Matthew Jackson
PHYS 513
October 11,2000
HUJ#6

and B= B.x(x,t)x+Boy(x,t)g+ Boz(x,t)2

6.2.1) Show Eylx.t), Ez(x,t), By(x,t) and Bz(x,t) each individually obey a wave equation of the form

$$\frac{\partial r_{5}}{\partial r_{5}} = \frac{C_{5}}{1} \frac{\partial t_{5}}{\partial r_{5}}$$

Where u is a place holder for one of the components stated above

Start with Earnday's law for Ey

\[\hat{x} \hat{y} \frac{2}{2} \left(0 - d_2 \hat{y} \right) \hat{x} \]

\[\hat{x} \hat{E}_y = \frac{1}{2} \hat{x} \frac{1}{2} \hat{y} \frac{1}{2} = 0 \hat{g} \left(\hat{3} \hat{x} \hat{E}_y - 0 \right) \hat{x} \]

\[\hat{x} \hat{E}_y = \frac{1}{2} \hat{x} \frac{1}{2} \hat{y} \frac{1}{2} = 0 \hat{g} \left(\hat{3} \hat{x} \hat{E}_y - 0 \right) \hat{x} \]

$$\nabla \times E_y = \frac{\partial E_y}{\partial x} = -\frac{\partial B}{\partial E}$$

 $\frac{\partial B}{\partial t} = -\frac{\partial E_y}{\partial x} = \frac{\partial E_y}{\partial x} = \frac{\partial$

Look at complete Ampere's Law when J=0

V*B = M.E. JE

dt

Apply time derivative to both sides

$$\frac{\partial}{\partial t} (\nabla \times B) = \frac{\partial}{\partial t} (u \cdot 6 \cdot \frac{\partial E}{\partial t})$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial^2 E}{\partial t^2}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial B}{\partial t}$$

$$\nabla \times \frac{\partial B}{\partial t} = u \cdot 6 \cdot \frac{\partial$$

VXB=MoE JE

Apply time derivative to both stoles

$$\frac{\partial}{\partial t} (\nabla \times B) = \frac{\partial}{\partial t} (M.60 \frac{\partial E}{\partial t})$$

$$W \times \frac{\partial B}{\partial t} = M.6. \frac{\partial^2 E}{\partial t^2}$$

$$\frac{\partial^2 E}{\partial x^2} = \frac{\partial^2 E}{\partial t^2} = M.6. \frac{\partial^2 E}{\partial$$

O de O ê

Mx T ABA &= - 95B

+
$$\frac{1}{\text{M.G.}} \frac{\partial^2 B_y}{\partial x^2} \hat{y} = \frac{1}{\partial t^2} \frac{\partial^2 B_y}{\partial t^2}$$

Take time derivative of faradays laws, in
$$V \times \frac{\partial E}{\partial t} = -\frac{\partial B}{\partial t^2}$$
 & $\hat{y} = \frac{\partial E}{\partial t} = \frac{\partial B}{\partial t}$ & $\hat{y} = \frac{\partial E}{\partial t} = \frac{\partial B}{\partial t}$ & $\hat{y} = \frac{\partial E}{\partial t} = \frac{\partial B}{\partial t} = \frac{\partial B}{\partial$

6. Z.Z) Does it follow that

$$E_{x}(x,t) = B_{x}(x,t) = 0$$
?

Given that $\nabla \cdot E = 0$ and $\nabla \cdot B = 0$

and $\nabla x \cdot E = -\frac{\partial B}{\partial t}$ and $\nabla x \cdot B = u \cdot 6 \cdot \frac{\partial E}{\partial t}$
 $\nabla \cdot E = 0$ use $E = E_{x}(x,t) \hat{x}$
 $\frac{\partial E_{x}}{\partial x} = 0$
 $\int dE_{x} = \int dx$
 $\int dE_{x} = \int dx$
 $\int dx = -\frac{\partial B}{\partial t}$
 $\int dx = -\frac{\partial B}{\partial t} = -\frac{\partial B}{\partial t} = 0$
 $\int dx = -\frac{\partial B}{\partial t} = -\frac{\partial B}{\partial t} = 0$

$$\nabla^2 \mathbf{E} = \frac{1}{c^2} \frac{\partial^2 \mathbf{E}}{\partial t^2}$$

$$\mathbb{V}^2 \mathbb{B} = \frac{1}{C^2} \frac{\partial \mathbb{B}}{\partial t^2}$$

$$\frac{\partial^2 E_y}{\partial x^2} = \frac{1}{C^2} \frac{\partial^2 E_y}{\partial t^2}, \qquad \frac{\partial^2 E_z}{\partial x^2} = \frac{1}{C^2} \frac{\partial^2 E_z}{\partial t^2}$$

$$\frac{\partial^2 B_y}{\partial x^2} = \frac{1}{c^2} \frac{\partial^2 B_y}{\partial t^2} \qquad \frac{\partial^2 B_z}{\partial x^2} = \frac{1}{c^2} \frac{\partial^2 B_z}{\partial t^2}$$

$$\nabla^2 E_u = \frac{\partial^2 E_u}{\partial x^2} + \frac{\partial^2 E_x}{\partial z^2}$$

$$\nabla^2 E_y = \frac{\partial^2 E_y}{\partial x^2} + \frac{\partial^2 E_y}{\partial y^2} + \frac{\partial^2 E_y}{\partial z^2}$$

$$\nabla^2 E_z = \frac{\partial^2 E_z}{\partial x^2} + \frac{\partial^2 E_z}{\partial y^2} + \frac{\partial^2 E_z}{\partial z^2}$$

expand time derivent ine

$$\triangle_{5}E^{4} = \frac{9F_{5}}{9_{5}E^{4}} \frac{C^{2}}{7^{5}E^{4}} \frac{G^{2}}{7^{5}E^{4}} \frac{G^{2}}{7^{5}$$

Et Ez depends only on x and t

D. the same for B

skipping to component step $\nabla^2 B_x = \frac{1}{C^2} \frac{\partial^2 B_x}{\partial t^2} \leftarrow Skip + Ws component$ V2By 2 1 2 8 By N2B= - T 92R= 3-By + 32By + 32By = 1 22 34By Et By depends only on x and & $\left(\frac{\partial^2 B_y}{\partial x^2} = \frac{1}{C^2} \frac{\partial^2 B_y}{\partial x^2}\right)$ $\frac{\partial^{2} B_{2}}{\partial x^{2}} + \frac{\partial^{2} B_{2}}{\partial u^{2}} + \frac{\partial^{2} B_{2}}{\partial z^{2}} = \frac{1}{c^{2}} \frac{\partial^{2} B_{2}}{\partial t^{2}}$ RR Bz depends only on x and 6 $\frac{\partial^2 B_z}{\partial x^2} = \frac{1}{C^2} \frac{\partial^2 B_z}{\partial t^2}$