

1) NAIVE STRING :

```
Algo:  
Start  
pat_len := pattern Size  
str_len := string size  
for i := 0 to (str_len - pat_len), do  
for j := 0 to pat_len, do  
if text[i+j] ≠ pattern[j], then  
break  
if j == patLen, then  
display the position i, as there pattern found  
End
```

TIME COMPLEXITY: The time complexity of the Naive Algorithm is $O(mn)$, where m is the size of the pattern to be searched and n is the size of the container string.

2) QUICK SORT BY D&C :

```
Algo:  
quickSort(arr[], low, high) {  
    if (low < high) {  
        /* pi is partitioning index, arr[pi] is now at right place */  
        pi = partition(arr, low, high);  
        quickSort(arr, low, pi - 1); // Before pi  
        quickSort(arr, pi + 1, high); // After pi  
    }  
}  
partition (arr[], low, high)  
{  
    // pivot (Element to be placed at right position)  
    pivot = arr[high];  
    i = (low - 1) // Index of smaller element and indicates the  
    // right position of pivot found so far  
    for (j = low; j <= high- 1; j++){  
        // If current element is smaller than the pivot  
        if (arr[j] < pivot){  
            i++; // increment index of smaller element  
            swap arr[i] and arr[j]  
        }  
    }  
    swap arr[i + 1] and arr[high])  
    return (i + 1)
```

Time Complexity

Best $O(n \log n)$

Worst $O(n^2)$

Average $O(n \log n)$

Space Complexity $O(\log n)$

3) SELECTION SORT

Algo:

```
void selectionSort(int arr[], int n)  
{  
    int i, j, min_idx;  
    // One by one move boundary of unsorted subarray
```

```

for (i = 0; i < n-1; i++)
{
// Find the minimum element in unsorted array
min_idx = i;
for (j = i+1; j < n; j++)
if (arr[j] < arr[min_idx])
min_idx = j;
// Swap the found minimum element with the first element
if(min_idx != i)
swap(&arr[min_idx], &arr[i]); }

```

Time Complex:

Best Case n2

Average Case n2

Worst Case n2

4) KNAPSACK BY GREEDY

Algo:

Greedy-fractional-knapsack (w, v, W)

FOR i =1 to n

do x[i] =0

weight = 0

while weight < W

do i = best remaining item

IF weight + w[i] ≤ W

then x[i] = 1

weight = weight + w[i]

else

x[i] = (w - weight) / w[i]

weight = W

return x

Time Complexity: O(2n)

5) BELLMAN FORD :

Algo:

function bellmanFord(G, S)

for each vertex V in G

distance[V] <- infinite

previous[V] <- NULL

distance[S] <- 0

for each vertex V in G

for each edge (U,V) in G

tempDistance <- distance[U] + edge_weight(U, V)

if tempDistance < distance[V]

distance[V] <- tempDistance

for each edge (U,V) in G

If distance[U] + edge_weight(U, V) < distance[V]

Error: Negative Cycle Exists

return distance[]

TIME COMPLEXITY:

O(V * E), where V is the number of vertices in the graph and E is the number of edges in the graph

6) MERGE SORT :

Algo:

```
void merge(int arr[], int l, int m, int r)
{
    int i, j, k;
    int n1 = m - l + 1;
    int n2 = r - m;
```

Thus, time complexity of merge sort algorithm is $T(n) = \Theta(n\log n)$.

7) BINARY SEARCH :

Algo:

```
Algorithm BinSearch(a,n,x)
{
    low := 1; high := n;
    while (low <= high) do
    {
        mid = |(low+high)/2|;
        if(x < a[mid]) then high = mid-1;
        else if(x > a[mid]) then low = mid+1;
        else return mid;
    }
    return 0;
}
```

Time Complexity:

After each comparison the input size decreases by half.

- Best case complexity: $O(1)$
- Average case complexity: $O(\log n)$
- Worst case complexity: $O(\log n)$

8) INSERTION SORT :

Insertion sort algorithm:

```
for j = 2 to A.length
key ← A[j]
// Insert A[j] into the sorted sequence A[1 .. j-1]
i ← j - 1
while i > 0 and A[i] > key
A[i+1] ← A[i]
i ← i - 1
A[i+1] ← key
```

Best Case n

Average Case n^2

Worst Case n^2

9) LCS :

Algo:

```
X.label = X
Y.label = Y
LCS[0][0] = 0
LCS[0][0] = 0
Start from LCS[1][1]
```

Compare X[i] and Y[j]

If X[i] = Y[j]

LCS[i][j] = 1 + LCS[i-1, j-1]

Point an arrow to LCS[i][j]

Else

LCS[i][j] = max(LCS[i-1][j], LCS[i][j-1])

Point an arrow to max(LCS[i-1][j], LCS[i][j-1])

Time Complexity: O(m*n)

10) N QUEENS :

Algorithm for N-Queens Problem using Backtracking

Step 1 - Place the queen row-wise, starting from the left-most cell.

Step 2 - If all queens are placed then return true and print the solution matrix.

Step 3 - Else try all columns in the current row.

Condition 1 - Check if the queen can be placed safely in this column then mark the current cell [Row, Column] in the solution matrix as 1 and try to check the rest of the problem recursively by placing the queen here leads to a solution or not.

Condition 2 - If placing the queen [Row, Column] can lead to the solution return true and print the solution for each queen's position.

Condition 3 - If placing the queen cannot lead to the solution then unmark this [row, column] in the solution matrix as 0, BACKTRACK, and go back to condition 1 to try other rows.

Step 4 - If all the rows have been tried and nothing worked, return false to trigger backtracking.

Time Complexity: O(N!)

11) TRAVELLING SALESMAN PROBLEM :

ALGO :

TSP(N,S)

VISITED[S]=1;

if(n=2)and k is not equal to s then

 cost(n,k)=cost(s,k);

 return cost;

else

 for jEn do (E is belongs to)

 for iEn and visited[i]=0 (E is belongs to)

 if j is not equal to i and j is not equal to s then

 cost(n,j)=min(tsp(n-{i},j)+cost(j,i))

 visited[j]=1

 end

 end

 end

 return cost

end

TIME COMPLEXITY : O(N RAISED TO 2 . 2 RAISED TO N)