

QUESTION 1

Define Covariance and explain how it differs from Correlation in terms of scale and interpretation.

ANSWER

Covariance is a statistical measure that indicates the direction of the linear relationship between two variables. It shows whether the variables tend to increase or decrease together

Two variables X and Y

Positive covariance: Variables move in the same direction

Negative covariance: One variable increases while the other decreases

Zero covariance: No linear relationship

Difference Between Covariance and Correlation		Scale & Interpretation
Aspect	Covariance	Correlation
Scale	Depends on the units of XXX and YYY	Unit-free (dimensionless)
Range	No fixed range	Always between -1 and +1
Interpretation	Indicates direction only	Indicates both direction and strength
Comparability	Cannot be compared across datasets	Can be compared across datasets
Effect of Unit Change	Changes if units change	Remains unchanged

Covariance is useful for understanding the direction of a relationship.

Correlation offers more practical insight than covariance in most applications.

QUESTION 3	Discuss the limitations of covariance as a measure of relationship between two variables. Why is correlation preferred in many cases?
ANSWER	Covariance indicates whether two variables move together (positive covariance) or in opposite directions (negative covariance).
No Standardized Scale	<p>Covariance has no fixed range.</p> <p>Its value depends on the units of measurement of the variables</p> <p>A large covariance does not necessarily imply a strong relationship</p>
Difficult to Interpret Magnitude	The scale varies, we cannot compare covariances across different datasets.
	Why Correlation Is Preferred
	Correlation overcomes most of the drawbacks of covariance
	Standardized Measure
	<p>Correlation is unit-free.</p> <p>It is calculated by dividing covariance by the product of standard deviations.</p>
	Fixed Range
	Correlation values lie between -1 and $+1$.
	1 positive relationship
	-1 negative relationship
	0 no linear relationship

QUESTION 4	Explain the difference between Pearson's correlation coefficient and Spearman's rank correlation coefficient. When would you prefer to use Spearman's correlation?
ANSWER	Both Pearson's correlation coefficient and Spearman's rank correlation coefficient measure the relationship between two variables
	Pearson's Correlation Coefficient (r)
	Pearson's correlation measures the strength and direction of a linear relationship between two quantitative (continuous) variable
	Based on actual data values
	Measures linear relationships only
	Example: Relationship between height and weight.
	Spearman's Rank Correlation Coefficient (ρ or r_s)
	Spearman's correlation measures the strength and direction of a monotonic relationship using the ranks of data rather than actual values
	Based on ranks, not raw data
	Measures monotonic (increasing or decreasing) relationships
	Non-parametric
	Less affected by outliers
	When to Prefer Spearman's Correlation
	Data is ordinal (ranked data)
	he relationship is non-linear but monotonic
	Data contains outliers
	Use Pearson's correlation for linear relationships with normally distributed data.

QUESTION 5	If the correlation coefficient between two variables X and Y is 0.85, interpret this value in context. Can you infer causation from this value? Why or why not?
ANSWER	<p>Interpretation of a Correlation Coefficient of 0.85</p> <p>(r) = 0.85 indicates a strong positive linear relationship between variables X and Y.</p> <p>X increases, Y tends to increase as well.</p> <p>The points on a scatter plot would lie close to an upward-sloping straight line</p> <p>The relationship is strong, though not perfect (which would be $r = 1$).</p> <p>Can You Infer Causation from This Value?</p> <p>No, causation cannot be inferred from correlation alone</p> <p>X may affect Y, Y may affect X, or both may influence each other</p> <p>Hidden variable may be causing changes in both X and Y.</p> <p>A correlation coefficient of 0.85 shows a strong positive association between X and Y.</p>

QUESTION 6	Using the dataset below, calculate the covariance between X and Y				
		X	2	4	6
		Y	3	7	5
					8
					10
ANSWER	No of observation , N= 4				
		CALCULATE THE MEAN=	X= 2+4+6+8/4	20/4 =5	
			y= 3+7+5+10/4	25/4=6.25	
		Calculate Deviations and Their products			
		X	Y	(X-MEAN)	(Y-MEAN)
		2	3	-3	-3.25
		4	7	-1	0.75
		6	5	1	-1.25
		8	10	3	3.75
					PRODUCT
					9.75
					-0.75
					-1.25
					11.25
		SUM OF PRODUCTS			
			PRODUCT		
			9.75		
			-0.75		
			-1.25		
			11.25		
			TOTAL = 19		

QUESTION 7	Compute the Pearson correlation coefficient between variables A and B:					
	A	10	20	30	40	50
	B	8	14	18	24	28
ANSWER	NUMBERS OF OBSERVATION =5					
	calculate the mean A= 10+20+30+40+50/5= 150/5= 30					
		B= 8+14+18+24+28/5= 92/5= 18.4				
	CALCULATE THE STD					
	A	B	(A-MEAN)	(B MEAN)	PRODUCT	(A-A)*2
	10	8	-20	-10.4	208	400
	20	14	-10	4.4	44	100
	30	18	0	-0.4	0	0
	40	24	10	5.6	56	100
	50	28	20	9.6	192	400
	$\sum(A-A)(B-B)=208+44+0+56+192=500$					
	$\sum(A-A)^2=400+100+0+100+400=1000$					
	$r=\frac{\sum(A-A)\sum(B-B)}{\sqrt{\sum(A-A)^2\sum(B-B)^2}}$					
	$r= 500/\sqrt{1000*25}$					
	$r=500/\sqrt{251200}=$					

			$r=500/501.2$					
			$r=0.998$					

QUESTION 8

The following table shows heights (in cm) and weights (in kg) of 5 students. Find the correlation coefficient between Height and Weight.

HEIGHT	150	160	165	170	180
WEIGHT	50	55	58	62	70

ANSWER

Numbers of observation =5

calculate the mean $150+160+165+170+180/5= 825/5=165$

$50+55+58+62+70/=295/5=59$

calculate the std

students	Heigts	Weight	(Height-mean)	(Weight-mean)	products	(x-x)*2	(Y-Y)*2
1	150	50	-15	-9	135	225	81
2	160	55	-5	-4	20	25	16
3	165	58	0	-1	0	0	1
4	170	62	5	3	15	25	9
5	180	70	15	11	165	225	121

$$\sum(X-X)(Y-Y)=135+20+0+15+165=335$$

$$\sum(X-X)^2=225+25+0+25+225=500$$

$$\sum(Y-Y)^2=81+16+1+9+121=228$$

$$r=\frac{\sum(x-x)-(Y-Y)}{\sqrt{\sum(X-X)^2\sum(Y-Y)^2}}$$

			$r=335/\sqrt{500*228}$						
			$r=335/\sqrt{114000}$						
			$r=335/\sqrt{337.64}$						
			$r=0.99$						

QUESTION 9		Given the dataset below, determine whether there is a positive or negative correlation between X and Y. (No need for exact calculation, just reasoning.)								
		X	1	2	3	4	5			
		Y	15	12	9	7	3			
ANSWER										
		As X increases from 1 to 5,								
		Y consistently decreases from 15 to 3.								
		When one variable goes up, the other goes down.								
		There is a negative correlation between X and Y.								

QUESTION 10

Two investment portfolios have the following returns (%) over 5 years. Compute the covariance and correlation coefficient, and interpret whether the portfolios move together.

YEAR	PORTFOLIO A	PORTFOLIO B
1	8	6
2	10	9
3	12	11
4	9	8
5	11	10

ANSWER

calculate the mean

$$X = \frac{8+10+12+9+11}{5} = 50/5 = 10$$

$$Y = \frac{6+9+11+8+10}{5} = 44/5 = 8.8$$

YEAR	A	B	(X-MEAN)	(Y-MEAN)	PRODUCT	(X-X)*2	(Y-Y)*2
1	8	6	-2	-2.8	5.6	4	7.84
2	10	9	0	0.2	0	0	0.04
3	12	11	2	2.2	4.4	4	4.84
4	9	8	-1	0.8	0.8	1	0.64
5	11	10	1	1.2	1.2	1	1.44

$$\sum(X-X)(Y-Y) = 5.6+0+4.4+0.8+1.2=12$$

$$\sum(X-X)^2 = 4+0+4+1+1=10$$

$$\sum(Y-Y)^2 = 7.84+0.04+4.84+0.64+1.44=14.8$$

$$\text{COV}(X,Y) = \frac{12}{N-1} = \frac{12}{4} = 3$$

$$r = \frac{\sum(X-X)(Y-Y)}{\sqrt{\sum(X-X)^2 \sum(Y-Y)^2}}$$

$$r = \frac{12}{\sqrt{10 \cdot 14.8}}$$

$$\frac{12}{\sqrt{148}}$$

$$\frac{12}{12.17}$$

$$r = 0.99$$