in terms of growth rates:

$$\begin{aligned} g_{\omega t} &\simeq (1-\sigma) (g_{h_{u_t}} - g_{h_{s_t}}) + \sigma (g_{\psi_t^s} - g_{\psi_t^u}) \\ &\quad + (\sigma-\rho) \lambda \left( \frac{k_{e_t}}{s_t} \right)^\rho (g_{k_{e_t}} - g_{h_{s_t}} - g_{\psi_t^s}). \end{aligned} \quad (8)$$

where  $g_x$  denotes the growth rate of variable  $x$ , details on the derivations are include in Appendix A. Equation (8) has the nice property that it is a linear combination of the growth rates of the inputs in the production function, this allows us to decompose the growth rate of the skill premium into three components that are easy to analyze:

- (i)  $(1 - \sigma)(g_{h_{u_t}} - g_{h_{s_t}})$  depends on the growth rate of one type of labor over the other. We assume that both types of labor are substitutes i.e  $\sigma_u < 0 \implies (1 - \sigma) < 0$ . This means that if skilled labor grows at a faster rate than unskilled labor, will decrease the skill premium.
- (ii)  $\sigma(g_{\psi_t^s} - g_{\psi_t^u})$  depends on the growth rate of the productivity of one type of labor over the other. I follow (Krusell et al., 2000) in making the following stochastic assumptions about labor productivity:

$$\psi_t^i = \psi_0^i + \epsilon \quad \epsilon \sim N(0, \eta_\omega^2) \quad i \in \{s, u\} \quad (9)$$

This assumption guarantees that on average  $\sigma(g_{\psi_t^s} - g_{\psi_t^u})$  is constant over time and does not affect the skill premium growth rate.

- (iii)  $(\sigma - \rho)\lambda \left(\frac{k_{e_t}}{s_t}\right)^\rho (g_{k_{e_t}} - (g_{h_{s_t}} + g_{\psi_{s_t}}))$ . This component depends on two factors:

- (a) The growth rate of equipment relative to the growth rates of skilled labor input. This allows us to characterize the capital-skill complementarity hypothesis as  $\sigma > \rho$ , if equipment capital grows faster than skilled labor, the skill-premium will increase.
- (b) The ratio of capital equipment to efficiency units of skilled labor input (given our assumptions amounts to the growth rate of skilled labor input), this effect will get larger (smaller) over time if  $\rho > 0$  ( $\rho < 0$ ).

## 5 Estimation

I follow the same methodology as (Krusell et al., 2000) to estimate the model parameter. To simplify notation from now on I will refer to the unobservable labor efficiencies as,  $\psi_t = \{\psi_t^u, \psi_t^s\}$ , the inputs of the production function as  $X_t = \{k_{s_t}, k_{e_t}, h_{s_t}, h_{u_t}\}$  and the set of parameters to be estimated as  $\Phi = \{\alpha, \sigma, \rho, \mu, \lambda, \psi_0^u, \psi_0^s, \eta_\omega\}$ .

Firms decide investment in structures based on expectations about future prices  $q_{t+1}$ . This is captured using a "no arbitrage" condition, firms equate marginal returns on investment on both types of capital. On the one hand marginal return on investment in capital structures is given by given by the sum of the marginal product of structures in  $t + 1$ ,  $A_{t+1}G_{k_s}(X_{t+1}, \psi_{t+1} \mid \Phi)$  and undepreciated structures on  $(1 - \delta_s)$ . On the other hand marginal return on investment

in equipment is given by the sum of the marginal product of equipment in next period,  $q_t A_{t+1} G_{k_s}(X_{t+1}, \psi_{t+1} | \Phi)$  and depreciated structures  $\mathbb{E}(q_t/q_{t+1})(1 - \delta_e)$  the term  $\mathbb{E}(q_t/q_{t+1})$ , as in (Krusell et al., 2000) I make the simplifying assumption of  $(1 - \delta_e)\mathbb{E}(q_t/q_{t+1}) = (1 - \delta_e)(q_t/q_{t+1}) + v_t$  where  $v_t$  is normally distributed with mean zero and variance  $\eta_v^2$  this parameter is calibrated using data on  $q_t$ .<sup>6</sup> Putting everything together we have the following equation:

$$A_{t+1} G_{k_s}(X_{t+1}, \psi_{t+1} | \Phi) = q_t A_{t+1} G_{k_s}(X_{t+1}, \psi_{t+1} | \Phi) + (1 - \delta_e) \left( \frac{q_t}{q_{t+1}} \right) + v_t \quad (10)$$

The other two structural equations used to estimate the model compare the labor share observed in the data to labor share predicted by the model  $lsh(X_{t+1}, \psi_{t+1} | \Phi)$  and the wage-bill ratio observed in the data to wage-bill ratio predicted by the model  $wbr(X_{t+1}, \psi_{t+1} | \Phi)$ :

$$\frac{w_{s_t} h_{s_t} + w_{u_t} h_{u_t}}{Y_t} = lsh(X_t, \psi_t | \Phi) \quad (11)$$

$$\frac{w_{s_t} h_{s_t}}{w_{u_t} h_{u_t}} = wbr(X_t, \psi_t | \Phi) \quad (12)$$

Since the parameters  $\mu, \lambda, \psi_0^u, \psi_0^s$  act as scaling parameters, to estimate the model one must be fixed, I follow (Krusell et al., 2000) in fixing  $\psi_0^s$ , the initial value of the productivity of skilled labor. When replicating their result on an extended sample I choose to fix  $\psi_0^u = 6$  as in the original, but choose different variants when estimating each industry to improve fitness. Finally, the parameter  $\eta_\omega$  is chosen to minimize the distance between the skill premium in the data and the skill premium predicted by the model.

The estimation process is a simulated two-stage pseudo-maximum likelihood estimation (SPMLE) developed by (White, 1996). Is reasonable that the choice of labor is influenced by the shocks in labor productivity, therefore skilled and unskilled labor is treated as endogenous.

To allow for the possible dependence of hours worked on shocks, we use the two-stage SPML developed by, which is similar in spirit to two-stage least squares. We treat skilled and unskilled labor input as endogenous. To deal with the endogeneity, labor input is projected onto a constant, current, and lagged stock of capital equipment and structures, the lagged relative price of equipment, and a trend. The model is estimated using the instrumented labor input series, the series of capital, and prices as the inputs of the model.

The the next stage we proceed as follows: taking the variance  $\eta_\omega$  as given, for each date  $t$  generate  $S$  realizations the stochastic components of the model  $\varphi_t$  use those as inputs to generate  $S$  realization of the structural equations (10), (11) and (12), to simplify notation I refer to each of those values as  $\tilde{Z}_t^i(X_t, \psi_t | \Phi)$ , (note that this is a vector of three values, one for each of the equations). Using the simulated data we obtain the first and second moments of the

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<sup>6</sup>Since I use the same series of relative prices as KORV I take their calibration of  $\eta_v = 0.02$

model:

$$m(X_t, \psi_t | \Phi) = \frac{1}{S} \sum_{i=1}^S \tilde{Z}_t^i(X_t, \psi_t | \Phi) \quad (13)$$

and

$$V(X_t, \psi_t | \Phi) = \frac{1}{S-1} \sum_{i=1}^S \left( \tilde{Z}_t^i(X_t, \psi_t | \Phi) - m(X_t, \psi_t | \Phi) \right) \left( \tilde{Z}_t^i(X_t, \psi_t | \Phi) - m(X_t, \psi_t | \Phi) \right)' \quad (14)$$

Finally, we minimize the same objective function as (Krusell et al., 2000):

$$\begin{aligned} \ell(Z^T; X_t, \psi_t | \Phi) = & -\frac{1}{2T} \sum_{t=1}^T \left\{ [Z_t - m_S(\tilde{X}_t; \phi)]' (V_S(\tilde{X}_t; \phi))^{-1} [Z_t - m_S(\tilde{X}_t; \phi)] \right. \\ & \left. - \log \det(V_S(\tilde{X}_t; \phi)) \right\} \end{aligned} \quad (15)$$

where  $Z_t$  is the vector of model counterparts of  $\tilde{Z}_t^i(X_t, \psi_t | \Phi)$ .

## 6 Results

This section presents the results of the estimation process. I first show the result of the replication of KORV for different periods and then summarize the results of estimating the model for each industry.

### 6.1 KORV Replication

Table 1 compares the results obtained by (Krusell et al., 2000) to this replication using their original data (1963 - 1992)<sup>7</sup>. I present also the estimation on the extended sample (1963 - 2018) and on the subset of the extended sample for which there is coverage at the industry level (1988 - 2018).

	KORV Estimation 1963 - 1992	Replication 1963 - 1992	Updated Data 1963 - 2018	Updated Data 1988 - 2018
$\alpha$	0.117	0.113	0.118	0.08
$\sigma$	0.401	0.464	0.503	0.313
$\rho$	-0.495	-0.56	-0.343	-0.154
$\eta_\omega$	0.043	0.043	0.083	0.043

Table 1: Parameter estimates KORV model.

<sup>7</sup>Available at Gianluca Violante's website: [http://violante.mycpanel.princeton.edu/Journals/Data\\_KORV.txt](http://violante.mycpanel.princeton.edu/Journals/Data_KORV.txt)

Table 2 compares elasticities of substitution implied by the different parameter estimates obtained.

	KORV Estimation 1963 - 1992	Replication 1963 - 1992	Updated Data 1963 - 2018	Updated Data 1988 - 2018
$\sigma_s$	0.668896	0.641107	0.744831	0.857268
$\sigma_u$	1.66945	1.86506	2.01136	1.8599

Table 2: Implied Elasticities of Substitution

Figures 5, 6 and 7 show the fit of the estimation process for three samples described.

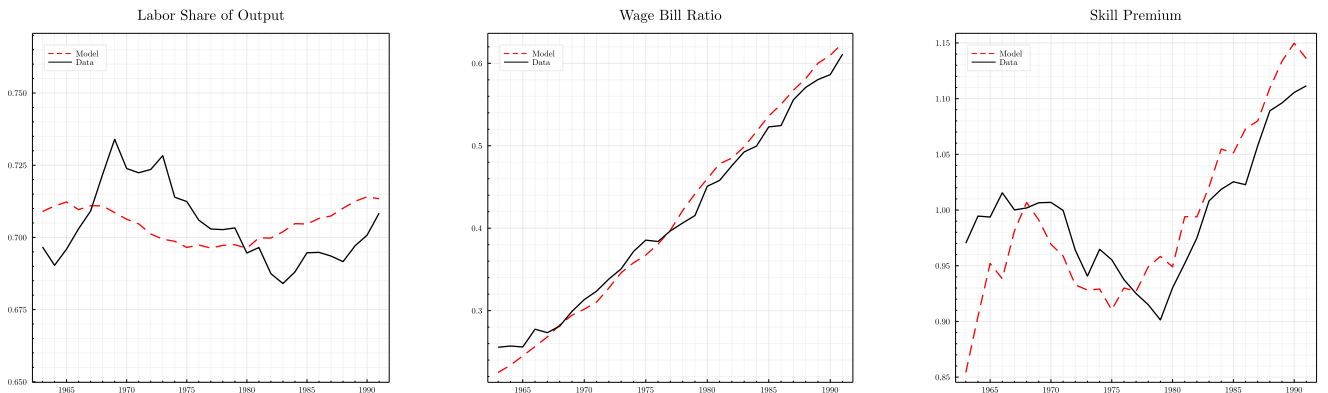


Figure 5: The model Fit for the 1963 - 1992 period with KORV Data.

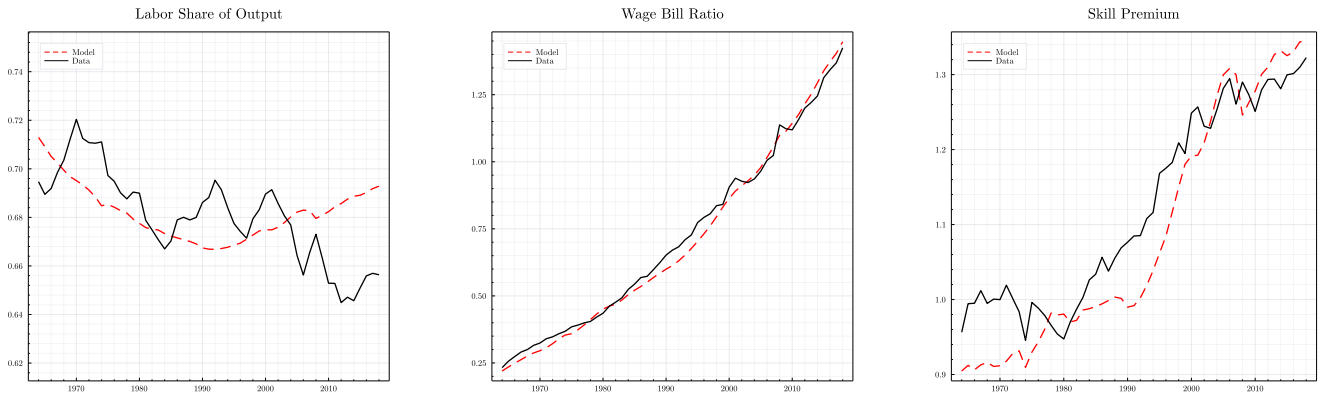


Figure 6: The model Fit for the 1963 - 2018 period with Updated Data.

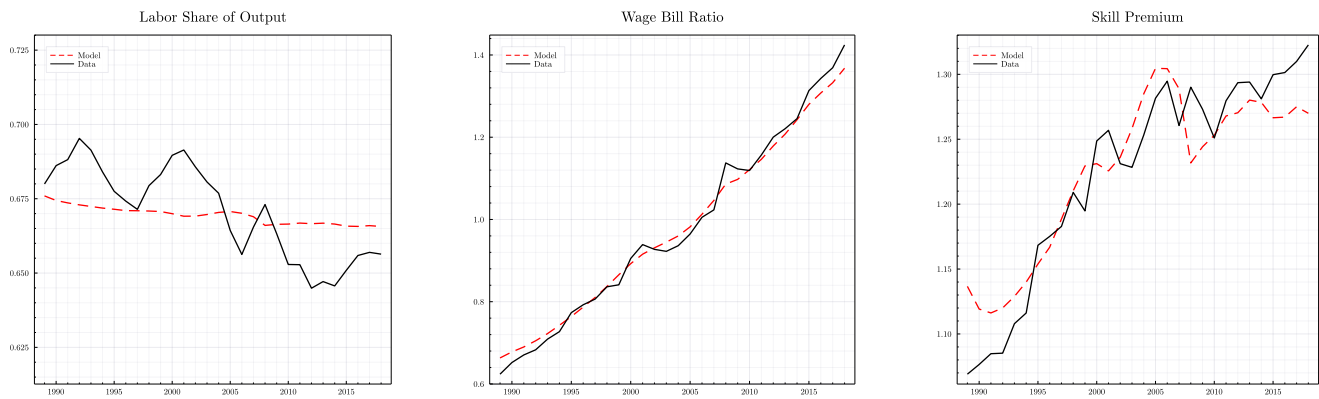


Figure 7: The model Fit for the 1988 - 2018 period with Updated Data.

As seen in table 1 **Describe results...**

## 6.2 Estimation by Industry

## References

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## A Ommited Derivations

Outline:

- FOC of Labor and Skill premium
- Log Linearization
- Write it as growth rates

To obtain a version of skill premium in terms of growth rates, start by writing a continuous time version of Equaiton (7):

$$\ln \omega(t) = \lambda \frac{\sigma - \rho}{\rho} \left( \frac{k_e(t)}{\psi^s(t)s(t)} \right)^\rho + (1 - \sigma) \ln \left( \frac{u(t)}{s(t)} \right) + \sigma \ln \left( \frac{\psi^s(t)}{\psi^u(t)} \right) \quad (16)$$

Start with the first term of the sum in the RHS:

$$\begin{aligned} \frac{\partial}{\partial t} \left( \left( \frac{k_e(t)}{\psi^s(t)s(t)} \right)^\rho \right) &= \rho \left( \frac{k'_e(t)}{\psi^s(t)s(t)} - k_e(t) \frac{\psi'^s(t)s(t) + \psi^s(t)s'(t)}{(\psi^s(t)s(t))^2} \right) \left( \frac{k_e(t)}{\psi^s(t)s(t)} \right)^{\rho-1} \\ &= \rho \left( \frac{k'_e(t)k_e(t)}{k_e(t)(\psi^s(t)s(t))} - k_e(t) \frac{\psi'^s(t)s(t) + \psi^s(t)s'(t)}{(\psi^s(t)s(t))^2} \right) \left( \frac{k_e(t)}{\psi^s(t)s(t)} \right)^{\rho-1} \\ &= \rho \left( \frac{k_e(t)}{\psi^s(t)s(t)} \right)^\rho \left( \frac{k'_e(t)}{k_e(t)} - \frac{\psi'^s(t)s(t) + \psi^s(t)s'(t)}{\psi^s(t)s(t)} \right) \\ &= \rho \left( \frac{k_e(t)}{\psi^s(t)s(t)} \right)^\rho \left( \frac{k'_e(t)}{k_e(t)} - \frac{\psi'^s(t)}{\psi^s(t)} - \frac{s'(t)}{s(t)} \right) \\ &= \rho \left( \frac{k_e(t)}{\psi^s(t)s(t)} \right)^\rho (g_{k_{e_t}} - g_{\psi^s_t} - g_{s_t}) \end{aligned}$$

The next two terms in the sum are very similar, for the first term we have:

$$\frac{\partial}{\partial t} \left( \ln \left( \frac{\ell(t)}{s(t)} \right) \right) = \frac{\partial}{\partial t} (\ln \ell(t) - \ln(s(t))) = \frac{\ell'(t)}{\ell(t)} - \frac{s'(t)}{s(t)} = g_{\ell_t} - g_{s_t} \quad (17)$$

Differentiating the LHS we get:

$$\frac{\partial}{\partial t} (\ln \omega(t)) = \frac{\omega'(t)}{\omega(t)} = g_{\omega_t}$$

## B Data Construction

### B.1 Capital Inputs and Labor Share

OUTLINE



- Mention why are those delators used.
- How is the depreciation rate constructed?

## B.2 Labor Inputs and Wage Rates

I include all observations excluding agents: younger than 16 or older than 70, unpaid family workers, those working in the military, those who report working less than 40 weeks a year and/or 35 hours a week, individuals with allocated income, those with hourly wages below half of the minimum federal wage rate, those did not report their education level and self-employed workers.

For each person, I record their characteristics age, sex, and race. Their employment statistics: employment status (`empstat`), class of worker (`classwly`), weeks worked last year (`wkswork1` and `wkswork2`), usual hours worked per week last year (`uhrsworkly` and hours work last week `ahrsworkt`). Their income: total wage and salary income `incwage` and the CPS personal supplement weights: `asecwt`.

To homogenize the data I create the following groups based on individual characteristics, age is divided into 11 five-year groups: 16 – 20, 21 – 25, 26 – 30, 31 – 35, 36 – 40, 41 – 45, 46 – 50 race is divided into white black and others. Sex is divided into, male and female and education is divided into four groups without high school, high school, some college and college graduates, and beyond. Then, each person is assigned to one of 264 groups created by age, race, sex, and skill (education).

For the period between 1963 to 1975 the variables weeks worked last year (`wkswork1`) and hours worked last year (`uhrsworkly`) are not recorded so I did the following substitution: For `wkswork1` we can use the variable `wkswork2` that consist of intervals of hours worked, and then perform the substitution with the average hours worked by individuals in the same group reporting the same value of `wkswork2` for the post 1975 period. For `uhrsworkly` I used hours worked last week (`ahrsworkt`) as a proxy.

For every individual I create the following variables:

- $\ell_{i,t}$  the hours worked by individual  $i$  in year  $t$ , is the product of hours worked per week times weeks worked that year.
- $w_{i,t}$  the hourly wage of individual  $i$  in year  $t$ , obtained by dividing yearly wage income by hours worked in year  $t$ .

Let  $\mathcal{G}$  be the collection of all groups we can calculate the weight of each group as  $\mu_{g,t} = \sum_{i \in g} \mu_{i,t}$  where  $\mu_{i,t}$  is the CPS weight of the individual. Average hours worked for each group  $g \in \mathcal{G}$ :

$$\ell_{g,t-1} = \frac{\sum_{i \in g} \ell_{i,t-1} \mu_{i,t}}{\mu_{g,t}}$$

and wages:

$$w_{g,t-1} = \frac{\sum_{i \in g} w_{i,t-1} \mu_{i,t}}{\mu_{g,t}}$$

Finally to obtain skilled and unskilled series labor input and wage series I partitioned the set  $\mathcal{G}$  in two subsets  $(\mathcal{S}, \mathcal{U})$  based on education (college graduates and non-college graduates). Let  $\{H, L\}$  indicate the group type, then the total labor input is:

$$L_{t-1}^U = \sum_{g \in \mathcal{U}} \ell_{g,t-1} \mu_{g,t} w_{g,80}$$

$$L_{t-1}^S = \sum_{g \in \mathcal{S}} \ell_{g,t-1} \mu_{g,t} w_{g,80}$$

$w_{g,80}$  is the wage of the group in 1980 and is used as a scaling factor. Then wages for each skill level are obtained as:

$$W_{t-1}^U = \frac{\sum_{g \in \mathcal{U}} w_{g,t-1} \ell_{g,t-1} \mu_{g,t}}{L_{t-1}^U}$$

$$W_{t-1}^S = \frac{\sum_{g \in \mathcal{S}} w_{g,t-1} \ell_{g,t-1} \mu_{g,t}}{L_{t-1}^S}$$

## C Industry Specific Trends