

Question 4:

Prove that the Big-O of the following loop is $O(N)$

```
for (int i = 1; i <= n; i += c) {  
    // some  $O(1)$  expressions  
}
```

Ans:

Here $c = \text{Constant}$, means during the loop i will be increased by c .

The loop will be executed n times, means $O(1)$ will be executed n time

So the Complexity of the loop Will be: $n * O(1)$

$$= O(n * 1)$$

$$= O(n)$$

Question 5:

Find the Big-O of the following loops // c is constant

```
for (int i = 1; i <= n; i += c) {  
    for (int j = 1; j <= n; j = pow(i, c)) {  
        // some  $O(1)$  expressions  
    }  
}  
for (int i = n; i > 0; i += c) {  
    for (int j = i+1; j <= n; j *= c) {  
        // some  $O(1)$  expressions  
    }  
}
```

Ans:

```
for (int i = 1; i <= n; i += c) {  
    for (int j = 1; j <= n; j = pow(i, c)) {  
        // some  $O(1)$  expressions  
    }  
}
```

$O(\log \log n)$

$O(n) * O(\log \log n)$

```
for (int i = n; i > 0; i += c) {  
    for (int j = i+1; j <= n; j *= c) {  
        // some  $O(1)$  expressions  
    }  
}
```

$O(\log n)$

$O(n) * O(\log n)$

$$\begin{aligned} &= O(n) * O(\log \log n) + O(n) * O(\log n) \\ &= O(n * \log \log n) + O(n * \log n) \end{aligned}$$