HW 1.3 9/1/20 PHYS 513 a,) Show that E from a finite line 2 length 2L with charge density 2 is the same as Gaussis when the Taylor approx of the E field. PR.da = Qenc

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Starting with E Riebol From line charge

$$\dot{E}_{z}(z) = \frac{1}{4\pi\epsilon_{o}} \frac{2\lambda L}{z\sqrt{z^{2}+L^{2}}} = \frac{1}{2\sqrt{z^{2}+L^{2}}} = \frac{2\lambda L}{2\sqrt{z^{2}+L^{2}}}$$
 example Z.Z

$$= \frac{2\lambda}{4\pi\epsilon_{o}} \frac{\frac{L/2^{2}}{\sqrt{1+(L/2^{2})}} \cdot \frac{L}{2}}{\frac{2}{4\pi\epsilon_{o}L}}$$

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define 
$$f(x) = \frac{x}{\sqrt{1+x}}$$
 so  $x = \frac{L^2}{2^2} \left( \frac{L^2}{2^2} \left( \frac{L}{2^2} \right) \right)$ 

$$F(x) = F(0) + x - F'(0) + O(x^{2})$$

$$F(0) = \frac{0}{\sqrt{1+0}} = 0$$

$$F'(x) = (x+2) \longrightarrow F'(0) = \frac{8+2}{2(1+8)^{3/2}} = 0$$

$$f'(x) = \frac{(x+2)}{2(1+x)^{3/2}} \longrightarrow f'(0) = \frac{8+2}{2(1+8)^{3/2}} = 1$$

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$$\vec{E}_{\xi}(z) = \frac{2\lambda}{4\pi\epsilon_{0}L} f(x)\hat{z} \rightarrow \frac{2\lambda}{4\pi\epsilon_{0}L} \cdot \times \hat{z}$$

$$\vec{E}_{\xi}(z) = \frac{2\lambda}{4\pi\epsilon_{0}K} \frac{L^{2}}{Z^{2}} \rightarrow \vec{E}_{\xi}(z) - \frac{2\lambda L}{4\pi\epsilon_{0}Z} \hat{z}$$

b.) Show that E from sheet-charge of sides w and w with charge density of is the same as Gauss's law when taking the Taylor approx of the € Field. Gauss's Law JE. da = Denc E. 4Tr2 = 5w2 E FOWZ ? -> 9 4TTEO 12

Start 
$$E_{z}(z) = \frac{\sigma_{o}}{\pi \epsilon_{o}} + \tan^{-1} \left[ \frac{W^{2}}{4z} \sqrt{z^{2} + \frac{W^{2}}{2}} \right] \hat{z}$$

$$= \frac{\sigma}{\pi \epsilon_{o}} + \tan^{-1} \left[ \frac{W^{2}}{4z} - \frac{1}{2z^{2}} \right] \hat{z}$$

$$= \frac{\sigma}{\pi \epsilon_{o}} + \tan^{-1} \left[ \frac{1}{2} \frac{W^{2}}{2z^{2}} - \frac{1}{1 + \frac{W^{2}}{2z^{2}}} \right] \hat{z}$$

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$$\hat{E}_{2}(z) = \frac{\sigma}{\pi e_{0}} \frac{1}{2} \frac{\omega^{2}}{2z^{2}} \hat{z}$$

$$\hat{E}_{2}(z) = \frac{\omega^{2}\sigma}{4\pi e_{0}} \hat{z}^{2}$$