

BIAS AND VARIANCE TRADE-OFF

↳ Characteristics of a model

2 properties for generalization →

① Low training error

— Bias

② Train & test error is similar

— Variance

Bias (assumptions)

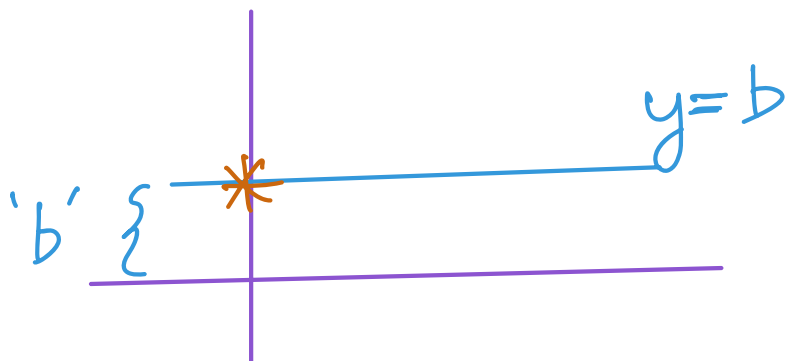
- "Inability of a model to capture the relationship in the training data"

$$y = wx + \textcircled{b} \rightarrow \text{bias}$$

Task : Relationship $X \rightarrow Y$

When do you fail?

- ① If 'b' is very large, it'll dominate the output
- ② When input isn't present ($x=0$), $y=b$, dictates the "assumptions" of the model



What are the consequences of making these assumptions ?

① High Bias

\Rightarrow Inability to map $X \rightarrow Y$

\Rightarrow High training error

② Low Bias

\rightarrow DESIRED

\Rightarrow Low training error

VARIANCE

"Difference of fit in between different datasets"

↙
train & test

① High variance

→ Diff. b/w train & test error is large

② Low variance

→ Diff. b/w train & test is low

↘

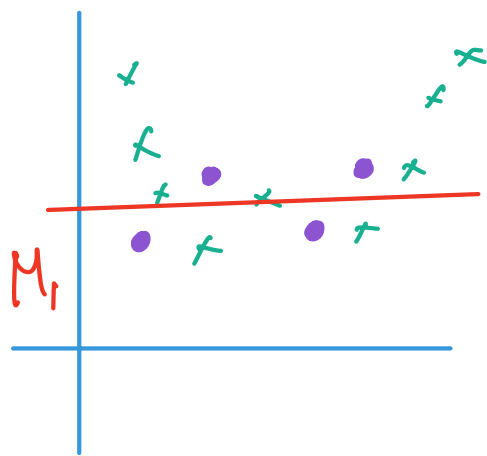
DESIRED

$$(Low\ train\ error) + (Train\ error \sim Test\ error)$$

↓
Low bias

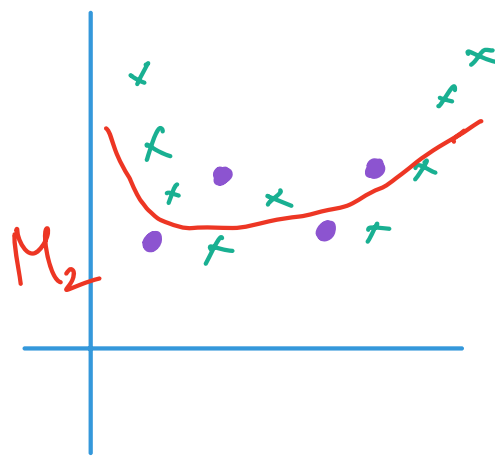
↓
Low variance

● TRAIN × TEST



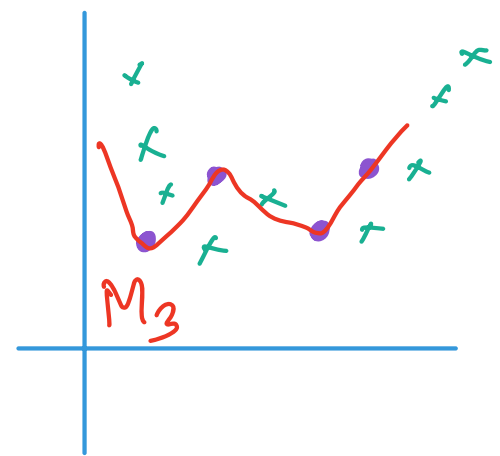
HIGH BIAS

LOW VARIANCE



LOW BIAS

LOW VARIANCE



LOW BIAS

HIGH VARIANCE



↓
OVER
FITTING

PREVENTION OF OVERFITTING

① Regularization

② Bagging

③ Boosting

PREVENTION OF OVERFITTING

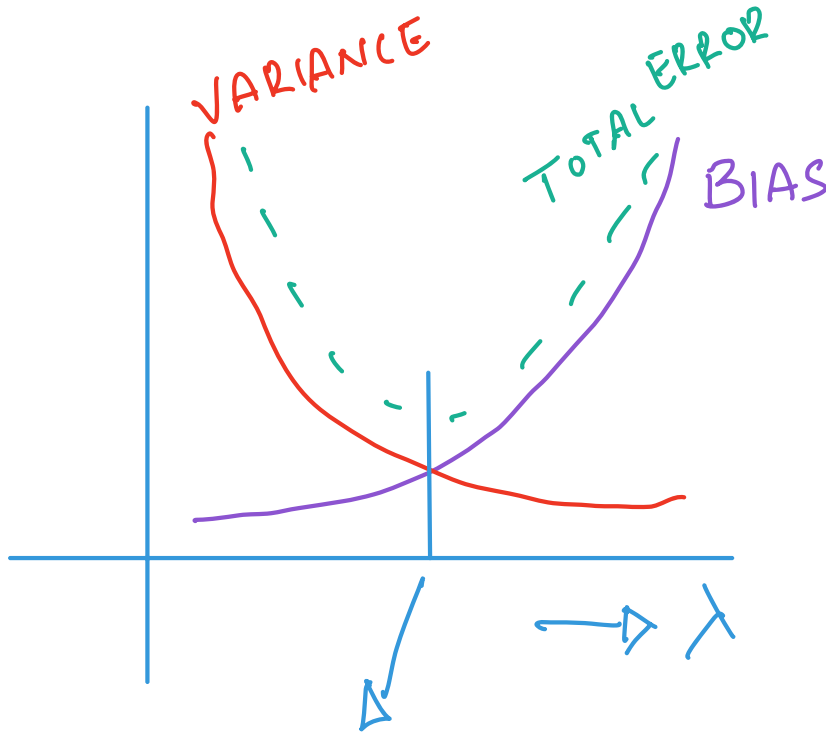
① Regularization

→ Reducing reliance on training data

(by changing slope)

⇒ ↑ BIAS

⇒ ↓ VARIANCE



"Choose this λ "
(Model complexity)

$$J = \|\hat{y} - y\|_2^2 + \lambda \omega^2$$