2.1) t yol b xo Matthew Jackson PHYS 513 September 7,2020 HW 2

Calculate the potential with the following Boundary conditions

1.)
$$X=0 \rightarrow \mathcal{D}_{\ell}(0,y) = V_{\ell}(i)$$

 $X=X_0 \rightarrow \mathcal{D}_{\ell}(X_0,y) = \mathcal{O}(ii)$
 $Y=0 \rightarrow \mathcal{D}_{\ell}(X_0,y) = \mathcal{O}(iii)$
 $Y=Y_0 \rightarrow \mathcal{D}_{\ell}(X_0,y_0) = \mathcal{O}(iv)$

$$\frac{X(x)}{X''(x)} = k^2 \quad \vec{q} \quad \frac{Y(y)}{Y''(y)} = -k^2$$



Enter Boundary condition (i) $\overline{\Phi}_{s}(x,y) = 2CA \sinh\left(\frac{n\pi}{y_{o}}(x_{o}-x)\right) \sin\left(\frac{n\pi}{y_{o}}\right)$ $D_{x}(x,y) = \sum_{n=1}^{\infty} A_{n} \sinh\left(\frac{n\pi}{y_{n}}(x_{n}-x)\right) \sin\left(\frac{n\pi y}{y_{n}}\right)$ Delo,y) = Ve = & Ansinh (ntx) sin (nty) Former's Trick Ansinh (ntro) = 2 Ja Vasin (ntry) dy - An = Inh (n\pi xo) = 2 · V1 · \(\times - \times \cos (\pi n) \) \(\times \times \) when n is add, else $\frac{4 V_{x}}{\pi n \sinh \left(\frac{n \pi x_{o}}{v}\right)} \quad \text{where } n = 1, 3, 5, ...$ $\overline{\Phi}_{\lambda}(x,y) = \sum_{n=1,3,5,-}^{\infty} \frac{4 V_4}{\pi n} \frac{\sinh(\frac{n\pi}{4}(x_0-x))\sin(\frac{n\pi y}{40})}{\sinh(\frac{n\pi x_0}{40})}$

3

2.) (alc with following boundary conditions

Ib(0,y)=0

\$ b(x0,y) = 0

0 b(x,0) = Vb

Do(x, y0) = 0

Same set up as part 1, but x and y are switched.

Thus the solution is

$$\overline{D}_{b}(x,y) = \sum_{n=1,3,5}^{\infty} \frac{4V_{b}}{\pi n} \sinh\left(\frac{n\pi}{x_{o}}(y_{o}-y)\sin\left(\frac{n\pi x}{x_{o}}\right)\right)$$

$$\sinh\left(\frac{n\pi y_{o}}{x_{o}}\right)$$

Boundary condition at yo is the same for y=0, in part 2

Since Boundary condition leads to the same value for An (Cn)

The answer is

$$\frac{1}{2} \left(x_{1} y_{1} \right) = \sum_{n=1,3,5,...} \frac{4 V_{0}}{\pi n} \quad \frac{1}{3} \left(\frac{n \pi y_{0}}{x_{0}} \right) \quad \frac$$

Note: the difference in this solution is that sinh (nt (y-y.)) becomes sinh (nt y)

5

4.) Cake with following boundary conditions Dr(0,y)=0 Dr(x0,y)=Vr

J-(x,0)=0

Or(x, y0) = 0

Same as geometry from 3, except switch x and

 $\frac{1}{2} \left[D_{r}(x,y) = \frac{8}{2} \frac{4V_{o}}{\pi n} \right] \frac{4V_{o}}{\pi n} \frac{S_{inh}(\frac{n\pi y}{y_{o}})}{S_{inh}(\frac{n\pi y}{y_{o}})} \frac{1}{S_{inh}(\frac{n\pi y}{y_{o}})}$