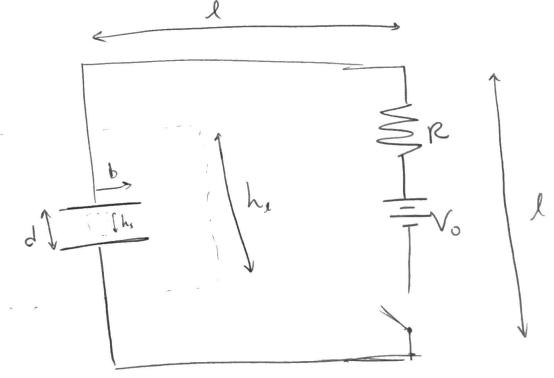
5.2) Show Poynting's theorem holds true For the areas below Mathew Jackson PHYS 513 September 30,2020 HW #5



Area 1-> rs and hs where hs <d

Area 2-> rs and hs where d < hs < 1

Area 1
Assumptions:
-charge on plates are evenly distributed
by of. This allows for an E-field
that is ofe, at the center of
the plates
- (s << b. This allows for fringe fields
to go to O, and allows E to

Area 2
Assumptions: (same as first" with abelow)

- ra >>d such that B>0 at ra

- Assume that E in current carrying

wire is D so E.J=0

be spatially constant

E is time dependent, but I will leave it as -E€ until the end Poynting's Theorem [ = (B.H) + = (D.E) + E. ] dV = - § (ÉxH)· ds Find B field TXB = M. E. JE ITTE €B.JĪ = SMOE. JĒ.JŠ 2 AV. B = Arx MOBOFDE) B=-M.E. [ JE &

$$-\frac{1}{s}(\vec{E}\times\vec{H})\cdot J\vec{S} \rightarrow -\frac{1}{m}\cdot \delta(\vec{E}\times\vec{B})\cdot J\vec{S}$$

$$-\frac{1}{m}\cdot \delta_{s}(\vec{E}\times\vec{B})\cdot d\vec{S}$$

$$-\frac{1}{m}\cdot \delta_{s}(tE\hat{\epsilon}\times tm\cdot \epsilon_{s})\cdot d\vec{S}$$

$$-\frac{m\cdot \epsilon_{s}}{m}\cdot d\vec{E} \qquad \int_{s} (\hat{\epsilon}\times\hat{\beta})\cdot d\vec{S} \qquad \hat{\epsilon} = c$$

$$+\frac{1}{m}\cdot d\vec{E} \qquad \int_{s} (\hat{\epsilon}\times\hat{\beta})\cdot d\vec{S} \qquad \hat{\epsilon} = c$$

$$+\frac{1}{m}\cdot d\vec{E} \qquad \int_{s} (\hat{\epsilon}\times\hat{\beta})\cdot d\vec{S} \qquad \hat{\epsilon} = c$$

$$+\frac{1}{m}\cdot d\vec{E} \qquad \hat{\epsilon} \qquad \hat{$$



$$\int_{V} \left[ \frac{1}{2} \left( \frac{\vec{B} \cdot \vec{H}}{2} \right) + \frac{1}{2} \left( \frac{\vec{D} \cdot \vec{E}}{2} \right) + \vec{E} \cdot \vec{J} \right] dV$$

$$\vec{B} \cdot \vec{H} = + \mu \cdot \epsilon_{0} \leq \frac{1}{2} \cdot \epsilon_{0} \leq \frac{1}{2} \cdot \epsilon_{0}$$

$$= \mu \cdot \epsilon^{2} \cdot \vec{J} \cdot$$

$$\epsilon$$
 of  $(\underline{\mathbb{E}}^2)$   $\pi$   $r_s^2$   $h_s = \epsilon$  or  $\pi$   $r_s^2$   $h_s$   $\frac{1}{2}$   $(\underline{\mathbb{E}}^2)$ 

E is only time dependent which I will leave as -Ez Poynting's theorem 「最(一部)+ま(戸)ナモ・ナーノリー - f (ĒxH)·13 Find B Field マ×B=M.C. 度多は= JM.C. 違しる B-271 = -11, Go X 62 JE B=-M.E.b2 JE &

$$-\frac{1}{3} \frac{1}{16} \left( \frac{1}{6} \times \frac{1}{8} \right) \cdot \frac{1}{3}$$

$$-\frac{1}{3} \frac{1}{6} \left( \frac{1}{6} \times \frac{1}{8} \right) \cdot \frac{1}{3}$$

$$+\frac{1}{6} \frac{1}{3} \frac{1}{6} \left( \frac{1}{6} \times \frac{1}{2} \right) \cdot \frac{1}{3} \frac{1}{3}$$

$$+\frac{1}{6} \frac{1}{3} \frac{1}{6} \left( \frac{1}{6} \times \frac{1}{2} \right) \cdot \frac{1}{3} \frac{1}{3} \frac{1}{6} \left( \frac{1}{6} \times \frac{1}{2} \right) \cdot \frac{1}{3} \frac{1}{3}$$

$$+\frac{1}{6} \frac{1}{3} \frac{1}{3} \left( \frac{1}{6} \times \frac{1}{2} \right) \cdot \frac{1}{3} \frac{$$

$$\int_{V} \left[ \frac{1}{M_{0}} \frac{d}{dt} \left( \frac{B^{2}}{2} \right) + \epsilon_{0} \frac{d}{dt} \left( \frac{E^{2}}{2} \right) + \epsilon_{0} \frac{d}{dt} \right) \right] dV$$

$$\int_{V} \left[ \frac{1}{M_{0}} \frac{d}{dt} \left( \frac{B^{2}}{2} \right) \right] dV$$

$$\int_{V} \frac{d}{dt} \left( \frac{M_{0}}{2} \frac{\epsilon_{0}}{2} \frac{d}{dt} \right) \left( \frac{M_{0}}{2} \frac{\epsilon_{0}}{2} \frac{d}{dt} \right) \left( \frac{E^{2}}{2} \right) + \epsilon_{0} \frac{d}{dt} \left( \frac{E^{2}}{2} \right) + \epsilon_{0} \frac{dt}{dt} \left( \frac{E^{2}}{2} \right) + \epsilon_{0} \frac{d}{dt} \left( \frac{E^{2}}{2} \right) + \epsilon_{0} \frac{d}{dt$$