CS5787: Exercises 1

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Mitchell Krieger mak483 Meitong (Estelle) He mh2585

1 Theory: Question 1 [12.5 pts]

- a. What is the input X? There are m samples in the batch with 10 features each so the input shape is (m, 10)
- b. What is the shape of the hidden layer's weight vector W_h , and the shape of its bias vector b_h ?

 To transform an (m, 10) input into a hidden layer of 50 neurons we need a shape

To transform an (m, 10) input into a hidden layer of 50 neurons we need a shape W_h to have a shape of (10, 50) so that we get a (m, 50) result. After the weight matrix is applied, we then add the bias b_h to each row of W_h , which means that the result needs to be (1, 50)

- c. What is the shape of the output layer's weight vector W_o , and its bias vector b_o ? W_h : (50,3), b_h : (1,3)
- d. What is the shape of the network's output matrix Y? (m,3)
- e. Write an equation that computes the network's output matrix Y as a function of X, W_h , b_h , W_o , and b_o ?

 $Y = W_o a(W_h X + b_h) + b_o$

Where *a* is the ReLU activation function, $a(x) = \max(0, x)$.

2 Theory: Question 2 [12.5 pts]

For the first layer there are 3x3x3 parameters in each of the 100 kernels, and then we need bias parameters for each kernel as well. This totals 3x3x3x100 + 100 = 2800 parameters. In the second layer there are 3x3x100 parameters in each of the 200 kernels, and then we need bias parameters for each kernel as well. This totals 3x3x100x200 + 200 = 180200. In the final layer there are 3x3x200 parameters in each of the 200 kernels, and then we need bias parameters for each kernel as well. This totals 3x3x200x400 + 400 = 720400. Adding all the layers together we get 2800 + 180200 + 720400 = 903400 total parameters.

3 Theory: Question 3 [25 pts]

a.

$$\frac{\partial f}{\partial \gamma} = \frac{\partial f}{\partial y_i} \frac{\partial y_i}{\partial \gamma}$$
$$= \sum_{i=1}^{m} \frac{\partial f}{\partial y_i} \widehat{x}_i$$

b.

$$\frac{\partial f}{\partial \beta} = \frac{\partial f}{\partial y_i} \frac{\partial y_i}{\partial \beta}$$
$$= \sum_{i=1}^{m} \frac{\partial f}{\partial y_i}$$

c.
$$\frac{\partial f}{\partial \widehat{x_i}} = \frac{\partial f}{\partial y_i} \frac{\partial y_i}{\partial \widehat{x_i}}$$

$$= \frac{\partial f}{\partial y_i} \gamma$$
d.
$$\frac{\partial f}{\partial \sigma^2} = \frac{\partial f}{\partial y_i} \frac{\partial y_i}{\partial \widehat{x_i}} \frac{\partial \widehat{x_i}}{\partial \sigma^2}$$

$$= \sum_{i=i}^m \frac{\partial f}{\partial y_i} \gamma \frac{1}{2} \frac{(x_i - \mu)}{\sqrt{(\sigma^2 + \epsilon)^3}}$$
e.
$$\frac{\partial f}{\partial \mu} = \frac{\partial f}{\partial y_i} \frac{\partial y_i}{\partial \widehat{x_i}} \frac{\partial \widehat{x_i}}{\partial \mu} + \frac{\partial f}{\partial y_i} \frac{\partial y_i}{\partial \widehat{x_i}} \frac{\partial \widehat{x_i}}{\partial \sigma^2} \frac{\partial \sigma^2}{\partial \mu}$$

$$= \sum_{i=i}^m \frac{\partial f}{\partial y_i} \gamma \frac{-1}{\sqrt{(\sigma^2 + \epsilon)}}$$

$$+ \sum_{i=i}^m \frac{\partial f}{\partial y_i} \gamma \frac{-1}{2} \frac{(x_i - \mu)}{\sqrt{(\sigma^2 + \epsilon)^3}} \frac{-2}{m} \sum_{i=1}^m (x_i - \mu)$$
f.
$$\frac{\partial f}{\partial x_i} = \frac{\partial f}{\partial \widehat{x_i}} \frac{\partial \widehat{x_i}}{\partial x_i} + \frac{\partial f}{\partial \sigma^2} \frac{\partial \sigma^2}{\partial x_i} + \frac{\partial f}{\partial \mu} \frac{\partial \mu}{\partial x_i}$$

$$\frac{\partial f}{\partial x_i} = \frac{\partial f}{\partial y_i} \gamma \frac{1}{\sqrt{(\sigma^2 + \epsilon)^3}}$$

$$+ \frac{\partial f}{\partial y_i} \gamma \frac{-1}{2} \frac{(x_i - \mu)}{\sqrt{(\sigma^2 + \epsilon)^3}} \frac{2}{m} (x_i - \mu)$$

$$+ \frac{\partial f}{\partial y_i} \gamma \frac{-1}{\sqrt{(\sigma^2 + \epsilon)^3}}$$

4 Practical [50 pts]

TODO: Provide a report detailing your experiments, results and discussion in this section.

 $+\frac{\partial f}{\partial y_i}\gamma \frac{-1}{2} \frac{(x_i - \mu)}{\sqrt{(\sigma^2 + \epsilon)^3}} \frac{-2}{m} \sum_{i=1}^m (x_i - \mu) \frac{1}{m}$