

Figure 1: SDE and SGD loss comparison under our linear regression setup with different LRS and α, β 's

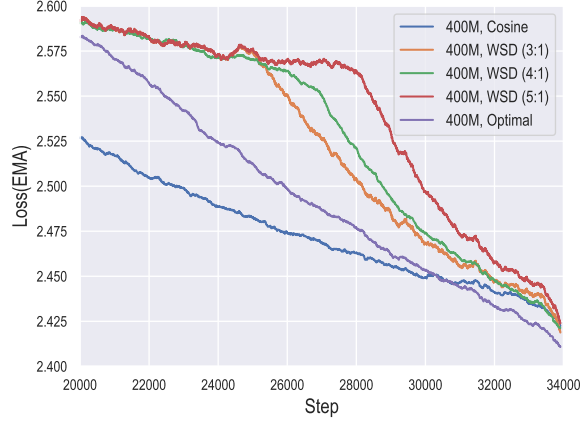


Figure 2: 400M Llama (dense) model, 20B data. WSD with different decaying ratio compared with the optimal

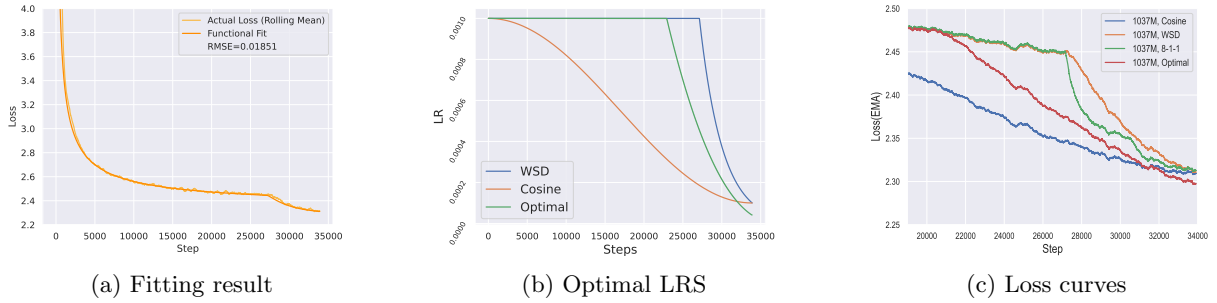
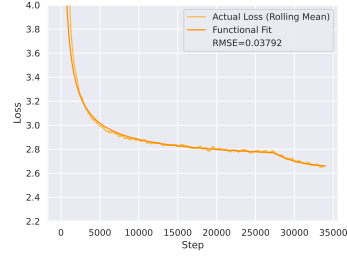
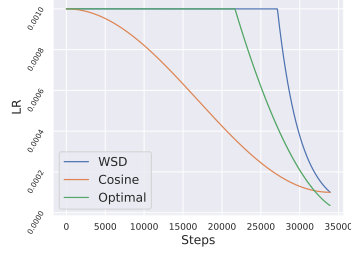


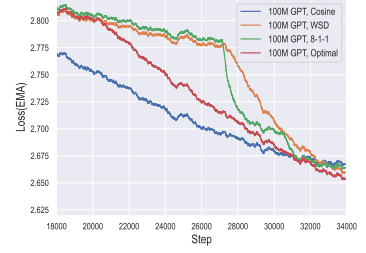
Figure 3: 1B Llama (dense) model, 20B data



(a) Fitting result

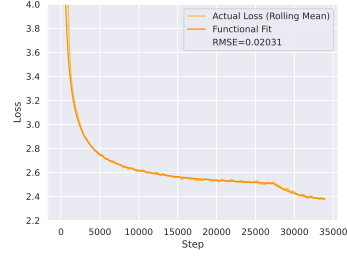


(b) Optimal learning rate

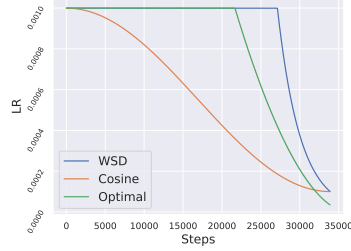


(c) Loss curves

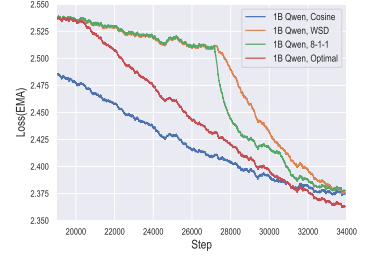
Figure 4: 100M GPT2 (dense) model, 20B data



(a) Fitting result

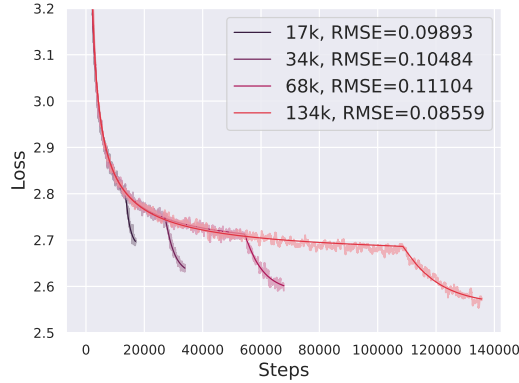


(b) Optimal learning rate

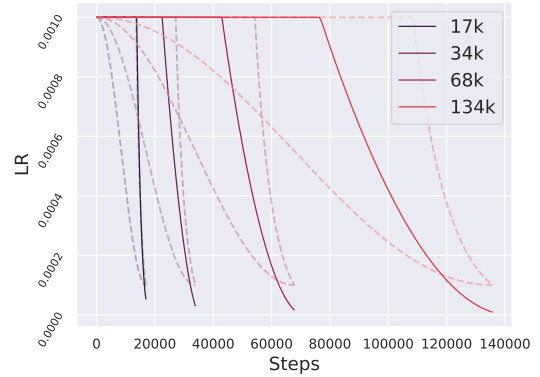


(c) Loss curves

Figure 5: 1B Qwen (MoE) model, 20B data

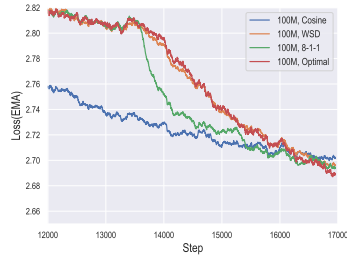


(a) Fitting result

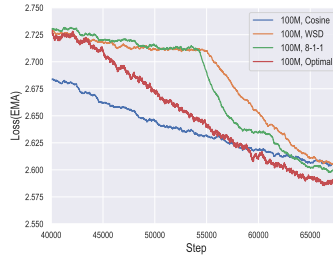


(b) Optimal learning rate

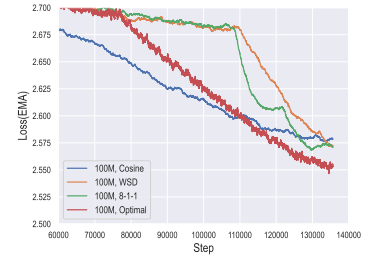
Figure 6: Fitted functional scaling laws and optimal LRS on different total training steps



(a) 17k steps



(b) 68k steps



(c) 134k steps

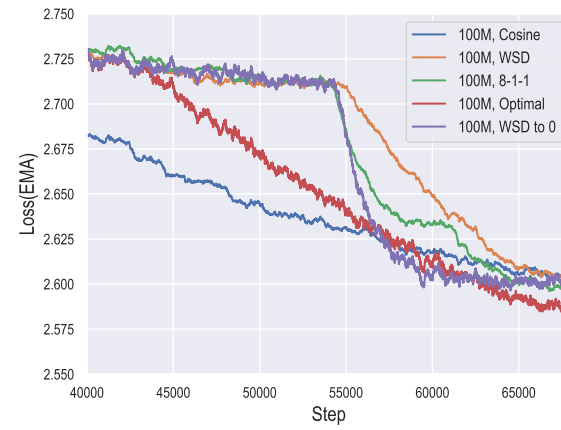


Figure 8: 100M Llama (dense) model, 40B data. WSD decaying to zero does not bring significant loss reduction