

### 1) NAIVE STRING :

Algo:

Start

pat\_len := pattern Size

str\_len := string size

for i := 0 to (str\_len - pat\_len), do

for j := 0 to pat\_len, do

if text[i+j] ≠ pattern[j], then

break

if j == patLen, then

display the position i, as there pattern found

End

TIME COMPLEXITY: The time complexity of the Naive Algorithm is  $O(mn)$ , where  $m$  is the size of the pattern to be searched and  $n$  is the size of the container string.

### 2) QUICK SORT BY D&C :

Algo:

quickSort(arr[], low, high) {

if (low < high) {

/\* pi is partitioning index, arr[pi] is now at right place \*/

pi = partition(arr, low, high);

quickSort(arr, low, pi - 1); // Before pi

quickSort(arr, pi + 1, high); // After pi

}

}

partition (arr[], low, high)

{

// pivot (Element to be placed at right position)

pivot = arr[high];

i = (low - 1) // Index of smaller element and indicates the

// right position of pivot found so far

for (j = low; j <= high- 1; j++){

// If current element is smaller than the pivot

if (arr[j] < pivot){

i++; // increment index of smaller element

swap arr[i] and arr[j]

}

}

swap arr[i + 1] and arr[high])

return (i + 1)

Time Complexity

Best  $O(n \log n)$

Worst  $O(n^2)$

Average  $O(n \log n)$

Space Complexity  $O(\log n)$

### 3) SELECTION SORT

Algo:

void selectionSort(int arr[], int n)

{

int i, j, min\_idx;

// One by one move boundary of unsorted subarray

```

for (i = 0; i < n-1; i++)
{
// Find the minimum element in unsorted array
min_idx = i;
for (j = i+1; j < n; j++)
if (arr[j] < arr[min_idx])
min_idx = j;
// Swap the found minimum element with the first element
if(min_idx != i)
swap(&arr[min_idx], &arr[i]); }

```

Time Complex:

Best Case  $n^2$

Average Case  $n^2$

Worst Case  $n^2$

#### 4) KNAPSACK BY GREEDY

Algo:

Greedy-fractional-knapsack (w, v, W)

FOR i =1 to n

do x[i] =0

weight = 0

while weight < W

do i = best remaining item

IF weight + w[i] ≤ W

then x[i] = 1

weight = weight + w[i]

else

x[i] = (w - weight) / w[i]

weight = W

return x

Time Complexity:  $O(2n)$

#### 5) BELLMAN FORD :

Algo:

function bellmanFord(G, S)

for each vertex V in G

distance[V] <- infinite

previous[V] <- NULL

distance[S] <- 0

for each vertex V in G

for each edge (U,V) in G

tempDistance <- distance[U] + edge\_weight(U, V)

if tempDistance < distance[V]

distance[V] <- tempDistance

for each edge (U,V) in G

If distance[U] + edge\_weight(U, V) < distance[V]

Error: Negative Cycle Exists

return distance[]

TIME COMPLEXITY:

$O(V * E)$ , where V is the number of vertices in the graph and E is the number of edges in the graph

## 6) MERGE SORT :

Algo:

```
void merge(int arr[], int l, int m, int r)
{
    int i, j, k;
    int n1 = m - l + 1;
    int n2 = r - m;
```

Thus, time complexity of merge sort algorithm is  $T(n) = \Theta(n \log n)$ .

## 7) BINARY SEARCH :

Algo:

Algorithm BinSearch(a,n,x)

```
{
    low := 1; high := n;
    while (low <= high) do
    {
        mid = |(low+high)/2|;
        if (x < a[mid]) then high = mid-1;
        else if (x > a[mid]) then low = mid+1;
        else return mid;
    }
    return 0;
}
```

Time Complexity:

After each comparison the input size decreases by half.

- Best case complexity:  $O(1)$
- Average case complexity:  $O(\log n)$
- Worst case complexity:  $O(\log n)$

## 8) INSERTION SORT :

Insertion sort algorithm:

```
for j = 2 to A.length
    key ← A[j]
    // Insert A[j] into the sorted sequence A[1 .. j-1]
    i ← j - 1
    while i > 0 and A[i] > key
        A[i+1] ← A[i]
        i ← i - 1
    A[i+1] ← key
```

Best Case  $n$

Average Case  $n^2$

Worst Case  $n^2$

## 9) LCS :

Algo:

X.label = X

Y.label = Y

LCS[0][ ] = 0

LCS[ ][0] = 0

Start from LCS[1][1]

Compare  $X[i]$  and  $Y[j]$

If  $X[i] = Y[j]$

$LCS[i][j] = 1 + LCS[i-1, j-1]$

Point an arrow to  $LCS[i][j]$

Else

$LCS[i][j] = \max(LCS[i-1][j], LCS[i][j-1])$

Point an arrow to  $\max(LCS[i-1][j], LCS[i][j-1])$

Time Complexity:  $O(m*n)$

10) N QUEENS :

Algorithm for N-Queens Problem using Backtracking

Step 1 - Place the queen row-wise, starting from the left-most cell.

Step 2 - If all queens are placed then return true and print the solution matrix.

Step 3 - Else try all columns in the current row.

Condition 1 - Check if the queen can be placed safely in this column then mark the current cell [Row, Column] in the solution matrix as 1 and try to check the rest of the problem recursively by placing the queen here leads to a solution or not.

Condition 2 - If placing the queen [Row, Column] can lead to the solution return true and print the solution for each queen's position.

Condition 3 - If placing the queen cannot lead to the solution then unmark this [row, column] in the solution matrix as 0, BACKTRACK, and go back to condition 1 to try other rows.

Step 4 - If all the rows have been tried and nothing worked, return false to trigger backtracking.

Time Complexity:  $O(N!)$

11) TRAVELLING SALESMAN PROBLEM :

ALGO :

TSP(N,S)

VISITED[S]=1;

if(n=2) and k is not equal to s then

$cost(n,k)=cost(s,k);$

return cost;

else

for  $j \in E$  do ( E is belongs to )

for  $i \in E$  and  $visited[i]=0$  ( E is belongs to )

if j is not equal to i and j is not equal to s then

$cost(n,j)=\min(cost(n-\{i\},j)+cost(j,i))$

$visited[j]=1$

end

end

end

return cost

end

TIME COMPLEXITY :  $O(N \text{ RAISED TO } 2 \cdot 2 \text{ RAISED TO } N)$