

## Q.10

Document	Size	Color	Shape	Category
d1	small	red	circle	positive
d2	large	red	circle	positive
d3	small	red	triangle	negative
d4	large	blue	circle	negative
d5	medium	red	circle	??????

### 1. Find Following Values

**P (Medium | Positive)**

**P (Red | Positive)**

**P (Circle | Positive)**

**P (Medium | Negative)**

**P (Red | Negative)**

**P (Circle | Negative)**

**P(Positive)**

**P(Negative)**

$$P(\text{Medium} | \text{Positive}) = (0+1) / (6+7) = 1/13$$

$$P(\text{Red} | \text{Positive}) = (2+1) / (6+7) = 3/13$$

$$P(\text{Circle} | \text{Positive}) = (2+1) / (6+7) = 3/13$$

$$P(\text{Medium} | \text{Negative}) = (0+1) / (6+7) = 1/13$$

$$P(\text{Red} | \text{Negative}) = (1+1) / (6+7) = 2/13$$

$$P(\text{Circle} | \text{Negative}) = (1+1) / (6+7) = 2/13$$

$$P(\text{Positive}) = 2/4 = 1/2$$

$$P(\text{Negative}) = 2/4 = 1/2$$

$$\begin{aligned}
 2. \quad & \mathbf{P(\text{Positive} | d5)} = P(\text{Positive}) * P(d5 | \text{Positive}) / P(d5) \\
 &= P(\text{Positive}) * P(\text{Medium} \cap \text{Red} \cap \text{Circle} | \text{Positive}) / P(d5) \\
 &= (P(\text{Positive}) * (P(\text{Medium} | \text{Positive}) * P(\text{Red} | \text{Positive}) * P(\text{Circle} | \text{Positive}))) / P(d5) \\
 &\propto (P(\text{Positive}) * (P(\text{Medium} | \text{Positive}) * P(\text{Red} | \text{Positive}) * P(\text{Circle} | \text{Positive}))) \\
 &= (1/2) * (1/13) * (3/13) * (3/13) \\
 &= \mathbf{0.0020}
 \end{aligned}$$

$$\begin{aligned}
3. \quad P(\text{Negative} | d5) &= P(\text{Negative}) * P(d5 | \text{Negative}) / P(d5) \\
&= P(\text{Negative}) * P(\text{Medium} \cap \text{Red} \cap \text{Circle} | \text{Negative}) / P(d5) \\
&= (P(\text{Negative}) * (P(\text{Medium} | \text{Negative}) * P(\text{Red} | \text{Negative}) * P(\text{Circle} | \text{Negative}))) / P(d5) \\
&\propto (P(\text{Negative}) * (P(\text{Medium} | \text{Negative}) * P(\text{Red} | \text{Negative}) * P(\text{Circle} | \text{Negative}))) \\
&= (1/2) * (1/13) * (2/13) * (2*13) \\
&= \mathbf{0.0009}
\end{aligned}$$

**So, D5 should belong to Positive Category.**

**Q.12**

	Doc	Words	Author
<b>Training</b>	1	W1 W2 W3 W4 W5	C (Christopher Marlowe)
	2	W1 W1 W4 W3	C (Christopher Marlowe)
	3	W1 W2 W5	C (Christopher Marlowe)
	4	W5 W6 W1 W2 W3	W (William Stanley)
	5	W4 W5 W6	W (William Stanley)
	6	W4 W6 W3	F (Francis Bacon)
	7	W2 W2 W4 W3 W5 W5	F (Francis Bacon)
<b>Test</b>	8 (Hamlet)	W1 W4 W6 W5 W3	?

**1. Find Following Values**

$P(W1 | C)$                        $P(W4 | C)$   
 $P(W6 | C)$                        $P(W5 | C)$   
 $P(W3 | C)$

$P(W1 | W)$                        $P(W4 | W)$   
 $P(W6 | W)$                        $P(W5 | W)$   
 $P(W3 | W)$

$P(W1 | F)$                        $P(W4 | F)$   
 $P(W6 | F)$                        $P(W5 | F)$   
 $P(W3 | F)$

$P(C)$                        $P(W)$   
 $P(F)$

$P(W1 | C) = (4+1) / (12+ 6) = 5/ 18$   
 $P(W4 | C) = (2+1) / (12+ 6) = 3/ 18 = 1/6$   
 $P(W6 | C) = (0+1) / (12+ 6) = 1/ 18$   
 $P(W5 | C) = (2+1) / (12+ 6) = 3/ 18 = 1/6$   
 $P(W3 | C) = (2+1) / (12+ 6) = 3/ 18 = 1/6$

$P(W1 | W) = (1+1) / (8+ 6) = 2/ 14 = 1/7$   
 $P(W4 | W) = (1+1) / (8+ 6) = 2/ 14 = 1/7$   
 $P(W6 | W) = (2+1) / (8+ 6) = 3/ 14$   
 $P(W5 | W) = (2+1) / (8+ 6) = 3/ 14$

$$P(W_3 | W) = (1+1) / (8+6) = 2 / 14 = 1/7$$

$$P(W_1 | F) = (0+1) / (9+6) = 1 / 15$$

$$P(W_4 | F) = (2+1) / (9+6) = 3 / 15 = 1/5$$

$$P(W_6 | F) = (1+1) / (9+6) = 2 / 15$$

$$P(W_5 | F) = (2+1) / (9+6) = 3 / 15 = 1/5$$

$$P(W_3 | F) = (2+1) / (9+6) = 3 / 15 = 1/5$$

$$P(C) = 3/7$$

$$P(W) = 2/7$$

$$P(F) = 2/7$$

$$\begin{aligned} 2. \quad P(C|d8) &= P(C) * P(d8 | C) / P(d8) \\ &= P(C) * P(W_1 \cap W_4 \cap W_6 \cap W_5 \cap W_3 | C) / P(d8) \\ &= (P(C) * (P(W_1 | C) * P(W_4 | C) * P(W_6 | C) * P(W_5 | C) * P(W_3 | C))) / \\ &\quad P(d8) \\ &\propto (P(C) * (P(W_1 | C) * P(W_4 | C) * P(W_6 | C) * P(W_5 | C) * P(W_3 | C))) \\ &= (3/7) * (5/18) * (1/6) * (1/18) * (1/6) * (1/6) \\ &= \mathbf{0.000030} \end{aligned}$$

$$\begin{aligned} 3. \quad P(W|d8) &= P(W) * P(d8 | W) / P(d8) \\ &= P(W) * P(W_1 \cap W_4 \cap W_6 \cap W_5 \cap W_3 | W) / P(d8) \\ &= (P(W) * (P(W_1 | W) * P(W_4 | W) * P(W_6 | W) * P(W_5 | W) * P(W_3 | \\ &\quad W))) / P(d8) \\ &\propto (P(W) * (P(W_1 | W) * P(W_4 | W) * P(W_6 | W) * P(W_5 | W) * P(W_3 | \\ &\quad W))) \\ &= (2/7) * (1/7) * (1/7) * (3/14) * (3/14) * (1/7) \\ &= \mathbf{0.000038} \end{aligned}$$

$$\begin{aligned} 4. \quad P(F|d8) &= P(F) * P(d8 | F) / P(d8) \\ &= P(F) * P(W_1 \cap W_4 \cap W_6 \cap W_5 \cap W_3 | F) / P(d8) \\ &= (P(F) * (P(W_1 | F) * P(W_4 | F) * P(W_6 | F) * P(W_5 | F) * P(W_3 | \\ &\quad F))) / P(d8) \\ &\propto (P(F) * (P(W_1 | F) * P(W_4 | F) * P(W_6 | F) * P(W_5 | F) * P(W_3 | \\ &\quad F))) \\ &= (2/7) * (1/15) * (1/5) * (2/15) * (1/5) * (1/5) \\ &= \mathbf{0.000020} \end{aligned}$$

**So, D8 (Hamlet) Belongs to W (William Stanley)**