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Homework 4

CS 6515: Introduction to Graduate Algorithms

**Approach:**

- a.) To find if a path between  $s$  and  $t$  is made up of only white or gold edges within a graph, we first make a copy of the original graph, remove all gold edges, and call it  $G^{white}$ . We run  $G^{white}$  through the DFS algorithm to check if vertices  $s$  and  $t$  are connected components, if so, return TRUE. If not, we make another copy of the original graph, remove all white edges, and call it  $G^{gold}$ . We then run  $G^{gold}$  through the DFS algorithm again. If vertices  $s$  and  $t$  are connected components, return TRUE, if not, return FALSE as there is no path from  $s$  to  $t$  made up of only white edges or only gold edges.
- b.) To find if a path between  $s$  and  $t$  where all white edges appear before all gold edges within a graph, we first make a copy of the original graph, remove all gold edges, and call it  $G^{white}$ . We then run  $G^{white}$  through the DFS algorithm to see which vertices are connected components of  $s$ . Next, we make another copy of the original graph, remove all white edges from it, and call it  $G^{gold}$ . We then run  $G^{gold}$  through the DFS algorithm again, seeing which vertices are connected components of  $t$ . We then see if there's a vertex reachable from  $s$  only using white edges and reachable from  $t$  only using gold edges. Return TRUE if such a vertex exists, or FALSE otherwise.

**Correctness:**

- a.) Running  $G^{white}$  and  $G^{gold}$  through the DFS algorithm will show if a path between  $s$  and  $t$  containing only white or gold edges exists if  $s$  and  $t$  are within the same connected component.
- b.) Running  $G^{white}$  and  $G^{gold}$  through the DFS algorithm will show if there's a vertex reachable from  $s$  using only white edges, and from  $t$  using only gold edges. This vertex would indicate that a path between  $s$  and  $t$  with only white edges appearing before gold edges exists.

**Runtime:**

- a.) Copying the original graph takes  $O(n + m)$  time. Removing either all white or gold edges takes  $O(m)$  time. Finally, running DFS as a black box on either modified graph takes  $O(n + m)$  time. Making the overall runtime  $O(n + m)$ .

b.) Copying the original graph takes  $O(n + m)$  time. Removing the white and gold edges takes  $O(m)$  time. Running DFS as a black box on either modified graph takes  $O(n + m)$  time. Finally, scanning vertices takes  $O(n)$  time. Making the overall runtime  $O(n + m)$ .

**Collaborators:**

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