5 RESULTS

$\begin{array}{c} {\bf Efficient} \,\, {\bf Execution} \,\, {\bf of} \,\, {\bf DG\text{-}FEM} \,\, {\bf workloads} \,\, {\bf on} \\ {\bf GPUs} \,\, {\bf via} \,\, {\bf CUDAGraphs} \end{array}$

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ABSTRACT

Array programming paradigm offers routines to express the computation cleanly for for a wide variety of scientific computing applications (Finite Element Method, Stencil Codes, Image Processing, Machine Learning, etc.). While these routines are optimized to provide efficient data structures and fast library implementations for many common array operations, the performance benefits are tied to optimized method calls and vectorized array operations, both of which evaporate in larger scientific codes that do not adhere to these constraints. While there have been a lot of efforts in scaling up n-d array applications through kernel and loop fusion, very little attention has been paid towards harnessing the concurrency across array operations. The dependency pattern between these array operations allow multiple array operations to be executed concurrently. This concurrency can be targeted to accelarate the application's performance. NVIDIA's CUDAGraph API offers a task programming model that can help realise this concurrency by overcoming kernel launch latencies and exploiting kernel overlap by scheduling multiple kernel executions in parallel. In this work we create a task-based lazy-evaluation array programming interface by mapping array operations onto CUDAGraphs using Pytato's IR and PyCUDA's GPU scripting interface. To evaluate the soundness of this approach, we port a suite of complex operators that represent real world workloads to our framework and compare the performance with a version where the array operations are executed one after the other. We observe a performance of upto X for Wave operators, Y for Euler Operators and X for Compressible Navier Stokes.

1. INTRODUCTION

Array programming is a fundamental computation model that supports a wide variety of features, including array slicing and arbitary element-wise, reduction and broadcast operators allowing the interface to correspond closely to the mathematical needs of the applications. PyCUDA and several other array-based frameworks serve as drop-in replacements for accelarating Numpy-like operations on GPUs. While abstractions like GPUArray's offer a very convenient abstraction for doing "stream" computing on these arrays, they are not yet able to automatically schedule and manage overlapping array operations onto multiple streams. The concurrency available in the dependency pattern for these array routines can be exploited to saturate all of the available execution units [Fig. 1].

Currently the only way to tap into this concurrency is by manually scheduling array operations onto mutliple CUDA streams which typically requires a lot of experimentation since information about demand resources of a kernel such as GPU threads, registers and shared memory is only accessible at runtime.

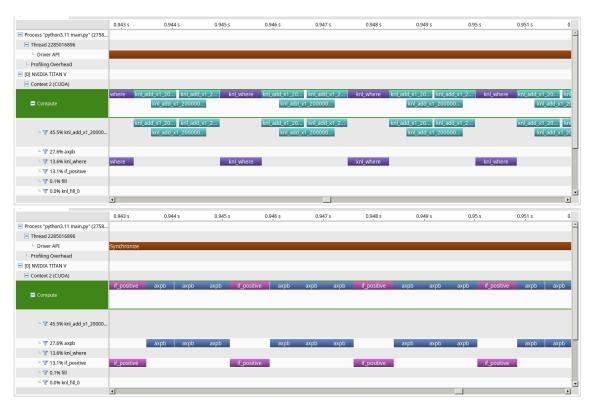


Figure 1. Profiles for CUDAGraph (top) and PyCUDA (bottom) for where (condition, if, else) + 1

Our framework realises this concurrency across array operations through NVIDIA's CUDAGraph API. CUDAGraph, first introduced in CUDA 10, is a task-based programming model that allows asynchronous execution of a user-defined Directed Acyclic Graph (DAG). These DAGs are made up of a set of node representing operations such as memory copies and kernel launches, connected by edges representing run-after dependencies which are defined separetly from its execution through a custom API.

2 Related work 5

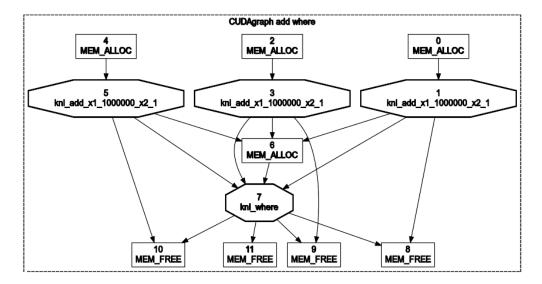


Figure 2. CUDAGraph API generated graph for where (condition, if, else) + 1

We formulate our system by building a CUDAGraph-based PyCUDA target for Pytato's IR which captures the user-defined DAG. The key technical contributions of our system involve:

- 1. Extending PyCUDA to allow calls to the CUDAGraph API
- 2. Mapping the array operations onto a DAG through Pytato's IR to generate PyCUDA-CUDAGraph code.

2. Related work

The literature on task-based array programming can be classified roughly according to their choice of task granularity.

Function: Castro et give an overview of the current task-based Python computing land-scape by mentioning several libraries that rely on decorators. A decorator is an instruction set before the definition of a function. The decorator function transforms the user function (if applicable) into a parallelization-friendly version. Libraries such as PyCOMPs, Pygion, PyKoKKos and Legion make use of this core principle to accelarate vanilla Python code. PyCOMPs and Pygion both rely on @task decorator to build a task dependency graph and define the order of execution. PyKoKKos ports into the KoKKos API and passes the @pk.workunit decorator into the parallel_for() function. Legion uses a data-centric programming model which relies on software out-of-order processor (SOOP), for scheduling tasks which takes locality and independence properties captured by logical regions while making scheduling decisions.

In Jug, arguments take values or outputs of another tasks and parallelization is achieved by running more than one Jug processes for distributing the tasks. In Pydron, decorated functions are first translated into an intermediate representation and then analyzed by a scheduler which updates the execution graph as each task is finished.

Since all of these frameworks rely on explicit taks declarations, they are not able to realise the concurrency available across array operations.

Stream: CuPy serves as a drop-in replacement to Numpy and uses NVIDIA's in-house CUDA frameworks such as cuBLAS, cuDNN and cuSPARSE to accelerate its performance. Julia GPU programming models use CUDA.jl to provide a high level mechanics to define multidimenstional arrays (CUArray). Both CuPy and Julia offer interfaces for *implcit* graph construction which *captures* a CUDAGraph using existing stream-based APIs. Implicit CUDAGraph construction is more flexible and general, but requires to wrangle with conconcurrency details through events and streams.

Although capturing all the operations on a stream leads to a terse application code, staging computations within a user-code with interleaving in-graph and out-of-graph operations cannot be expressed. This leads to multiple DAGs which can potentially trigger recomputations for each graph launch.

Delayed Execution model: JAX optimizes GPU performance by translating high-level traces into XL HLO and then performing vectorization/parallelization and JIT compilation. Deep learning symbolic mathematical libraries such as TensorFlow and Pytorch allow neural networks to be specified as DAGs along which data is transformed. Just like CUDAGraphs, in TensorFlow, computational DAGs are defined statically to achieve close to . PyTorch on the other hand offers more control at runtime by allowing the modification of executing nodes facilitating the implementation of sophosticated training routines.

Kernel: StarPU supports a task-based programming model by scheduling tasks efficiently using well-known generic dynamic and task graph scheduling policies from the literature, and optimizing data transfers using prefetching and overallaping. Each StarPU task describes the computation kernel, possible implementations on different architectures (CPUs/GPUs), what data is being accessed and how its accessed during computation (read/write mode). Task dependencies are inferred from data dependencies.

3. OVERVIEW

3.1. CUDA Graphs

CUDAGraphs provide a way to execute a partially ordered set of compute/memory operations on a GPU, compared to the fully ordered CUDA streams: a stream in CUDA is a queue of copy and compute commands. Within a stream, enqueueud operations are implicitly synchronized by the GPU in order to execute them in the same order as they are placed into the stream by the programmer. Streams allow for aschnronous compute and copy, meaning that CPU cores dispatch commands without waiting for their GPU-side completition: even in asynchronous submissions, little to no control is left to the programmer with respect to when commands are inserted/fetched to/from the stream and then dispatched to the GPU engines, with these operations potentially overallaping in time.

CUDAGraphs faciliate the mapping of independent A CUDAGraph is a set of nodes representing memory/compute operations, connected by edges representing run-after dependencies. CUDA 10 introduces explicit APIs for creating graphs, e.g. cuGraphCreate, to create a graph; cuGraphAddMemAllocNode/cuGraphAddKernelNode/cuGraphMemFreeNode, to add a new node to the graph with the corresponding run-after dependencies with previous nodes to be exected on the GPU; cuGraphInstantiate, to create an executable graph in a stream; and a cuGraphLaunch, to launch an executable graph. We wrapped this API using PyCUDA which provided a high level Python scripting interface for GPU programming. The table below lists commonly used PyCUDA-CUDAGraph functions. Refer to [link] for a comprehensive list of wrapped functions.

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Operations	PyCUDA routines
Memory Allocation	add_memalloc_node
Kernel Execution Host to Device Copy	add_kernel_node add_memcpy_htod_node
Device to Device Copy Device to Host Copy	add_memcpy_dtod_node add_memcpy_dtoh_node
Memory Free Graph Creation	add_memfree_node Graph
Graph Instantiation Update ExecGraph arguments	<pre>GraphExec batched_set_kernel_node_arguments</pre>
Graph Launch	launch

Table 1. PyCUDA wrapper functions around CUDAGraph API

Here's a simple example demonstrating CUDAGraph functionality:

```
# Create Graph
g = drv.Graph()
# Create and load kernel module
mod = SourceModule("
      #define bIdx(N) ((int) blockIdx.N)\n#define tIdx(N) ((int)
      threadIdx.N)\n\nextern "C" __global__ void __launch_bounds__(16)
      doublify(double
      *_restrict__ out, double const <math>*_restrict__ in1)\n{\n }
      int const ibatch = 0; \n\n out [4 * (tIdx(x) / 4) + tIdx(x) + -4 *
     (tIdx(x) / 4)] = 2.0 * _in1[4 * (tIdx(x) / 4) + tIdx(x) + -4 * (
      tIdx(x) / 4); \n \n\")
# Get kernel function
doublify = mod.get_function("doublify")
# Initialize input array
a = np.random.randn(4, 4).astype(np.float64)
# Initialize result array
a_doubled = np.empty_like(a)
# Allocate memory on GPU for input array
a_gpu = drv.mem_alloc(a.nbytes)
# Add memcpy node for host to device transfer
memcpy_htod_node = g.add_memcpy_htod_node(a_gpu, a, a.nbytes)
# Add kernel node for array operation
kernel_node = g.add_kernel_node(a_gpu, func=doublify, block=(4, 4, 1),
                                dependencies=[memcpy_htod_node])
# Add memcpy node for device to host transfer
memcpy_dtoh_node = g.add_memcpy_dtoh_node(a_doubled, a_gpu, a.nbytes,
                                [kernel_node, memcpy_htod_node])
```

```
# Instantite execution graph
g_exec = drv.GraphExec(g)

# Launch execution graph on default stream
g_exec.launch()
```

3.2. Loopy

Loopy is a Python-based transformation toolkit to generate transformed kernels. We make use of the following components in our pipeline to generate performance tuned CUDA kernels:

- 1. Loop Domains: The upper and lower bounds of the result array's memory access pattern in the OpenCL format sourced from the shape attribute within IndexLambda and expressed using the isl library.
- 2. Statement: A set of instructions specificed in conjuction with an iteration domain which encodes an assignment to an entry of an array. The right-hand side of an assignment consists of an expression that may consist of arithmetic operations and calls to functions.
- 3. Kernel Data: A sorted list of arguments capturing all of the array node's dependencies.

3.3. Pytato

Pytato is a lazy-evaluation programming based Python package that offers a subset of Numpy operations for manipulating multidimensional arrays. This provides the convenience of realzing one-dimensional layout of memory buffer for large scale multidimensional scientific computing workloads (PDE-based numerical methods, deep learning, computational statistics etc.) where the higher dimensional vizualization of data is close to the mathematical notation.

Pytato offers an IR which encodes user defined array computations as a DAG where nodes correspond to array operations and edges representing dependencies between inputs/outputs of these operations. We map the set of nodes provided by Pytato's IR onto the following two node to simplify code generation:

- 1. Placeholder: A named abstract array whose shape and dtype is known with data supplied during runtime. This permits the automated gathering of a self-contained description of a piece of code without incurring the penalty faced by repeated memory transfers from the device's DRAM to lower levels of cache.
- 2. IndexLambda: Represents an array comprehension recording a scalar expression containing per index value of the array computation. This helps create a generalized

Here's a simple example demonstrating Pytato usage

```
# CreatePlaceholder node for storing array description
x = pt.make_placeholder(name="x", shape=(4,4), dtype="float64")
# Express array computation as a scalar expression using Indexlambda
result = 2*x
# {{{ execute }
import pyopencl as cl
ctx = cl.create_some_context()
queue = cl.CommandQueue(ctx)
prg = pt.generate_loopy(result, cl_device=queue.device)
a = np.random.randn(4, 4).astype(np.float64)
_, out = prg(queue, x=x)
# }}
```

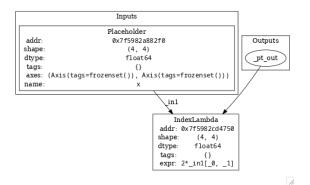


Figure 3. Pytato IR corresponding to doubling operation

4. Array Operations to CudaGraph Transformation

Pytato provides a pt.compile decorator which triggers a two-stage code generation process that traces the array program and generates PyCUDA-CUDAGraph code.

```
# {{{ Stage 1: Build and cache CUDAGraph
@cache
def exec_graph_builder():
   _pt_g = _pt_drv.Graph()
   _pt_buffer_acc = {}
    _pt_node_acc = {}
    _pt_memalloc, _pt_array = _pt_g.add_memalloc_node(size=128,
dependencies=[])
    _pt_kernel_0 = _pt_g.add_kernel_node(_pt_array, 139712027164672,
func=_pt_mod_0.get_function('knl_indexlambda'), block=(16, 1, 1),
grid=(1, 1, 1), dependencies=[_pt_memalloc])
    _pt_buffer_acc['_pt_array'] = _pt_array
   _pt_node_acc['_pt_kernel_0'] = _pt_kernel_0
   _pt_g.add_memfree_node(_pt_array, [_pt_kernel_0])
    return (_pt_g.get_exec_graph(), _pt_g, _pt_node_acc, _pt_buffer_acc)
# }}}
# {{{ Stage 2: Update execution graph
def _pt_kernel(allocator=cuda_allocator, dev=cuda_dev, *, _pt_data):
    _pt_result = _pt_gpuarray.GPUArray((4, 4), dtype='float64',
allocator=allocator, dev=dev)
    _pt_exec_g, _pt_g, _pt_node_acc, _pt_buffer_acc =
exec_graph_builder()
    _pt_exec_g.batched_set_kernel_node_arguments({_pt_node_acc['_pt_kernel_0']:
_pt_drv.KernelNodeParams(args=[_pt_result.gpudata, _pt_data.gpudata])})
   _pt_exec_g.launch()
    _pt_tmp = {'2a': _pt_result}
   return _pt_tmp
# }}}
```

4.1. Stage 1: Build CUDAGraph

Alg 1 only gets executed only once during compilation with a $\Theta(V+E)$ complexity for Alg 2

Algorithm 1: DAG Discovery for building CUDAGraph

Step 1: Run a topological sort on Pytato IR using Kahn's algorithm. This frontloads the *sink* nodes which helps avoid array recomputations during DAG discovery. Initialize a pycuda. Graph object.

Step 2

```
for n \in \text{nodes} in Pytato IR which only have incoming edges do GRAPHTRAVERSE(n) done
```

Step 3: Instantiate pycuda. Graph object and cache the resultant pycuda. GraphExec object to avoid triggering traversals of the entire graph for subsequent launches.

Algorithm 2: Pytato IR Traversal

```
function GraphTraverse(n)
    if n \in \{PlaceHolder, DataWrapper\} {
            PLACEHOLDERMAPPER(n)
            Link to user provided buffers or generate new buffers via GPUArrays.
        return \{n\}
    }
    else {
```

- IndexLambdaMapper(n)
- Generate kernel string and launch dimensions by plugging IndexLambda expression into lp.make_kernel.
- Add kernel node with temporary buffer arguments and corresponding result memalloc node to pycuda. Graph object with dependencies sourced from Pytato IR.
- Update Pytato IR with termporary buffer information.

```
n \ deps \leftarrow \{\}
        for c \epsilon n dependencies sourced from Pytato IR do
             c \ deps \leftarrow \text{GRAPHTRAVERSE}(c)
             n\_deps \leftarrow n\_deps \cup c\_deps
        done
        return n\_deps
end function
```

4.2. Stage 2: Update CUDAGraphExec

Algorithm 3 gets executed for every graph launch.

Algorithm 3: Buffer update in CUDAGraphExec

for n ϵ kernel nodes in pycuda. GraphExec with temporary buffers do

Replace temporary buffers with allocated/linked buffers from corresponding PlaceHolder nodes.

done

5. RESULTS

We evaluate the performance of our framework on three end-to-end DG-FEM operators with real-world applications on NVIDIA Titan V. We evaluate these operators on 3D meshes with tetrahedral cells and evaluate our speedup against PyOpenCL which supports sequential stream execution. Table 2. summarizes our experimental parameters.

Equation	Polynomial Degree	No. of mesh elements
3D Wave	1	1.25×10^5
	2	5.0×10^4
	3	2.5×10^{4}
	4	1.4×10^{4}

Table 2. Experimental parameters for DG-FEM operators

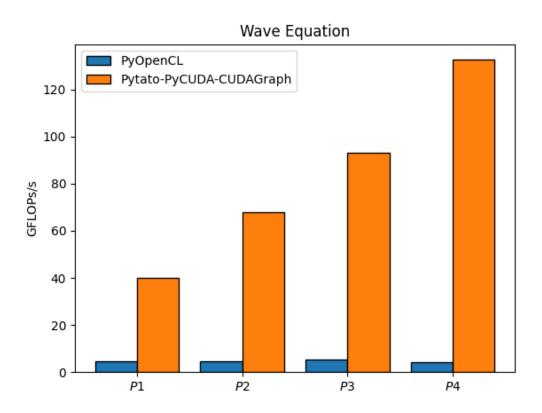


Figure 4. Performance of our framework (Pytato-PyCUDA-CUDAGraph) over sequentual stream execution (PyOpenCL)