



Data-Driven Behavioral Analytics: Observations, Representations and Models

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<http://www.meng-jiang.com/tutorial-cikm16.html>



I. Mining behavior networks with social and spatiotemporal contexts

I.1. Behavior prediction and recommendation



Behavior in Social Networks

❑ Facebook: Post, Like, Comment, Share

Update Status | Add Photos/Videos | Create Photo Album

What's on your mind?

Public Post

132 Likes 20 Comments



Like



Comment



Share

❑ Twitter: Post, Reply, Retweet, Favorite

What's happening?

Media Location 140 Tweet



5



7



❑ YouTube: Upload, Subscribe, Download, Share, Comment

Upload

Notification bell icon

Top 10 NBA Plays: October 18

NBA Subscribed 6,434,753 Download 720 126,540

Add to Share More

2,468 24

Behavior in Social Networks



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Share
Favorite
Retweet
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Social Recommender Systems

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from Kathy Novak Food and Fancies
124 · 251

Crockpot Caramel Apple Crumble
from Fake Ginger
Slow Cooker Caramel Apple Crumble
from Kathy Novak Food and Fancies
1732 · 251

Crispy Potato Roast
from Kathy Novak Food and Fancies
1732 · 251

Parmesan Garlic Noodles
from Expand Pin
Crockpot Caramel Apple Crumble - the most delicious dessert ever! And it's made in the crockpot!
from Kathy Novak Food and Fancies
104 · 146

Deep Dish Fudgy Oatmeal Bars
from Domestic Superhero
One Pot Spicy Thai Noodles
from Her House Looked Normal From The Outside, But When They
This house takes meal prep to a whole new level. Doesn't it take you forever to boil a pot of soda fountains and clean up all those bottles?
106 · 11

Deep Dish Fudgy Oatmeal Bars
from High Heels and Deep Dish Fudgy Oatmeal Bars. This is a super easy recipe that has big taste!
1233 · 230

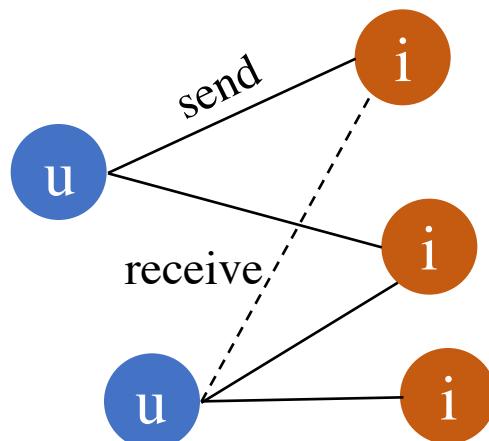
SAMOA SHEET CAKE
from High Heels and Deep Dish Fudgy Oatmeal Bars
Deep Dish Fudgy Oatmeal Bars. This is a super easy recipe that has big taste!
1233 · 230

Facebook

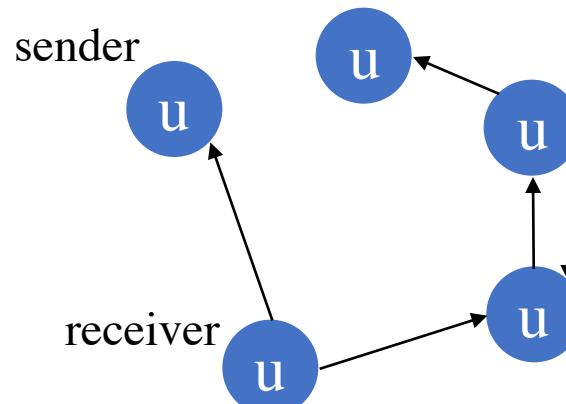
Social Recommender Systems

- ❑ April 20, 2011: Tencent Weibo visited Tsinghua University
 - ❑ Low *conversion rate* (< 6%): #retweets per feed request
 - ❑ Can we build a *social recommender system*?
 - ❑ Given

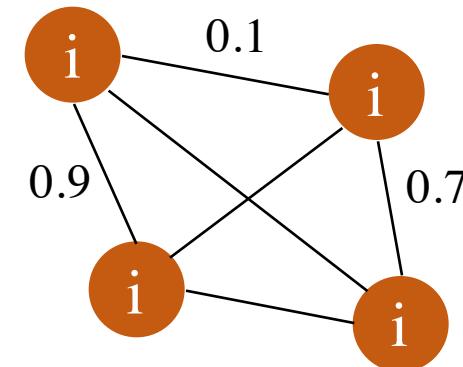
User-item behavior network



User-user social network



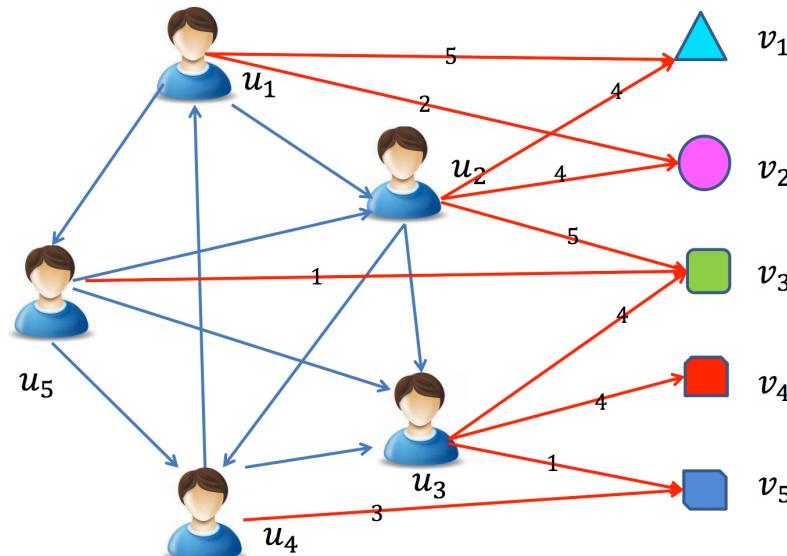
Content similarity
(topic level) [Blei *et al.*]



- ❑ Predict which tweet/item a user will retweet.

Traditional Recommender Systems

- ❑ Assumed that users are independent and identically distributed (user-movie, user-book, *etc.*)



| | v_1 | v_2 | v_3 | v_4 | v_5 |
|-------|-------|-------|-------|-------|-------|
| u_1 | 5 | ? | 2 | ? | ? |
| u_2 | 4 | 4 | 5 | ? | ? |
| u_3 | ? | ? | 4 | 4 | 1 |
| u_4 | ? | ? | ? | ? | 3 |
| u_5 | ? | ? | 1 | ? | ? |

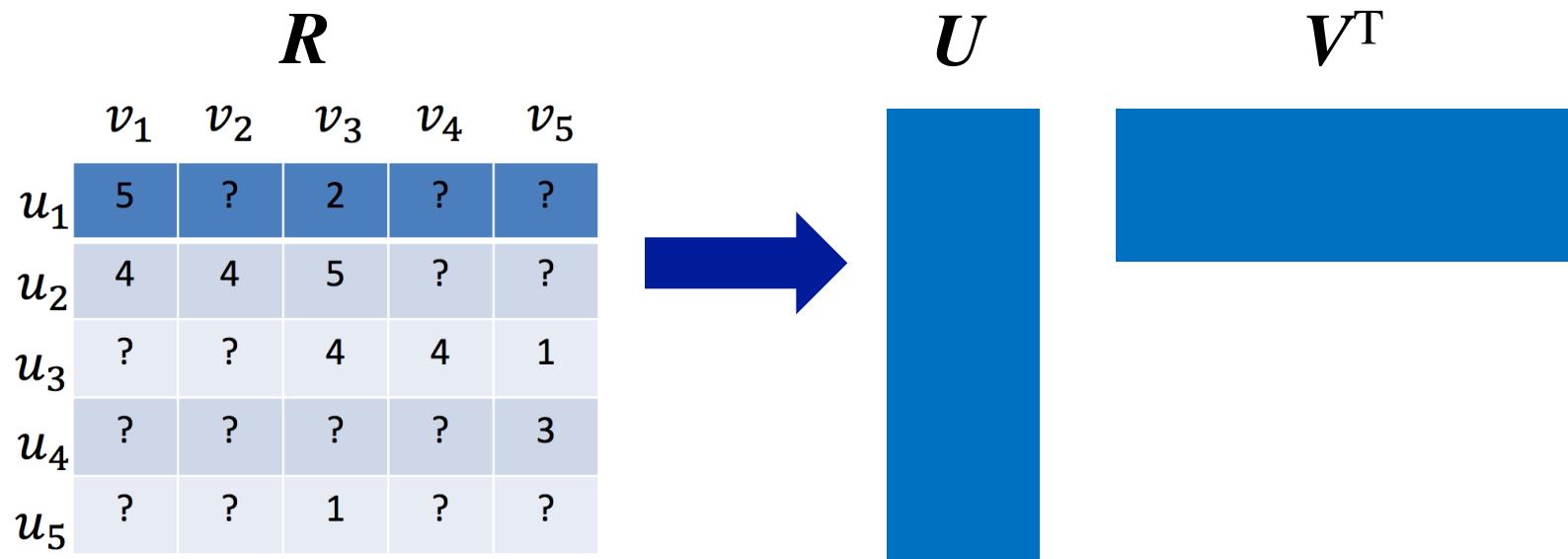


Traditional Recommender Systems

- ❑ Content-based recommender (e.g., TF-IDF)
 - ❑ For textual information (e.g., news, documents)
 - ❑ *Limitation: limited content analysis, over-specialization*
- ❑ Collaborative filtering based recommender
 - ❑ Memory-based CF (e.g., PCC, similarity)
 - ❑ Model-based CF (e.g., factorization based)
 - ❑ *Limitation: data sparsity, cold-start problem*
- ❑ Hybrid recommender system

Matrix Factorization (MF) based CF

- Low-rank MF on the user-item rating matrix R
- User preference vector U
- Item characteristic vector V



Matrix Factorization (MF) based CF

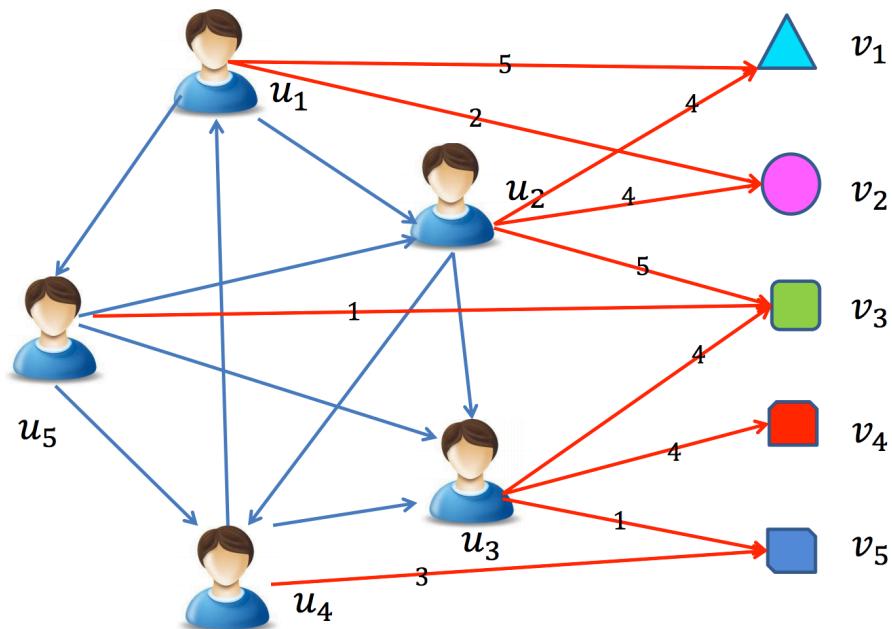
- ❑ Low-rank MF on the user-item rating matrix R
- ❑ User preference vector U
- ❑ Item characteristic vector V
- ❑ Observed weight matrix W

$$\min_{\mathbf{U}, \mathbf{V}} \sum_{i=1}^n \sum_{j=1}^m \boxed{\mathbf{W}_{ij}} (\mathbf{R}_{ij} - \mathbf{U}_i \mathbf{V}_j^\top)^2 + \boxed{\alpha(\|\mathbf{U}\|_F^2 + \|\mathbf{V}\|_F^2)}$$

avoid **over-fitting**,
controlled by the **parameter**

Social Recommendation

Social relations



| | u_1 | u_2 | u_3 | u_4 | u_5 |
|-------|-------|-------|-------|-------|-------|
| u_1 | 0 | 1 | 0 | 0 | 1 |
| u_2 | 0 | 0 | 1 | 1 | 0 |
| u_3 | 0 | 0 | 0 | 0 | 0 |
| u_4 | 1 | 0 | 1 | 0 | 0 |
| u_5 | 0 | 1 | 1 | 1 | 0 |

| | v_1 | v_2 | v_3 | v_4 | v_5 |
|-------|-------|-------|-------|-------|-------|
| u_1 | 5 | ? | 2 | ? | ? |
| u_2 | 4 | 4 | 5 | ? | ? |
| u_3 | ? | ? | 4 | 4 | 1 |
| u_4 | ? | ? | ? | ? | 3 |
| u_5 | ? | ? | 1 | ? | ? |

Memory based Social Recommender

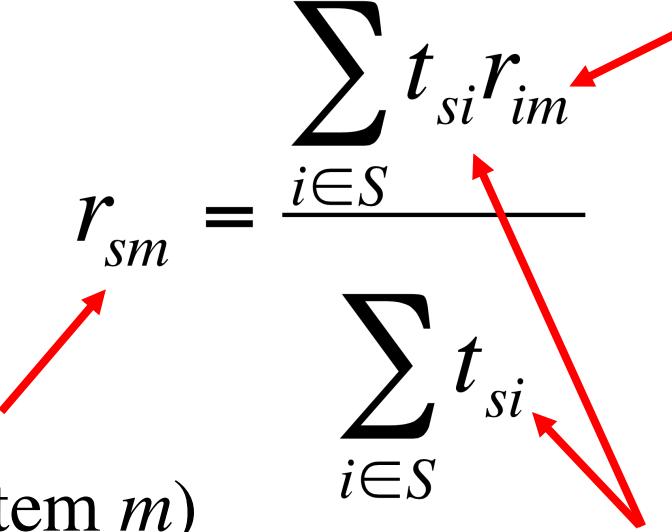
□ TidalTrust

$$r_{sm} = \frac{\sum_{i \in S} t_{si} r_{im}}{\sum_{i \in S} t_{si}}$$

rating (user i , item m)

rating (user s , item m)

trust from social relation (user s , user i)



Memory based Social Recommender

□ MoleTrust

$$p_{a,i} = \bar{r}_a + \frac{\sum_{u=1}^k w_{a,u}(r_{u,i} - \bar{r}_u)}{\sum_{u=1}^k w_{a,u}}$$

average rating (user a)

rating (user u , item i)

predicted rating (user a , item i)

trust from social relation (user a , user u)

average rating (user u)

The diagram illustrates the MoleTrust formula with red arrows indicating the flow of information from the labels to the terms in the equation. The labels are: 'average rating (user a)', 'rating (user u , item i)', 'predicted rating (user a , item i)', and 'trust from social relation (user a , user u)'. The first two labels point to the terms \bar{r}_a and $r_{u,i}$ respectively. The third label points to the entire fraction. The fourth label points to the term $w_{a,u}$.

Memory based Social Recommender

□ TrustWalker

probability of
user u 's random walk
from item i to item j

$$P(Y_{u,i} = j) = \frac{sim(i, j)}{\sum_{l \in RI_u} sim(i, l)}$$

similarity measure
(item i , item j)

Pearson correlation
of (item i , item j)

$$sim(i, j) = \frac{1}{1 + e^{-\frac{|UC_{i,j}|}{2}}} \times corr(i, j)$$

common user set
of (item i , item j)



Model based Social Recommender

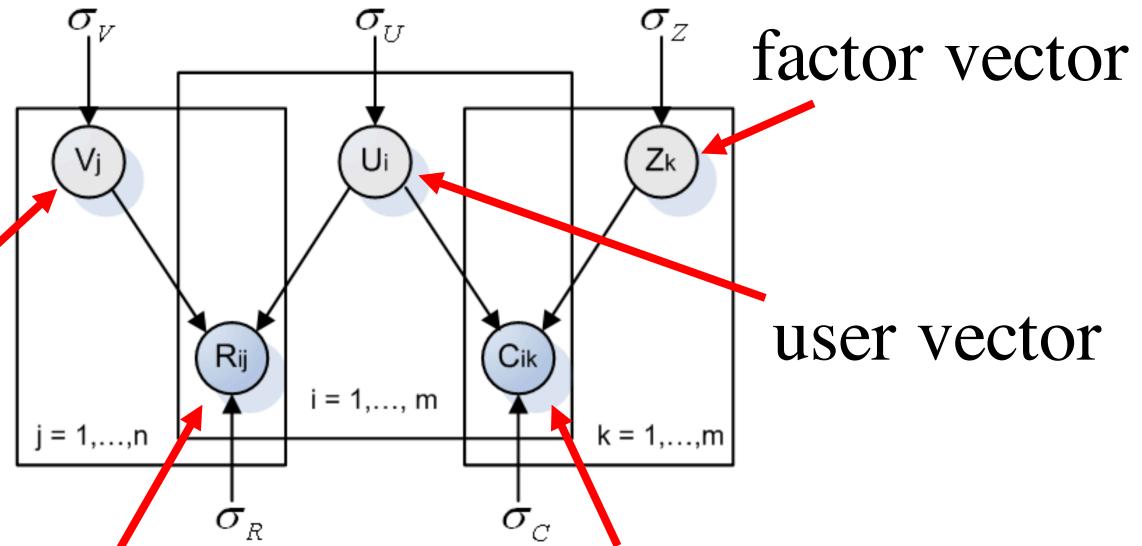
- Optimization methods such as gradient based methods can be applied to find a well-worked optimal solution.
- MF has a nice probabilistic interpretation with Gaussian noise.
- MF is very flexible and allows us to include prior knowledge.

$$\begin{aligned} & \textit{Social Recommendation CF} \\ &= \textit{Basic CF} + \textit{Social Information Model} \end{aligned}$$

Model based Social Recommender

□ SoRec

item vector



factor vector

user vector

R : user-item
rating matrix

| | v_1 | v_2 | v_3 | v_4 | v_5 |
|-------|-------|-------|-------|-------|-------|
| u_1 | 5 | ? | 2 | ? | ? |
| u_2 | 4 | 4 | 5 | ? | ? |
| u_3 | ? | ? | 4 | 4 | 1 |
| u_4 | ? | ? | ? | ? | 3 |
| u_5 | ? | ? | 1 | ? | ? |

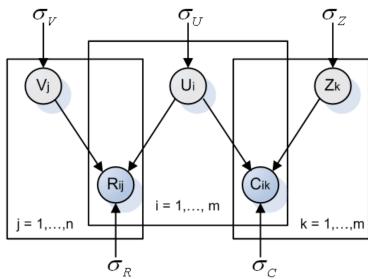
C : user-user
social matrix

| | u_1 | u_2 | u_3 | u_4 | u_5 |
|-------|-------|-------|-------|-------|-------|
| u_1 | 0 | 1 | 0 | 0 | 1 |
| u_2 | 0 | 0 | 1 | 1 | 0 |
| u_3 | 0 | 0 | 0 | 0 | 0 |
| u_4 | 1 | 0 | 1 | 0 | 0 |
| u_5 | 0 | 1 | 1 | 1 | 0 |

Model based Social Recommender

□ SoRec

$$p(\mathcal{C}|U, V, \sigma_R^2) = \prod_{i=1}^m \prod_{j=1}^n \mathcal{N} \left[\left(r_{ij} | g(U_i^T V_j), \sigma_R^2 \right) \right]^{I_{ij}^R}$$



Gaussian distribution

Logistic function Observed

$$p(C|U, Z, \sigma_C^2) = \prod_{i=1}^m \prod_{k=1}^m \mathcal{N} \left[\left(c_{ik} | g(U_i^T Z_k), \sigma_C^2 \right) \right]^{I_{ik}^C}$$

Model based Social Recommender

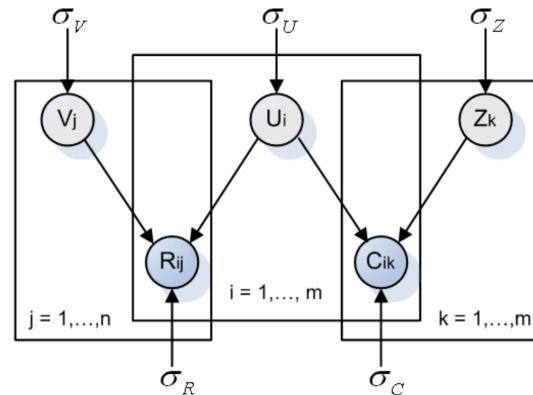
□ SoRec

behavioral term

$$\mathcal{L}(R, C, U, V, Z) =$$

$$\frac{1}{2} \sum_{i=1}^m \sum_{j=1}^n I_{ij}^R \underbrace{(r_{ij} - g(U_i^T V_j))^2}_{social\ term} + \frac{\lambda_C}{2} \sum_{i=1}^m \sum_{k=1}^m I_{ik}^C \underbrace{(c_{ik}^* - g(U_i^T Z_k))^2}_{regularization\ terms}$$

$$+ \frac{\lambda_U}{2} \|U\|_F^2 + \frac{\lambda_V}{2} \|V\|_F^2 + \frac{\lambda_Z}{2} \|Z\|_F^2, \quad (9)$$



Model based Social Recommender

□ SoRec

Gradient Descent Methods

$$\frac{\partial \mathcal{L}}{\partial U_i} = \sum_{j=1}^n I_{ij}^R g'(U_i^T V_j) \underline{(g(U_i^T V_j) - r_{ij}) V_j}$$

deviate of
Logistic
function

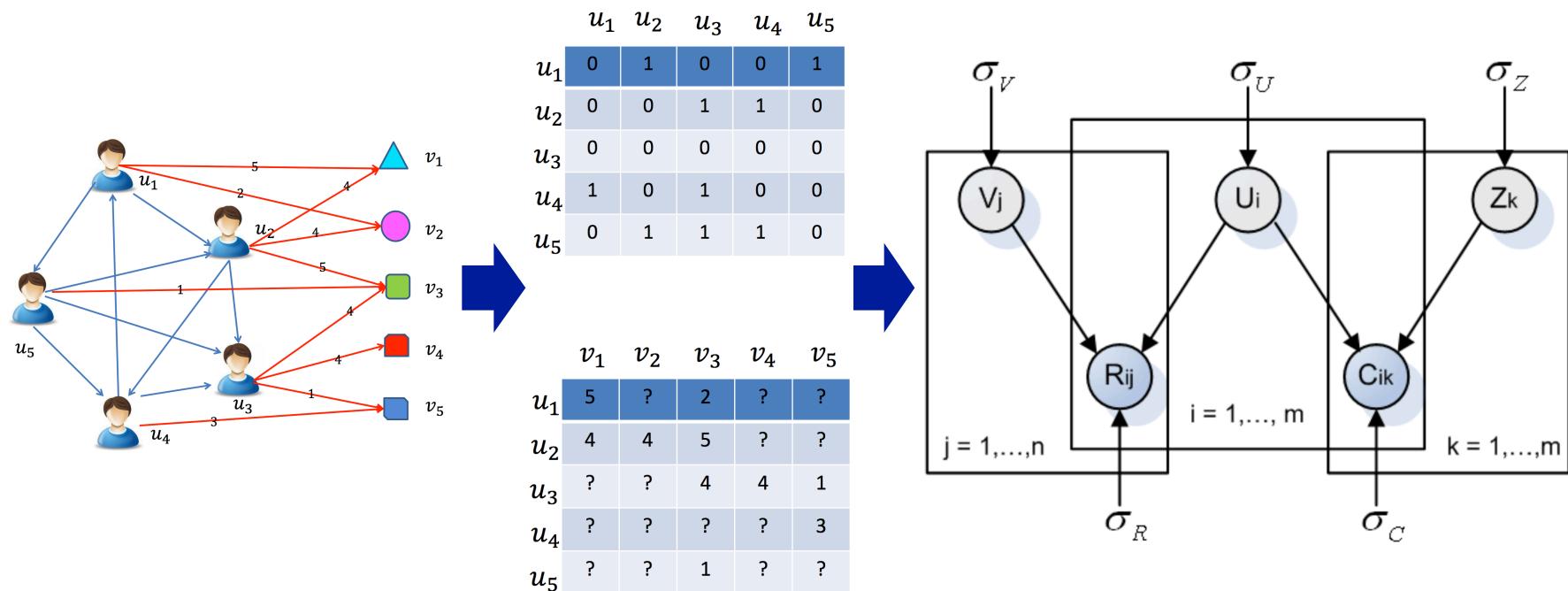
$$+ \lambda_C \sum_{k=1}^m I_{ik}^C g'(U_i^T Z_k) \underline{(g(U_i^T Z_k) - c_{ik}^*) Z_k} + \lambda_U U_i,$$

$$\frac{\partial \mathcal{L}}{\partial V_j} = \sum_{i=1}^m I_{ij}^R g'(U_i^T V_j) \underline{(g(U_i^T V_j) - r_{ij}) U_i} + \lambda_V V_j,$$

$$\frac{\partial \mathcal{L}}{\partial Z_k} = \lambda_C \sum_{i=1}^m I_{ik}^C g'(U_i^T Z_k) \underline{(g(U_i^T Z_k) - c_{ik}^*) U_i} + \lambda_Z Z_k, (10)$$

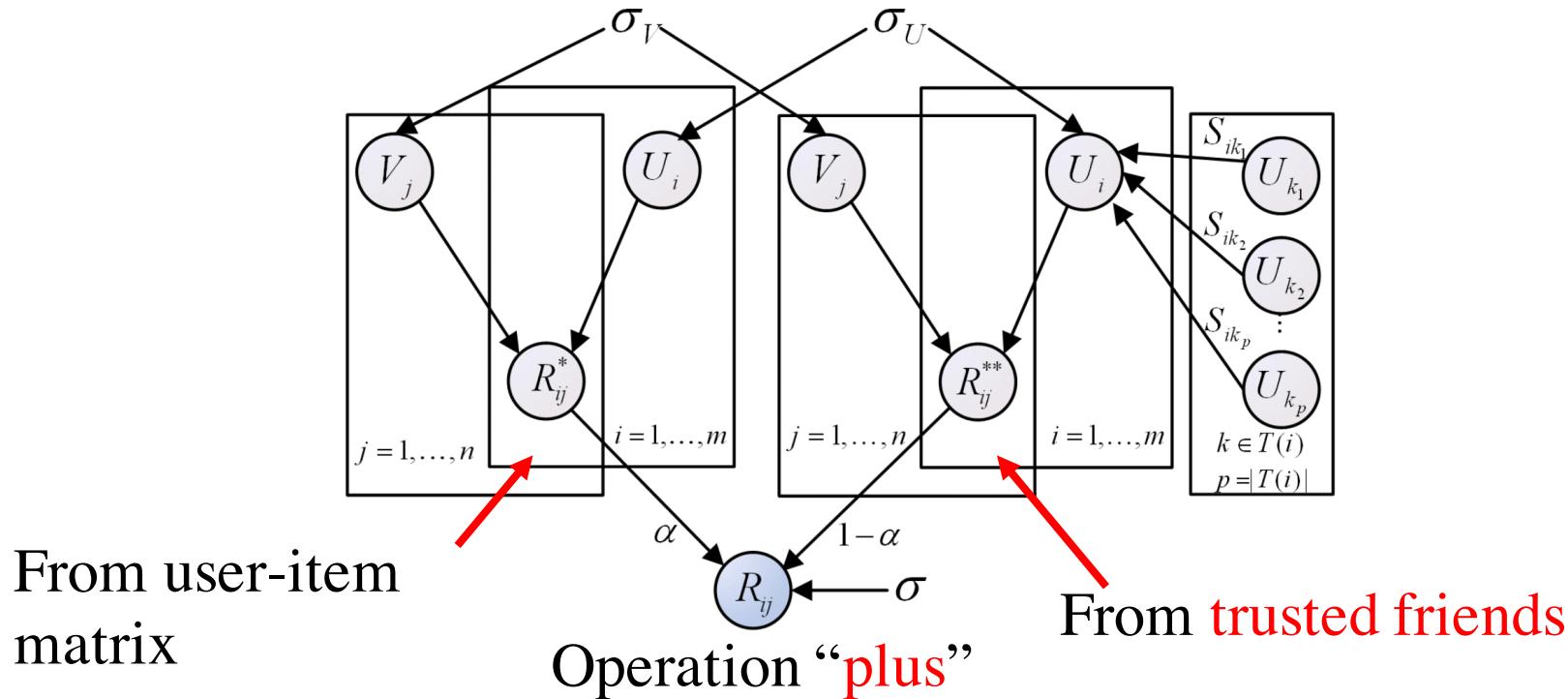
Model based Social Recommender

□ SoRec



Model based Social Recommender

- Replacing social with trust
- “Social Trust” Ensemble for Epinion data



Model based Social Recommender

□ “Social Trust” Ensemble

$$\begin{aligned} \mathcal{L}(R, S, U, V) & \quad \text{From user-item matrix} \\ &= \frac{1}{2} \sum_{i=1}^m \sum_{j=1}^n I_{ij}^R (R_{ij} - g(\underline{\alpha U_i^T V_j} + \underline{(1-\alpha) \sum_{k \in \mathcal{T}(i)} S_{ik} U_k^T V_j}))^2 \\ &+ \frac{\lambda_U}{2} \|U\|_F^2 + \frac{\lambda_V}{2} \|V\|_F^2, \end{aligned} \tag{13}$$

Model based Social Recommender

□ “Social Trust” Ensemble

*Gradient
Descent
Methods*

$$\begin{aligned}
 \frac{\partial \mathcal{L}}{\partial U_i} = & \alpha \sum_{j=1}^n I_{ij}^R g'(\alpha U_i^T V_j + (1 - \alpha) \sum_{k \in \mathcal{T}(i)} S_{ik} U_k^T V_j) V_j \\
 & \times (g(\alpha U_i^T V_j + (1 - \alpha) \sum_{k \in \mathcal{T}(i)} S_{ik} U_k^T V_j) - R_{ij}) \\
 & + (1 - \alpha) \sum_{p \in \mathcal{B}(i)} \sum_{j=1}^n I_{pj}^R g'(\alpha U_p^T V_j + (1 - \alpha) \sum_{k \in \mathcal{T}(p)} S_{pk} U_k^T V_j) \\
 & \times (g(\alpha U_p^T V_j + (1 - \alpha) \sum_{k \in \mathcal{T}(p)} S_{pk} U_k^T V_j) - R_{pj}) S_{pi} V_j + \lambda_U U_i, \\
 \frac{\partial \mathcal{L}}{\partial V_j} = & \sum_{i=1}^m I_{ij}^R g'(\alpha U_i^T V_j + (1 - \alpha) \sum_{k \in \mathcal{T}(i)} S_{ik} U_k^T V_j) \\
 & \times (g(\alpha U_i^T V_j + (1 - \alpha) \sum_{k \in \mathcal{T}(i)} S_{ik} U_k^T V_j) - R_{ij}) \\
 & \times (\alpha U_i + (1 - \alpha) \sum_{k \in \mathcal{T}(i)} S_{ik} U_k^T) + \lambda_V V_j, \tag{14}
 \end{aligned}$$

Model based Social Recommender

□ SoReg

Average-based regularization:

Regularize with the average of friends' tastes

$$\min_{U, V} \mathcal{L}_1(R, U, V) = \frac{1}{2} \sum_{i=1}^m \sum_{j=1}^n I_{ij} (R_{ij} - U_i^T V_j)^2$$



$$+ \frac{\alpha}{2} \sum_{i=1}^m \|U_i - \frac{\sum_{f \in \mathcal{F}^+(i)} \text{Sim}(i, f) \times U_f}{\sum_{f \in \mathcal{F}^+(i)} \text{Sim}(i, f)}\|_F^2,$$

$$+ \frac{\lambda_1}{2} \|U\|_F^2 + \frac{\lambda_2}{2} \|V\|_F^2. \quad (8)$$

Information loss: Friends may have diverse tastes!!!

Model based Social Recommender

□ SoReg

Individual-based regularization:

Regularize with friends individually

$$\begin{aligned} \min_{U, V} \mathcal{L}_2(R, U, V) &= \frac{1}{2} \sum_{i=1}^m \sum_{j=1}^n I_{ij} (R_{ij} - U_i^T V_j)^2 \\ &+ \frac{\beta}{2} \sum_{i=1}^m \sum_{f \in \mathcal{F}^+(i)} Sim(i, f) \|U_i - U_f\|_F^2 \\ &+ \lambda_1 \|U\|_F^2 + \lambda_2 \|V\|_F^2. \end{aligned} \tag{11}$$

Related Work

| | Behavior | Content | Social | Trust |
|---|----------|---------|--------|-------|
| Collaborative filtering (CF) [Herlocker <i>et al.</i> . TOIS; Koren KDD] | ✓ | | | |
| Content-based filtering with CF [Balabanovic <i>et al.</i> ; Liu <i>et al.</i> . CIKM;] | ✓ | ✓ | | |
| SoRec [Ma <i>et al.</i> . CIKM, TIS] SoReg [Ma <i>et al.</i> . WSDM] | ✓ | | ✓ | |
| Trust-based methods [Massa <i>et al.</i> . RecSys; Jamali <i>et al.</i> . KDD; Ma <i>et al.</i> . SIGIR, TIST] | ✓ | | | ✓ |

❑ **Q:** What are the **factors** of users' decisions on retweeting?
Can we **observe** them from the data? How to **integrate** the information for accurate prediction?

Observation: Social Contextual Factors

- Will Michelle Obama share this message?
- Please list your reasons.



Barack Obama

Happy birthday, Michelle Obama!

[Like](#) · [Comment](#) · [Share](#) · January 18, 2013

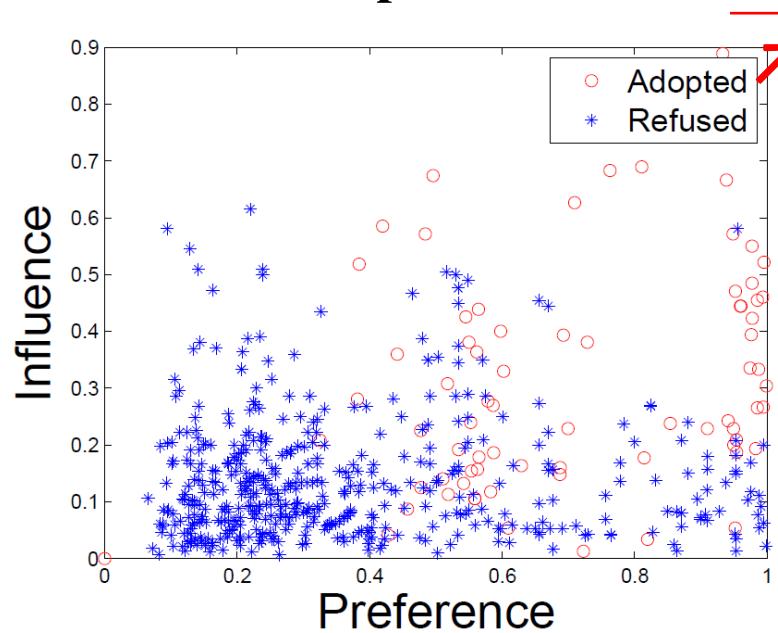
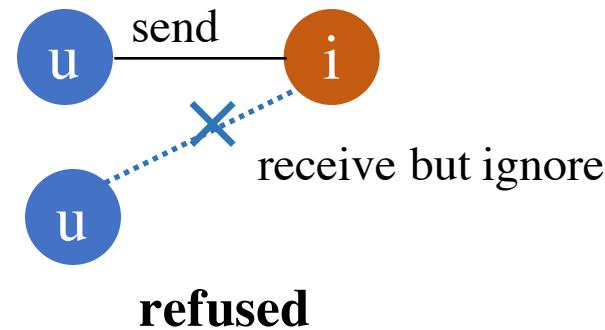
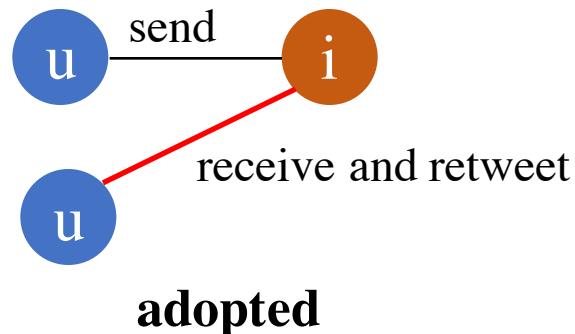


Michelle Obama shared Barack Obama's photo.

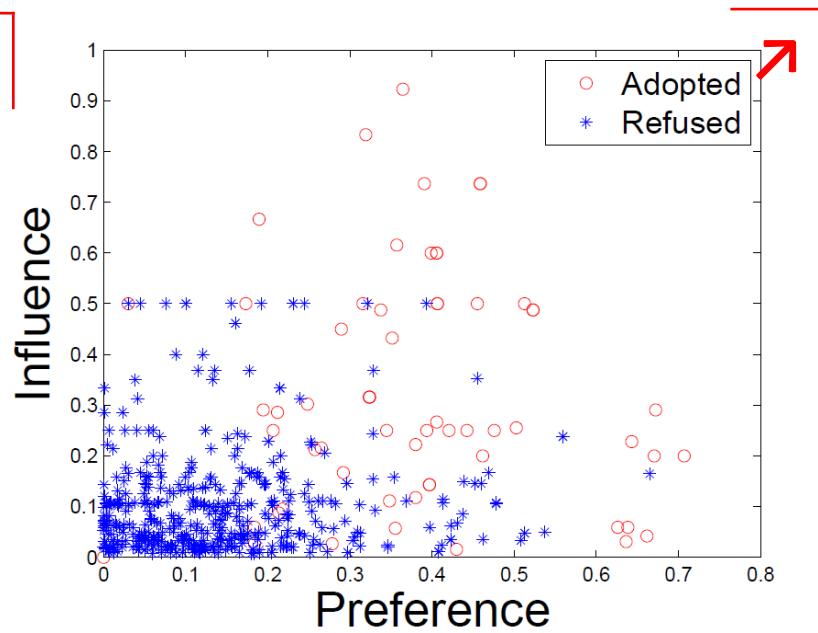
January 18, 2013 ·



Observation: Social Contextual Factors



China's Facebook: Renren



China's Twitter: Tencent Weibo

Representation: From Contextual Information to Contextual Factors

Content

Item-item similarity

Item latent features V

Behavior

User-item interaction

User latent features U

Social

User-user social relation

Item sender G

Interaction frequency

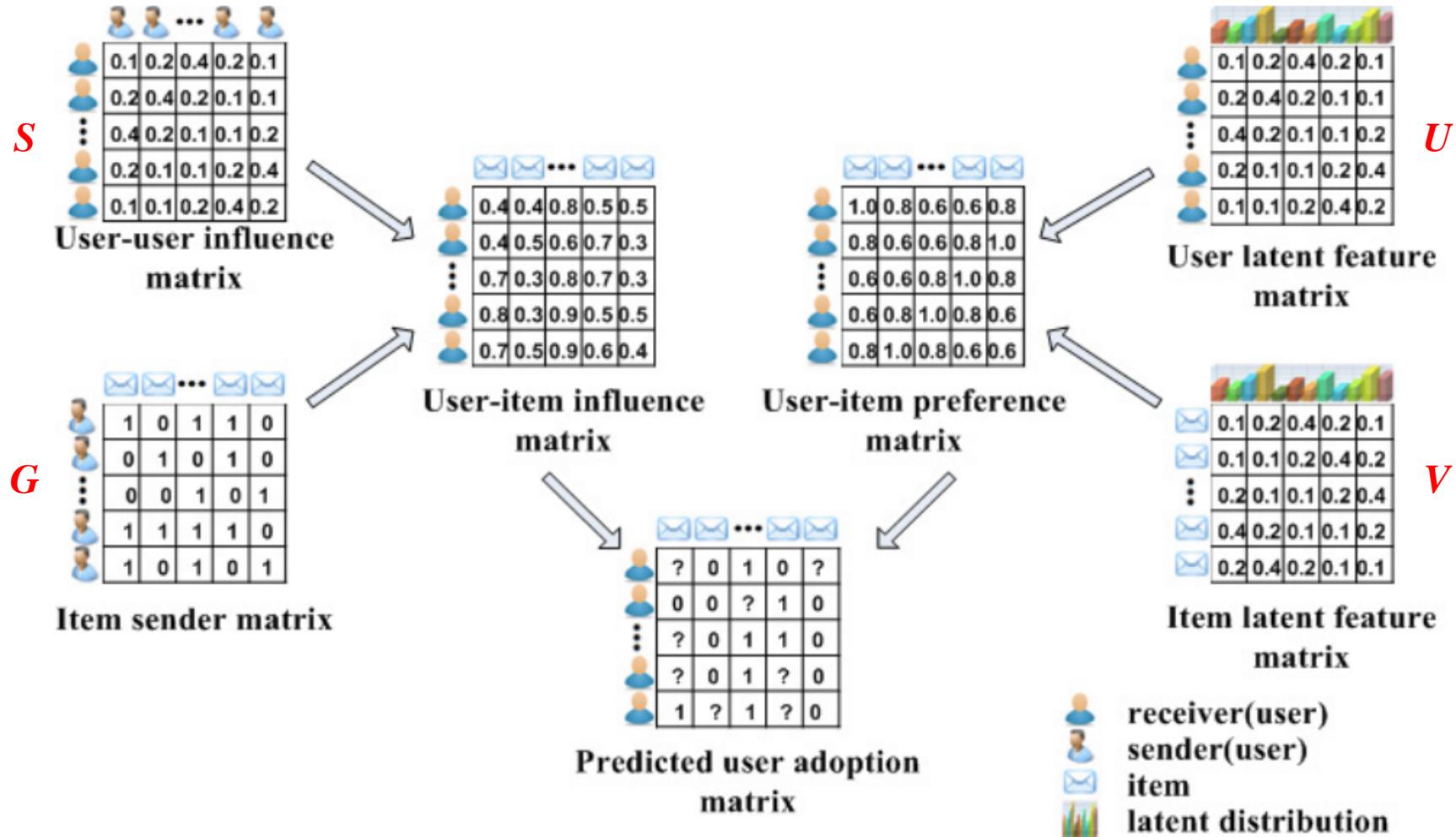
User-user interaction

User-user influence S

Personal preference
on the given item

Interpersonal influence
from the item's sender

Model: ContextMF



Model: ContextMF

behavior influence preference

$$P(\mathbf{R}|\mathbf{S}, \mathbf{U}, \mathbf{V}, \sigma_R^2) = \prod_{i=1}^M \prod_{j=1}^N \mathcal{N}(\underline{\mathbf{R}_{ij}} | \underline{\mathbf{S}_i \mathbf{G}_j^\top} \odot \underline{\mathbf{U}_i^\top \mathbf{V}_j}, \sigma_R^2)$$

behavior interaction frequency/trust

item content

$$\begin{aligned} \mathcal{J} = & ||\mathbf{R} - \mathbf{S}\mathbf{G}^\top \odot \mathbf{U}^\top \mathbf{V}||_F^2 + \alpha ||\mathbf{W} - \mathbf{U}^\top \mathbf{U}||_F^2 \\ & + \beta ||\mathbf{C} - \mathbf{V}^\top \mathbf{V}||_F^2 + \gamma ||\mathbf{S} - \mathbf{F}||_F^2 \\ & + \delta ||\mathbf{S}||_F^2 + \eta ||\mathbf{U}||_F^2 + \lambda ||\mathbf{V}||_F^2 \end{aligned}$$

social relation

Model: ContextMF

- Gradient descent method

$$\frac{\partial \mathcal{J}}{\partial \mathbf{S}} = 2 \left(-\mathbf{R}(\mathbf{G} \odot \mathbf{V}^\top \mathbf{U}) + (\mathbf{S}\mathbf{G}^\top \odot \mathbf{U}^\top \mathbf{V})\mathbf{G} \right. \\ \left. + \gamma(\mathbf{S} - \mathbf{F}) + \delta\mathbf{S} \right)$$

$$\frac{\partial \mathcal{J}}{\partial \mathbf{U}} = 2 \left(-\mathbf{V}\mathbf{R}^\top + \mathbf{V}(\mathbf{G}\mathbf{S}^\top \odot \mathbf{V}^\top \mathbf{U}) - 2\alpha\mathbf{U}\mathbf{W} \right. \\ \left. + 2\alpha\mathbf{U}\mathbf{U}^\top \mathbf{U} + \eta\mathbf{U} \right)$$

$$\frac{\partial \mathcal{J}}{\partial \mathbf{V}} = 2 \left(-\mathbf{U}\mathbf{R} + \mathbf{U}(\mathbf{S}\mathbf{G}^\top \odot \mathbf{U}^\top \mathbf{V}) - 2\beta\mathbf{V}\mathbf{C} \right. \\ \left. + 2\beta\mathbf{V}\mathbf{V}^\top \mathbf{V} + \lambda\mathbf{V} \right)$$



Experimental Results

| Method | MAE | RMSE | $\hat{\tau}$ | $\hat{\rho}$ |
|---------------------|---------------|---------------|---------------|---------------|
| Renren Dataset | | | | |
| Content-based [1] | 0.3842 | 0.4769 | 0.5409 | 0.5404 |
| Item CF [25] | 0.3601 | 0.4513 | 0.5896 | 0.5988 |
| FeedbackTrust [22] | 0.3764 | 0.4684 | 0.5433 | 0.5469 |
| Influence-based [9] | 0.3859 | 0.4686 | 0.5394 | 0.5446 |
| SoRec [19] | 0.3276 | 0.4127 | 0.6168 | 0.6204 |
| SoReg [20] | 0.2985 | 0.3537 | 0.7086 | 0.7140 |
| Influence MF | 0.3102 | 0.3771 | 0.6861 | 0.7006 |
| Preference MF | 0.3032 | 0.3762 | 0.6937 | 0.7036 |
| Context MF | 0.2416 | 0.3086 | 0.7782 | 0.7896 |

Tencent Weibo Dataset

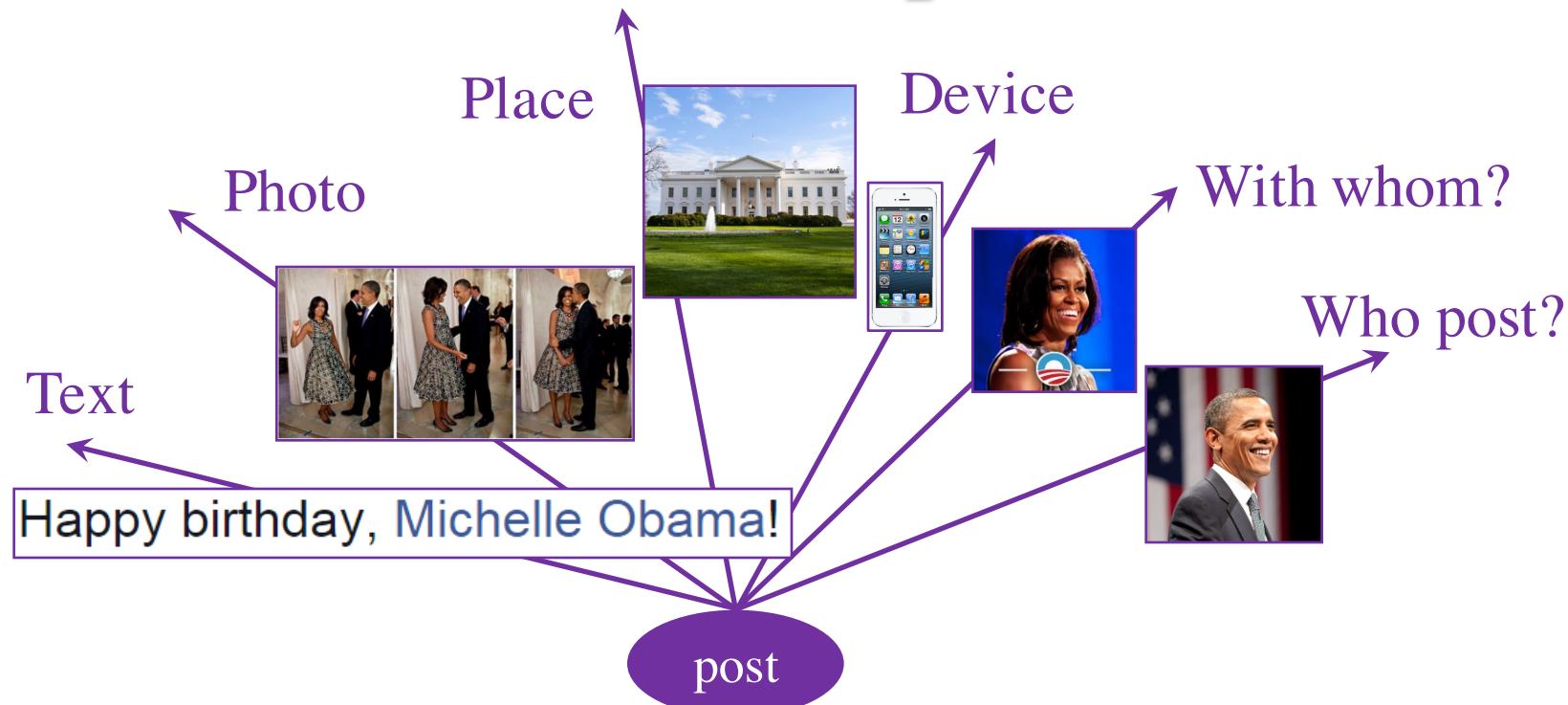
| | | | | |
|---------------------|---------------|---------------|---------------|---------------|
| Content-based [1] | 0.2576 | 0.3643 | 0.7728 | 0.7777 |
| Item CF [25] | 0.2375 | 0.3372 | 0.7867 | 0.8049 |
| FeedbackTrust [22] | 0.2830 | 0.3887 | 0.7094 | 0.7115 |
| Influence-based [9] | 0.2651 | 0.3813 | 0.7163 | 0.7275 |
| SoRec [19] | 0.2256 | 0.3325 | 0.7973 | 0.8064 |
| SoReg [20] | 0.1997 | 0.2962 | 0.8390 | 0.8423 |
| Influence MF | 0.2183 | 0.3206 | 0.8179 | 0.8258 |
| Preference MF | 0.2111 | 0.3088 | 0.8384 | 0.8453 |
| Context MF | 0.1514 | 0.2348 | 0.8570 | 0.8685 |

| vs. SoReg [TIST'11] | Renren | Tencent Weibo |
|------------------------|---------------------|---------------------|
| MAE | $\downarrow 19.1\%$ | $\downarrow 24.2\%$ |
| RMSE | $\downarrow 12.8\%$ | $\downarrow 20.7\%$ |
| Kendall's | $\uparrow 9.82\%$ | $\uparrow 2.1\%$ |
| Spearman's | $\uparrow 10.6\%$ | $\uparrow 3.1\%$ |

□ **Deployed in Weibo News Feed.** Improved conversion rate from 5.78% to 8.27% (relatively **43%**).

□ #citations = **149**

Observation: Spatial Context

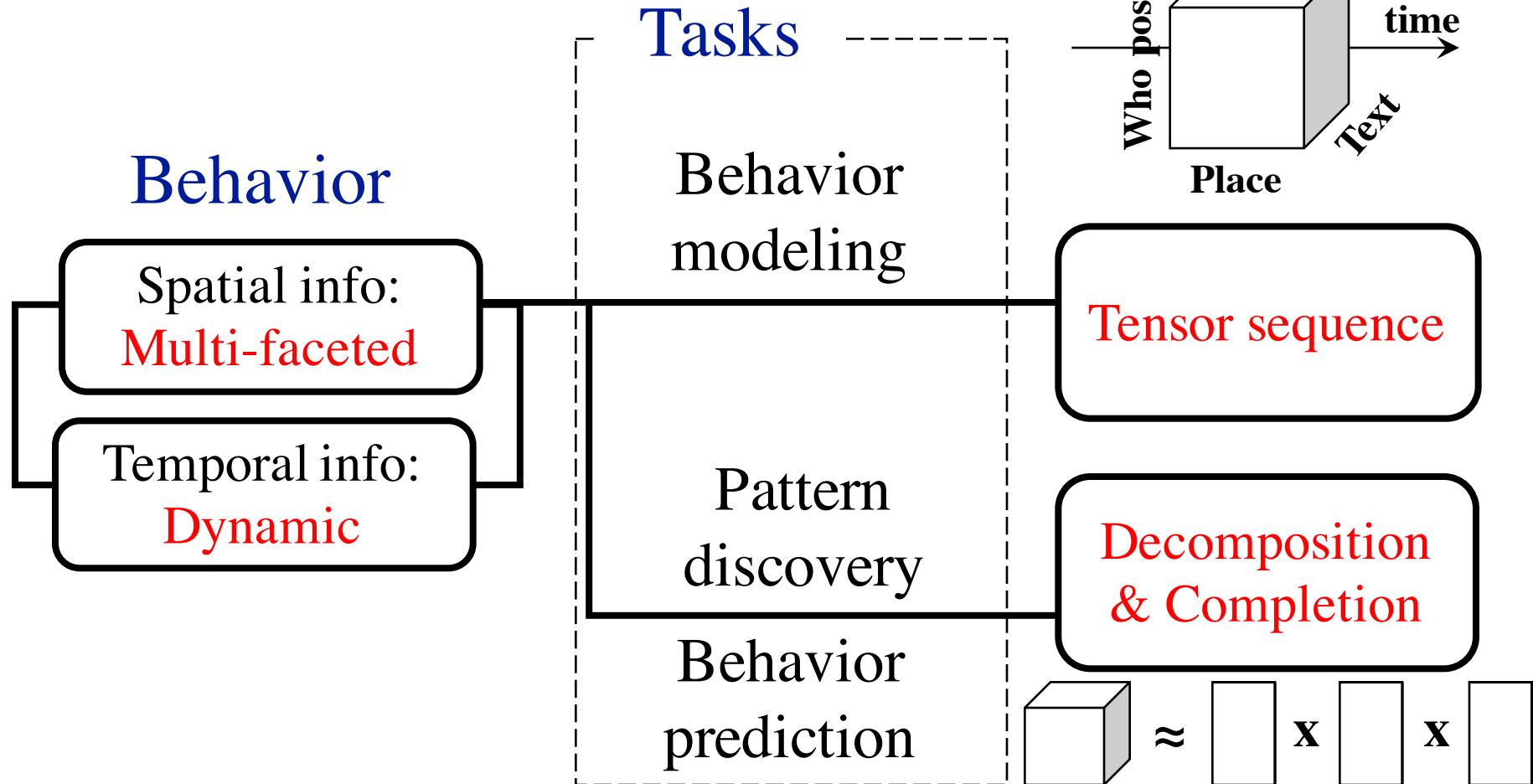


Jan. 18
Birthday party
@ White house

Observation: Temporal Context

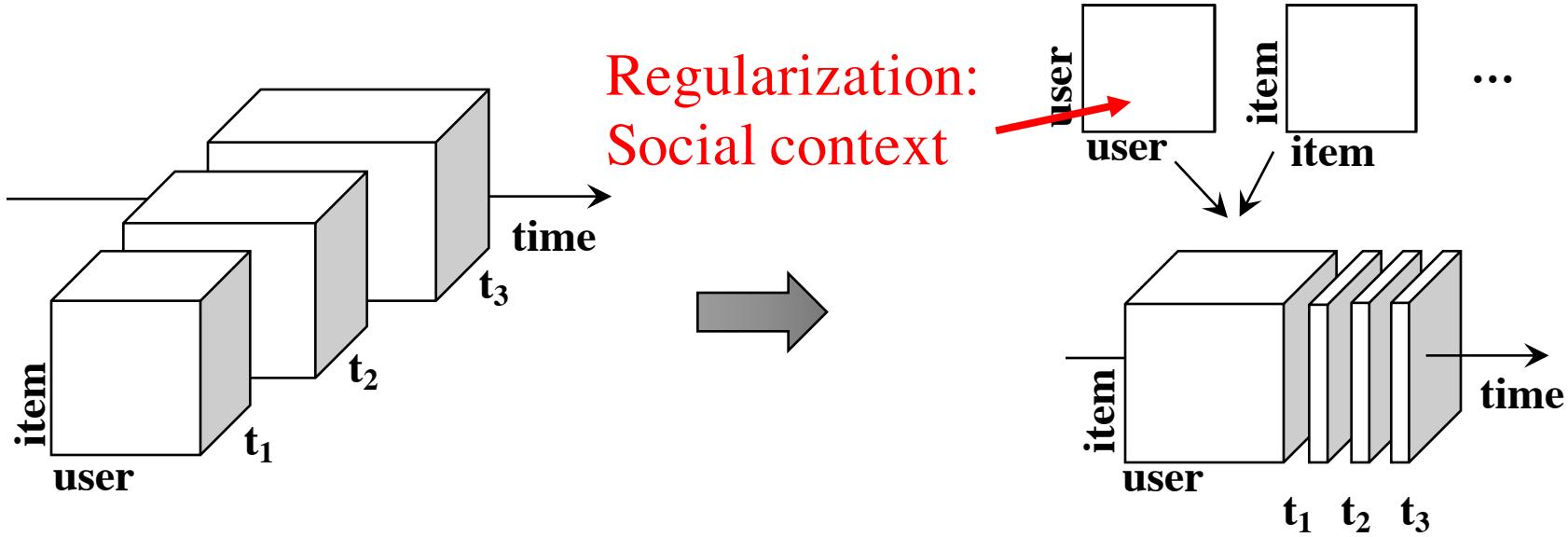


Representation: Tensor Sequence



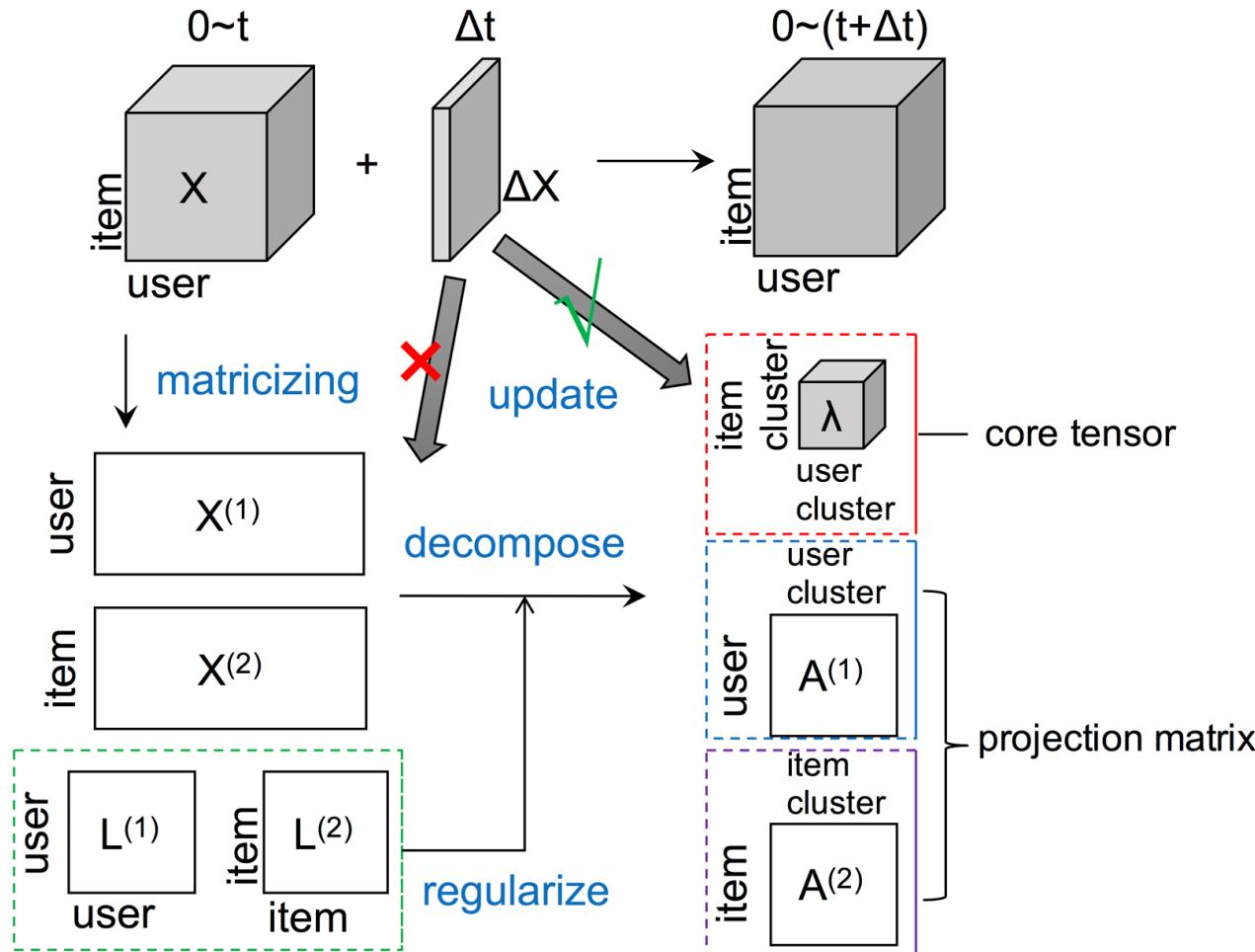
Challenges: Sparsity and Complexity

- Addressing **sparsity**: *Flexible regularization with auxiliary data*
- Addressing **high complexity**: *Incremental updates for projection matrix*



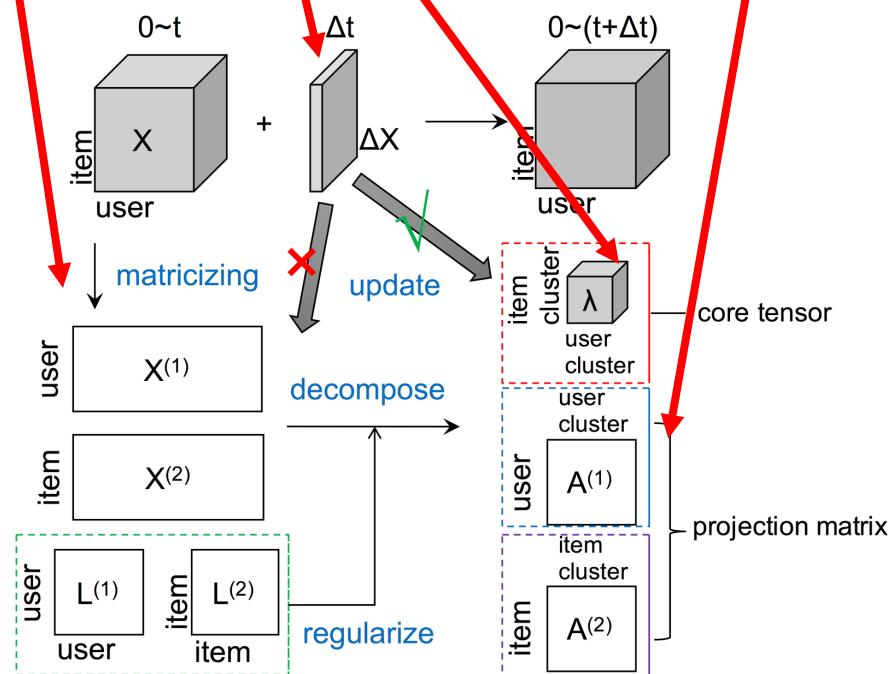
Model: FEMA

Flexible Evolutionary Multi-faceted Analysis



Tensor Perturbation Theory

$$[(\mathbf{X}^{(m)} + \Delta\mathbf{X}^{(m)})(\mathbf{X}^{(m)} + \Delta\mathbf{X}^{(m)})^\top + \mu^{(m)} \mathbf{L}^{(m)}] \cdot (\mathbf{a}_i^{(m)} + \Delta\mathbf{a}_i^{(m)}) = (\lambda_i^{(m)} + \Delta\lambda_i^{(m)}) (\mathbf{a}_i^{(m)} + \Delta\mathbf{a}_i^{(m)})$$



Algorithm: FEMA

Approximation

Require: $\mathcal{X}_t, \Delta\mathcal{X}_t, \mathbf{A}_t^{(m)}|_{m=1}^M, \lambda_t^{(m)}|_{m=1}^M$

for $m = 1, \dots, M$ **do**

for $i = 1, \dots, r^{(m)}$ **do**

 Compute $\Delta\lambda_{t,i}^{(m)}$ using

$$\Delta\lambda_i^{(m)} = \mathbf{a}_i^{(m)\top} (\mathbf{X}^{(m)} \Delta\mathbf{X}^{(m)\top} + \Delta\mathbf{X}^{(m)} \mathbf{X}^{(m)\top}) \mathbf{a}_i^{(m)}$$

 and compute

$$\lambda_{t+1,i}^{(m)} = \lambda_{t,i}^{(m)} + \Delta\lambda_{t,i}^{(m)};$$

 Compute $\Delta\mathbf{a}_{t,i}^{(m)}$ using

$$\Delta\mathbf{a}_i^{(m)} = \sum_{j \neq i} \frac{\mathbf{a}_j^{(m)\top} (\mathbf{X}^{(m)} \Delta\mathbf{X}^{(m)\top} + \Delta\mathbf{X}^{(m)} \mathbf{X}^{(m)\top}) \mathbf{a}_i^{(m)}}{\lambda_i^{(m)} - \lambda_j^{(m)}} \mathbf{a}_j^{(m)}$$

 and compute

$$\mathbf{a}_{t+1,i}^{(m)} = \mathbf{a}_{t,i}^{(m)} + \Delta\mathbf{a}_{t,i}^{(m)} \text{ and } \mathbf{A}_{t+1}^{(m)} = \{\mathbf{a}_{t+1,i}^{(m)}\};$$

end for

end for

$$\mathcal{Y}_{t+1} = (\mathcal{X}_t + \Delta\mathcal{X}_t) \prod_{m=1}^M \times_{(m)} \mathbf{A}_{t+1}^{(m)\top};$$

return $\mathbf{A}_{t+1}^{(m)}|_{m=1}^M, \lambda_{t+1}^{(m)}|_{m=1}^M, \mathcal{Y}_{t+1}$

Bound Guarantee

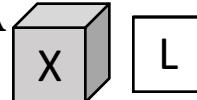
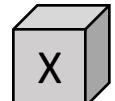
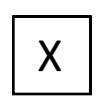
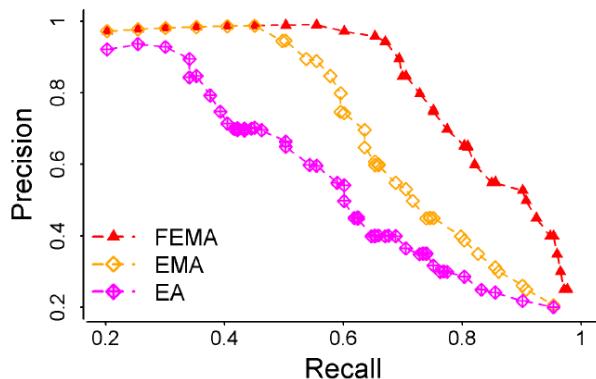
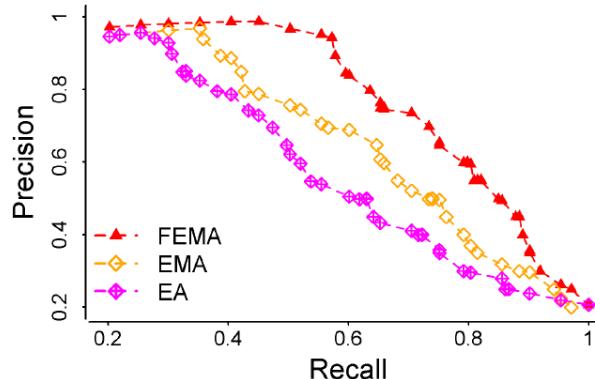
core tensor

$$|\Delta\lambda_i^{(m)}| \leq 2(\lambda_{\mathbf{X}^{(m)\top} \mathbf{X}^{(m)}}^{\max})^{\frac{1}{2}} \|\Delta\mathbf{X}^{(m)}\|_2$$

$$|\Delta\mathbf{a}_i^{(m)}| \leq 2\|\Delta\mathbf{X}^{(m)}\|_2 \sum_{j \neq i} \frac{(\lambda_{\mathbf{X}^{(m)\top} \mathbf{X}^{(m)}}^{\max})^{\frac{1}{2}}}{|\lambda_i^{(m)} - \lambda_j^{(m)}|}$$

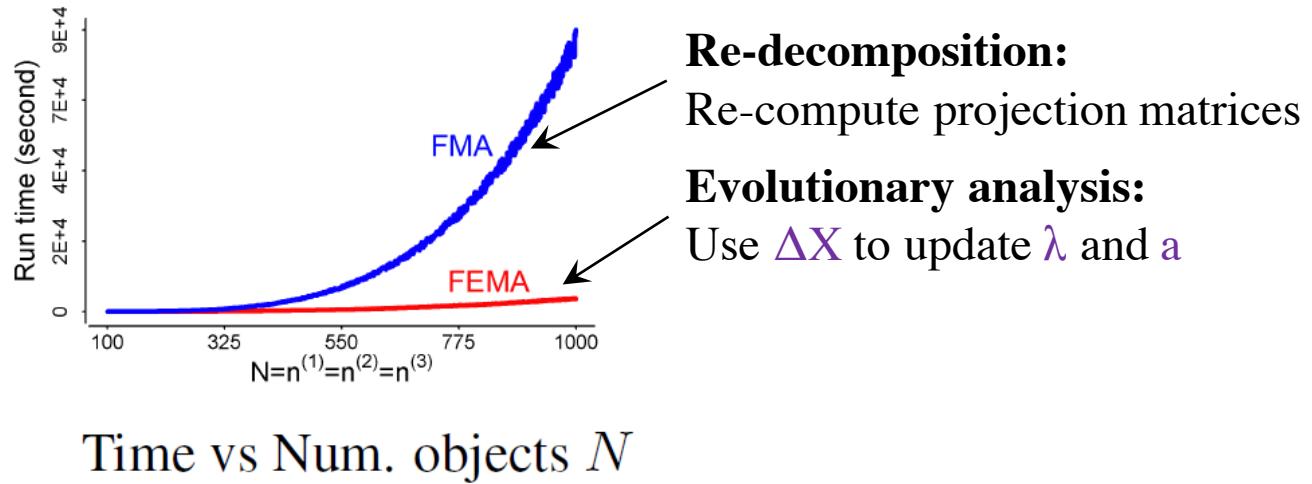
projection matrix

Results: FEMA > EMA > EA

| | Microsoft Academic Search | | Tencent Weibo mentions “@” | |
|---|---|--|----------------------------|--------------|
| | MAE | RMSE | MAE | RMSE |
| FEMA  | 0.735 | 0.944 | 0.894 | 1.312 |
| EMA  | 0.794 | 1.130 | 0.932 | 1.556 |
| EA  | 0.979 | 1.364 | 1.120 | 1.873 |
| Precision vs Recall |  |  | | |

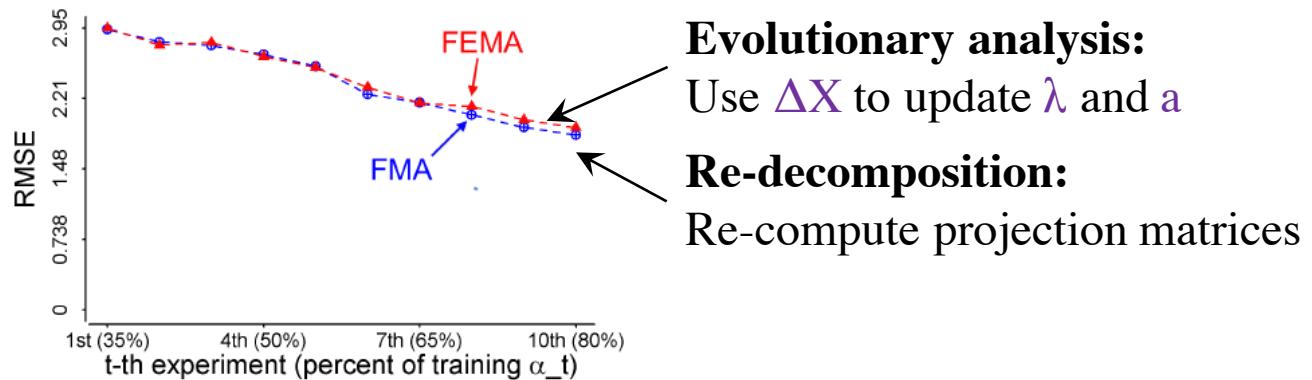


Results: Efficiency



Re-decomposition:
Re-compute projection matrices

Evolutionary analysis:
Use ΔX to update λ and a



Evolutionary analysis:
Use ΔX to update λ and a

Re-decomposition:
Re-compute projection matrices

The loss is small.

Observation: Multiple Domains

 **Osmar Zaiane**
20 hrs · Twitter · 

#DataScientists need ability to tell the story about #data and convey #business value <https://t.co/VNN2rXaLuV> #BigData #datascience #dataviz

 Like  Comment  Share

 The Globe and Mail shared Globe Politics's video.
19 hrs · 

Watch highlights from Stephen Harper's concession speech





 Philip Bohannon shared a link.
5 hrs · 



British Library offers over 1 million free vintage images for download

9#
Closed Group

Joined  Share  ...

Discussion Members Events Photos Files Search this group

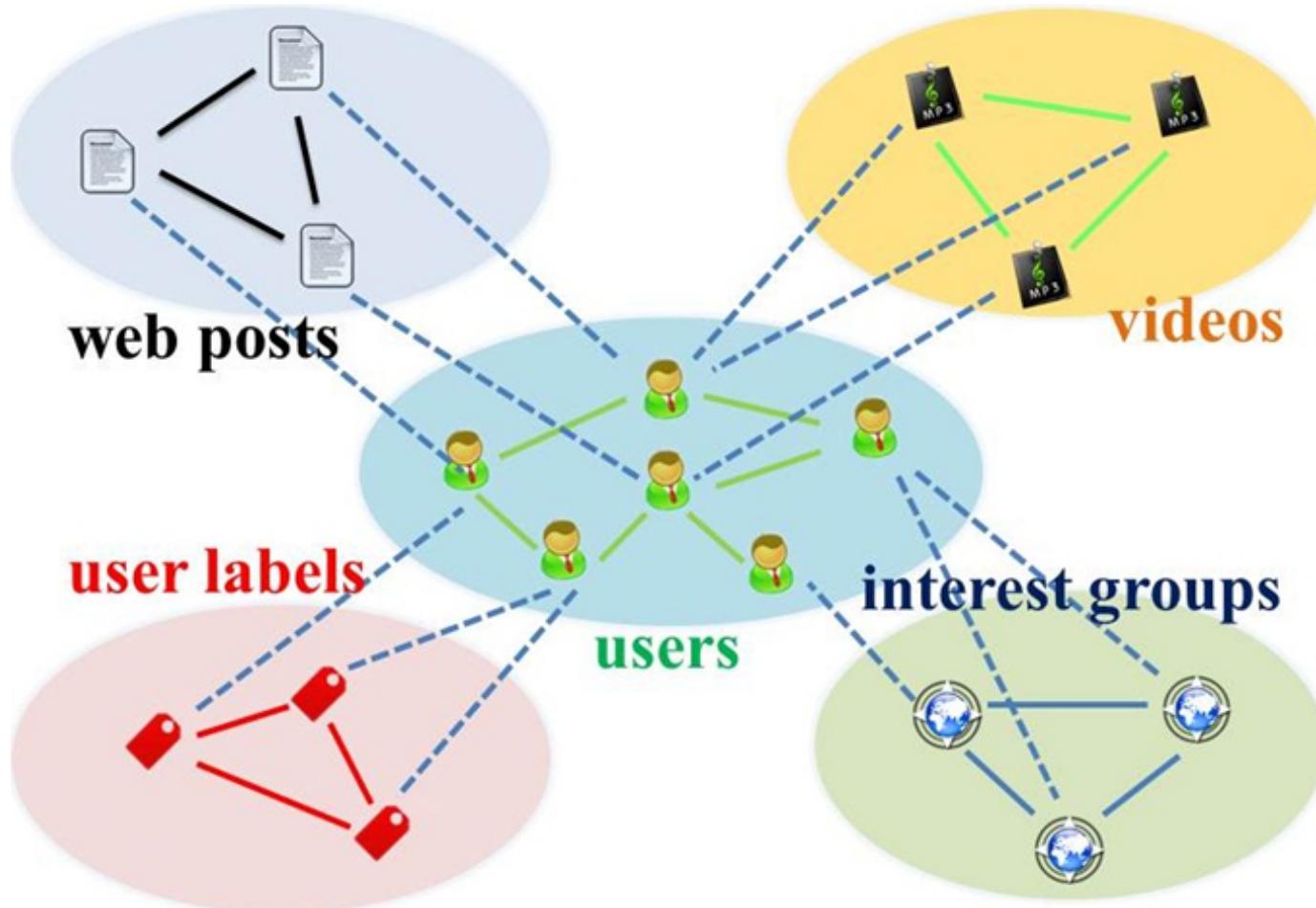
Write Post Add Photo / Video Ask Question Add File

Write something...

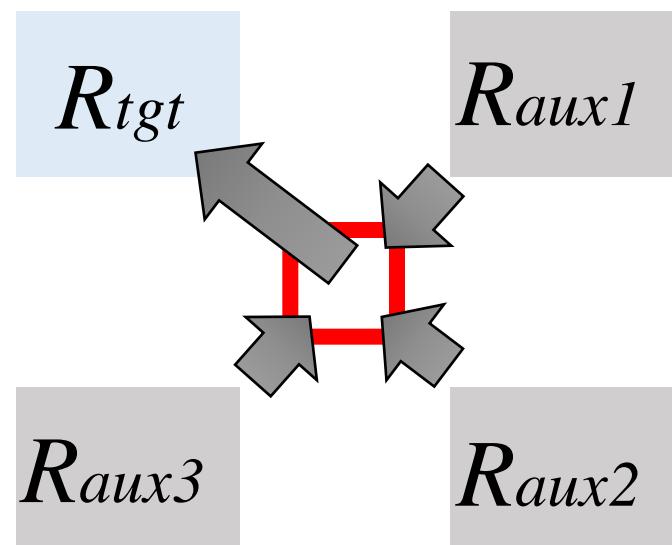
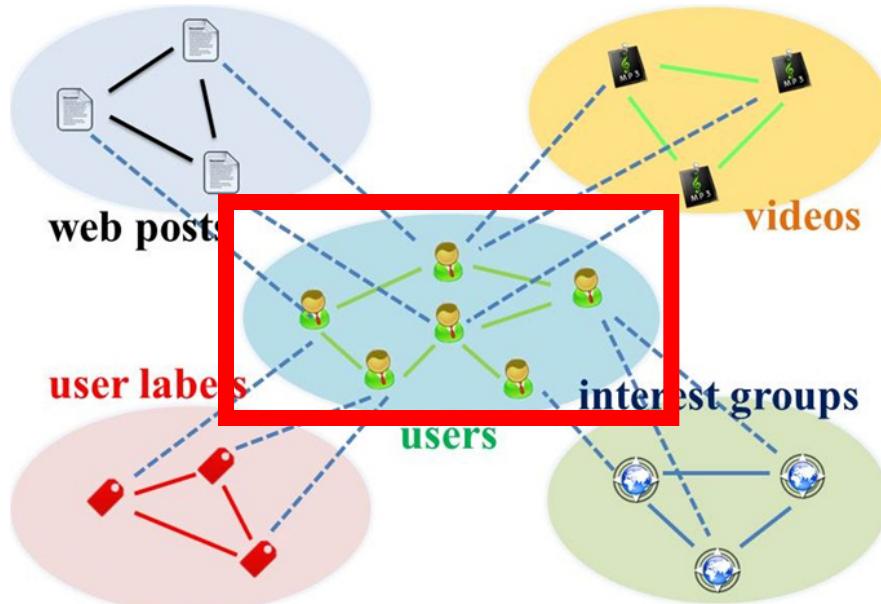
RECENT ACTIVITY

| | |
|---------------------|--|
| Religious Views | Christian |
| Interests | Basketball, writing, spending time w/ kids |
| Favorite Music | Miles Davis, John Coltrane, Bob Dylan, Stevie Wonder, Johann Sebastian Bach (cello suites), and The Fugees |
| Favorite Movies | Casablanca, Godfather I & II, Lawrence of Arabia and One Flew Over the Cuckoo's Nest |
| Favorite TV Shows | Sportscenter |
| Favorite Quotations | "The Arc of the moral universe is long, but it bends towards justice." (MLK) |

Representation: Star-Structured Graph



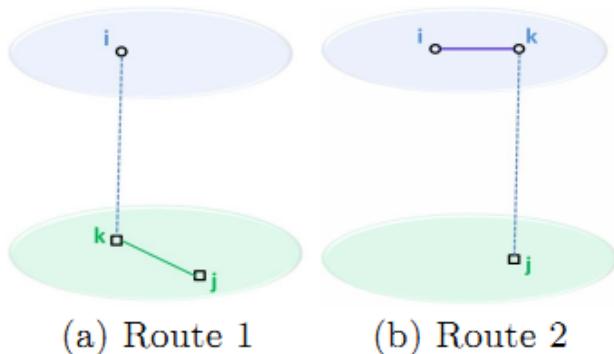
Representation: Social Bridge



Bridge: Tie strength

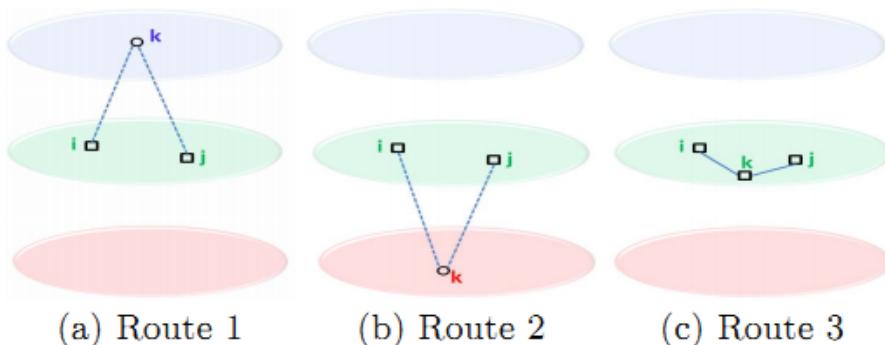
Algorithm: Hybrid Random Walk

□ Updating cross-domain links



$$\begin{aligned}
 p_{ij}^{(\mathcal{UP})+} &= \delta \sum_{u_k \in \mathcal{U}} r_{ik}^{(\mathcal{U})} p_{kj}^{(\mathcal{UP})+} + (1 - \delta) \sum_{p_k \in \mathcal{P}} p_{ik}^{(\mathcal{UP})+} r_{kj}^{(\mathcal{P})} \\
 p_{ij}^{(\mathcal{UP})-} &= \delta \sum_{u_k \in \mathcal{U}} r_{ik}^{(\mathcal{U})} p_{kj}^{(\mathcal{UP})-} + (1 - \delta) \sum_{p_k \in \mathcal{P}} p_{ik}^{(\mathcal{UP})-} r_{kj}^{(\mathcal{P})} \\
 p_{ij}^{(\mathcal{UT})+} &= \eta \sum_{u_k \in \mathcal{U}} r_{ik}^{(\mathcal{U})} p_{kj}^{(\mathcal{UT})+} + (1 - \eta) \sum_{t_k \in \mathcal{T}} p_{ik}^{(\mathcal{UT})+} r_{kj}^{(\mathcal{T})} \\
 \mathbf{P}^{(\mathcal{UP})+}(t+1) &= \delta \mathbf{R}^{(\mathcal{U})}(t) \mathbf{P}^{(\mathcal{UP})+}(t) + (1 - \delta) \mathbf{P}^{(\mathcal{UP})+}(t) \mathbf{R}^{(\mathcal{P})} \\
 \mathbf{P}^{(\mathcal{UP})-}(t+1) &= \delta \mathbf{R}^{(\mathcal{U})}(t) \mathbf{P}^{(\mathcal{UP})-}(t) + (1 - \delta) \mathbf{P}^{(\mathcal{UP})-}(t) \mathbf{R}^{(\mathcal{P})} \\
 \mathbf{P}^{(\mathcal{UT})+}(t+1) &= \eta \mathbf{R}^{(\mathcal{U})}(t) \mathbf{P}^{(\mathcal{UT})+}(t) + (1 - \eta) \mathbf{P}^{(\mathcal{UT})+}(t) \mathbf{R}^{(\mathcal{T})}
 \end{aligned}$$

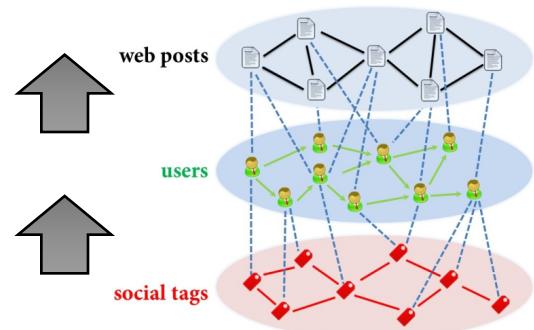
□ Updating within-domain links



$$\begin{aligned}
 r_{ij}^{(\mathcal{U})} &= \tau^{(\mathcal{P})} (\mu \sum_{p_k \in \mathcal{P}} p_{ik}^{(\mathcal{UP})+} p_{jk}^{(\mathcal{UP})+} + (1 - \mu) \sum_{p_k \in \mathcal{P}} p_{ik}^{(\mathcal{UP})-} p_{jk}^{(\mathcal{UP})-}) \\
 &\quad + \tau^{(\mathcal{T})} \sum_{t_k \in \mathcal{T}} p_{ik}^{(\mathcal{UT})+} p_{jk}^{(\mathcal{UT})+} + \tau^{(\mathcal{U})} \sum_{u_k \in \mathcal{U}} r_{ik}^{(\mathcal{U})} r_{kj}^{(\mathcal{U})}
 \end{aligned} \tag{12}$$

$$\begin{aligned}
 \mathbf{R}^{(\mathcal{U})}(t+1) &= \\
 &\quad \tau^{(\mathcal{P})} (\mu \mathbf{P}^{(\mathcal{UP})+}(t) \mathbf{P}^{(\mathcal{UP})+}(t)^T + (1 - \mu) \mathbf{P}^{(\mathcal{UP})-}(t) \mathbf{P}^{(\mathcal{UP})-}(t)^T) \\
 &\quad + \tau^{(\mathcal{T})} \mathbf{P}^{(\mathcal{UT})+}(t) \mathbf{P}^{(\mathcal{UT})+}(t)^T + \tau^{(\mathcal{U})} \mathbf{R}^{(\mathcal{U})}(t) \mathbf{R}^{(\mathcal{U})}(t)^T
 \end{aligned} \tag{13}$$

Results



Comparing with Random Walk with Restarts Models

| Algorithm | MAE | Precision | Recall | F1 | Kendall's $\hat{\tau}$ |
|-----------------------------|---------------------|---------------------|---------------------|---------------------|------------------------|
| HRW | 0.227±1.5e-3 | 0.711±1.3e-3 | 0.921±1.4e-3 | 0.802±1.1e-3 | 0.792±2.5e-3 |
| BRW- R_U -P (TrustWalker) | 0.276±1.1e-3 | 0.657±7.6e-4 | 0.935±9.8e-4 | 0.772±7.6e-4 | 0.774±1.6e-3 |
| BRW- R_U | 0.282±5.3e-3 | 0.655±4.0e-3 | 0.921±1.2e-2 | 0.765±7.7e-3 | 0.725±2.8e-3 |
| BRW- W_U -P | 0.292±1.1e-3 | 0.666±7.0e-4 | 0.900±5.2e-4 | 0.765±6.6e-4 | 0.725±8.5e-4 |
| BRW- W_U (ItemRank) | 0.318±1.4e-3 | 0.671±1.5e-3 | 0.713±2.4e-3 | 0.691±1.2e-3 | 0.661±2.2e-3 |
| BRW-P | 0.438±2.6e-4 | 0.571±3.4e-4 | 0.499±4.2e-4 | 0.532±3.2e-4 | 0.606±2.3e-4 |

Comparing with Social Recommendation Baselines

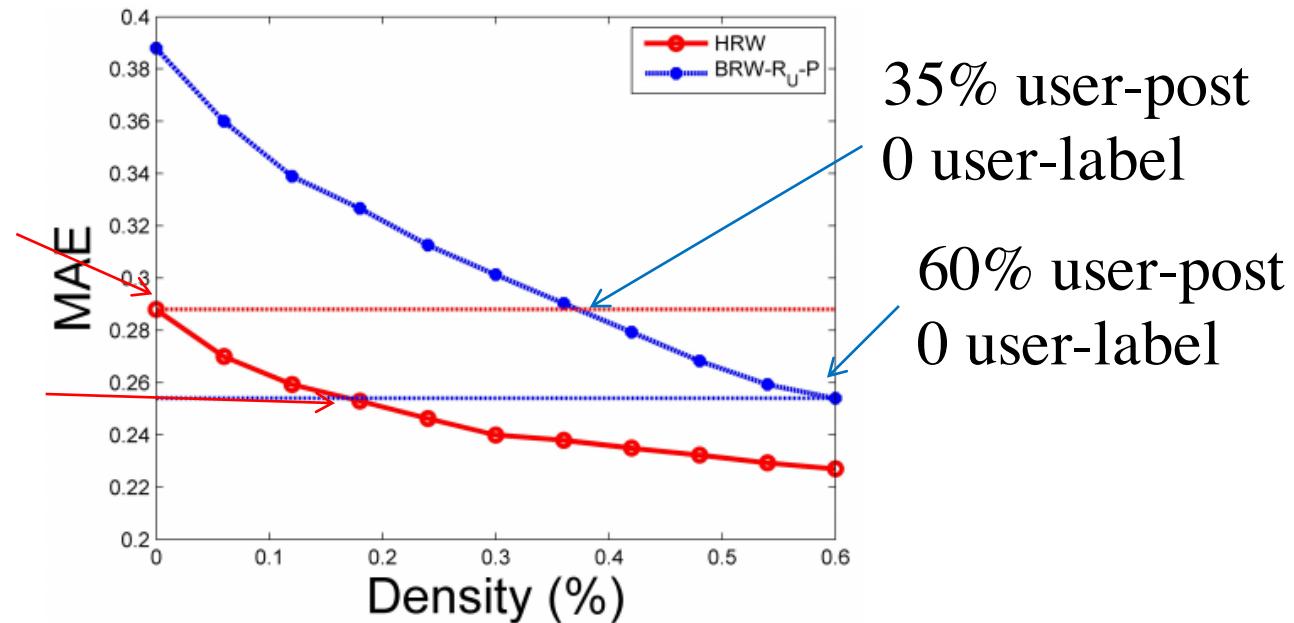
| Algorithm | MAE | Precision | Recall | F1 | Kendall's $\hat{\tau}$ |
|----------------------------------|---------------------|---------------------|---------------------|---------------------|------------------------|
| HRW | 0.227±1.5e-3 | 0.711±1.3e-3 | 0.921±1.4e-3 | 0.802±1.1e-3 | 0.792±2.5e-3 |
| BRW- R_U -P (TrustWalker) [10] | 0.276±1.1e-3 | 0.657±7.6e-4 | 0.935±9.8e-4 | 0.772±7.6e-4 | 0.774±1.6e-3 |
| BRW- W_U (ItemRank) [8] | 0.318±1.4e-3 | 0.671±1.5e-3 | 0.713±2.4e-3 | 0.691±1.2e-3 | 0.661±2.2e-3 |
| MCF [5] | 0.352±2.3e-4 | 0.592±1.8e-3 | 0.951±6.0e-4 | 0.730±1.3e-3 | 0.582±4.3e-4 |
| CF [22] | 0.506±3.4e-4 | 0.552±1.5e-3 | 0.589±7.2e-4 | 0.570±1.0e-3 | 0.540±5.2e-4 |

Results: Insight

- ❑ Knowledge transfer from auxiliary domains improves cold-start users' behavior prediction
 - ❑ Using aux. (label) data, saving **60-70%** tgt. (post) data

0 user-post
100% user-label

18% user-post
100% user-label



Observation: Multiple Platforms



Observation: Cross-Platform

Add Facebook Login to Your App or Website

Facebook Login for Apps is a secure, fast and convenient way for people to log into your app or website.



iOS



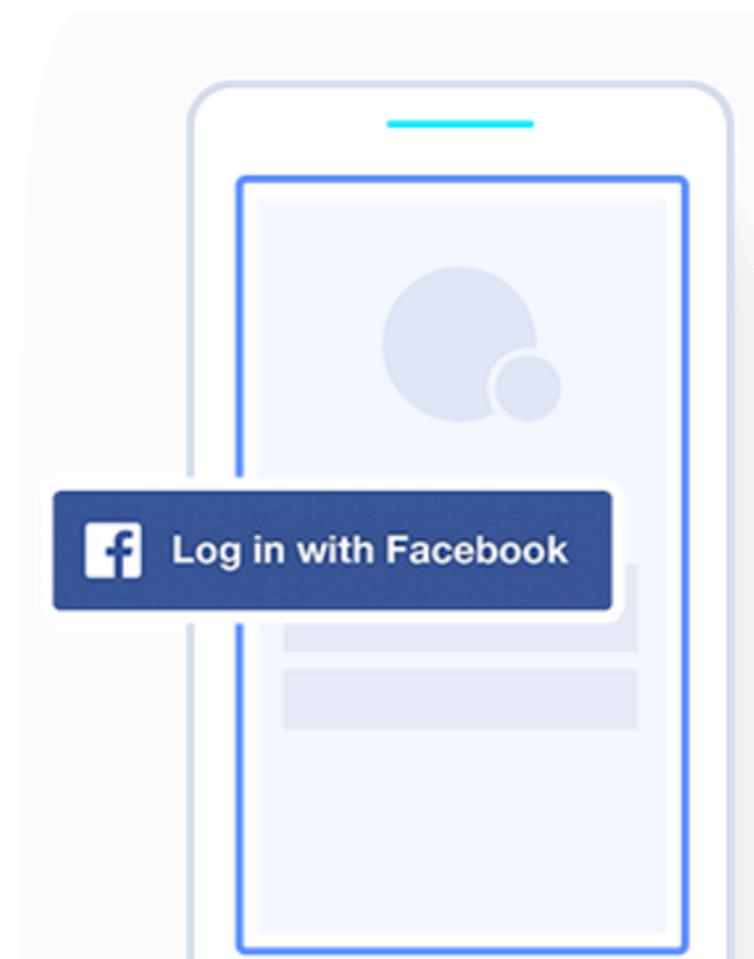
Android



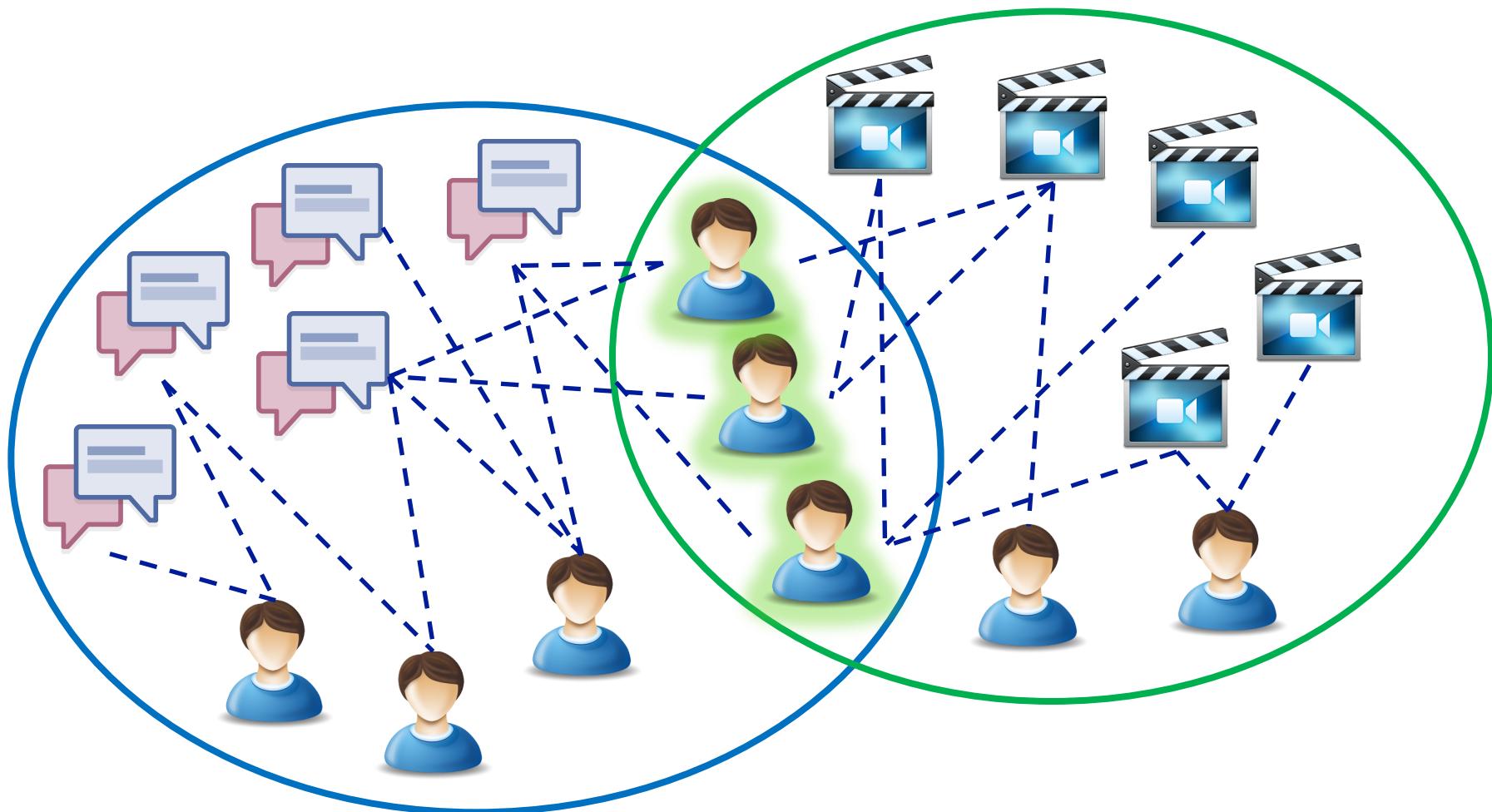
Websites or mobile websites



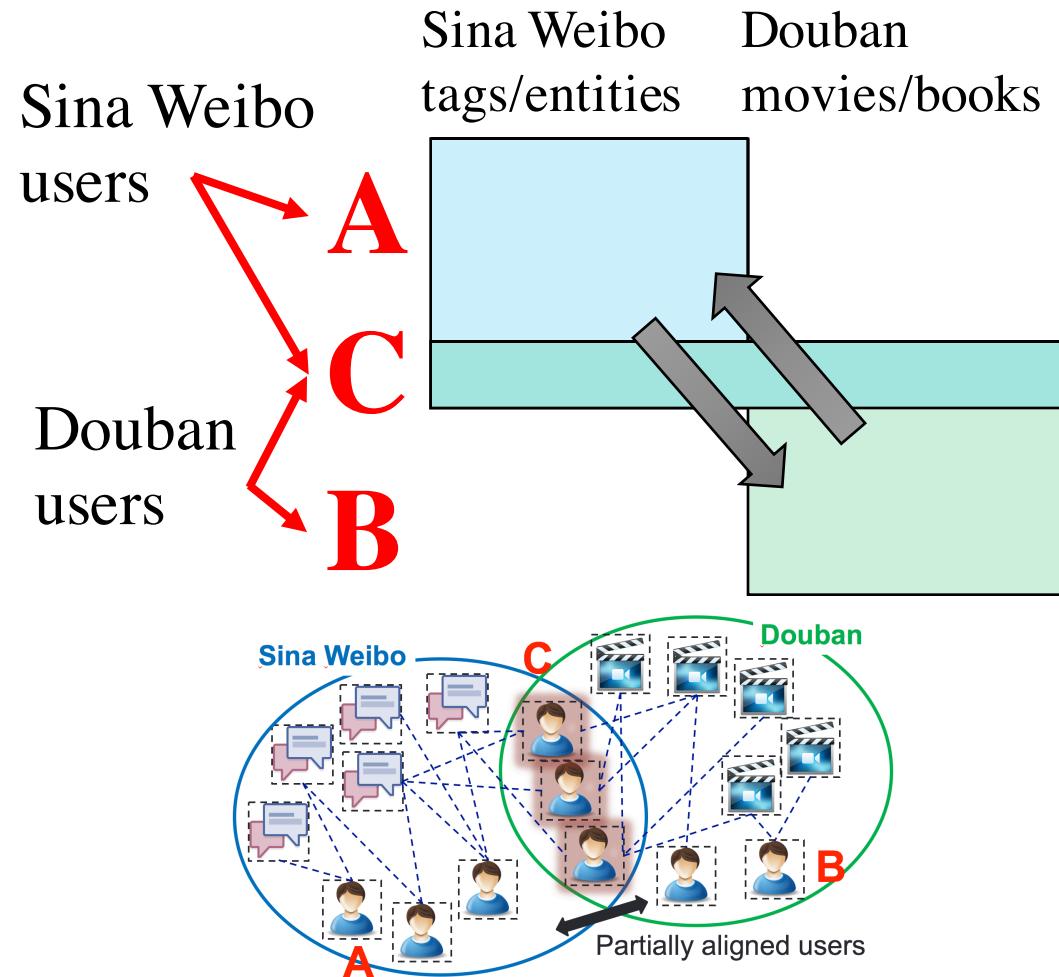
More platforms



Observation: Partially Overlapped Crowds



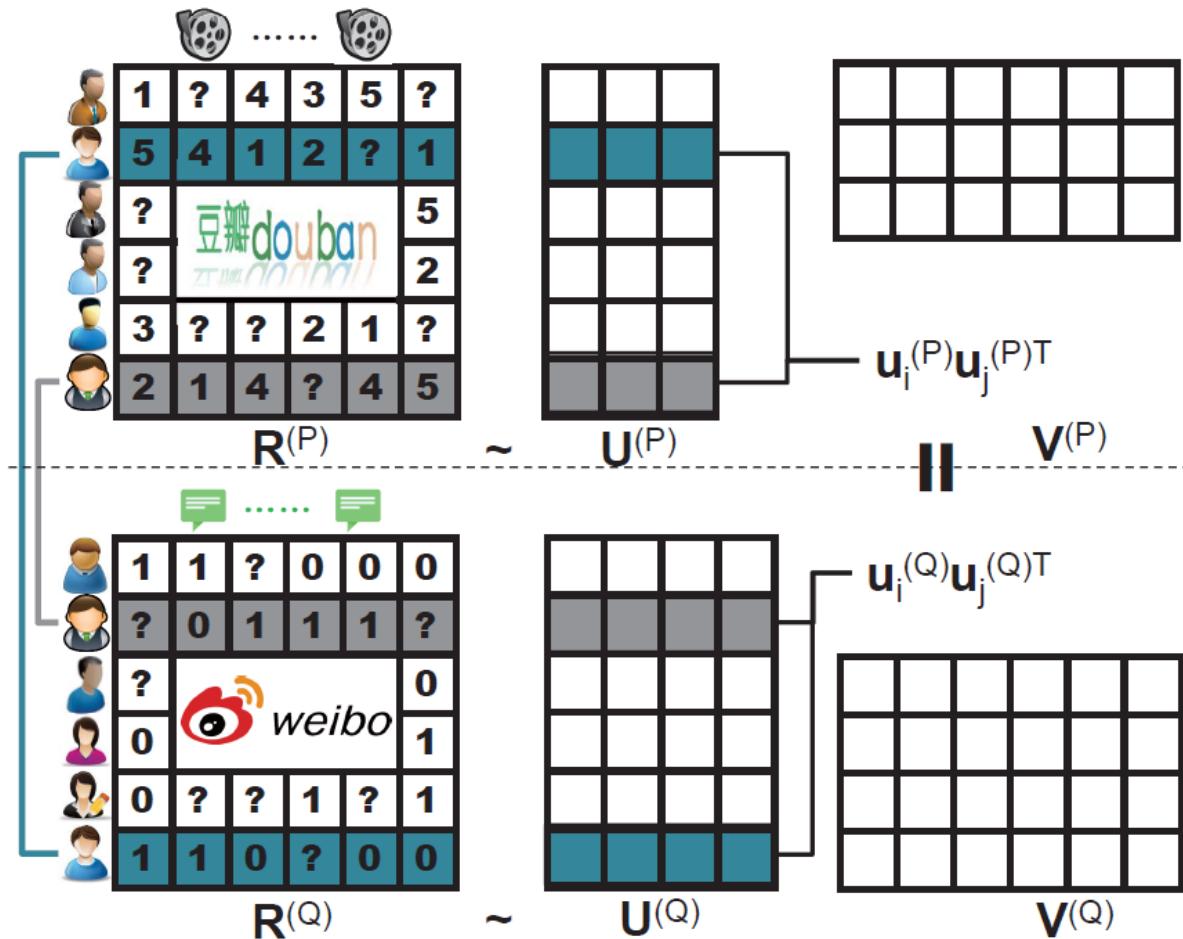
Representation: When NO Transfer



| User set | Weibo tweet entity to Douban movie | RMSE | MAP |
|----------|------------------------------------|--------------|-------|
| A | Auxiliary platform data! | | |
| C | 0.779 | 0.805 | |
| B | 1.439 | | 0.640 |

| User set | Douban book to Weibo social tag | RMSE | MAP |
|----------|---------------------------------|--------------|-------|
| A | | 0.429 | 0.464 |
| C | 0.267 | 0.666 | |
| B | Auxiliary platform data! | | |

Algorithm: XPTTrans



Algorithm: XPTTrans

□ Input

- Tgt./Aux. platform P/Q;
- Behavior data R(P)/R(Q);
- Observation W(P)/W(Q);
- Overlapping indicator W(P,Q),

□ Output

- User latent representation U(P)/U(Q);
- Item latent representation V(P)/V(Q);
- Missing values in R(P)

□ Objective function

Target platform Auxiliary platform

$$\mathcal{J} = \sum_{i,j} W_{i,j}^{(P)} \left(R_{i,j}^{(P)} - \sum_r U_{i,r}^{(P)} V_{r,j}^{(P)} \right)^2 + \lambda \sum_{i,j} W_{i,j}^{(Q)} \left(R_{i,j}^{(Q)} - \sum_r U_{i,r}^{(Q)} V_{r,j}^{(Q)} \right)^2 + \mu \sum_{i_1,j_1,i_2,j_2} W_{i_1,j_1}^{(P,Q)} W_{i_2,j_2}^{(P,Q)} \left(A_{i_1,i_2}^{(P)} - A_{j_1,j_2}^{(Q)} \right)^2$$

Overlapping user similarity
(Pair-wise regularization)

Results: Leveraging Auxiliary Platform Data

NO Transfer

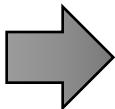
| User set | Weibo tweet entity to Douban movie | |
|----------|------------------------------------|--------------|
| | RMSE | MAP |
| A | Auxiliary platform data! | |
| C | 0.779 | 0.805 |
| B | 1.439 | 0.640 |

| User set | Douban book to Weibo social tag | |
|----------|---------------------------------|--------------|
| | RMSE | MAP |
| A | 0.429 | 0.464 |
| C | 0.267 | 0.666 |
| B | Auxiliary platform data! | |

Transfer via the Same Latent Space

| User set | Weibo tweet entity to Douban movie | |
|----------|------------------------------------|----------------------|
| | RMSE | MAP |
| A | | |
| C | 0.757 | 0.811 |
| B | 1.164 (-19%) | 0.702 (+9.7%) |

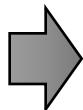
| User set | Douban book to Weibo social tag | |
|----------|---------------------------------|----------------------|
| | RMSE | MAP |
| A | 0.411 (-4.2%) | 0.487 (+5.0%) |
| C | 0.256 | 0.681 |
| B | | |



Results: Leveraging Different Latent Spaces

Transfer via the Same Latent Space

| User set | Weibo tweet entity to Douban movie | |
|----------|------------------------------------|--------------|
| | RMSE | MAP |
| A | | |
| C | 0.757 | 0.811 |
| B | 1.164 | 0.702 |
| User set | Douban book to Weibo social tag | |
| | RMSE | MAP |
| A | 0.411 | 0.487 |
| C | 0.256 | 0.681 |
| B | | |



Transfer via Different Latent Spaces

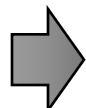
| User set | Weibo tweet entity to Douban movie | |
|----------|------------------------------------|----------------------|
| | RMSE | MAP |
| A | | |
| C | 0.715 | 0.821 |
| B | 0.722 (-38%) | 0.820 (+17%) |
| User set | Douban book to Weibo social tag | |
| | RMSE | MAP |
| A | 0.374 (-11 %) | 0.533 (+12 %) |
| C | 0.236 | 0.705 |
| B | | |

Results: Where Amazing Happens

NO Transfer

| User set | Weibo tweet entity to Douban movie | |
|----------|------------------------------------|-------|
| | RMSE | MAP |
| A | Auxiliary platform data! | |
| C | 0.779 | 0.805 |
| B | 1.439 | 0.640 |

| User set | Douban book to Weibo social tag | |
|----------|---------------------------------|-------|
| | RMSE | MAP |
| A | 0.429 | 0.464 |
| C | 0.267 | 0.666 |
| B | Auxiliary platform data! | |

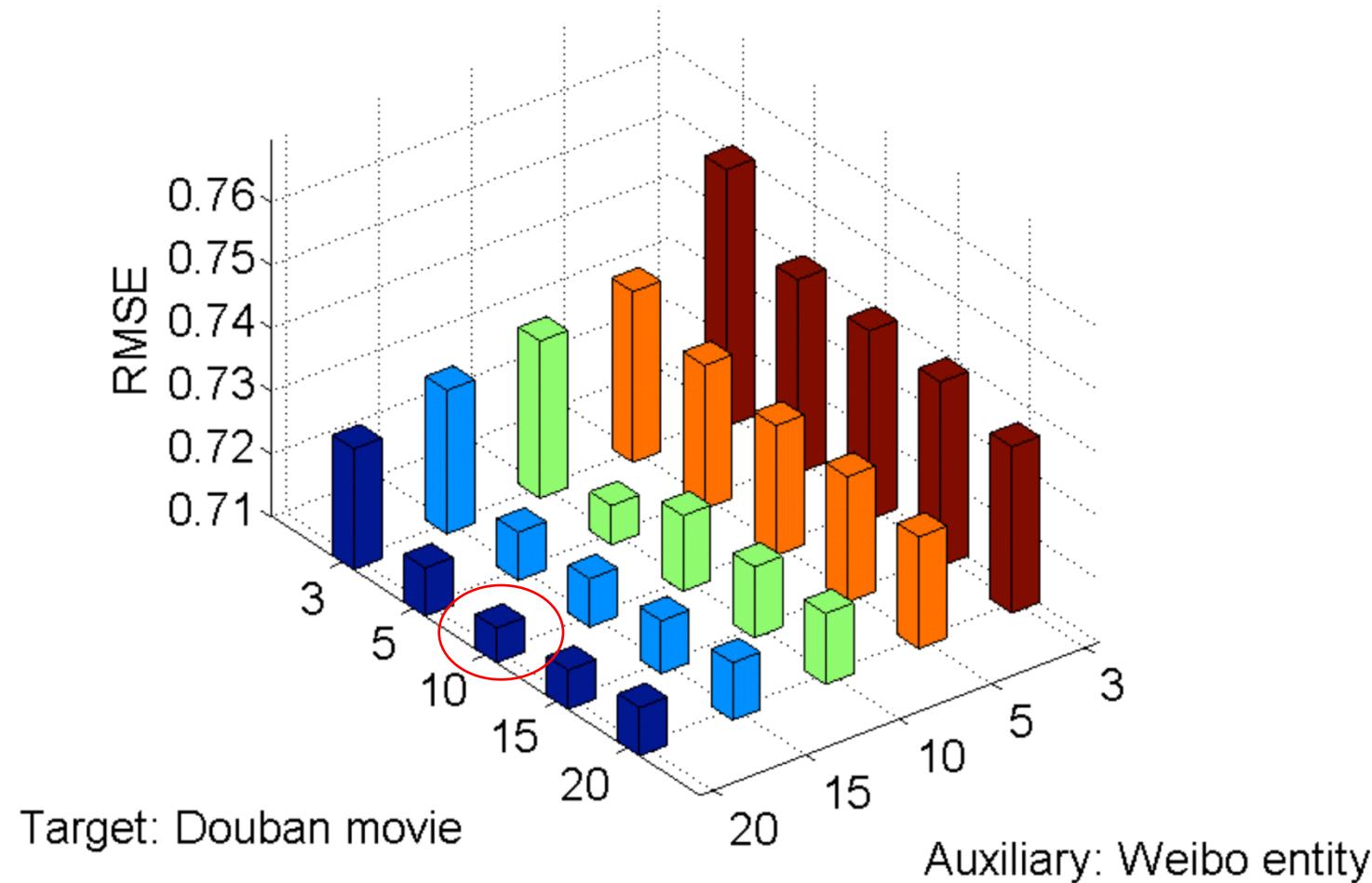


Transfer via Different Latent Spaces

| User set | Weibo tweet entity to Douban movie | |
|----------|------------------------------------|-------|
| | RMSE | MAP |
| A | | |
| C | 0.715 | 0.821 |
| B | 0.722 | 0.820 |

| User set | Douban book to Weibo social tag | |
|----------|---------------------------------|-------|
| | RMSE | MAP |
| A | 0.374 | 0.533 |
| C | 0.236 | 0.705 |
| B | | |

Results: Different Sizes of Latent Spaces





Summary

- ❑ Like, Reply, Share, Retweet, Favorite, Comment ...
- ❑ Memory based social recommenders
 - ❑ TidalTrust, MoleTrust, TrustWalker
- ❑ Model based social recommenders
 - ❑ SoRec, “Social Trust” Ensemble, SoReg
- ❑ **Observations, Representations, Models**
 - ❑ **ContextMF**: Social contexts (preference & influence)
 - ❑ **FEMA**: Spatiotemporal contexts (multidimensional)
 - ❑ **HybridRW**: Cross-domain behavior modeling
 - ❑ **XPTrans**: Cross-platform behavior modeling



Acknowledgement



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Microsoft®
Research
微软亚洲研究院



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Thank you!

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