References: Chapter 17 of Geron's book. For 1-Dim plots, Keras tutorial:

## https://www.tensorflow.org/tutorials/generative/autoencoder

This file trains a VAE with the instances of the normal ECGs in the training data. Then, it measures the reconstruction loss for the ECGs in the test data. The reconstruction loss for the instances of the abnormal ECGs in the test data is higher. A threshold is determined based on the distribution of the reconstruction losses of the normal training data (threshold = mean + 2.5\*std of this distribution). Then, if the reconstruction loss of a ECG in the test data is higher than this threshold, it is classified as abnormal. By comparing with the known labels of test data (with T for normal ECG(s) and F for abnormal ECG(s)), the confusion matrix and the accuracy is calculated.

## Import the necessary libraries:

```
import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
import tensorflow as tf
from tensorflow import keras

from sklearn.metrics import accuracy_score, precision_score, recall_score, confusion_r
from sklearn.model_selection import train_test_split
from keras import layers, losses
from keras.models import Model
```

## Loading the ECG5000 data:

```
# Download the dataset
dataframe = pd.read_csv('http://storage.googleapis.com/download.tensorflow.org/data/ec
raw_data = dataframe.values
dataframe.head()
```

Parse the data so it can be split creating a variable containing the labels and another containing the data. Splitting the data into train, validation, and test set.

```
# The last element contains the labels
labels = raw_data[:, -1]

# The other data points are the electrocadriogram data
data = raw_data[:, 0:-1]

train_data, test_data, train_labels, test_labels = train_test_split(
    data, labels, test_size=0.2, random_state=21
)

train_data, valid_data, train_labels, valid_labels = train_test_split(
    train_data, train_labels, test_size=.1, random_state=21
)
```

Normalize the data so the features are treated equally, normalizing using the overall min and max value of all training data (train/validation set).

```
min_val = tf.reduce_min(tf.concat([train_data, valid_data], 0))
max_val = tf.reduce_max(tf.concat([train_data, valid_data], 0))

train_data = (train_data - min_val) / (max_val - min_val)
valid_data = (valid_data - min_val) / (max_val - min_val)
test_data = (test_data - min_val) / (max_val - min_val)

train_data = tf.cast(train_data, tf.float32)
valid_data = tf.cast(valid_data, tf.float32)
test_data = tf.cast(test_data, tf.float32)
```

The autoencoder is trained using only the normal rhythms, which are labeled in this dataset as 1. Here the normal rhythms is separated from the abnormal rhythms, and the labels are casted as type bool.

```
train_labels = train_labels.astype(bool)
valid_labels = valid_labels.astype(bool)
test_labels = test_labels.astype(bool)

normal_train_data = train_data[train_labels]
normal_valid_data = valid_data[valid_labels]
normal_test_data = test_data[test_labels]
```

```
anomalous_train_data = train_data[~train_labels]
anomalous_valid_data = valid_data[~valid_labels]
anomalous_test_data = test_data[~test_labels]
```

Initialize K with the Keras backend to utilize it's methods in the Sampling function.

```
K = keras.backend
```

This Sampling layer takes two inputs: mean ( $\mu$ ) and log\_var ( $\gamma$ ). It uses the function K.random\_normal() to sample a random vector (of the same shape as  $\gamma$ ) from the Normal distribution, with mean 0 and standard deviation 1. Then it multiplies it by  $\exp(\gamma/2)$  (which is equal to  $\sigma$ , as you can verify), and finally it adds  $\mu$  and returns the result. This samples a codings vector from the Normal distribution with mean  $\mu$  and standard deviation  $\sigma$ .

```
# For details please see Geron's book. Uses the reparametrization trick to d
# sampling from the MVN distribution, while allowing the 2 parallel layers c
# means and stds of the MVN distribution for each dimension to be trained vi
# backpropogation of the error signal.
class Sampling(keras.layers.Layer):
    def call(self, inputs):
        mean, log_var = inputs
        return K.random_normal(tf.shape(log_var)) * K.exp(log_var / 2) + mea
```

Create the encoder, using the Functional API because the model is not entirely sequential:

```
# For details please see Geron's book.
codings_size = 8  # The number of dimensions of the MVN distribution in the sampling
inputs = keras.layers.Input(shape=(normal_train_data.shape[1]))
z = keras.layers.Dense(32, activation="selu")(inputs)
z = keras.layers.Dense(16, activation="selu")(z)
z = keras.layers.Dense(codings_size, activation="selu")(z)

# Parallel layers at the end of the encoder for means
# and standard deviations of the Multivariate Normal (MVN) distribution
# in the dimensions of the coding size (here 8).
codings_mean = keras.layers.Dense(codings_size)(z)
codings_log_var = keras.layers.Dense(codings_size)(z)

# Sampling layer at the end of the encoder
codings = Sampling()([codings_mean, codings_log_var])
variational_encoder = keras.models.Model(
    inputs=[inputs], outputs=[codings_mean, codings_log_var, codings])
```

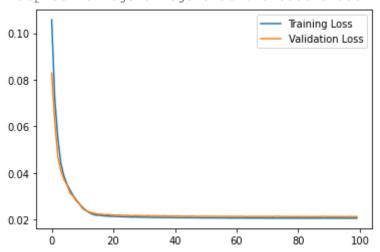
```
decoder inputs = keras.layers.Input(shape=[codings size])
x = keras.layers.Dense(16, activation="selu")(decoder inputs)
x = keras.layers.Dense(32, activation="selu")(x)
outputs = keras.layers.Dense(normal train data.shape[1], activation="sigmoid")(x)
variational_decoder = keras.models.Model(inputs=[decoder_inputs], outputs=[outputs])
_, _, codings = variational_encoder(inputs)
reconstructions = variational_decoder(codings)
variational ae = keras.models.Model(inputs=[inputs], outputs=[reconstructions])
# The latent loss function
latent_loss = -0.5 * K.sum(
  1 + codings log var - K.exp(codings log var) - K.square(codings mean),
  axis=-1)
# Add the latent loss to the reconstruction loss
variational ae.add loss(K.mean(latent loss) / 140.)
# For the reconstruction loss binary cross-entropy loss is used.
# For details please see Chapter 17 of Geron's book (Stacked AE and VAE sections)
variational ae.compile(loss="mae", optimizer="adam")
history = variational ae.fit(normal train data, normal train data, epochs=100, batch &
               validation data=(normal valid data, normal valid data), s
  Phocii /7/Inn
  Epoch 73/100
  Epoch 74/100
  Epoch 75/100
  Epoch 76/100
  Epoch 77/100
  Epoch 78/100
  Epoch 79/100
  Epoch 80/100
  Epoch 81/100
  Epoch 82/100
  Epoch 83/100
  Epoch 84/100
  Epoch 85/100
  Epoch 86/100
```

```
Epoch 87/100
Epoch 88/100
Epoch 89/100
Epoch 90/100
Epoch 91/100
Epoch 92/100
Epoch 93/100
Epoch 94/100
Epoch 95/100
Epoch 96/100
Epoch 97/100
Epoch 98/100
Epoch 99/100
Epoch 100/100
           val loss:
```

Plotting the training and validation loss for each epoch of training:

```
plt.plot(history.history["loss"], label="Training Loss")
plt.plot(history.history["val_loss"], label="Validation Loss")
plt.legend()
```

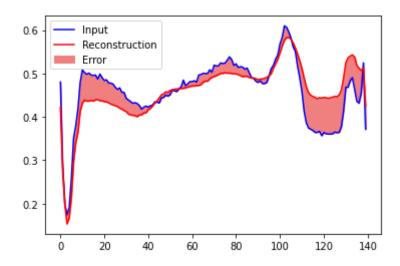




Plotting a normal ECG from the training set, the reconstruction after it's encoded and decoded by the autoencoder, and the reconstruction error.

```
_, _, codings = variational_encoder(normal_test_data)
decoded_imgs = variational_decoder(codings)

plt.plot(normal_test_data[0],'b')
plt.plot(decoded_imgs[0],'r')
plt.fill_between(np.arange(140), decoded_imgs[0], normal_test_data[0], color='lightcomplt.legend(labels=["Input", "Reconstruction", "Error"])
plt.show()
```



Now, we will do the same for the anomalous data:

```
_, _, codings = variational_encoder(anomalous_test_data)
decoded_imgs = variational_decoder(codings)

plt.plot(normal_test_data[0],'b')
plt.plot(decoded_imgs[0],'r')
plt.fill_between(np.arange(140), decoded_imgs[0], normal_test_data[0], color='lightcomplt.legend(labels=["Input", "Reconstruction", "Error"])
plt.show()
```



Here will compute the normal/abnormal train/validation loss from the model using mean absolute error.

```
# Normal reconstructions
reconstructions_train = variational_ae.predict(normal_train_data)
train_loss = tf.keras.losses.mae(reconstructions_train, normal_train_data)
reconstructions_valid = variational_ae.predict(normal_valid_data)
valid_loss = tf.keras.losses.mae(reconstructions_valid, normal_valid_data)
# Abnormal reconstructions
ab_reconstructions_train = variational_ae.predict(anomalous_train_data)
ab_train_loss = tf.keras.losses.mae(ab_reconstructions_train, anomalous_train_data)
ab_reconstructions_valid = variational_ae.predict(anomalous_valid_data)
ab_valid_loss = tf.keras.losses.mae(ab_reconstructions_valid, anomalous_valid_data)
```

Defining a function predict which takes the model, data, and threshold. Computes the reconstruction loss and returns the truthy value for all elements if they are less than the threshold (True).

```
def predict(model, data, threshold):
    reconstructions = model.predict(data)
    loss = tf.keras.losses.mae(reconstructions, data)
    return tf.math.less(loss, threshold)
```

Computing the abnormal/normal mean of the validation loss

```
abnormal_valid_mean_loss = np.mean(ab_valid_loss)
normal valid mean loss = np.mean(valid loss)
```

Computing 100 different thresholds that start at the normal threshold and end at the abnormal threshold incrementing by their difference divided by 100.

```
increment = (abnormal_valid_mean_loss - normal_valid_mean_loss)/100
thresholds = np.arange(normal_valid_mean_loss, abnormal_valid_mean_loss,
increment)
```

Creating a numpy array to store the accuracy for each of the different threshold values.

```
thresh size = thresholds.shape[0]
```

```
accuracies = np.zeros(thresh_size)
```

Calculation of the threshold that gives the best accuracy on the validation data. This is done by going through all thresholds and testing the accuracy of the model with each threshold.

```
for i in range(thresh_size):
   preds = predict(variational_ae, valid_data, thresholds[i])
   accuracies[i] = accuracy_score(preds, valid_labels)
```

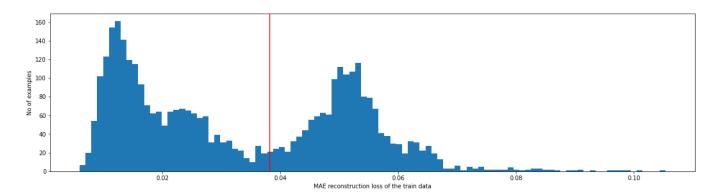
Setting the threshold to the one in thresholds which gave the best accuracy.

```
argmax = np.argmax(accuracies)
best_threshold = thresholds[argmax]
print("The best threshold based on validation data: ", best_threshold)
The best threshold based on validation data: 0.03820322118699557
```

We now detect anomalies by calculating whether the reconstruction loss is greater than a fixed threshold we just computed. We then will classify future examples as anomalous if the reconstruction error is higher than this threshold.

Plotting the reconstruction error on all ECGs from the training set

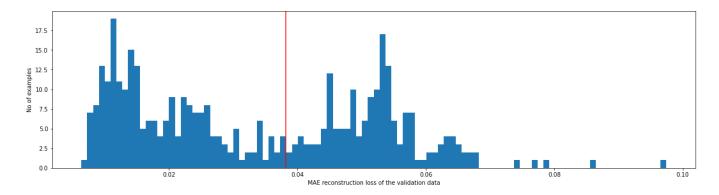
```
reconstructions = variational_ae.predict(train_data)
train_loss = tf.keras.losses.mae(reconstructions, train_data)
plt.figure(figsize=(20,5))
plt.hist(train_loss[None,:], bins=100)
plt.axvline(best_threshold, c='r')
plt.xlabel("MAE reconstruction loss of the train data")
plt.ylabel("No of examples")
plt.show()
```



Plotting the reconstruction error on all ECGs from the validation set

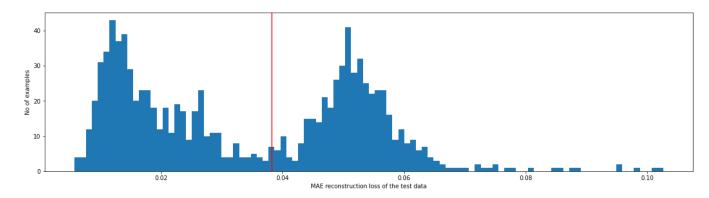
```
reconstructions = variational ae.predict(valid data)
```

```
valid_loss = tf.keras.losses.mae(reconstructions, valid_data)
plt.figure(figsize=(20,5))
plt.hist(valid_loss[None,:], bins=100)
plt.axvline(best_threshold, c='r')
plt.xlabel("MAE reconstruction loss of the validation data")
plt.ylabel("No of examples")
plt.show()
```



Plotting the reconstruction error on all ECGs from the test set

```
reconstructions = variational_ae.predict(test_data)
test_loss = tf.keras.losses.mae(reconstructions, test_data)
plt.figure(figsize=(20,5))
plt.hist(test_loss[None,:], bins=100)
plt.axvline(best_threshold, c='r')
plt.xlabel("MAE reconstruction loss of the test data")
plt.ylabel("No of examples")
plt.show()
```



Classify an ECG as an anomaly if the reconstruction error is greater than the threshold.

```
print("Accuracy = {}".format(accuracy score(labels, predictions)))
  reconstructions = model.predict(data[labels])
  nl test loss = tf.keras.losses.mae(reconstructions, data[labels])
  print("Normal Test Data Mean = {}".format(np.mean(nl test loss)))
  print("Normal Test Data Standard Deviation = {}".format(np.std(nl test loss)))
  reconstructions = model.predict(data[~labels])
  ab test loss = tf.keras.losses.mae(reconstructions, data[~labels])
  print("Abnormal Test Data Mean = {}".format(np.mean(ab_test_loss)))
  print("Abnormal Test Data Standard Deviation = {}".format(np.std(ab test loss)))
  print("Precision = {}".format(precision score(labels, predictions)))
  print("Recall = {}".format(recall score(labels, predictions)))
thr_acc = np.zeros((thresh_size, 2))
thr acc[:, 0] = thresholds
thr_acc[:, 1] = accuracies
thr acc[argmax - 2 : argmax + 3]
    array([[0.03758542, 0.9425
           [0.03789432, 0.9425
           [0.03820322, 0.95
           [0.03851212, 0.9475
                                  1,
           [0.03882102, 0.945
                                  11)
```

Calculation of the accuracy and the confusion matrix on the test data with threshold set based on the best threshold from the validation data

```
preds = predict(variational ae, test data, best threshold)
   print stats(preds, test labels, variational ae, test data)
        Confusion Matrix:
         prediction: F
                            Т
                     464 536
         label: F [[428 12]
                                    440
                    [36 524]]
                T
                                    560
        Accuracy = 0.952
        Normal Test Data Mean = 0.02027870900928974
        Normal Test Data Standard Deviation = 0.012544086202979088
        Abnormal Test Data Mean = 0.052306048572063446
        Abnormal Test Data Standard Deviation = 0.008525446988642216
        Precision = 0.9776119402985075
        Recall = 0.9357142857142857
   accuracy = (
       0.954 +
       0.952 +
       0.954 +
       0.954 +
       0.948 +
       0.955 +
       0.954 +
https://colab.research.google.com/drive/1uTvx_IVJpePQj9YBu0Qm-Jpe4qtQLLod#scrollTo=nwPtKjTHRG16
```

```
4/22/22, 1:54 PM
       0.952 +
   )/10.
   round(accuracy, 4)
          File "<ipython-input-25-02e3bb550434>", line 10
            )/10.
        SyntaxError: invalid syntax
         SEARCH STACK OVERFLOW
   norm mean = (
       0.020278330892324448 +
       0.02027731202542782 +
       0.02030421979725361 +
       0.020278800278902054 +
       0.0202984306961298 +
       0.020255139097571373 +
       0.02027713507413864 +
       0.02031519077718258 +
   )/10.
   round(norm mean, 4)
   norm sd = (
       0.012550999410450459 +
       0.012557352893054485 +
       0.012660929933190346 +
       0.01253422163426876 +
       0.01246469933539629 +
       0.012553111650049686 +
       0.012428902089595795 +
       0.012432349845767021 +
   )/10.
   round(norm sd, 4)
   ab mean = (
       0.052440300583839417 +
       0.052289411425590515 +
       0.05262962356209755 +
       0.05265740305185318 +
       0.05234095826745033 +
       0.05265644192695618 +
       0.052321240305900574 +
       0.052184123545885086 +
   )/10.
   round(ab mean, 4)
   ab sd = (
       0.008512615226209164 +
```

```
0.008569230325520039 +
0.008615327067673206 +
0.008519774302840233 +
0.008518102578818798 +
0.008527365513145924 +
0.008446901105344296 +
0.008458820171654224 +
)/10.
round(ab_sd, 4)
```

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