

Topics: Finding area under a curve; calculating distance traveled

An ancient problem of mathematics was to calculate areas of various shapes. While polygons were somewhat simple, shapes with curves (e.g., circles) were very difficult!

Example 1. *Use rectangles to estimate the area under the parabola $y = x^2$ from 0 to 1.*

Take-away:

The **area** A that lies under the graph of the continuous function f on the interval $[a, b]$ is the limit of the sum of the areas of approximating rectangles of width $\Delta x = \frac{b-a}{n}$:

$$A =$$

Sigma notation

We have the following nice notation for our work today:

$$\sum_{i=1}^n f(x_i) \Delta x =$$

$$1. \sum_{i=1}^5 i =$$

$$2. \sum_{i=1}^n i^2 =$$

$$3. \sum_{i=1}^n 1 =$$

$$4. \frac{1}{10} \Delta x + \frac{2}{10} \Delta x + \cdots + \frac{10}{10} \Delta x =$$

$$5. \frac{1}{1} + \frac{1}{4} + \frac{1}{9} + \cdots + \frac{1}{81} =$$

Example 2. *Approximate the area under the curve of e^{-x} between $x = 0$ and $x = 2$ using L_4 and R_4 .*

Example 3. *Is L_4 an over estimate or under estimate?*

Take-away:

The Distance Problem

Recall that if velocity is constant then $d = rt$. However, if velocity is not constant, then how would we compute distance traveled?

Example 4. *Consider the following measured values:*

<i>Time</i>	0	5	10	15	20	25	30
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<i>Velocity</i>	25	31	35	43	47	46	41.
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Approximate the distance traveled.