

Q.32 $T(n) = 0$ if $n = 1$

$T(n) = T(n-1) + n - 1$ if $n \geq 2$

$$= T(n-1) + n - 1$$

$$= T(n-2) + n - 2 + n - 1$$

$$= T(n-2) + 2n - 3$$

$$= T(n-3) + n - 3 + 2n - 2$$

$$= T(n-3) + 3n - 5$$

$$= T(n-4) + n - 4 + 3n - 5$$

$$= T(n-4) + n - 1 + n - 2 + n - 3 + n - 4$$

$$= (n^2 - n) / 2$$

$$= O(n^2)$$

Q.8 $T(n) = 7 * T * (n/2) + 500 * n^2$

Here $a=7$, $b=2$, $d=2$ ($f(n) = 500 * n^2$)

$$\text{So, } b^d = 2^2 = 4$$

Therefore, $a > b^d$

$$\text{So, } T(n) = O(n^{\log_2(7)})$$

Q.5 Binary Search (Search 76)

6	12	28	29	45	54	62	76
$l=0$			$m=3$			$r=7$	

Here, $m = l + (r - l) / 2$

$$\text{So, } m = 0 + (7 - 0) / 2$$

$$m = 3.5 \text{ (Approx. 3)}$$

76 is at 7th Index.

Q. 10 Merge Sort

