CS224N Assignment 1: Exploring Word Vectors (25 Points)

Due 4:30pm, Tue Jan 17

Welcome to CS224N!

Before you start, make sure you read the README.txt in the same directory as this notebook for important setup information. A lot of code is provided in this notebook, and we highly encourage you to read and understand it as part of the learning:)

If you aren't super familiar with Python, Numpy, or Matplotlib, we recommend you check out the review session on Friday. The session will be recorded and the material will be made available on our website (http://web.stanford.edu/class/cs224n/index.html#schedule). The CS231N Python/Numpy tutorial (https://cs231n.github.io/python-numpy-tutorial) is also a great resource.

Assignment Notes: Please make sure to save the notebook as you go along. Submission Instructions are located at the bottom of the notebook.

In []: !pip install gensim --upgrade
!pip install numpy==1.22.4

```
Looking in indexes: https://pypi.org/simple, (https://pypi.org/simple,) http
s://us-python.pkg.dev/colab-wheels/public/simple/ (https://us-python.pkg.dev/
colab-wheels/public/simple/)
Requirement already satisfied: gensim in /usr/local/lib/python3.8/dist-packag
es (3.6.0)
Collecting gensim
  Downloading gensim-4.3.0-cp38-cp38-manylinux 2 12 x86 64.manylinux2010 x86
64.whl (24.1 MB)
                                           -- 24.1/24.1 MB 52.6 MB/s eta 0:0
0:00
Requirement already satisfied: smart-open>=1.8.1 in /usr/local/lib/python3.8/
dist-packages (from gensim) (6.3.0)
Requirement already satisfied: scipy>=1.7.0 in /usr/local/lib/python3.8/dist-
packages (from gensim) (1.7.3)
Requirement already satisfied: numpy>=1.18.5 in /usr/local/lib/python3.8/dist
-packages (from gensim) (1.21.6)
Collecting FuzzyTM>=0.4.0
  Downloading FuzzyTM-2.0.5-py3-none-any.whl (29 kB)
Collecting pyfume
  Downloading pyFUME-0.2.25-py3-none-any.whl (67 kB)
                                             - 67.1/67.1 KB 6.1 MB/s eta 0:00:
00
Requirement already satisfied: pandas in /usr/local/lib/python3.8/dist-packag
es (from FuzzyTM>=0.4.0->gensim) (1.3.5)
Requirement already satisfied: python-dateutil>=2.7.3 in /usr/local/lib/pytho
n3.8/dist-packages (from pandas->FuzzyTM>=0.4.0->gensim) (2.8.2)
Requirement already satisfied: pytz>=2017.3 in /usr/local/lib/python3.8/dist-
packages (from pandas->FuzzyTM>=0.4.0->gensim) (2022.7.1)
Collecting simpful
  Downloading simpful-2.9.0-py3-none-any.whl (30 kB)
Collecting fst-pso
  Downloading fst-pso-1.8.1.tar.gz (18 kB)
  Preparing metadata (setup.py) ... done
Requirement already satisfied: six>=1.5 in /usr/local/lib/python3.8/dist-pack
ages (from python-dateutil>=2.7.3->pandas->FuzzyTM>=0.4.0->gensim) (1.15.0)
Collecting miniful
  Downloading miniful-0.0.6.tar.gz (2.8 kB)
  Preparing metadata (setup.py) ... done
Requirement already satisfied: requests in /usr/local/lib/python3.8/dist-pack
ages (from simpful->pyfume->FuzzyTM>=0.4.0->gensim) (2.25.1)
Requirement already satisfied: idna<3,>=2.5 in /usr/local/lib/python3.8/dist-
packages (from requests->simpful->pyfume->FuzzyTM>=0.4.0->gensim) (2.10)
Requirement already satisfied: chardet<5,>=3.0.2 in /usr/local/lib/python3.8/
dist-packages (from requests->simpful->pyfume->FuzzyTM>=0.4.0->gensim) (4.0.
Requirement already satisfied: urllib3<1.27,>=1.21.1 in /usr/local/lib/python
3.8/dist-packages (from requests->simpful->pyfume->FuzzyTM>=0.4.0->gensim)
(1.24.3)
Requirement already satisfied: certifi>=2017.4.17 in /usr/local/lib/python3.
8/dist-packages (from requests->simpful->pyfume->FuzzyTM>=0.4.0->gensim) (202
2.12.7)
Building wheels for collected packages: fst-pso, miniful
  Building wheel for fst-pso (setup.py) ... done
 Created wheel for fst-pso: filename=fst pso-1.8.1-py3-none-any.whl size=204
43 sha256=40d70db1a912342655149de7519aa07ae983923e839f1a11d375c8fd1cabf6af
  Stored in directory: /root/.cache/pip/wheels/6a/65/c4/d27eeee9ba3fc150a0dae
150519591103b9e0dbffde3ae77dc
```

```
Building wheel for miniful (setup.py) ... done
  Created wheel for miniful: filename=miniful-0.0.6-py3-none-any.whl size=353
0 sha256=f002a5429022e4cf20d4637db055eee921363aeacb14fc12b619f3638618487d
  Stored in directory: /root/.cache/pip/wheels/ba/d9/a0/ddd93af16d5855dd9bad4
17623e70948fdac119d1d34fb17c8
Successfully built fst-pso miniful
Installing collected packages: simpful, miniful, fst-pso, pyfume, FuzzyTM, ge
  Attempting uninstall: gensim
    Found existing installation: gensim 3.6.0
   Uninstalling gensim-3.6.0:
      Successfully uninstalled gensim-3.6.0
Successfully installed FuzzyTM-2.0.5 fst-pso-1.8.1 gensim-4.3.0 miniful-0.0.6
pyfume-0.2.25 simpful-2.9.0
Looking in indexes: https://pypi.org/simple, (https://pypi.org/simple,) http
s://us-python.pkg.dev/colab-wheels/public/simple/ (https://us-python.pkg.dev/
colab-wheels/public/simple/)
Collecting numpy==1.22.4
  Downloading numpy-1.22.4-cp38-cp38-manylinux 2 17 x86 64.manylinux2014 x86
64.whl (16.9 MB)
                                           -- 16.9/16.9 MB 68.8 MB/s eta 0:0
0:00
Installing collected packages: numpy
 Attempting uninstall: numpy
    Found existing installation: numpy 1.21.6
   Uninstalling numpy-1.21.6:
      Successfully uninstalled numpy-1.21.6
Successfully installed numpy-1.22.4
```

```
In [ ]: # All Import Statements Defined Here
        # Note: Do not add to this list.
        import sys
        assert sys.version info[0]==3
        assert sys.version info[1] >= 5
        from platform import python version
        assert int(python_version().split(".")[1]) >= 5, "Please upgrade your Python v
            the README.txt file found in the same directory as this notebook. Your Pyt
        from gensim.models import KeyedVectors
        from gensim.test.utils import datapath
        import pprint
        import matplotlib.pyplot as plt
        plt.rcParams['figure.figsize'] = [10, 5]
        import nltk
        nltk.download('reuters') #to specify download location, optionally add the arq
        from nltk.corpus import reuters
        import numpy as np
        import random
        import scipy as sp
        from sklearn.decomposition import TruncatedSVD
        from sklearn.decomposition import PCA
        START TOKEN = '<START>'
        END TOKEN = '<END>'
        np.random.seed(0)
        random.seed(0)
        # -----
```

[nltk_data] Downloading package reuters to /root/nltk_data...

Word Vectors

Word Vectors are often used as a fundamental component for downstream NLP tasks, e.g. question answering, text generation, translation, etc., so it is important to build some intuitions as to their strengths and weaknesses. Here, you will explore two types of word vectors: those derived from *co-occurrence matrices*, and those derived via *GloVe*.

Note on Terminology: The terms "word vectors" and "word embeddings" are often used interchangeably. The term "embedding" refers to the fact that we are encoding aspects of a word's meaning in a lower dimensional space. As Wikipedia

(https://en.wikipedia.org/wiki/Word_embedding) states, "conceptually it involves a mathematical embedding from a space with one dimension per word to a continuous vector space with a much lower dimension".

Part 1: Count-Based Word Vectors (10 points)

Most word vector models start from the following idea:

You shall know a word by the company it keeps (<u>Firth, J. R. 1957:11</u> (<u>https://en.wikipedia.org/wiki/John_Rupert_Firth</u>))

Many word vector implementations are driven by the idea that similar words, i.e., (near) synonyms, will be used in similar contexts. As a result, similar words will often be spoken or written along with a shared subset of words, i.e., contexts. By examining these contexts, we can try to develop embeddings for our words. With this intuition in mind, many "old school" approaches to constructing word vectors relied on word counts. Here we elaborate upon one of those strategies, *co-occurrence matrices* (for more information, see here (here (here (<a href="https://medium.com/data-science-group-iitr/word-embedding-2d05d270b285)).

Co-Occurrence

A co-occurrence matrix counts how often things co-occur in some environment. Given some word w_i occurring in the document, we consider the *context window* surrounding w_i . Supposing our fixed window size is n, then this is the n preceding and n subsequent words in that document, i.e. words $w_{i-n} \dots w_{i-1}$ and $w_{i+1} \dots w_{i+n}$. We build a *co-occurrence matrix* M, which is a symmetric word-by-word matrix in which M_{ij} is the number of times w_j appears inside w_i 's window among all documents.

Example: Co-Occurrence with Fixed Window of n=1:

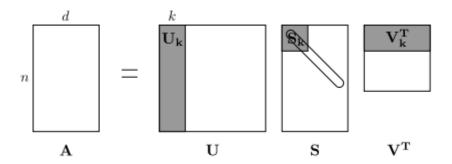
Document 1: "all that glitters is not gold"

Document 2: "all is well that ends well"

*	<start></start>	all	that	glitters	is	not	gold	well	ends	<end></end>
<start></start>	0	2	0	0	0	0	0	0	0	0
all	2	0	1	0	1	0	0	0	0	0
that	0	1	0	1	0	0	0	1	1	0
glitters	0	0	1	0	1	0	0	0	0	0
is	0	1	0	1	0	1	0	1	0	0
not	0	0	0	0	1	0	1	0	0	0
gold	0	0	0	0	0	1	0	0	0	1
well	0	0	1	0	1	0	0	0	1	1
ends	0	0	1	0	0	0	0	1	0	0
<end></end>	0	0	0	0	0	0	1	1	0	0

Note: In NLP, we often add <START> and <END> tokens to represent the beginning and end of sentences, paragraphs or documents. In this case we imagine <START> and <END> tokens encapsulating each document, e.g., " <START> All that glitters is not gold <END> ", and include these tokens in our co-occurrence counts.

The rows (or columns) of this matrix provide one type of word vectors (those based on wordword co-occurrence), but the vectors will be large in general (linear in the number of distinct words in a corpus). Thus, our next step is to run *dimensionality reduction*. In particular, we will run SVD (Singular Value Decomposition), which is a kind of generalized PCA (Principal Components Analysis) to select the top k principal components. Here's a visualization of dimensionality reduction with SVD. In this picture our co-occurrence matrix is A with n rows corresponding to n words. We obtain a full matrix decomposition, with the singular values ordered in the diagonal S matrix, and our new, shorter length-k word vectors in U_k .



This reduced-dimensionality co-occurrence representation preserves semantic relationships between words, e.g. *doctor* and *hospital* will be closer than *doctor* and *dog*.

Notes: If you can barely remember what an eigenvalue is, here's <u>a slow, friendly introduction to SVD (https://davetang.org/file/Singular_Value_Decomposition_Tutorial.pdf)</u>. If you want to learn more thoroughly about PCA or SVD, feel free to check out lectures $\underline{7}$ (https://web.stanford.edu/class/cs168/l/I7.pdf), <u>8 (http://theory.stanford.edu/~tim/s15/l/I8.pdf)</u>, and <u>9 (https://web.stanford.edu/class/cs168/l/I9.pdf)</u> of CS168. These course notes provide a great high-level treatment of these general purpose algorithms. Though, for the purpose of this class, you only need to know how to extract the k-dimensional embeddings by utilizing preprogrammed implementations of these algorithms from the numpy, scipy, or sklearn python packages. In practice, it is challenging to apply full SVD to large corpora because of the memory needed to perform PCA or SVD. However, if you only want the top k vector components for relatively small k— known as $\underline{\text{Truncated SVD}}$ (https://en.wikipedia.org/wiki/Singular_value_decomposition# $\underline{\text{Truncated SVD}}$) — then there are reasonably scalable techniques to compute those iteratively.

Plotting Co-Occurrence Word Embeddings

Here, we will be using the Reuters (business and financial news) corpus. If you haven't run the import cell at the top of this page, please run it now (click it and press SHIFT-RETURN). The corpus consists of 10,788 news documents totaling 1.3 million words. These documents span 90 categories and are split into train and test. For more details, please see https://www.nltk.org/book/ch02.html (https://www.nltk.org/book/ch02.html). We provide a read corpus function below that pulls out only articles from the "gold" (i.e. news articles

about gold, mining, etc.) category. The function also adds <START> and <END> tokens to each of the documents, and lowercases words. You do **not** have to perform any other kind of pre-processing.

Let's have a look what these documents are like....

```
In [ ]: reuters_corpus = read_corpus()
pprint.pprint(reuters_corpus[:3], compact=True, width=100)
```

```
[['<START>', 'western', 'mining', 'to', 'open', 'new', 'gold', 'mine', 'in',
'australia', 'western',
  'mining', 'corp', 'holdings', 'ltd', '&', 'lt', ';', 'wmng', '.', 's', '>',
'(', 'wmc', ')',
  'said', 'it', 'will', 'establish', 'a', 'new', 'joint', 'venture', 'gold',
'mine', 'in', 'the',
  'northern', 'territory', 'at', 'a', 'cost', 'of', 'about', '21', 'mln', 'dl
rs', '.', 'the',
  'mine', ',', 'to', 'be', 'known', 'as', 'the', 'goodall', 'project', ',',
'will', 'be', 'owned',
  '60', 'pct', 'by', 'wmc', 'and', '40', 'pct', 'by', 'a', 'local', 'w', '.',
'r', '.', 'grace',
  'and', 'co', '&', 'lt', ';', 'gra', '>', 'unit', '.', 'it', 'is', 'locate
d', '30', 'kms', 'east',
  'of', 'the', 'adelaide', 'river', 'at', 'mt', '.', 'bundey', ',', 'wmc', 's
aid', 'in', 'a',
  'statement', 'it', 'said', 'the', 'open', '-', 'pit', 'mine', ',', 'with',
'a', 'conventional',
  'leach', 'treatment', 'plant', ',', 'is', 'expected', 'to', 'produce', 'abo
ut', '50', ',', '000', 'ounces', 'of', 'gold', 'in', 'its', 'first', 'year', 'of', 'production',
'from', 'mid', '-',
  '1988', '.', 'annual', 'ore', 'capacity', 'will', 'be', 'about', '750',
',', '000', 'tonnes', '.',
  '<END>'],
 ['<START>', 'belgium', 'to', 'issue', 'gold', 'warrants', ',', 'sources', 's
ay', 'belgium',
  'plans', 'to', 'issue', 'swiss', 'franc', 'warrants', 'to', 'buy', 'gold',
 ,', 'with', 'credit',
  'suisse', 'as', 'lead', 'manager', ',', 'market', 'sources', 'said', '.',
'no', 'confirmation',
  'or', 'further', 'details', 'were', 'immediately', 'available', '.', '<END
>'],
 ['<START>', 'belgium', 'launches', 'bonds', 'with', 'gold', 'warrants', 'th
e', 'kingdom', 'of',
  'belgium', 'is', 'launching', '100', 'mln', 'swiss', 'francs', 'of', 'seve
n', 'year', 'notes',
  'with', 'warrants', 'attached', 'to', 'buy', 'gold', ',', 'lead', 'manange
r', 'credit', 'suisse',
  'said', '.', 'the', 'notes', 'themselves', 'have', 'a', '3', '-', '3', '/',
'8', 'pct', 'coupon',
  'and', 'are', 'priced', 'at', 'par', '.', 'payment', 'is', 'due', 'april',
          '1987',
  'and', 'final', 'maturity', 'april', '30', ',', '1994', '.', 'each', '50',
 ,', '000', 'franc',
  'note', 'carries', '15', 'warrants', '.', 'two', 'warrants', 'are', 'requir
ed', 'to', 'allow',
  'the', 'holder', 'to', 'buy', '100', 'grammes', 'of', 'gold', 'at', 'a', 'p
rice', 'of', '2',
  '450', 'francs', ',', 'during', 'the', 'entire', 'life', 'of', 'the', 'bon
d', '.', 'the',
  'latest', 'gold', 'price', 'in', 'zurich', 'was', '2', ',', '045', '/',
'2', ',', '070', 'francs',
  'per', '100', 'grammes', '.', '<END>']]
```

Question 1.1: Implement distinct_words [code] (2 points)

Write a method to work out the distinct words (word types) that occur in the corpus. You can do this with for loops, but it's more efficient to do it with Python list comprehensions. In particular, this://coderwall.com/p/rcmaea/flatten-a-list-of-lists-in-one-line-in-python) may be useful to flatten a list of lists. If you're not familiar with Python list comprehensions in general, here's more information (https://python-3-patterns-idioms-test.readthedocs.io/en/latest/Comprehensions.html">test.readthedocs.io/en/latest/Comprehensions.html).

Your returned corpus_words should be sorted. You can use python's sorted function for this.

You may find it useful to use Python sets (https://www.w3schools.com/python/python_sets.asp) to remove duplicate words.

```
In [ ]: |#
        # Run this sanity check
        # Note that this not an exhaustive check for correctness.
        # Define toy corpus
        test_corpus = ["{} All that glitters isn't gold {}".format(START_TOKEN, END_TO
        test corpus words, num corpus words = distinct words(test corpus)
        # Correct answers
        ans test corpus words = sorted([START TOKEN, "All", "ends", "that", "gold", "A
        ans_num_corpus_words = len(ans_test_corpus_words)
        # Test correct number of words
        assert(num corpus words == ans num corpus words), "Incorrect number of distind
        # Test correct words
        assert (test_corpus_words == ans_test_corpus_words), "Incorrect corpus_words.\
        # Print Success
        print ("-" * 80)
        print("Passed All Tests!")
        print ("-" * 80)
        Passed All Tests!
```

Question 1.2: Implement compute_co_occurrence_matrix [code] (3 points)

Write a method that constructs a co-occurrence matrix for a certain window-size n (with a default of 4), considering words n before and n after the word in the center of the window. Here, we start to use numpy (np) to represent vectors, matrices, and tensors. If you're not familiar with NumPy, there's a NumPy tutorial in the second half of this cs231n <u>Python NumPy tutorial</u> (http://cs231n.github.io/python-numpy-tutorial/).

```
In [ ]: | def compute co occurrence matrix(corpus, window size=4):
            """ Compute co-occurrence matrix for the given corpus and window_size (def
                Note: Each word in a document should be at the center of a window. Wor
                      number of co-occurring words.
                      For example, if we take the document "<START> All that glitters
                      "All" will co-occur with "<START>", "that", "glitters", "is", an
                Params:
                    corpus (list of list of strings): corpus of documents
                    window_size (int): size of context window
                Return:
                    M (a symmetric numpy matrix of shape (number of unique words in th
                        Co-occurence matrix of word counts.
                        The ordering of the words in the rows/columns should be the sa
                    word2ind (dict): dictionary that maps word to index (i.e. row/colu
            words, n_words = distinct_words(corpus)
            M = np.zeros((n words, n words))
            word2ind = dict(zip(words, range(len(words))))
            # ["all", "my", "window", "cure", "you", "cure", "heart", "what", "have"]
            for sentence in corpus:
              for idx, word in enumerate(sentence):
                left_window = idx - window_size if idx > window_size else 0
                right window = idx + window size + 1
                left words, right words = sentence[left window : idx], sentence[idx +
                all surrroundings = left words + right words
                curr ind = word2ind[word]
                for neighbor in all surrroundings:
                  neighbor ind = word2ind[neighbor]
                  M[curr ind, neighbor ind] += 1
            ### SOLUTION BEGIN
            ### SOLUTION END
            return M, word2ind
```

```
In [ ]: #
        # Run this sanity check
        # Note that this is not an exhaustive check for correctness.
        # Define toy corpus and get student's co-occurrence matrix
        test_corpus = ["{} All that glitters isn't gold {}".format(START_TOKEN, END_TO
        M test, word2ind test = compute co occurrence matrix(test corpus, window size=
        # Correct M and word2ind
        M test ans = np.array(
            [[0., 0., 0., 0., 0., 0., 1., 0., 0., 1.,],
             [0., 0., 1., 1., 0., 0., 0., 0., 0., 0., 0.,]
             [0., 1., 0., 0., 0., 0., 0., 0., 1., 0.,],
             [0., 1., 0., 0., 0., 0., 0., 0., 0., 1.,],
             [0., 0., 0., 0., 0., 0., 0., 0., 1., 1.,],
             [0., 0., 0., 0., 0., 0., 0., 1., 1., 0.,],
             [1., 0., 0., 0., 0., 0., 0., 1., 0., 0.,],
             [0., 0., 0., 0., 0., 1., 1., 0., 0., 0.,],
             [0., 0., 1., 0., 1., 1., 0., 0., 0., 1.,],
             [1., 0., 0., 1., 1., 0., 0., 0., 1., 0.,]]
        ans test corpus words = sorted([START TOKEN, "All", "ends", "that", "gold", "A
        word2ind_ans = dict(zip(ans_test_corpus_words, range(len(ans_test_corpus_words)
        print(word2ind ans)
        # Test correct word2ind
        assert (word2ind_ans == word2ind_test), "Your word2ind is incorrect:\nCorrect:
        # Test correct M shape
        assert (M_test.shape == M_test_ans.shape), "M matrix has incorrect shape.\nCor
        # Test correct M values
        for w1 in word2ind ans.keys():
            idx1 = word2ind_ans[w1]
            for w2 in word2ind ans.keys():
                idx2 = word2ind ans[w2]
                student = M_test[idx1, idx2]
                correct = M test ans[idx1, idx2]
                if student != correct:
                    print("Correct M:")
                    print(M test ans)
                    print("Your M: ")
                    print(M test)
                    raise AssertionError("Incorrect count at index ({}, {})=({}, {}) i
        # Print Success
        print ("-" * 80)
        print("Passed All Tests!")
        print ("-" * 80)
```

Question 1.3: Implement reduce_to_k_dim [code] (1 point)

Construct a method that performs dimensionality reduction on the matrix to produce k-dimensional embeddings. Use SVD to take the top k components and produce a new matrix of k-dimensional embeddings.

Note: All of numpy, scipy, and scikit-learn (sklearn) provide *some* implementation of SVD, but only scipy and sklearn provide an implementation of Truncated SVD, and only sklearn provides an efficient randomized algorithm for calculating large-scale Truncated SVD. So please use sklearn.decomposition.TruncatedSVD (https://scikit-learn.org/stable/modules/generated/sklearn.decomposition.TruncatedSVD.html).

```
In [ ]: def reduce to k dim(M, k=2):
                                           """ Reduce a co-occurence count matrix of dimensionality (num_corpus_words
                                                        to a matrix of dimensionality (num corpus words, k) using the following
                                                                       http://scikit-learn.org/stable/modules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklearn.decompodules/generated/sklea
                                                        Params:
                                                                      M (numpy matrix of shape (number of unique words in the corpus , n
                                                                      k (int): embedding size of each word after dimension reduction
                                                                      M reduced (numpy matrix of shape (number of corpus words, k)): mat
                                                                                                  In terms of the SVD from math class, this actually returns
                                          n iters = 10
                                                                                                     # Use this parameter in your call to `TruncatedSVD`
                                          M reduced = None
                                          print("Running Truncated SVD over %i words..." % (M.shape[0]))
                                           ### SOLUTION BEGIN
                                          svd = TruncatedSVD(n components=k, n iter=n iters)
                                           svd.fit(M)
                                          M_reduced = svd.transform(M)
                                           ### SOLUTION END
                                          print("Done.")
                                          return M_reduced
```

```
In [ ]: # -
        # Run this sanity check
        # Note that this is not an exhaustive check for correctness
        # In fact we only check that your M reduced has the right dimensions.
        # Define toy corpus and run student code
        test corpus = ["{} All that glitters isn't gold {}".format(START TOKEN, END TO
        M test, word2ind test = compute co occurrence matrix(test corpus, window size=
        M_test_reduced = reduce_to_k_dim(M_test, k=2)
        print(M test reduced)
        # Test proper dimensions
        assert (M_test_reduced.shape[0] == 10), "M_reduced has {} rows; should have {}
        assert (M_test_reduced.shape[1] == 2), "M_reduced has {} columns; should have
        # Print Success
        print ("-" * 80)
        print("Passed All Tests!")
        print ("-" * 80)
        Running Truncated SVD over 10 words...
        Done.
        [[ 6.54802087e-01 7.83221122e-01]
         [ 5.20200324e-01 -4.44089210e-16]
           7.05647176e-01 -4.84057274e-01]
         [ 7.05647176e-01 4.84057274e-01]
         [ 1.02780472e+00  0.00000000e+00]
         [ 6.54802087e-01 -7.83221122e-01]
         [ 3.82258491e-01 -6.56224003e-01]
         [ 3.82258491e-01 6.56224003e-01]
         [ 1.39420808e+00 1.06179274e+00]
           1.39420808e+00 -1.06179274e+00]]
        Passed All Tests!
```

Question 1.4: Implement plot_embeddings [code] (1 point)

Here you will write a function to plot a set of 2D vectors in 2D space. For graphs, we will use Matplotlib (plt).

For this example, you may find it useful to adapt this code

(http://web.archive.org/web/20190924160434/https://www.pythonmembers.club/2018/05/08/matpscatter-plot-annotate-set-text-at-label-each-point/). In the future, a good way to make a plot is to look at the Matplotlib gallery (https://matplotlib.org/gallery/index.html), find a plot that looks somewhat like what you want, and adapt the code they give.

•

```
In [ ]: def plot_embeddings(M_reduced, word2ind, words):
            """ Plot in a scatterplot the embeddings of the words specified in the lis
                NOTE: do not plot all the words listed in M_reduced / word2ind.
                Include a label next to each point.
                Params:
                    M_reduced (numpy matrix of shape (number of unique words in the co
                    word2ind (dict): dictionary that maps word to indices for matrix M
                    words (list of strings): words whose embeddings we want to visuali
            .....
            ### SOLUTION BEGIN
            for word in words:
                word idx = word2ind[word]
                x = M reduced[word idx, 0]
                y = M_reduced[word_idx, 1]
                plt.scatter(x, y, marker='x', color="red")
                plt.text(x, y, word)
            ### SOLUTION END
```

```
In [ ]:
        # Run this sanity check
        # Note that this is not an exhaustive check for correctness.
        # The plot produced should look like the "test solution plot" depicted below.
        print ("-" * 80)
        print ("Outputted Plot:")
        M_reduced_plot_test = np.array([[1, 1], [-1, -1], [1, -1], [-1, 1], [0, 0]])
        word2ind_plot_test = {'test1': 0, 'test2': 1, 'test3': 2, 'test4': 3, 'test5':
        words = ['test1', 'test2', 'test3', 'test4', 'test5']
        plot_embeddings(M_reduced_plot_test, word2ind_plot_test, words)
        print ("-" * 80)
        Outputted Plot:
                  ≰est4
                                                                                      ≠est1
           1.00
           0.75
           0.50
           0.25
                                                    test5
           0.00
          -0.25
          -0.50
          -0.75
          -1.00
                                                                                      Jest3
```

Question 1.5: Co-Occurrence Plot Analysis [written] (3 points)

-0.25

Now we will put together all the parts you have written! We will compute the co-occurrence matrix with fixed window of 4 (the default window size), over the Reuters "gold" corpus. Then we will use TruncatedSVD to compute 2-dimensional embeddings of each word. TruncatedSVD returns U*S, so we need to normalize the returned vectors, so that all the vectors will appear around the unit circle (therefore closeness is directional closeness). **Note**: The line of code below that does the normalizing uses the NumPy concept of *broadcasting*. If you don't know about broadcasting, check out Computation on Arrays: Broadcasting by Jake VanderPlas (https://jakevdp.github.io/PythonDataScienceHandbook/02.05-computation-on-arrays-broadcasting.html).

000

0.25

0.50

0.75

1.00

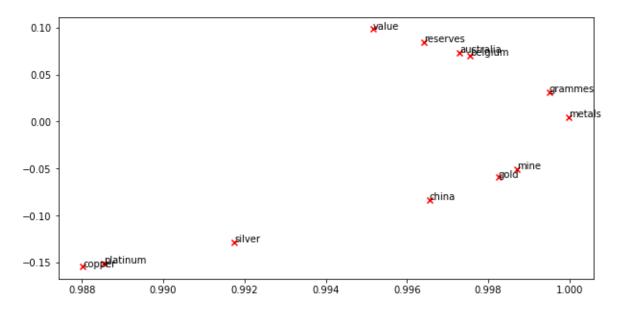
Run the below cell to produce the plot. It'll probably take a few seconds to run.

-1.00

-0.75

-0.50

Running Truncated SVD over 2830 words...
Done.



Verify that your figure matches "question_1.5.png" in the assignment zip. If not, use that figure to answer the next two questions.

a. Find at least two groups of words that cluster together in 2-dimensional embedding space. Give an explanation for each cluster you observe.

SOLUTION BEGIN

SOLUTION END

b. What doesn't cluster together that you might think should have? Describe at least two examples.

SOLUTION END

Part 2: Prediction-Based Word Vectors (15 points)

As discussed in class, more recently prediction-based word vectors have demonstrated better performance, such as word2vec and GloVe (which also utilizes the benefit of counts). Here, we shall explore the embeddings produced by GloVe. Please revisit the class notes and lecture slides for more details on the word2vec and GloVe algorithms. If you're feeling adventurous, challenge yourself and try reading GloVe's original paper (https://nlp.stanford.edu/pubs/glove.pdf).

Then run the following cells to load the GloVe vectors into memory. **Note**: If this is your first time to run these cells, i.e. download the embedding model, it will take a couple minutes to run. If you've run these cells before, rerunning them will load the model without redownloading it, which will take about 1 to 2 minutes.

```
In []: # ------
# Run Cell to Load Word Vectors
# Note: This will take a couple minutes
# ------
wv_from_bin = load_embedding_model()
```

```
[=======] 100.0% 252.1/252.1MB dow nloaded Loaded vocab size 400000
```

Note: If you are receiving a "reset by peer" error, rerun the cell to restart the download. If you run into an "attribute" error, you may need to update to the most recent version of gensim and numpy. You can upgrade them inline by uncommenting and running the below cell:

Reducing dimensionality of Word Embeddings

Let's directly compare the GloVe embeddings to those of the co-occurrence matrix. In order to avoid running out of memory, we will work with a sample of 10000 GloVe vectors instead. Run the following cells to:

- 1. Put 10000 Glove vectors into a matrix M
- 2. Run reduce_to_k_dim (your Truncated SVD function) to reduce the vectors from 200-dimensional to 2-dimensional.

```
In [ ]: def get_matrix_of_vectors(wv_from_bin, required_words):
            """ Put the GloVe vectors into a matrix M.
                    wv from bin: KeyedVectors object; the 400000 GloVe vectors loaded
                Return:
                    M: numpy matrix shape (num words, 200) containing the vectors
                    word2ind: dictionary mapping each word to its row number in M
            import random
            words = list(wv from bin.index to key)
            print("Shuffling words ...")
            random.seed(225)
            random.shuffle(words)
            words = words[:10000]
            print("Putting %i words into word2ind and matrix M..." % len(words))
            word2ind = {}
            M = []
            curInd = 0
            for w in words:
                try:
                    M.append(wv from bin.get vector(w))
                    word2ind[w] = curInd
                    curInd += 1
                except KeyError:
                    continue
            for w in required words:
                if w in words:
                    continue
                try:
                    M.append(wv from bin.get vector(w))
                    word2ind[w] = curInd
                    curInd += 1
                except KeyError:
                    continue
            M = np.stack(M)
            print("Done.")
            return M, word2ind
```

Note: If you are receiving out of memory issues on your local machine, try closing other applications to free more memory on your device. You may want to try restarting your machine so that you can free up extra memory. Then immediately run the jupyter notebook and see if you can load the word vectors properly. If you still have problems with loading the embeddings onto your local machine after this, please go to office hours or contact course staff.

Question 2.1: GloVe Plot Analysis [written] (3 points)

```
Run the cell below to plot the 2D GloVe embeddings for ['value', 'gold', 'platinum', 'reserves', 'silver', 'metals', 'copper', 'belgium', 'australia', 'china', 'grammes', "mine"].
```

```
In [ ]: words = ['value', 'gold', 'platinum', 'reserves', 'silver', 'metals', 'copper'
          plot_embeddings(M_reduced_normalized, word2ind, words)
             0.1
                                                                                                      File∀€alls
             0.0
                                                                                                     Wolde
            -0.1
                                                                                                     china
eserves
            -0.2
            -0.3
                                                                                                  yalue
            -0.4
                                                                                               ∡copper
            -0.5
            -0.6
                                                                                         yplatinum
                     grammes .
            -0.7
                                                                 0.25
                                                                             0.50
                                                                                        0.75
                                                                                                    1.00
                             -0.50
                                         -0.25
                                                     0.00
                 -0.75
```

a. What is one way the plot is different from the one generated earlier from the co-occurrence matrix? What is one way it's similar?

SOLUTION BEGIN

the range of values are different and captured similarities better. but both have some sense of knowing words meaning

SOLUTION END

b. What is a possible cause for the difference?

SOLUTION BEGIN

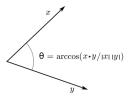
cause glove beyond using co-occurence matrix it uses ratio between two words happening with some other sample word and captures similarities better

SOLUTION END

Cosine Similarity

Now that we have word vectors, we need a way to quantify the similarity between individual words, according to these vectors. One such metric is cosine-similarity. We will be using this to find words that are "close" and "far" from one another.

We can think of n-dimensional vectors as points in n-dimensional space. If we take this perspective <u>L1 (http://mathworld.wolfram.com/L1-Norm.html)</u> and <u>L2 (http://mathworld.wolfram.com/L2-Norm.html)</u> Distances help quantify the amount of space "we must travel" to get between these two points. Another approach is to examine the angle between two vectors. From trigonometry we know that:



Instead of computing the actual angle, we can leave the similarity in terms of $similarity = cos(\Theta)$. Formally the Cosine Similarity (https://en.wikipedia.org/wiki/Cosine_similarity) s between two vectors s and s is defined as:

$$s = \frac{p \cdot q}{||p||||q||}$$
, where $s \in [-1, 1]$

Question 2.2: Words with Multiple Meanings (1.5 points) [code +

written]

Polysemes and homonyms are words that have more than one meaning (see this wiki-page (https://en.wikipedia.org/wiki/Polysemy) to learn more about the difference between polysemes and homonyms). Find a word with at least two different meanings such that the top-10 most similar words (according to cosine similarity) contain related words from both meanings. For example, "leaves" has both "go_away" and "a_structure_of_a_plant" meaning in the top 10, and "scoop" has both "handed_waffle_cone" and "lowdown". You will probably need to try several polysemous or homonymic words before you find one.

Please state the word you discover and the multiple meanings that occur in the top 10. Why do you think many of the polysemous or homonymic words you tried didn't work (i.e. the top-10 most similar words only contain **one** of the meanings of the words)?

Note: You should use the wv_from_bin.most_similar(word) function to get the top 10 similar words. This function ranks all other words in the vocabulary with respect to their cosine similarity to the given word. For further assistance, please check the **GenSim documentation** (https://radimrehurek.com/gensim/models/keyedvectors.html#gensim.models.keyedvectors.html#gensim.html#gensim.html#gensim.html#gensim.html#gensim.html#gensim.html#gensim.html#gensim.html#gensim.html#gensim.html#gensim.html#gensim.html#gensim.html#gensim.html#gensim.

SOLUTION BEGIN

like means both want or love sth, and such becuase it depends on dataset and how much frequent the similar words happened together.

SOLUTION END

Question 2.3: Synonyms & Antonyms (2 points) [code + written]

When considering Cosine Similarity, it's often more convenient to think of Cosine Distance, which is simply 1 - Cosine Similarity.

Find three words (w_1, w_2, w_3) where w_1 and w_2 are synonyms and w_1 and w_3 are antonyms, but Cosine Distance (w_1, w_3) < Cosine Distance (w_1, w_2) .

As an example, w_1 ="happy" is closer to w_3 ="sad" than to w_2 ="cheerful". Please find a different example that satisfies the above. Once you have found your example, please give a possible explanation for why this counter-intuitive result may have happened.

You should use the the wv_from_bin.distance(w1, w2) function here in order to compute the cosine distance between two words. Please see the <u>GenSim documentation</u> (https://radimrehurek.com/gensim/models/keyedvectors.html#gensim.models.keyedvector for further assistance.

```
In []: ### SOLUTION BEGIN

w1 = "buy"
w2 = "purchase"
w3 = "sell"
w1_w2_dist = wv_from_bin.distance(w1, w2)
w1_w3_dist = wv_from_bin.distance(w1, w3)

print("Synonyms {}, {} have cosine distance: {}".format(w1, w2, w1_w2_dist))
print("Antonyms {}, {} have cosine distance: {}".format(w1, w3, w1_w3_dist))
### SOLUTION END
```

Synonyms buy, purchase have cosine distance: 0.18561452627182007 Antonyms buy, sell have cosine distance: 0.10369592905044556

SOLUTION BEGIN

becuase these 2 antonyms might have happened next to each other much more common than those 2 synonyms

SOLUTION END

Question 2.4: Analogies with Word Vectors [written] (1.5 points)

Word vectors have been shown to *sometimes* exhibit the ability to solve analogies.

As an example, for the analogy "man : grandfather :: woman : x" (read: man is to grandfather as woman is to x), what is x?

In the cell below, we show you how to use word vectors to find x using the <code>most_similar</code> function from the <code>GenSim documentation</code>

(https://radimrehurek.com/gensim/models/keyedvectors.html#gensim.models.keyedvector

The function finds words that are most similar to the words in the positive list and most dissimilar from the words in the negative list (while omitting the input words, which are often the most similar; see this://www.aclweb.org/anthology/N18-2039.pdf). The answer to the analogy will have the highest cosine similarity (largest returned numerical value).

```
→
```

Let m, g, w, and x denote the word vectors for man , grandfather , woman , and the answer, respectively. Using **only** vectors m, g, w, and the vector arithmetic operators + and - in your answer, to what expression are we maximizing x's cosine similarity?

Hint: Recall that word vectors are simply multi-dimensional vectors that represent a word. It might help to draw out a 2D example using arbitrary locations of each vector. Where would man and woman lie in the coordinate plane relative to grandfather and the answer?

SOLUTION BEGIN

g - m + w

SOLUTION END

Question 2.5: Finding Analogies [code + written] (1.5 points)

a. For the previous example, it's clear that "grandmother" completes the analogy. But give an intuitive explanation as to why the <code>most_similar</code> function gives us words like "granddaughter", "daughter", or "mother?

SOLUTION BEGIN

because those word vector are close to "grandmother" vector and when difference to "grandmother" is close hence distance to those word are roughly the same.

SOLUTION END

b. Find an example of analogy that holds according to these vectors (i.e. the intended word is ranked top). In your solution please state the full analogy in the form x:y :: a:b. If you believe the analogy is complicated, explain why the analogy holds in one or two sentences.

Note: You may have to try many analogies to find one that works!

```
In [ ]: ### SOLUTION BEGIN

x, y, a, b = "teacher" , "school", "professor", "university"
print(f"expected similar {b} ,the most similar predicted {wv_from_bin.most_sim assert wv_from_bin.most_similar(positive=[a, y], negative=[x])[0][0] == b

### SOLUTION END
```

expected similar university ,the most similar predicted university

SOLUTION BEGIN

SOLUTION END

Question 2.6: Incorrect Analogy [code + written] (1.5 points)

a. Below, we expect to see the intended analogy "hand : glove :: foot : **sock**", but we see an unexpected result instead. Give a potential reason as to why this particular analogy turned out the way it did?

SOLUTION BEGIN

it depends on both context and the co-occurence of words

SOLUTION END

b. Find another example of analogy that does *not* hold according to these vectors. In your solution, state the intended analogy in the form x:y :: a:b, and state the **incorrect** value of b according to the word vectors (in the previous example, this would be **'45,000-square'**).

```
In [ ]: ### SOLUTION BEGIN

x, y, a, b = "winter", "snowy", "summer", "sunny"
    pprint.pprint(wv_from_bin.most_similar(positive=[a, y], negative=[x]))

### SOLUTION END

[('icy', 0.5042672157287598),
    ('windy', 0.5003271698951721),
    ('chilly', 0.4808270037174225),
    ('mountains', 0.4792238473892212),
    ('foggy', 0.4760406017303467),
    ('frigid', 0.4677150249481201),
    ('sunny', 0.4671117663383484),
```

winter:snowy :: summer:sunny which doesn't hold

('rainy', 0.45712020993232727), ('hillside', 0.4396189749240875), ('picturesque', 0.4370409846305847)]

SOLUTION END

Question 2.7: Guided Analysis of Bias in Word Vectors [written] (1 point)

It's important to be cognizant of the biases (gender, race, sexual orientation etc.) implicit in our word embeddings. Bias can be dangerous because it can reinforce stereotypes through applications that employ these models.

Run the cell below, to examine (a) which terms are most similar to "woman" and "profession" and most dissimilar to "man", and (b) which terms are most similar to "man" and "profession" and most dissimilar to "woman". Point out the difference between the list of female-associated words and the list of male-associated words, and explain how it is reflecting gender bias.

```
In [ ]: # Run this cell
        # Here `positive` indicates the list of words to be similar to and `negative`
        # most dissimilar from.
        pprint.pprint(wv from bin.most similar(positive=['man', 'profession'], negative
        print()
        pprint.pprint(wv_from_bin.most_similar(positive=['woman', 'profession'], negat
        [('reputation', 0.5250176787376404),
         ('professions', 0.5178037881851196),
         ('skill', 0.49046966433525085),
         ('skills', 0.49005505442619324),
         ('ethic', 0.4897659420967102),
         ('business', 0.4875852167606354),
          ('respected', 0.485920250415802),
         ('practice', 0.482104629278183),
         ('regarded', 0.4778572618961334),
         ('life', 0.4760662019252777)]
        [('professions', 0.5957457423210144),
          ('practitioner', 0.49884122610092163),
         ('teaching', 0.48292139172554016),
         ('nursing', 0.48211804032325745),
         ('vocation', 0.4788965880870819),
         ('teacher', 0.47160351276397705),
         ('practicing', 0.46937814354896545),
         ('educator', 0.46524327993392944),
         ('physicians', 0.4628995358943939),
         ('professionals', 0.4601394236087799)]
```

in first list we see words such as bussiness which is more likely to be man's job but in second we can see nursing which happens for women more.

SOLUTION END

Question 2.8: Independent Analysis of Bias in Word Vectors [code + written] (1 point)

Use the <code>most_similar</code> function to find another pair of analogies that demonstrates some bias is exhibited by the vectors. Please briefly explain the example of bias that you discover.

```
In [ ]: ### SOLUTION BEGIN
        A = "sad"
        B = "happy"
        word = "rich"
        pprint.pprint(wv_from_bin.most_similar(positive=[A, word], negative=[B]))
        pprint.pprint(wv from bin.most similar(positive=[B, word], negative=[A]))
        ### SOLUTION END
        [('impoverished', 0.4315524995326996),
          ('vast', 0.42239266633987427),
         ('shaba', 0.41426998376846313),
          ('irony', 0.39768147468566895),
         ('bordering', 0.39472928643226624),
          ('fascinating', 0.38359835743904114),
         ('gedman', 0.3820772171020508),
          ('vivid', 0.3790566027164459),
         ('khuzestan', 0.37842991948127747),
         ('particularly', 0.37810227274894714)]
        [('wealthy', 0.5879704356193542),
          ('enjoy', 0.5397048592567444),
          ('free', 0.5100708603858948),
         ('always', 0.5020256638526917),
         ('good', 0.49898460507392883),
         ('wealth', 0.498134046792984),
          ('want', 0.4942720830440521),
```

('get', 0.48958635330200195), ('richer', 0.48772722482681274), ('enough', 0.4760766923427582)]

we'd expect that we get poor or impoverished which first is true but in the second one because should be negative of sad it gets wealthy

SOLUTION END

Question 2.9: Thinking About Bias [written] (2 points)

a. Give one explanation of how bias gets into the word vectors. Briefly describe a real-world example that demonstrates this source of bias.

SOLUTION BEGIN

becuase of the corpus which our model is trained, it sees words such as computer programmer more assigned to boys so our model decides to pick it as gender specific, which should be gender neutral. man:Computer programmer :: woman : homemaker

SOLUTION END

b. What is one method you can use to mitigate bias exhibited by word vectors? Briefly describe a real-world example that demonstrates this method.

SOLUTION BEGIN

for example for gender, we define bias direction such as "male - female" or "he - she" or "son - daughter" and then take those words which has been biased by gender and remove gender bias from their axis, such that their difference in gender bias get zero

SOLUTION END

Submission Instructions

- 1. Click the Save button at the top of the Jupyter Notebook.
- 2. Select Cell -> All Output -> Clear. This will clear all the outputs from all cells (but will keep the content of all cells).
- 3. Select Cell -> Run All. This will run all the cells in order, and will take several minutes.
- 4. Once you've rerun everything, select File -> Download as -> PDF via LaTeX (If you have trouble using "PDF via LaTex", you can also save the webpage as pdf. Make sure all your solutions especially the coding parts are displayed in the pdf, it's okay if the provided codes get cut off because lines are not wrapped in code cells).
- 5. Look at the PDF file and make sure all your solutions are there, displayed correctly. The PDF is the only thing your graders will see!
- 6. Submit your PDF on Gradescope.