



Bit Manipulation

Bitwise Operator

- |
- &
- ^
- ~
- << (left shift)
- >> (right shift)

Odd & Even Number

```
void bitwise_even_odd(int num)
{
    if(num & 1==0)
    {
        cout<<"even"<<endl;
    }
    else
    {
        cout<<"odd"<<endl;
    }
}
```

Swap

```
void bitwise_swap(int &a,int &b)
{
    a=a^b;
    b=a^b;
    a=a^b;
}
```

Bit Masking

Find i'th bit

4th bit of a number

n → 1 0 0 0 0 1 0 1 0

mask → 0 0 0 0 0 1 0 0 0 (i << 4)

n&mask → 0 0 0 0 0 1 0 0 0

```
bool find_i'th_bit(int n,int p)
{
    int mask=1<<p;
    mask=n&mask;
    mask=mask>>p;
}
```

```
return mask&1;
}
```

Set i'th bit

set 4th bit of a number

num → 1 0 0 0 1 0

mask → 0 0 0 1 0 0 0

num | mask → 1 0 0 1 0 1 0

```
void set_i'th_bit(int n,int p)
{
    int mask=1<<p;
    n=n| mask;
}
```

Clear i'th bit

clear 4 th bit of num

num → 1 0 0 1 1 0 1 1

mask → 1 1 1 1 0 1 1 1

num & mask → 1 0 0 1 0 0 1 1

```
void clear_i'th_bit(int n,int p)
{
    int mask=1<<p
    mask=~mask;
    n=n & mask;
}
```

#Find number of bit to change a to b

a → 1 0 1 1 0

b → 1 1 0 1 1

$a^b \rightarrow 0 1 1 0 1 \rightarrow 13$

count=1

13 → 1 1 0 1

12 → 1 1 0 0

$(13 \& 12) \rightarrow 1 1 0 0 \rightarrow 12$

count=2

12 → 1 1 0 0

11 → 1 0 1 1

12 & 11 → 1 0 0 0 → 8

count = 3


8 → 1 0 0 0


7 → 0 1 1 1

8 & 7 → 0 0 0 0

```
int different_bit(int x, int y)
{
    x = x ^ y;
    int count = 0;
    while(x)
    {
        x = x & (x - 1);
        count++;
    }
    return count;
}
```

#Find the only non repeating element in an array where every element repeat twice?

 $x = 0^x$


 $0 = x^x$;

$a[] \rightarrow [1, 2, 5, 1, 2]$

$x = 1^1 \wedge 2^2 \wedge 5^5 \wedge 1^1 \wedge 2^2 = 5$

```
int non_repeating_element(int a[], int n)
{
    x = 0;
    for(i = 0; i < n; i++)
    {
        x = x ^ a[i];
    }
    return x;
}
```

Find two non repeating element in an array where every element repeat twice?

 $x = x^0$



$$0 = x^x$$

$a[] \rightarrow [1, 2, 3, 2, 5, 1]$

$x = 1^1 2^2 3^2 5^1$

$x = 3^5 = 6 = 110$

2nd bit 1 $\rightarrow 2, 3, 2$

2nd bit 0 $\rightarrow 1, 5, 1$

$2^3 \cdot 2 \rightarrow 3$

$x^3 \rightarrow 5$

```
void non_repeating_two_element(int a[],int n)
{
    int x=0;
    for(int i=0;i<n;i++)
    {
        x=x^a[i];
    }
    int p=0;
    while(!find_i'th_bit(x,p))
    {
        p++;
    }
    int one_element=0;
    for(int i=0;i<n;i++)
    {
        one_element=one_element^a[i];
    }
    int another_element=x^one_element;

    cout<<one_element<<" "<<another_element<<endl;
}
```

#Find the only non repeating element in an array where every element repeat k time?

$a[] \rightarrow [2, 2, 1, 5, 1, 1, 2]$

$k=3$

number of bit for every bit position of array

rest of bit which is zero for this example	0	0	0	0	0	0	1
--	---	---	---	---	---	---	---

perform % k from every bit position

rest of bit which is zero for this example	0	0	0	0	0	0	1
--	---	---	---	---	---	---	---

$ans = 1 * 4 + 0 * 2 + 1 * 1$

```
int non_repeating_element(int a[],int n, int k)
{

```

```
vector<int> b(64);
for(int i=0;i<64;i++)
{
    for(int j=0;j<n;j++)
    {
        b[i]=b[i]+find_i'th_bit(a[j],i);
    }
}
int ans=0;
for(i=0;i<64;i++)
{
    if(b[i]%k)
        ans=ans+pow(2,i);
}
return ans;
}
```