References: Chapter 17 of Geron's book. For 1-Dim plots, Keras tutorial:

https://www.tensorflow.org/tutorials/generative/autoencoder

This file trains a VAE with the instances of the normal digits in the training data.

Then, it measures the reconstruction loss for the digits in the test data.

The reconstruction loss for the instances of the abnormal digits in the test data is higher.

A threshold is determined based on the distribution of the reconstruction losses of the normal training data (threshold = mean + 2.5\*std of this distribution).

Then, if the reconstruction loss of a digit in the test data is higher than this threshold, it is classified as abnormal.

By comparing with the known labels of test data (with T for normal digit(s) and F for abnormal digit(s)), the confusion matrix and the accuracy is calculated.

```
import sklearn
import tensorflow as tf
from tensorflow import keras
import numpy as np

import matplotlib as mpl
import matplotlib.pyplot as plt
mpl.rc('axes', labelsize=14)
mpl.rc('xtick', labelsize=12)
mpl.rc('ytick', labelsize=12)

from sklearn.metrics import accuracy_score, precision_score, recall_score, confusion_matrix
from sklearn.model_selection import train_test_split
```

# Loading the MNIST data and forming arrays of the normal training data, the validation data (normal and abnormal) and the test data (normal and abnormal)

```
# 0 T-shirt/top
# 1 Trouser
# 2 Pullover
# 3 Dress
# 4 Coat
# 5 Sandal
# 6 Shirt
# 7 Sneaker
# 8 Bag
# 9 Ankle boot

nl1 = 9
nl2 = 9
abn1 - 3
```

#Labels

```
abn2 = 3
(x_train_0, y_train_0), (x_test, y_test) = keras.datasets.fashion_mnist.load_data()
x_train_0 = x_train_0.astype(np.float32) / 255
x_{test} = x_{test.astype}(np.float32) / 255
train_size = x_{train_0.shape[0]} * 9 // 10
x_train, x_valid, y_train, y_valid = train_test_split(x_train_0, y_train_0, train_size = train_size)
normal_data = x_train[(y_train == nl1) | (y_train == nl2)]
                                                                  # Normal training data (Normal digits
normal_labels = y_train[(y_train == nl1) | (y_train == nl2)]
valid_data = x_valid[(y_valid == abn1) | (y_valid == abn2) | (y_valid == nl1) | (y_valid == nl2)]
valid_labels = y_valid[(y_valid == abn1) | (y_valid == abn2) | (y_valid == nl1) | (y_valid == nl2)]
test_data = x_test[(y_test == abn1) | (y_test == abn2) | (y_test == nl1) | (y_test == nl2)]
                                                                                                # Test d
test_labels = y_test[(y_test == abn1) | (y_test == abn2) | (y_test == nl1) | (y_test == nl2)]
test_labels_T_F = np.where((test_labels == nl1) | (test_labels == nl2), True, False)
# Array of T and F, T where test digits are normal and F where test digits are abnormal
valid_labels_T_F = np.where((valid_labels == nl1) | (valid_labels == nl2), True, False)
# Array of T and F, T where test digits are normal and F where test digits are abnormal
normal_data.shape, normal_labels.shape, valid_data.shape, valid_labels.shape, test_data.shape, test_lab
     ((5413, 28, 28), (5413,), (1165, 28, 28), (1165,), (2000, 28, 28), (2000,))
normal_test_data = test_data[(test_labels == nl1) | (test_labels == nl2)]
                                                                                      # The normal digit
abnormal_test_data = test_data[(test_labels == abn1) | (test_labels == abn2)]
                                                                                      # The abnormal dig
normal_test_labels = test_labels[(test_labels == nl1) | (test_labels == nl2)]
                                                                                     # Their labels
abnormal_test_labels = test_labels[(test_labels == abn1) | (test_labels == abn2)]
                                                                                     # Their labels
normal_test_data.shape, abnormal_test_data.shape
     ((1000, 28, 28), (1000, 28, 28))
normal_valid_data = valid_data[(valid_labels == nl1) | (valid_labels == nl2)]
                                                                                          # The normal d
abnormal_valid_data = valid_data[(valid_labels == abn1) | (valid_labels == abn2)]
                                                                                          # The abnormal
normal_valid_labels = valid_labels[(valid_labels == nl1) | (valid_labels == nl2)]
                                                                                          # Their labels
                                                                                          # Their labels
abnormal_valid_labels = valid_labels[(valid_labels == abn1) | (valid_labels == abn1)]
normal_valid_data.shape, abnormal_valid_data.shape
     ((587, 28, 28), (578, 28, 28))
```

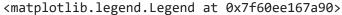
# Building and training the network

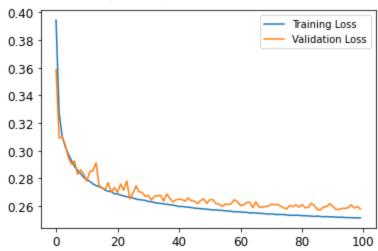
```
K = keras.backend
# def rounded_accuracy(y_true, y_pred):
  # return keras.metrics.binary_accuracy(tf.round(y_true), tf.round(y_pred))
# For details please see Geron's book. Uses the reparametrization trick to do stochastic
# sampling from the MVN distribution, while allowing the 2 parallel layers containing the
# means and stds of the MVN distribution for each dimension to be trained via
# backpropogation of the error signal.
class Sampling(keras.layers.Layer):
    def call(self, inputs):
        mean, log_var = inputs
        return K.random_normal(tf.shape(log_var)) * K.exp(log_var / 2) + mean
# For details please see Geron's book.
codings_size = 16  # The number of dimensions of the MVN distribution in the sampling layer
inputs = keras.layers.Input(shape=[28, 28])
z = keras.layers.Flatten()(inputs)
z = keras.layers.Dense(256, activation="selu")(z)
z = keras.layers.Dense(128, activation="selu")(z)
z = keras.layers.Dense(64, activation="selu")(z)
# Parallel layers at the end of the encoder for means
# and standard deviations of the Multivariate Normal (MVN) distribution
# in the dimensions of the coding size (here 32).
codings_mean = keras.layers.Dense(codings_size)(z)
codings_log_var = keras.layers.Dense(codings_size)(z)
# Sampling layer at the end of the encoder
codings = Sampling()([codings_mean, codings_log_var])
variational_encoder = keras.models.Model(
    inputs=[inputs], outputs=[codings_mean, codings_log_var, codings])
decoder_inputs = keras.layers.Input(shape=[codings_size])
x = keras.layers.Dense(64, activation="selu")(decoder_inputs)
x = keras.layers.Dense(128, activation="selu")(x)
x = keras.layers.Dense(256, activation="selu")(x)
x = keras.layers.Dense(28 * 28, activation="sigmoid")(x)
outputs = keras.layers.Reshape([28, 28])(x)
variational_decoder = keras.models.Model(inputs=[decoder_inputs], outputs=[outputs])
_, _, codings = variational_encoder(inputs)
reconstructions = variational_decoder(codings)
variational_ae = keras.models.Model(inputs=[inputs], outputs=[reconstructions])
# The latent loss function
\# latent loss = -0.5 * K.sum(
     1 + codings_log_var - K.exp(codings_log_var) - K.square(codings_mean),
#
     axis=-1)
# Add the latent loss to the reconstruction loss
# variational_ae.add_loss(K.mean(latent_loss) / 784.)
```

```
# For details please see Chapter 17 of Geron's book (Stacked AE and VAE sections)
variational_ae.compile(loss="binary_crossentropy", optimizer="rmsprop")
checkpoint_cb = keras.callbacks.ModelCheckpoint("wo_latent_VAE_model", monitor="val_loss", save_best_on
history = variational_ae.fit(normal_data, normal_data, epochs=100, batch_size=128, callbacks=[checkpoin
             validation_data=(normal_valid_data, normal_valid_data), shuffle=True)
  Epoch 73/100
  Epoch 74/100
  Epoch 75/100
  33/43 [==============>.....] - ETA: 0s - loss: 0.2536INFO:tensorflow:Assets written t
  Epoch 76/100
  33/43 [============>:.....] - ETA: 0s - loss: 0.2537INFO:tensorflow:Assets written t
  Epoch 77/100
  43/43 [================ ] - 0s 6ms/step - loss: 0.2534 - val_loss: 0.2603
  Epoch 78/100
  43/43 [=============== ] - 0s 6ms/step - loss: 0.2533 - val_loss: 0.2595
  Epoch 79/100
  43/43 [=============== ] - 0s 6ms/step - loss: 0.2533 - val_loss: 0.2609
  Epoch 80/100
  Epoch 81/100
  Epoch 82/100
  Epoch 83/100
  Epoch 84/100
  Epoch 85/100
  43/43 [=============== ] - 0s 6ms/step - loss: 0.2525 - val_loss: 0.2605
  Epoch 86/100
  Epoch 87/100
  33/43 [=============>.....] - ETA: 0s - loss: 0.2524INFO:tensorflow:Assets written t
  Epoch 88/100
  Epoch 89/100
  43/43 [=============== ] - 0s 5ms/step - loss: 0.2524 - val_loss: 0.2597
  Epoch 90/100
  Epoch 91/100
  43/43 [================ ] - 0s 7ms/step - loss: 0.2522 - val_loss: 0.2598
  Epoch 92/100
  Epoch 93/100
  Epoch 94/100
  Epoch 95/100
```

# For the reconstruction loss binary cross-entropy loss is used.

```
plt.plot(history.history["loss"], label="Training Loss")
plt.plot(history.history["val_loss"], label="Validation Loss")
plt.legend()
```





model = variational\_ae
model.summary(expand\_nested=True, show\_trainable=True)

Model: "model\_5"

Layer (type)	Output Shape	Param #	Trainable
input_3 (InputLayer)	[(None, 28, 28)]	0	Υ
model_3 (Functional)	[(None, 16), (None, 16), (None, 16)]	244192	Υ
   input_3 (InputLayer)	[(None, 28, 28)]	0	Υ
   flatten_1 (Flatten)	(None, 784)	0	Υ
dense_9 (Dense)	(None, 256)	200960	Υ
dense_10 (Dense)	(None, 128)	32896	Υ
dense_11 (Dense)	(None, 64)	8256	Υ
dense_12 (Dense)	(None, 16)	1040	Υ
dense_13 (Dense)	(None, 16)	1040	Υ
   sampling_1 (Sampling)	(None, 16)	0	Υ

```
model_4 (Functional)
                      (None, 28, 28)
                                           243920
input_4 (InputLayer) [(None, 16)]
                                                 Υ
dense_14 (Dense)
               (None, 64)
                                          1088 Y
dense_15 (Dense)
                    (None, 128)
                                          8320 Y
               (None, 256)
                                          33024 Y
dense 16 (Dense)
dense_17 (Dense)
                    (None, 784)
                                          201488
reshape_1 (Reshape) (None, 28, 28)
```

-----

Total params: 488,112 Trainable params: 488,112 Non-trainable params: 0

\_\_\_\_\_

```
model_encoder = variational_encoder
# model_encoder.summary(expand_nested=True, show_trainable=True)

model_decoder = variational_decoder
# model_decoder.summary(expand_nested=True, show_trainable=True)

model_layers = np.array(model.layers)
n_layers = model_layers.shape[0]
# np.concatenate((np.arange(n_layers).reshape(n_layers,1), model_layers.reshape(n_layers,1)), axis = 1)
```

# The original and reconstructed images for the first 30 instances of the normal training data, validation data, normal validation data, abnormal validation data, test data,

# normal test data, and abnormal test data

```
def plot_image(image):
    plt.imshow(image, cmap="binary")
    plt.axis("off")

def show_reconstructions(model, images, n_images=5):
    reconstructions = model.predict(images[:n_images])
    fig = plt.figure(figsize=(n_images * 1.5, 3))
    for image_index in range(n_images):
        plt.subplot(2, n_images, 1 + image_index)
        plot_image(images[image_index])
        plt.subplot(2, n_images, 1 + n_images + image_index)
        plot_image(reconstructions[image_index])

show_reconstructions(variational_ae, normal_data, 30)
plt.show()
```



show\_reconstructions(variational\_ae, valid\_data, 30)
plt.show()



show\_reconstructions(variational\_ae, normal\_valid\_data, 30)
plt.show()



show\_reconstructions(variational\_ae, abnormal\_valid\_data, 30)
plt.show()



show\_reconstructions(variational\_ae, test\_data, 30)
plt.show()





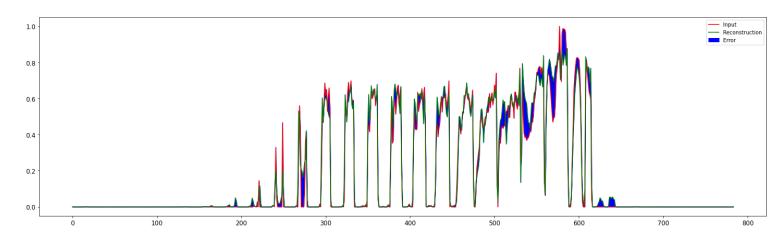
```
show_reconstructions(variational_ae, abnormal_test_data, 30)
plt.show()
```



# 1-Dim plot of pixels of the first normal test data

```
reconstructions_nl_test = variational_ae.predict(normal_test_data)
```

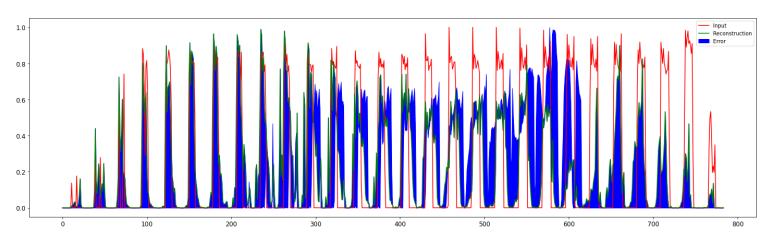
```
plt.figure(figsize=(25,7))
plt.plot(normal_test_data[0].ravel(), 'r')
plt.plot(reconstructions_nl_test[0].ravel(), 'g')
plt.fill_between(np.arange(28*28), reconstructions_nl_test[0].ravel(), normal_test_data[0].ravel(), col
plt.legend(labels=["Input", "Reconstruction", "Error"])
plt.show()
```



#### 1-Dim plot of pixels of the first abnormal test data

```
reconstructions_abn_test = variational_ae.predict(abnormal_test_data)

plt.figure(figsize=(25,7))
plt.plot(abnormal_test_data[0].ravel(), 'r')
plt.plot(reconstructions_abn_test[0].ravel(), 'g')
plt.fill_between(np.arange(28*28), reconstructions_abn_test[0].ravel(), normal_test_data[0].ravel(), coplt.legend(labels=["Input", "Reconstruction", "Error"])
plt.show()
```



### **▼** Distributions of the reconstruction losses and the calculation of the threshold.

#### Distribution of the reconstruction losses of the normal training data

```
reconstructions = variational_ae.predict(normal_data)
train_loss = tf.keras.losses.mae(reconstructions.reshape(-1, 784), normal_data.reshape(-1, 784))
plt.figure(figsize=(10,5))
plt.hist(train_loss[None,:], bins=100)
threshold1 = np.mean(train_loss) + 2.5*np.std(train_loss)
plt.axvline(threshold1,c='g')
plt.xlabel("MAE reconstruction loss of the normal training data")
plt.ylabel("No of examples")
plt.show()
```

```
200 -

175 -

150 -

100 -

50 -

25 -
```

```
print("Mean: ", np.mean(train_loss))
print("Std: ", np.std(train_loss))
```

Mean: 0.04907883 Std: 0.015340656

plt.show()

```
threshold_train_mean_2_5_std = np.mean(train_loss) + 2.5*np.std(train_loss) print("Threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based on the mean of the mean of the training data MAE reconstruction losses + 2.5 std: ", threshold based data MAE reconstruction data MA
```

Threshold based on the mean of the training data MAE reconstruction losses + 2.5 std: 0.087430469

threshold1 = threshold\_train\_mean\_2\_5\_std

#### Distribution of the reconstruction losses of the abnormal validation data

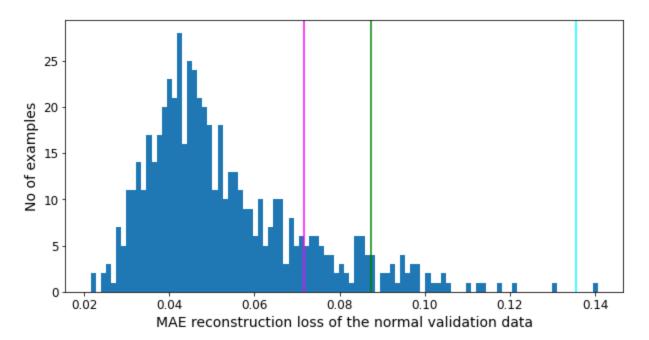
```
reconstructions = variational_ae.predict(abnormal_valid_data)
abn_valid_loss = tf.keras.losses.mae(reconstructions.reshape(-1,784), abnormal_valid_data.reshape(-1,784)
plt.figure(figsize=(10,5))
plt.hist(abn_valid_loss[None, :], bins=100)
threshold2 = np.mean(abn_valid_loss) - np.std(abn_valid_loss)
plt.axvline(threshold2,c='cyan')
plt.axvline(threshold1,c='g')
plt.xlabel("MAE reconstruction loss of the abnormal validation data")
plt.ylabel("No of examples")
```

```
20.0 - 17.5 - 15.0 - 12.5 - 15.0 - 12.5 - 12.5 - 15.0 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12.5 - 12
```

Threshold2: 0.13540947

#### Distribution of the reconstruction losses of the normal validation data

```
reconstructions = variational_ae.predict(normal_valid_data)
nl_valid_loss = tf.keras.losses.mae(reconstructions.reshape(-1,784), normal_valid_data.reshape(-1,784))
plt.figure(figsize=(10,5))
plt.hist(nl_valid_loss[None, :], bins=100)
threshold3 = np.mean(nl_valid_loss) + np.std(nl_valid_loss)
plt.axvline(threshold3, c='magenta')
plt.axvline(threshold2, c='cyan')
plt.axvline(threshold1, c='g')
plt.xlabel("MAE reconstruction loss of the normal validation data")
plt.ylabel("No of examples")
plt.show()
```



```
normal_valid_mean_loss , np.std(nl_valid_loss)
            (0.052981365, 0.018733146)

threshold3 = normal_valid_mean_loss + np.std(nl_valid_loss)
print("Threshold3: ", threshold3)

Threshold3: 0.07171451
```

Calculation of a preliminary threshold based on (threshold2 + threshold3) / 2 = Average of (mean + std of the distribution of the reconstruction losses of the normal validation data) and (mean - std of the distribution of the reconstruction losses of the abnormal validation data)

```
Avg_of_threshold_2_3 = (threshold2 + threshold3)/2
print("Average of threshold 2 and 3: ", Avg_of_threshold_2_3)
    Average of threshold 2 and 3: 0.10356199741363525
threshold4 = Avg_of_threshold_2_3
```

Calculation of the threshold that gives the best accuracy on the validation data and set this as the threshold.

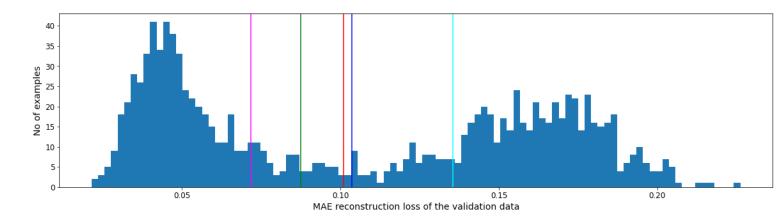
```
def predict(model, data, threshold):
 reconstructions = model.predict(data)
 loss = tf.keras.losses.mae(reconstructions.reshape(-1, 784), data.reshape(-1, 784))
 return tf.math.less(loss, threshold)
increment = (abnormal_valid_mean_loss- normal_valid_mean_loss)/100
thresholds = np.arange(normal_valid_mean_loss, abnormal_valid_mean_loss, increment)
thrs_size = thresholds.shape[0]
accuracies = np.zeros(thrs_size)
for i in range(thrs_size):
 preds = predict(variational_ae, valid_data, thresholds[i])
 accuracies[i] = accuracy_score(preds, valid_labels_T_F)
argmax = np.argmax(accuracies)
valid_data_best_threshold = thresholds[argmax]
print("The best threshold based on validation data: ", valid_data_best_threshold)
     The best threshold based on validation data: 0.10092985481023803
thr_acc = np.zeros((thrs_size, 2))
thr_acc[:, 0] = thresholds
thr_acc[:, 1] = accuracies
thr_acc[argmax-2:argmax+3]
```

# Distribution of the reconstruction losses of all the validation data (normal and abnormal)

The blue line is threshold4 (= the average of threshold3 [magenta] and threshold2 [cyan]).

The red line is the threshold that gives the best accuracy for the validation data.

```
reconstructions = variational_ae.predict(valid_data)
valid_loss = tf.keras.losses.mae(reconstructions.reshape(-1,784), valid_data.reshape(-1,784))
plt.figure(figsize=(20,5))
plt.hist(valid_loss[None, :], bins=100)
plt.axvline(threshold, c='r')
plt.axvline(threshold4, c='b')
plt.axvline(threshold2, c='cyan')
plt.axvline(threshold3, c='magenta')
plt.axvline(threshold1, c='green')
plt.xlabel("MAE reconstruction loss of the validation data")
plt.ylabel("No of examples")
plt.show()
```

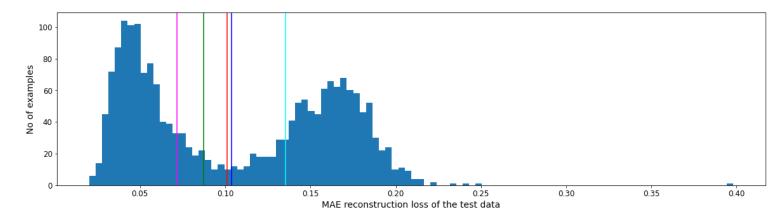


▼ Distribution of the reconstruction losses of the test data (normal and abnormal)

The blue line is threshold4 (= the average of threshold3 [magenta] and threshold2 [cyan]).

The red line is the threshold that gives the best accuracy for the validation data.

```
reconstructions = variational_ae.predict(test_data)
test_loss = tf.keras.losses.mae(reconstructions.reshape(-1,784), test_data.reshape(-1,784))
plt.figure(figsize=(20,5))
plt.hist(test_loss[None, :], bins=100)
plt.axvline(threshold, c='r')
plt.axvline(threshold4, c='b')
plt.axvline(threshold2, c='cyan')
plt.axvline(threshold3, c='magenta')
plt.axvline(threshold1, c='green')
plt.xlabel("MAE reconstruction loss of the test data")
plt.ylabel("No of examples")
plt.show()
```



### Mean and standard deviation of reconstruction losses for normal and abnormal test data

Calculation of the accuracy and the confusion matrix on the test data with threshold set based on the best threshold from the validation data

```
# def predict(model, data, threshold):
# reconstructions = model.predict(data)
# loss = tf.keras.losses.mae(reconstructions.reshape(-1, 784), data.reshape(-1, 784))
# return tf.math.less(loss, threshold)
def print_stats(predictions, labels):
  cf = confusion_matrix(labels, predictions)
  print("Confusion Matrix: \n prediction: F
                      {} \{\}\".format(\text{preds}[\text{preds} == False].\text{shape}[0], \text{preds}[\text{preds} == True].\text{shape}[0]))
  print("
  print(" label: F
                     [[{}
                                    {}".format(cf[0,0], cf[0,1], test_labels_T_F[test_labels_T_F == Fals
                            {}]
  print("
                 Т
                      [{}
                            {}]]
                                    {}".format(cf[1,0], cf[1,1], test_labels_T_F[test_labels_T_F == True
  print("Accuracy = {}".format(accuracy_score(labels, predictions)))
  print("Normal Test Data Mean = {}".format(np.mean(nl_test_loss)))
  print("Normal Test Data Standard Deviation = {}".format(np.std(nl_test_loss)))
  print("Abnormal Test Data Mean = {}".format(np.mean(abn_test_loss)))
  print("Abnormal Test Data Standard Deviation = {}".format(np.std(abn_test_loss)))
  print("Precision = {}".format(precision_score(labels, predictions)))
  print("Recall = {}".format(recall_score(labels, predictions)))
  print(accuracy_score(labels, predictions))
  print(np.mean(nl_test_loss))
  print(np.std(nl_test_loss))
  print(np.mean(abn_test_loss))
  print(np.std(abn_test_loss))
  print(precision_score(labels, predictions))
  print(recall_score(labels, predictions))
  print(accuracy_score(labels, predictions), np.mean(nl_test_loss), np.std(nl_test_loss), np.mean(abn_t
         precision_score(labels, predictions), recall_score(labels, predictions))
preds = predict(variational_ae, test_data, threshold)
print_stats(preds, test_labels_T_F)
    Confusion Matrix:
                         Τ
      prediction: F
                  1002
                         998
      label: F
                 [[985
                         15]
                                 1000
             Τ
                  [17
                        983]]
                                 1000
     Accuracy = 0.984
     Normal Test Data Mean = 0.053389281034469604
     Normal Test Data Standard Deviation = 0.021108437329530716
     Abnormal Test Data Mean = 0.15975765883922577
     Abnormal Test Data Standard Deviation = 0.024457454681396484
     Precision = 0.9849699398797596
     Recall = 0.983
     0.984
     0.05338928
     0.021108437
     0.15975766
     0.024457455
     0.9849699398797596
     0.983
     0.984 0.05338928 0.021108437 0.15975766 0.024457455 0.9849699398797596 0.983
```

print("Threshold =", valid\_data\_best\_threshold)

```
print(confusion_matrix(test_labels_T_F, preds))
[[985 15]
[ 17 983]]
```

Threshold = 0.10092985481023803

# Extra accuracy info

Just informative. Please record the above accuracy.

Accuracy on the test data with threshold set based on (threshold2 + threshold3) / 2 = Average of (mean + std of the distribution of the reconstruction losses of the normal validation data) and (mean - std of the distribution of the reconstruction losses of the abnormal validation data)

```
preds = predict(variational_ae, test_data, Avg_of_threshold_2_3)
print_stats(preds, test_labels_T_F)
     Confusion Matrix:
      prediction: F
                         Τ
                  997
                        1003
      label: F
                [[983
                         17]
                                1000
                        986]]
             Τ
                 [14
                                1000
     Accuracy = 0.9845
     Normal Test Data Mean = 0.053389281034469604
     Normal Test Data Standard Deviation = 0.021108437329530716
     Abnormal Test Data Mean = 0.15975765883922577
     Abnormal Test Data Standard Deviation = 0.024457454681396484
     Precision = 0.9830508474576272
     Recall = 0.986
     0.9845
     0.05338928
     0.021108437
     0.15975766
     0.024457455
     0.9830508474576272
     0.986
     0.9845 0.05338928 0.021108437 0.15975766 0.024457455 0.9830508474576272 0.986
```

Accuracy on the test data with threshold set based on the mean of the training data MAE reconstruction losses + 2.5 std

```
preds = predict(variational_ae, test_data, threshold_train_mean_2_5_std)
print_stats(preds, test_labels_T_F)
     Confusion Matrix:
      prediction: F
                         Τ
                  1049
                         951
      label: F
                 [[997
                         3]
                                1000
             Т
                  [52
                         948]]
                                 1000
     Accuracy = 0.9725
```

```
Normal Test Data Mean = 0.053389281034469604

Normal Test Data Standard Deviation = 0.021108437329530716

Abnormal Test Data Mean = 0.15975765883922577

Abnormal Test Data Standard Deviation = 0.024457454681396484

Precision = 0.9968454258675079

Recall = 0.948

0.9725

0.05338928

0.021108437

0.15975766

0.024457455

0.9968454258675079

0.948

0.9725 0.05338928 0.021108437 0.15975766 0.024457455 0.9968454258675079 0.948
```

#### **Extra Info**

Giving the VAE codings (please see book) (Just informative, not the goal here)

```
def plot_multiple_images(images, n_cols=None):
   n_cols = n_cols or len(images)
   n_rows = (len(images) - 1) // n_cols + 1
   if images.shape[-1] == 1:
       images = np.squeeze(images, axis=-1)
   plt.figure(figsize=(n_cols, n_rows))
   for index, image in enumerate(images):
       plt.subplot(n_rows, n_cols, index + 1)
       plt.imshow(image, cmap="binary")
       plt.axis("off")
codings = tf.random.normal(shape=[12, codings_size])
images = variational_decoder(codings).numpy()
plot_multiple_images(images, 4)
# save_fig("vae_generated_images_plot", tight_layout=False)
     是是是是
     P. C. C.
     AAAA
```

```
codings_grid = tf.reshape(codings, [1, 3, 4, codings_size])
larger_grid = tf.image.resize(codings_grid, size=[5, 7])
interpolated_codings = tf.reshape(larger_grid, [-1, codings_size])
images = variational_decoder(interpolated_codings).numpy()

plt.figure(figsize=(7, 5))
for index, image in enumerate(images):
    plt.subplot(5, 7, index + 1)
```

```
if index%7%2==0 and index//7%2==0:
    plt.gca().get_xaxis().set_visible(False)
    plt.gca().get_yaxis().set_visible(False)
else:
    plt.axis("off")
    plt.imshow(image, cmap="binary")
# save_fig("semantic_interpolation_plot", tight_layout=False)
```

