

Q1.

Given, $P=3$, $Q=11$, $e=7$, plaintext=5

Find d , ciphertext

Ans:

$$N = P * Q = 3 * 11 = 33$$

$$Z = (P-1) * (Q-1) = 2 * 10 = 20$$

Now,

d can be any prime number that have only one common factor with Z , i.e 1

Here, we can choose 3 or 7

also, From the below Formula we can find d .

$$e * d = 20 * n + 1$$

so,

$$\text{For } n=1, 7 * d = 21 \rightarrow \text{so, } d=3$$

Next step to Find Ciphertext

$$\begin{aligned} C &= E(M) \\ &= M^e \bmod N \\ &= (5^7) \bmod 33 \\ &= 14 \end{aligned}$$

So, $d=3$ and Ciphertext = 14

Q2.

