

Supply-Side Equilibria in Recommender Systems

Meena Jagadeesan (UC Berkeley)

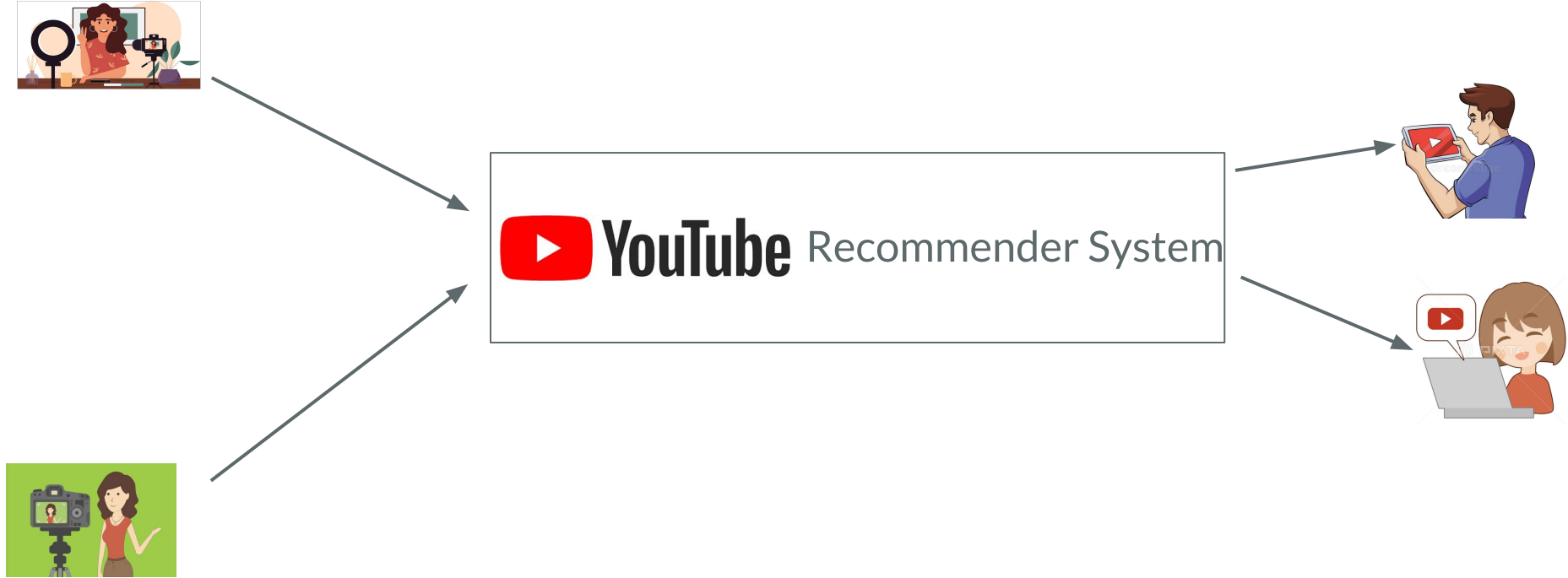
Joint work with Nikhil Garg (Cornell Tech) and Jacob Steinhardt (UC Berkeley)



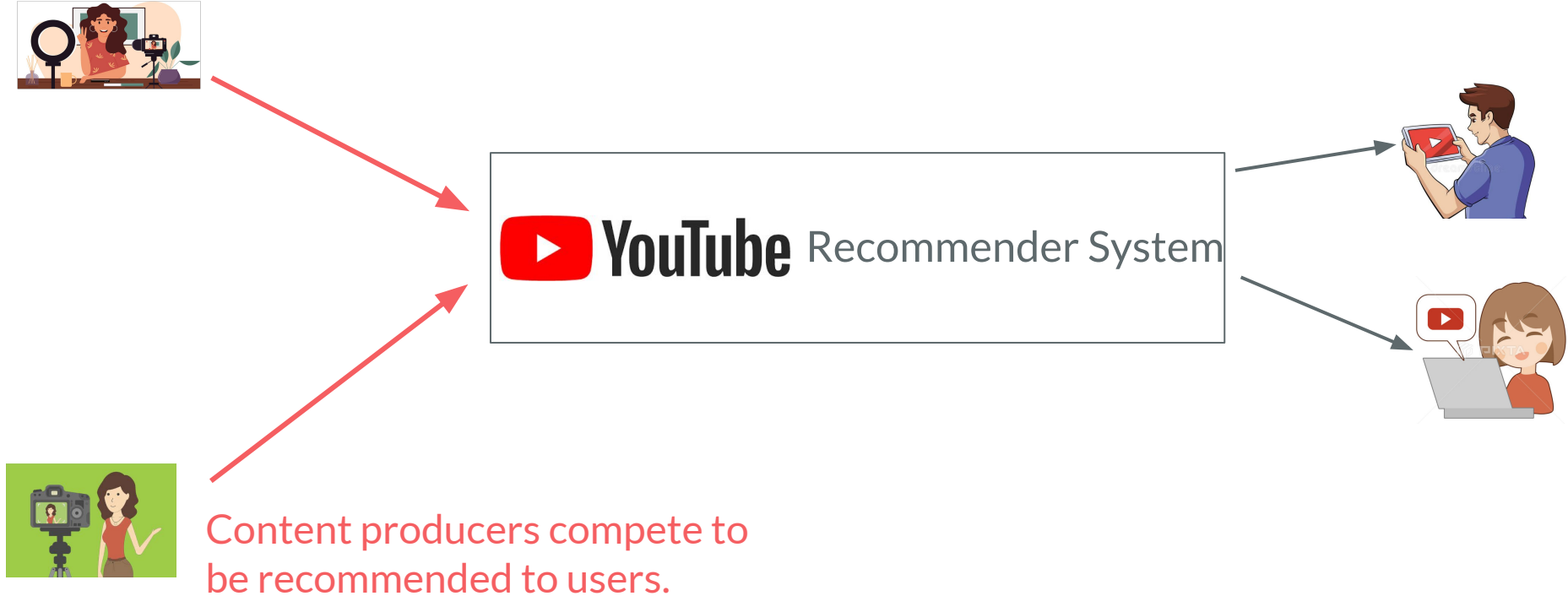
Classical view: Analyze ML as an Isolated System



Content recommendation in a marketplace



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Content recommendation in a marketplace



Strategically create
content that optimizes
for recommendations



Content producers compete to
be recommended to users.



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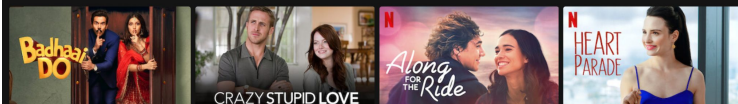


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How personalized recommendations impact producers

Romantic Movies



Niche content can reach the right audience!

Small Town Charm

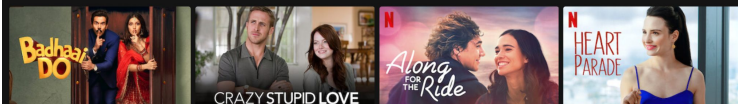


Binge-worthy Criminal Investigation TV Dramas



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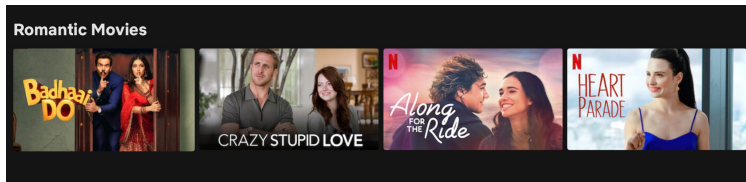
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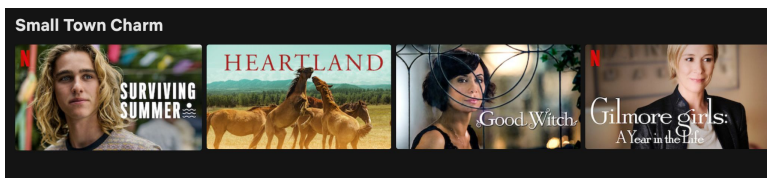


How personalized recommendations impact producers



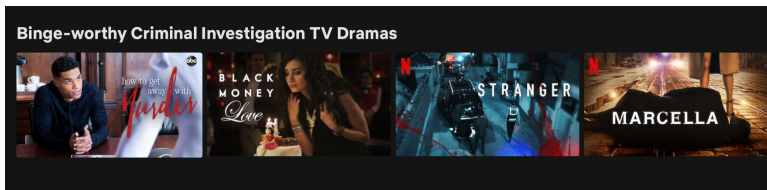
Niche content can reach the right audience!

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Producers may be incentivized to either:

1. Create **specialized content** catered to a subpopulation.
2. Create **mainstream content** catered to the “average” user.



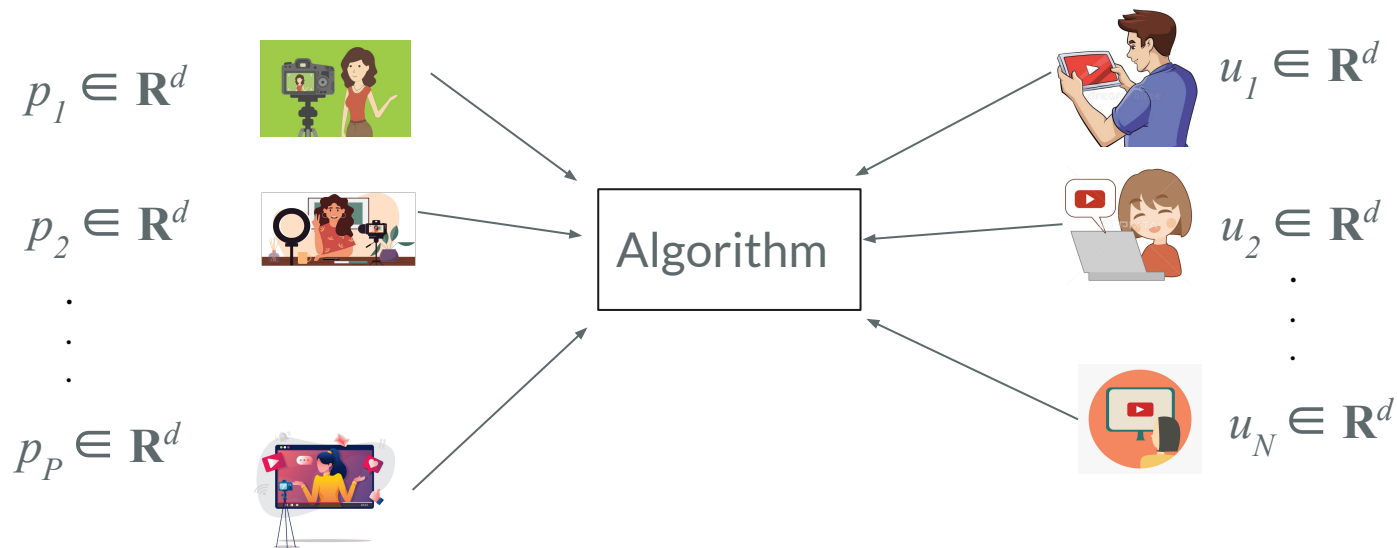
This paper

When do personalized recommendations lead to specialization?

What form does specialization take, and how does it impact market competitiveness?

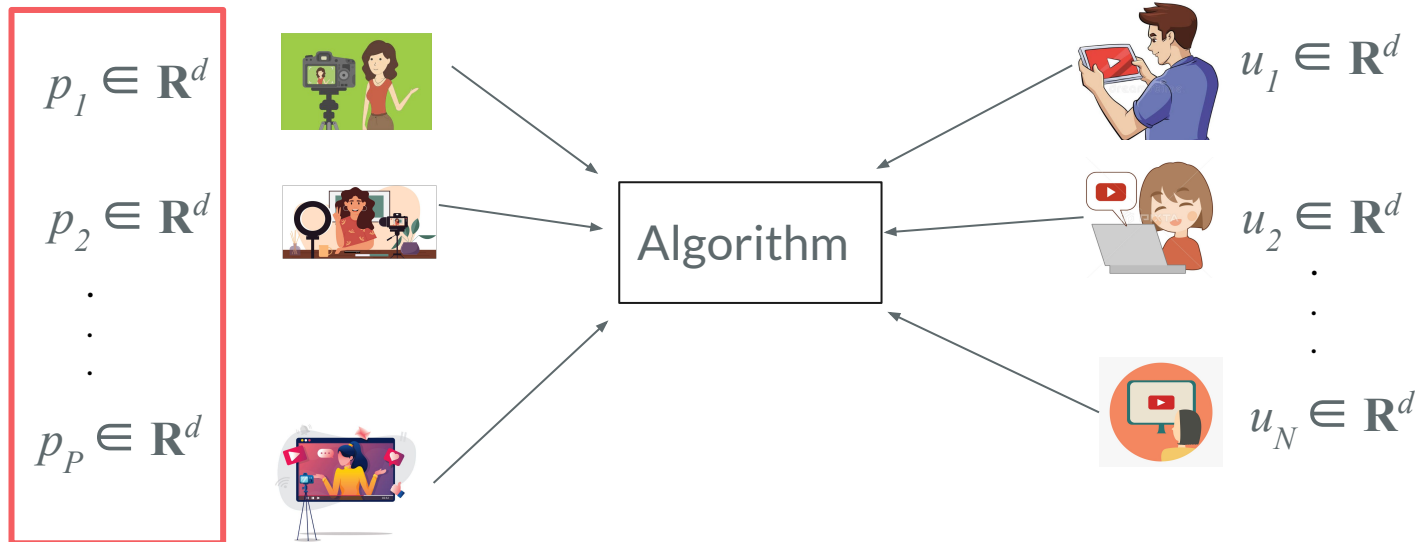
Our model

$$j^*(u) \in \{1, 2, \dots, P\}$$



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Each producer *selects* a D-dimensional content vector.

Our model

Producer profit:

$$\mathbf{P}(p_j \mid p_{-j}, u_{1:N}) = (\sum_{1 \leq i \leq N} \mathbf{I}[j^*(u_i) = j]) - c(p_j)$$

of users won

Fixed cost of
producing content

$$c(p) = ||p||^\beta$$

β captures difficulty of excelling
in many dimensions

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Value of p_j to user u

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Features of model: high-dimension action space & heterogeneous user values

Informal summary of results

We investigate the potential for specialization at equilibrium.

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Result 1: We give a **tight characterization** of when specialization occurs.

Result 2: We analyze **the specific form of specialization** in concrete instances.

Result 3: We show that specialization can **reduce market competitiveness**.

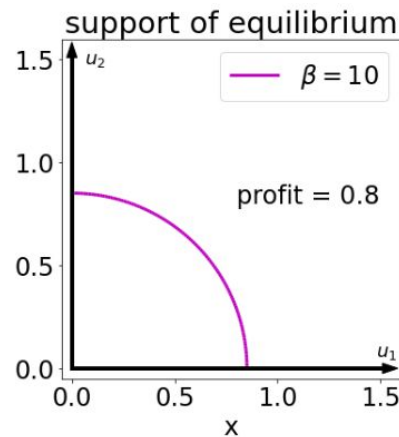
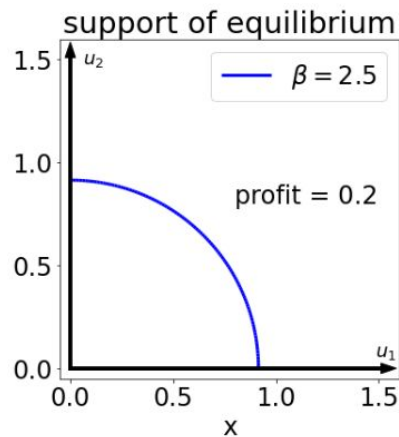
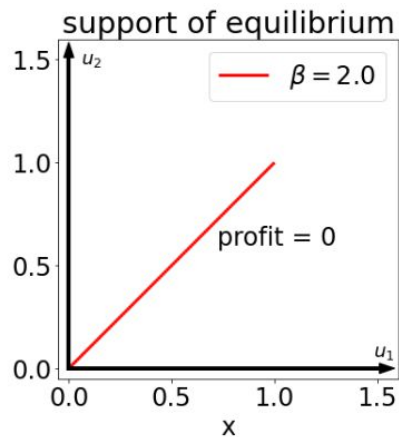
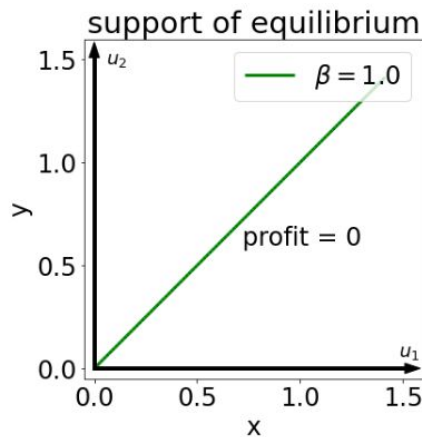
Example: 2 Populations of Users, $P = 2$ producers

Consider $u_1 = [1, 0]$ and $u_2 = [0, 1]$ with $P = 2$ producers and cost function $c(p) = \|p\|_2^\beta$.

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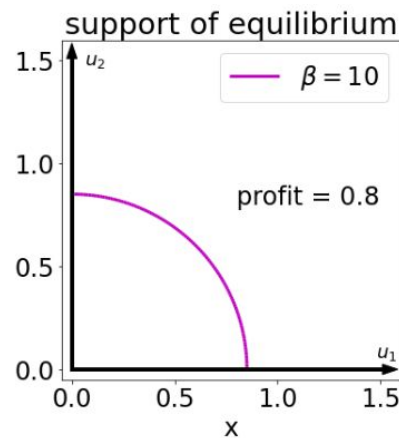
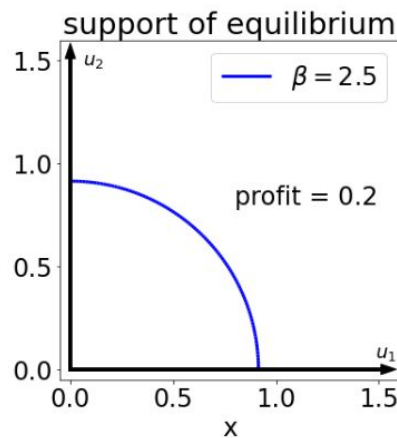
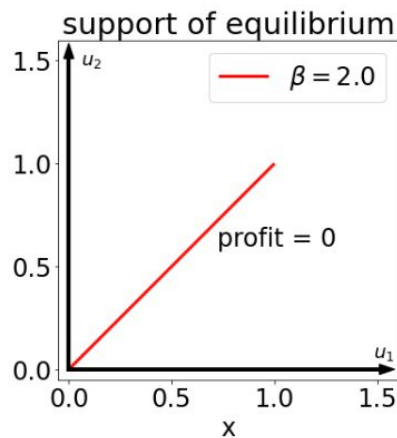
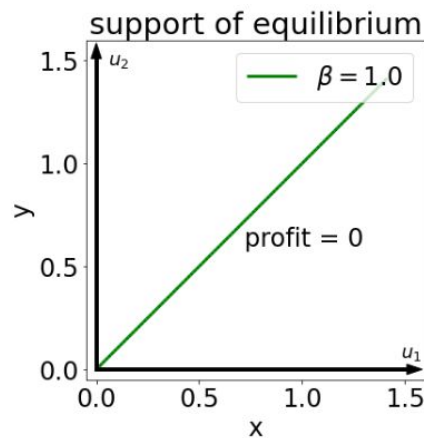


$\beta \leq 2$: single genre regime (no specialization)

$\beta \geq 2$: multi-genre regime (specialization)

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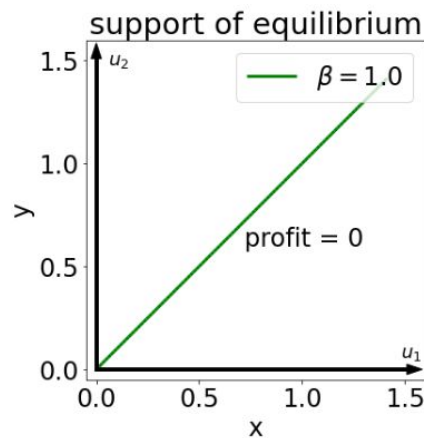
$\beta \geq 2$: multi-genre regime (specialization)

There is a phase transition at $\beta = 2$ between $\text{Genre}(\mu) = 1$ and $\text{Genre}(\mu) = \infty$.

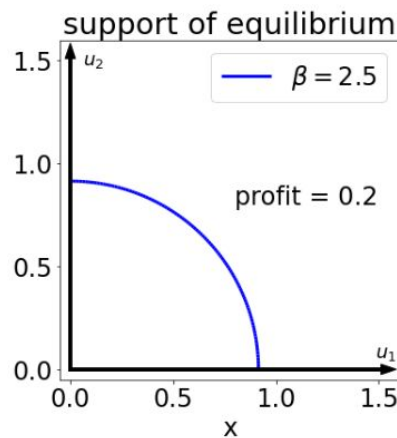
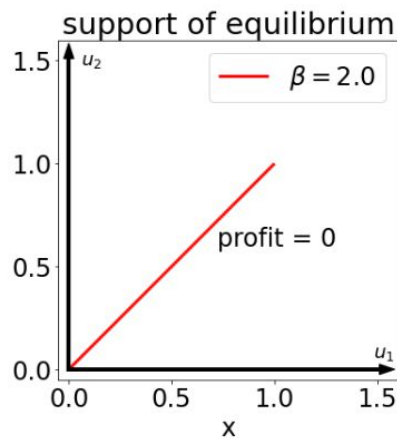
(Example of Result 1)

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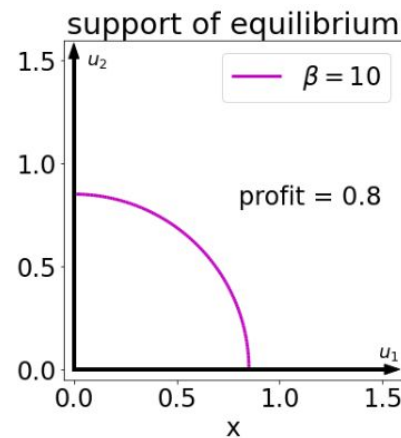
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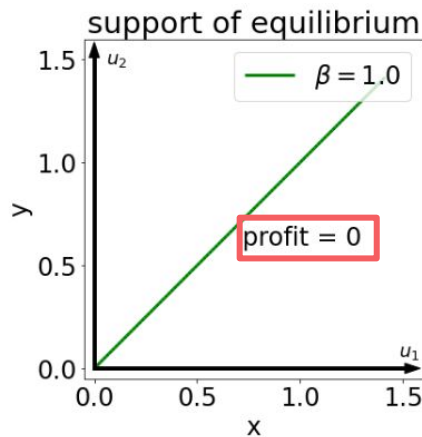


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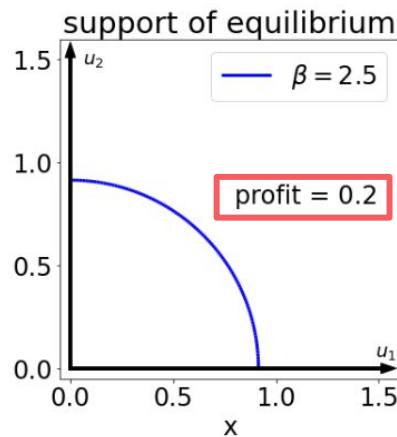
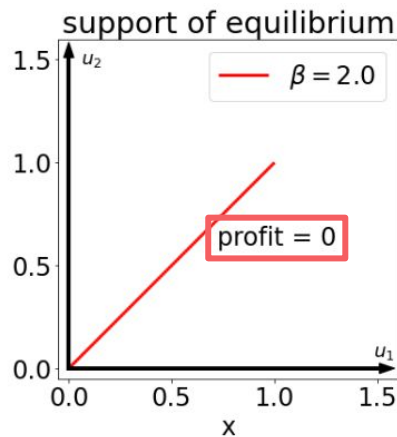
(Example of Result 2)

Example: 2 Populations of Users, $P = 2$ producers

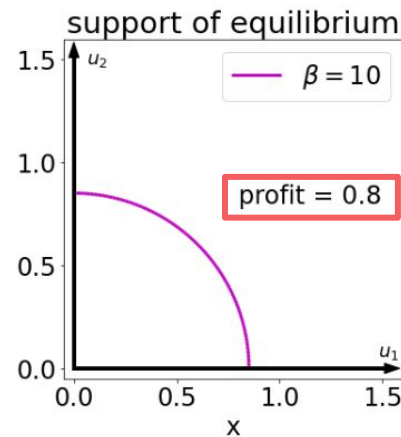
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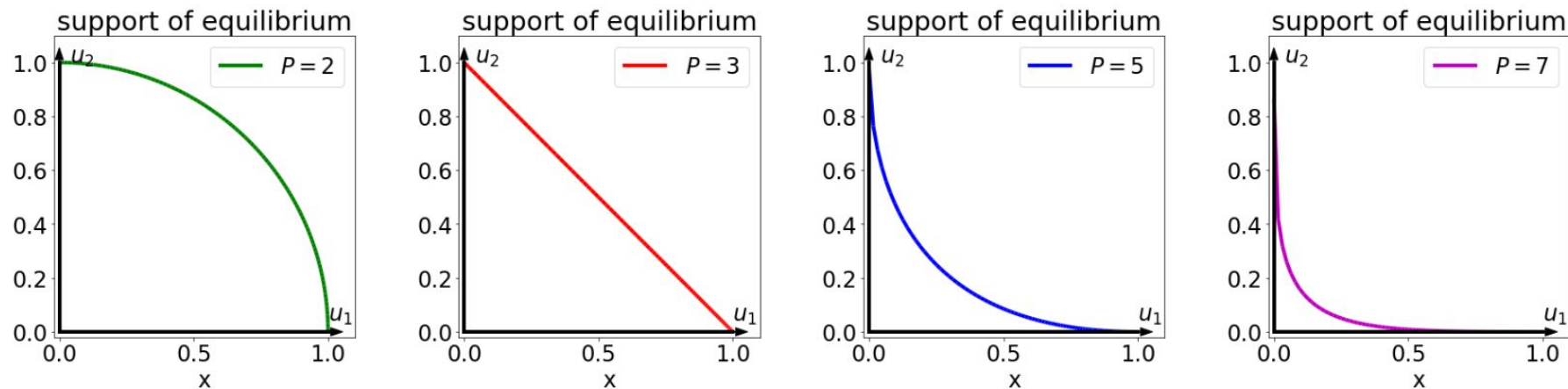


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(Example of Result 3)

Another example: $P \geq 2$ producers

Consider $u_1 = [1, 0]$ and $u_2 = [0, 1]$ with $P \geq 2$ producers and cost function $c(p) = \|p\|_2^2$.

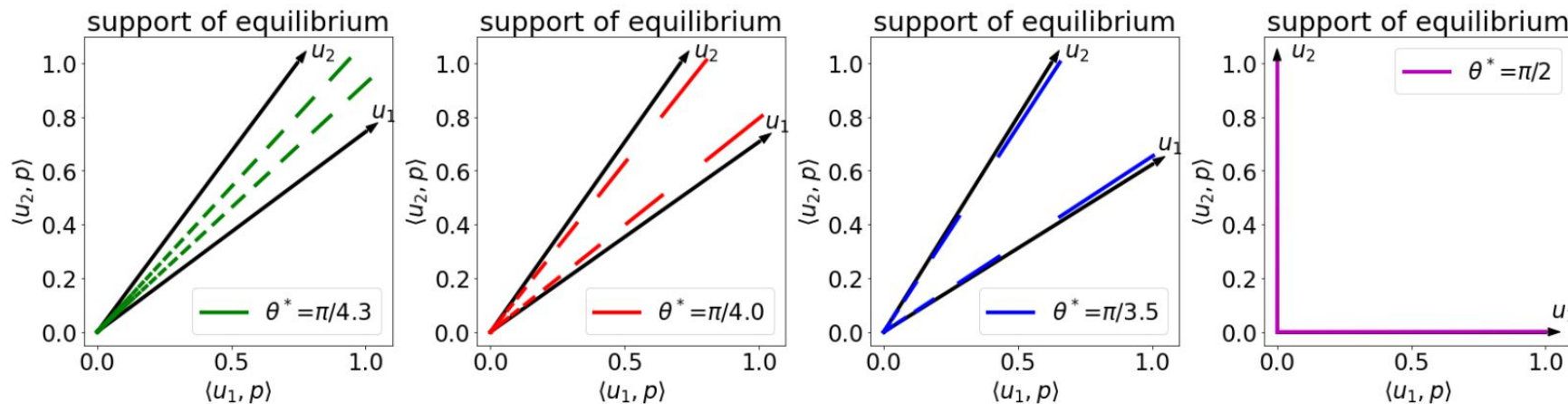


Specialization at infinite-genre equilibria takes different forms for different values of P .

(Another example of Result 2)

Another example: $P = \infty$ producers

Consider 2 users at u_1 and u_2 with $P = \infty$ producers and cost function $c(p) = \|p\|_2^\beta$.



Finite-genre re-emerge in the infinite-producer limit (but not exactly aligned with user vectors).

(Another example of Result 2)

Technical ingredients

We develop technical methods to analyze high-dimensional competition, including:

- We relate the existence of a single-genre equilibrium to **strong duality of an optimization program** that we construct.
- We show a **decoupling lemma** that transforms the high-dimensional action space into 1-dimensional functional equations.
- Our **formalization of specialization** does not require reasoning about asymmetric equilibria.

Discussion

Although consumer-side effects of recommendations have received a lot of attention, supply-side effects have been largely ignored.

We presented a **framework for supply-side competition in personalized rec systems** and investigated **the potential for specialization by producers**.

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We presented a **framework for supply-side competition in personalized rec systems** and investigated **the potential for specialization by producers**.

Opens the door to future investigation of supply-side behavior in recommender systems:

- Analyze how platform learning dynamics impact production over time (Hu*, **J.***, Jordan, Steinhardt)
- How is the welfare of users impacted by personalization and supply-side effects?
- How can the platform design a recommendation algorithm optimizes overall welfare?