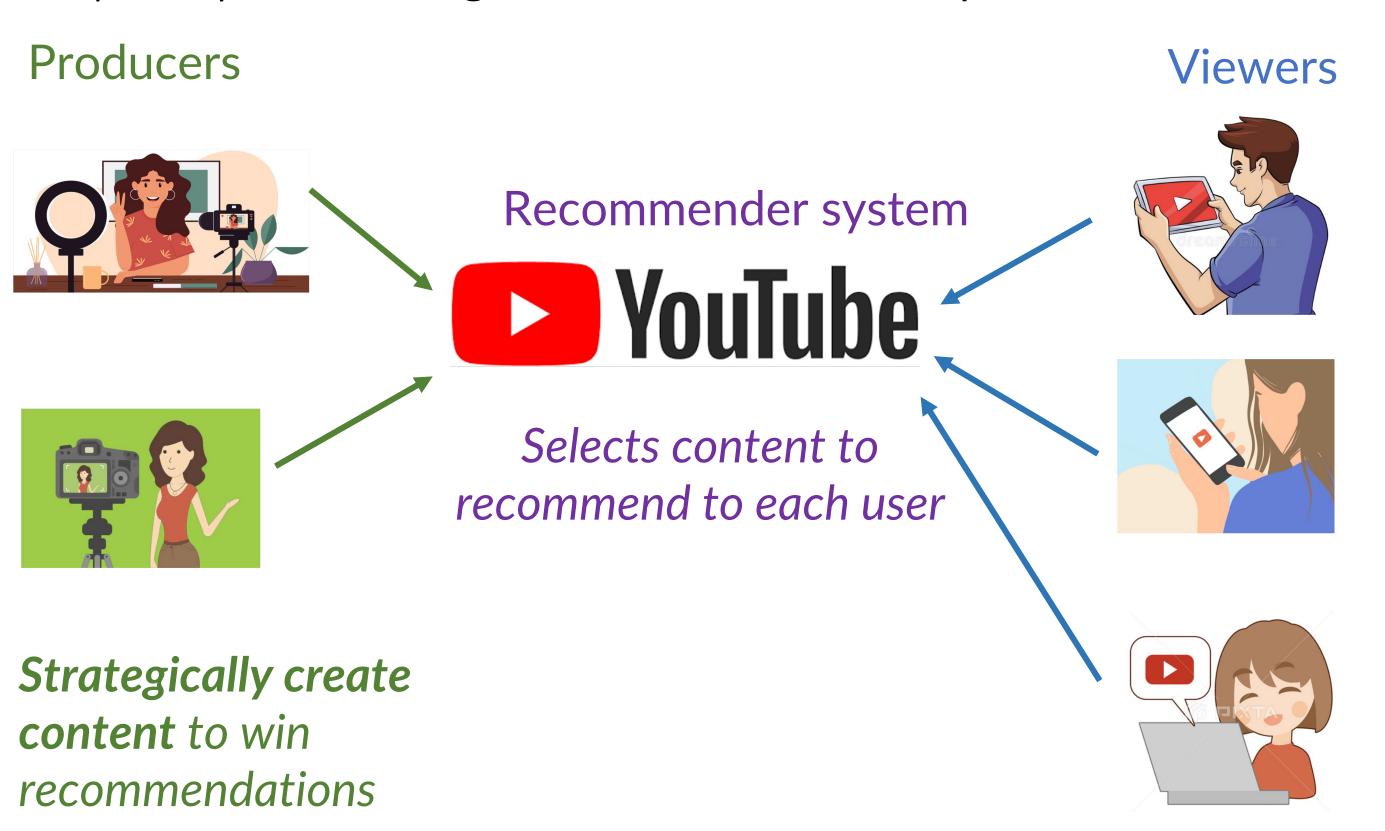
Supply-Side Equilibria in Recommender Systems

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Content Producer Incentives

In a recommender system, the content landscape is implicitly shaped by the **strategic choices of content producers**.



Main question: in content recommender systems, when are producers incentivized to create specialized content (versus mainstream content) at equilibrium?

Our model

Digital goods p and user vectors u embedded in $(\mathbb{R}_{\geq_0})^D$.

Each user $i \in [N]$ has preference vector $u_i \in (\mathbb{R}_{\geq_0})^D$.

Each producer $j \in [P]$ chooses content $p_i \in (\mathbb{R}_{\geq_0})^D$.

• Producer action space = $(\mathbb{R}_{\geq_0})^D$ (all digital goods)

Recommender system maximizes inferred value:

- $\langle u_i, p \rangle$ (inferred value of good p for user i)
- $j^*(u_i)$: = argmax_{$j \in [P]$} $\langle u_i, p_j \rangle$ (personalized recs)

Producer j's **profit function**:

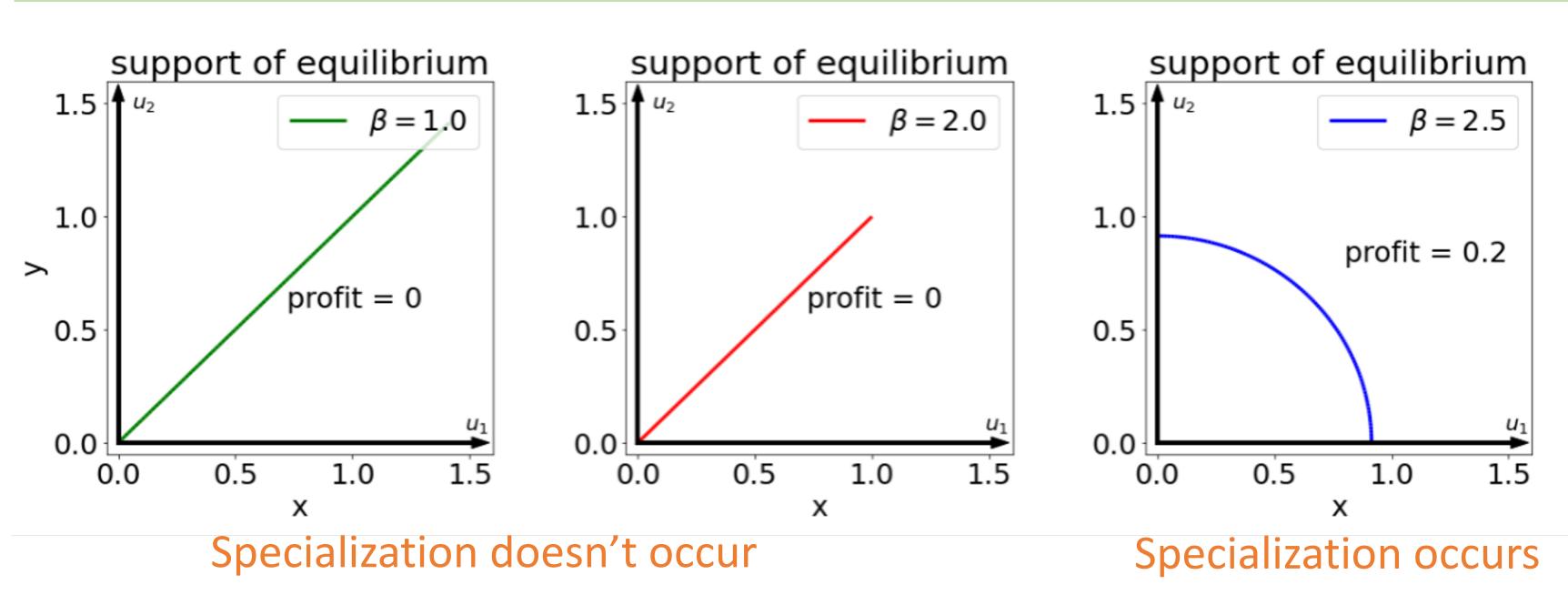
$$P(p_j|p_{-j},u_{1:N}):=\sum_{i\in[N]}1[j^*(u_i)=j]-c(p_j)$$
 Exposure Production costs follow the (# of users won) functional form: $c(p_j)=||p_j||^\beta$

 $\beta \approx$ difficulty of excelling in many dimensions at once

Our focus: symmetric mixed Nash equilibria μ of game between P producers (determines content landscape)

Creation of Specialized vs. Mainstream Content

Results: We characterize when specialization by content producers occurs, uncovering the role of producer costs & user embeddings. We analyze the form of specialization and impact on market competitiveness.



Definition (Specialization): Let μ be a symmetric mixed equilibrium.

- Genre $(\mu) := \{\frac{p}{||p||} \mid p \in \text{supp}(\mu) \}$ is set of directions in support
- Specialization occurs if and only if $|Genre(\mu)| = 1$.

Theoretical characterization of when specialization occurs

Theorem:

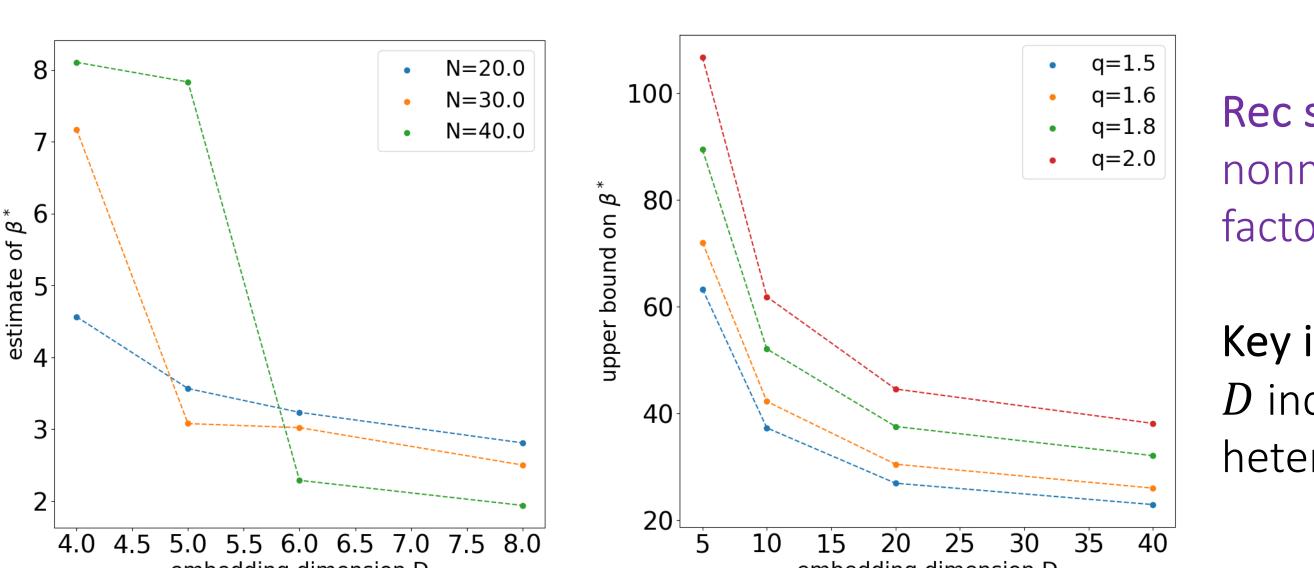
Let $S = \{ [\langle u_1, p \rangle, ... \langle u_N, p \rangle] \mid p \in (\mathbb{R}_{\geq_0})^{\mathsf{D}}, ||p|| \leq 1 \}$ and let S^β be the coordinate powers $\{ [\langle u_1, p \rangle^\beta, ... \langle u_N, p \rangle^\beta] \mid p \in (\mathbb{R}_{\geq_0})^{\mathsf{D}}, ||p|| \leq 1 \}$. There exists an equilibrium μ with $|\text{Genre}(\mu)| = 1$ if and only if: $\max\{ \prod_{i \in [N]} y_i \mid y \in S^\beta \} = \max\{ \prod_{i \in [N]} y_i \mid y \in \text{conv}(S^\beta) \}.$

Our characterization relates specialization to the lack of convexity of \mathcal{S}^{eta} .

(See the paper for corollaries with easier-to-interpret bounds.)

Nonnegative matrix factorization on the MovieLens dataset

Finding: Increasing the number of factors (dimensions D) used in nonnegative matrix factorization increases the likelihood that specialization occurs.

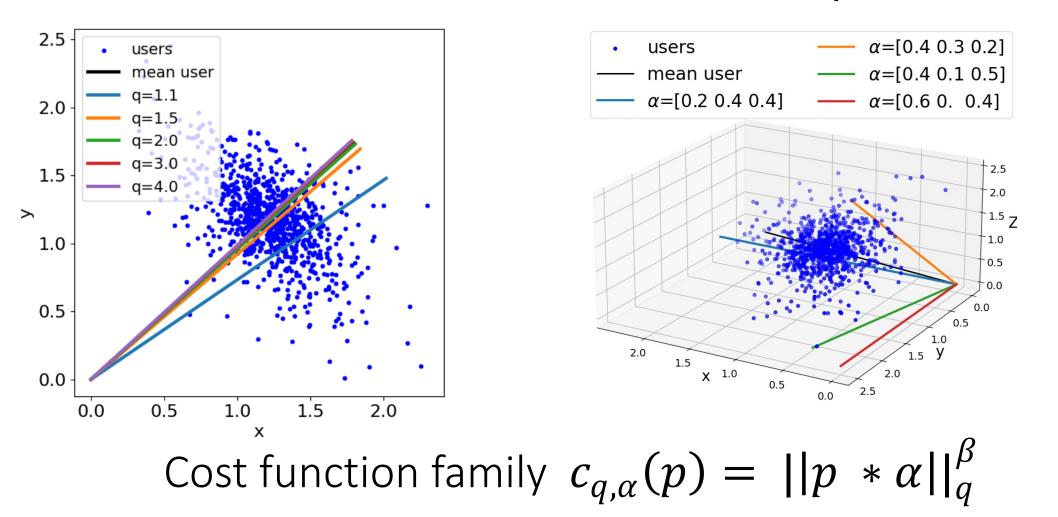


Rec sys algorithm = nonnegative matrix factorization w/ dim D

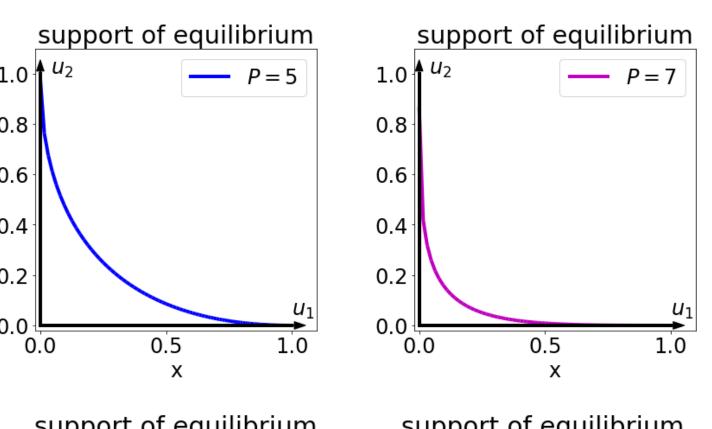
Key intuition: increasing *D* increases user vector heterogeneity

Genres of Content at Equilibrium

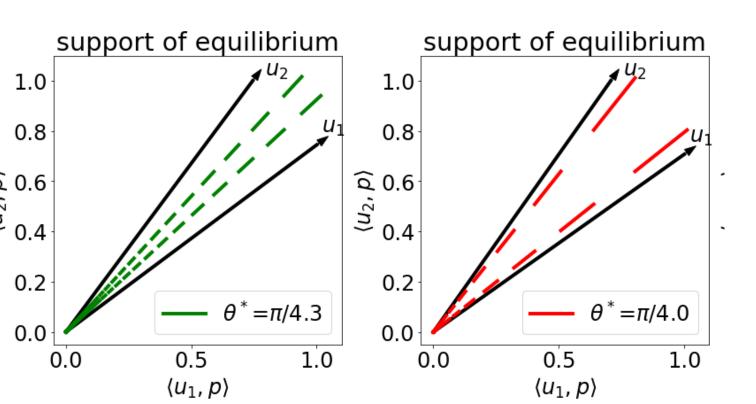
Genre location under no specialization



Genre location under specialization



Role of number of producers *P*



Role of user vectors u_1 and u_2

Specialization -> Producer Profit

Economic motivation: equilibrium profit of producers captures how competitive a marketplace is.

Proposition (Informal):

- With specialization: producers achieve **strictly positive profit** if β is sufficiently high.
- No specialization: producers achieve zero profit.

Takeaway: specialization can reduce competitiveness

Summary and Discussion

Personalized recommender systems implicitly shape the landscape of content created by producers.

We proposed a high-dimensional model for content producer incentives in recommender systems.

- We focused on the phenomena of **specialization**.
- We show how producer costs (determined by goods market) & user vectors (learned by the rec sys algorithm) both shape the content landscape.