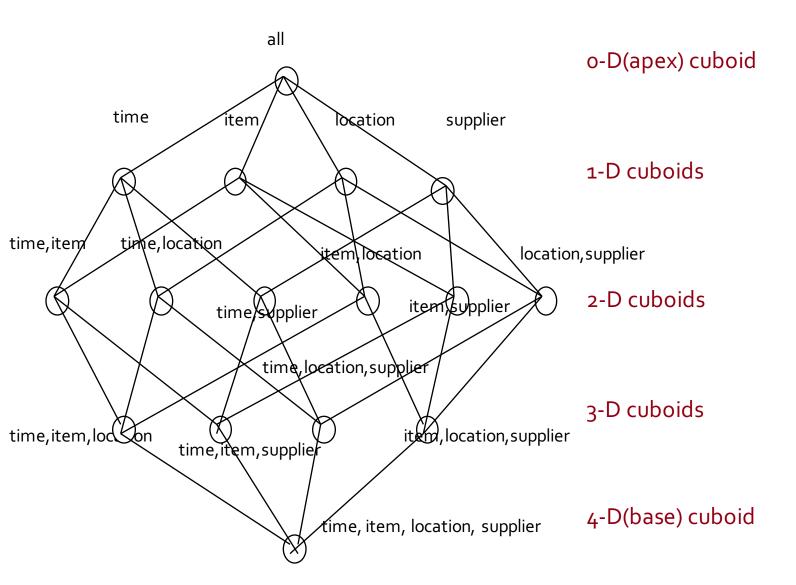


What the hell is that?!!

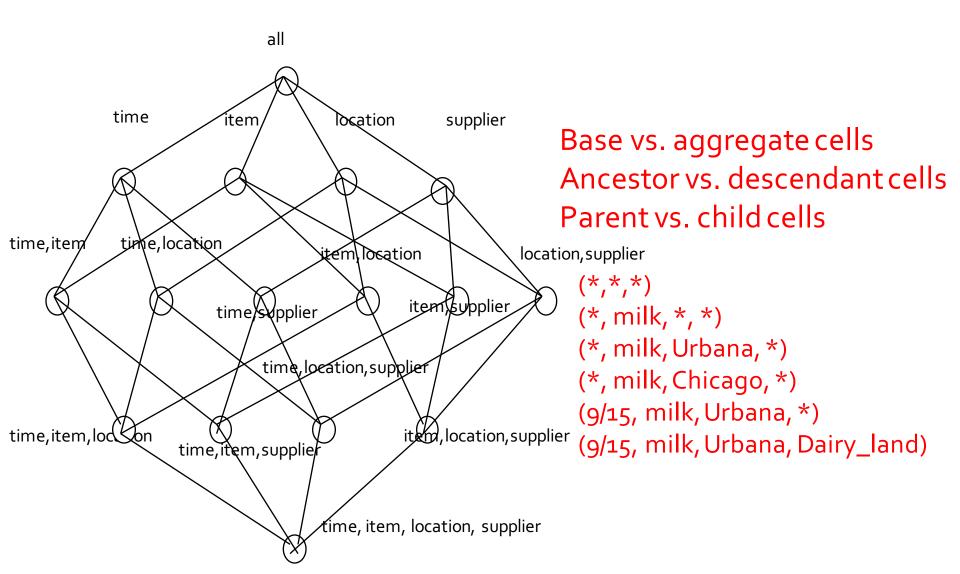
#### Data Cube Technology

- Data Cube Computation: Basic Concepts
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#### Cuboids in Data Cube

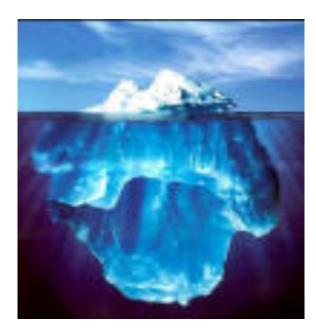


#### Cells in Cuboid



# Cube Materialization: Full Cube vs. Iceberg Cube

- Full cube vs. iceberg cube
  - compute cube sales iceberg as
    select month, city, customer group, count(\*)
    from salesInfo
    cube by month, city, customer group
    having count(\*) >= min support
- Compute only the cells whose measure satisfies the iceberg condition
- Only a small portion of cells may be "above the water" in a sparse cube
- Ex.: Show only those cells whose count is no less than 100



- Advantages of computing iceberg cubes
  - No need to save nor show those cells whose value is below the threshold (iceberg condition)
  - Efficient methods may even avoid computing the un-needed, intermediate cells
  - Avoid explosive growth
- Example: A cube with 100 dimensions
  - Suppose it contains only 2 base cells:  $\{(a_1, a_2, a_3, ..., a_{100}), (a_1, a_2, b_3, ..., b_{100})\}$
  - How many aggregate cells if "having count >= 1"?

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    - Answer:  $(2^{101}-2)-4$

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```
- Answer: (2^{101}-2)-4
```

- What about the iceberg cells, (i.e., with condition: "having count >= 2")?
  - Answer: 4

### Is Iceberg Cube Good Enough? Closed Cube & Cube Shell

- Let cube P have only 2 base cells:  $\{(a_1, a_2, a_3, ..., a_{100}):10, (a_1, a_2, b_3, ..., b_{100}):10\}$ 
  - How many cells will the iceberg cube contain if "having count(\*) ≥ 10"?
    - Answer: 2<sup>101</sup>—4 (still too big!)

#### Close cube:

- A cell c is *closed* if there exists no cell d, such that d is a descendant of c, and d has the same measure value as c
  - Ex. The same cube P has only 3 closed cells:
  - $\{(a_1, a_2, *, ..., *): 20, (a_1, a_2, a_3 ..., a_{100}): 10, (a_1, a_2, b_3, ..., b_{100}): 10\}$
- A closed cube is a cube consisting of only closed cells
- Cube Shell: The cuboids involving only a small # of dimensions, e.g., 2
  - Idea: Only compute cube shells, other dimension combinations can be computed on the fly

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#### Roadmap for Efficient Computation

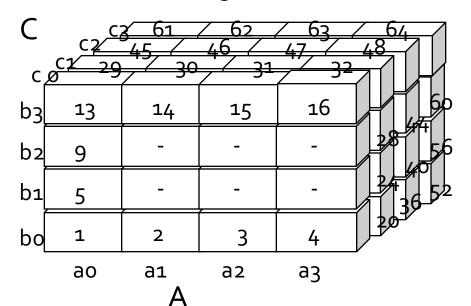
- General computation heuristics (Agarwal et al. '96)
- Computing full/iceberg cubes: 3 methodologies
  - Bottom-Up:
    - Multi-way array aggregation (Zhao, Deshpande & Naughton, SIGMOD'97)
  - Top-down:
    - BUC (Beyer & Ramarkrishnan, SIGMOD'99)
  - Integrating Top-Down and Bottom-Up:
    - Star-cubing algorithm (Xin, Han, Li & Wah: VLDB'03)
- High-dimensional OLAP:
  - A shell-fragment approach (Li, et al. VLDB'04)
- Computing alternative kinds of cubes:
  - Partial cube, closed cube, approximate cube, ......

### Efficient Data Cube Computation: General Heuristics

- Sorting, hashing, and grouping operations are applied to the dimension attributes in order to reorder and cluster related tuples
- Aggregates may be computed from previously computed aggregates, rather than from the base fact table
  - Smallest-child: computing a cuboid from the smallest, previously computed cuboid
  - Cache-results: caching results of a cuboid from which other cuboids are computed to reduce disk I/Os
  - Amortize-scans: computing as many as possible cuboids at the same time to amortize disk reads
  - Share-sorts: sharing sorting costs cross multiple cuboids when sortbased method is used
  - Share-partitions: sharing the partitioning cost across multiple cuboids when hash-based algorithms are used

# Cube Computation: Multi-Way Array Aggregation (MOLAP)

- Bottom-up: Partition a huge sparse array into chunks (a small subcube which fits in memory) and aggregation.
- Data addressing: Compressed sparse array addressing (chunk\_id, offset)
- Compute aggregates in "multiway" by visiting cube cells in the order which minimizes the # of times to visit each cell, and reduces memory access and storage cost



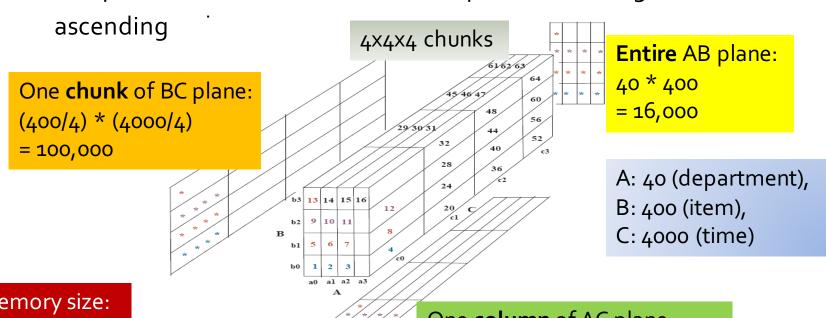
What is the best traversing order to do multi-way aggregation?

E

# Multi-way Array Aggregation (3-D to 2-D)

- How to minimizes the memory requirement and reduced I/Os?
  - Keep the smallest plane in main memory
  - Fetch and compute only one chunk at a time for the largest plane

The planes should be sorted and computed according to their size in



Min memory size: 156,000 < ... < 64,000,000

One **column** of AC plane: 40 \* (4000/4) = 40,000

### Multi-Way Array Aggregation

- Array-based "bottom-up" algorithm (from ABC to AB,...)
- Using multi-dimensional chunks
- Simultaneous aggregation on multiple dimensions
- Intermediate aggregate values are re-used for computing ancestor cuboids
- Cannot do Apriori pruning: No iceberg optimization
- Comments on the method
  - Efficient for computing the full cube for a small number of dimensions
  - If there are a large number of dimensions, "top-down"
     computation and iceberg cube computation methods (e.g., BUC)
     should be used

All

**AC** 

ABC

AB

### Cube Computation: Computing in Reverse Order

BUC (Beyer & Ramakrishnan, SIGMOD'99)

BUC: acronym of Bottom-Up (cube) Computation

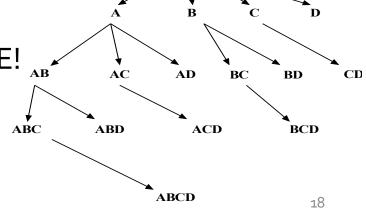
(Note: It is "top-down" in our view since we put Apex cuboid on the top!)

 Divides dimensions into partitions and facilitates iceberg pruning (it works now!)

 If a partition does not satisfy min\_sup, its descendants can be pruned

— If min\_sup = 1 b compute full CUBE!

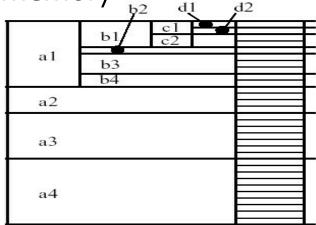
No simultaneous aggregation



all

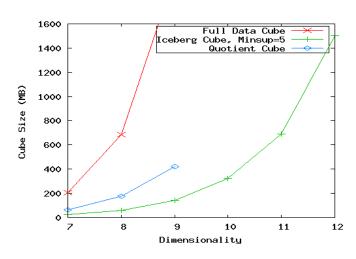
### BUC: Partitioning and Aggregating

- Usually, entire data set cannot fit in main memory
- Sort distinct values
  - partition into blocks that fit
- Continue processing
- Optimizations
  - Partitioning
    - External Sorting, Hashing, Counting Sort
  - Ordering dimensions to encourage pruning
    - Cardinality, Skew, Correlation
  - Collapsing duplicates
    - Cannot do holistic aggregates anymore!



## High-Dimensional OLAP? — The Curse of Dimensionality

- High-DOLAP: Needed in many applications
  - Science and engineering analysis
  - Bio-data analysis: thousands of genes
  - Statistical surveys: hundreds of variables
- None of the previous cubing method can handle high dimensionality!
  - Iceberg cube and compressed cubes: only delay the inevitable explosion
  - Full materialization: still significant overhead in accessing results on disk
- A shell-fragment approach: X. Li, J. Han, and H. Gonzalez, High-Dimensional OLAP: A Minimal Cubing Approach, VLDB'04



A curse of dimensionality: A database of 600,000 tuples. Each dimension has cardinality of 100 and *zipf* of 2.

# Fast High-Dimensional OLAP with Minimal Cubing

- Observation: OLAP occurs only on a small subset of dimensions at a time
- Semi-Online Computational Model
  - Partition the set of dimensions into shell fragments
  - Compute data cubes for each shell fragment while retaining inverted indices or value-list indices
  - Given the pre-computed fragment cubes, dynamically compute cube cells of the high-dimensional data cube online
- Major idea: Tradeoff between the amount of pre-computation and the speed of online computation
  - Reducing computing high-dimensional cube into precomputing a set of lower dimensional cubes
  - Online re-construction of original high-dimensional space
  - Lossless reduction

# Computing a 5-D Cube with 2-Shell Fragments

• Example: Let the cube aggregation function be count

tid	Α	В	С	D	E
1	a1	b1	C1	d1	<b>e</b> 1
2	a1	b2	C1	d2	e1
3	a1	b2	C1	d1	e2
4	a2	b1	C1	d1	e2
5	a2	b1	C1	d1	ез

•	Divide the 5-D table into
	2 shell fragments:

- (A, B, C) and (D, E)
- Build traditional invert index (TID) or RID list

Attribute Value	TID List	List Size
a1	123	3
a2	45	2
b1	145	3
b2	2 3	2
C1	12345	5
d1	1345	4
d2	2	1
e1	12	2
e2	3 4	2
ез	5	1

### Shell Fragment Cubes: Ideas

- Generalize the 1-D inverted indices to multi-dimensional inverted indices in the data cube sense
- Compute all cuboids for data cubes ABC and DE while retaining the inverted indices

Attribute Value	TID List	List Size
a1	123	3
a2	4 5	2
b1	145	3
b2	2 3	2
C1	12345	5
d1	1345	4
d2	2	1
e1	12	2
e2	3 4	2
ез	5	1

Cell	Intersection	TID List	List Size
a1 b1	123∩145	1	1
a1 b2	123∩23	2 3	2
a2 b1	45∩145	45	2
a2 b2	45∩23	ф	0

Cell	Intersection	TID List	List Size
d1 e1	?	?	?
d1 e2	?	?	?
d1 e3	?	?	?
d2 e1	?	?	?

Answer: <a href="http://hanj.cs.illinois.edu/pdf/vldbo4\_hdolap.pdf">http://hanj.cs.illinois.edu/pdf/vldbo4\_hdolap.pdf</a>

#### Shell Fragment Cubes: Size and Design

- Given a database of T tuples, D dimensions, and F shell fragment size, the fragment cubes' space requirement is:
  - For **F** < 5, the growth is sub-linear  $O\left(T\left[\frac{D}{F}\right](2^F-1)\right)$
- Shell fragments do not have to be disjoint
- Fragment groupings can be arbitrary to allow for maximum online performance
  - Known common combinations (e.g., <city, state>) should be grouped together
- Shell fragment sizes can be adjusted for optimal balance between offline and online computation

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### Data Mining in Cube Space

- Data cube greatly increases the analysis bandwidth
- Four ways to interact OLAP-styled analysis and data mining
  - Using cube space to define data space for mining
  - Using OLAP queries to generate features and targets for mining, e.g., multi-feature cube
  - Using data-mining models as building blocks in a multi-step mining process, e.g., prediction cube
  - Using data-cube computation techniques to speed up repeated model construction
    - Cube-space data mining may require building a model for each candidate data space
    - Sharing computation across model-construction for different candidates may lead to efficient mining

### Complex Aggregation at Multiple Granularities: Multi-Feature Cubes

- Multi-feature cubes (Ross, et al. 1998): Compute complex queries involving multiple dependent aggregates at multiple granularities
- Ex. Grouping by all subsets of {item, region, month}, find the maximum price in 2010 for each group, and the total sales among all maximum price tuples

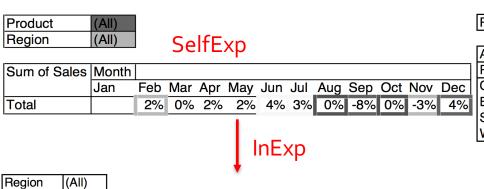
```
select item, region, month, max(price), sum(R.sales)
from purchases
where year = 2010
cube by item, region, month: R
such that R.price = max(price)
```

 Continuing the last example, among the max price tuples, find the min and max shelf life, and find the fraction of the total sales due to tuple that have min shelf life within the set of all max price tuples

### Discovery-Driven Exploration of Data Cubes

- Discovery-driven exploration of huge cube space (Sarawagi, et al.'98)
  - Effective navigation of large OLAP data cubes
  - Pre-compute measures indicating exceptions, guide user in the data analysis, at all levels of aggregation
  - Exception: significantly different from the value anticipated, based on a statistical model
  - Visual cues such as background color are used to reflect the degree of exception of each cell
- Kinds of exceptions
  - SelfExp: represents the surprise value of the cell relative to other cells at same level of aggregation
  - InExp: represents the degree of surprise somewhere beneath this cell if we drill down from the cell
  - PathExp: represents the degree of surprise for each drilldown path from the cell

#### Exceptions: SelfExp, InExp, PathExp



Product	Diet-S

Avg.Sales	Month											
	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
С		0%	-2%	0%	1%	4%	1%	5%	-6%	2%	-2%	-2%
E		0%	2%	-8%	7%	0%	5%	-40%	10%	-33%	2%	8%
s		0%	-1%	3%	-2%	2%	-2%	19%	-1%	12%	-1%	0%
C E S W		5%	1%	0%	-2%	6%	6%	2%	-17%	9%	-7%	2%

Avg.Sales	Month												
Product	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec	
Birch-B		10%	-7%	3%	-4%	15%	-12%	-3%	1%	42%	-14%	-10%	
Chery-S		1%	1%	4%	3%	5%	5%	-9%	-12%	1%	-5%	5%	
Cola		-1%	2%	3%	4%	9%	4%	1%	-11%	-8%	-2%	7%	
Cream-S		3%	1%	6%	3%	3%	8%	-3%	-12%	-2%	1%	10%	
Diet-B		1%	1%	-1%	2%	1%	2%	0%	-6%	-1%	-4%	2%	I
Diet-C		3%	2%	5%	2%	4%	7%	-7%	-12%	-2%	-2%	8%	
Diet-S		2%	-1%	0%	0%	4%	2%	4%	-9%	5%	-3%	0%	_
Grape-S		1%	1%	0%	4%	5%	1%	3%	-9%	-1%	-8%	4%	4
Jolt-C		-1%	-4%	2%	2%	0%	-4%	2%	6%	-2%	0%	0%	Ľ
Kiwi-S		2%	1%	4%	1%	-1%	3%	-1%	-4%	4%	0%	1%	ľ
Old-B		4%	-1%	0%	1%	5%	2%	7%	-10%	3%	-3%	1%	Į
Orang-S		1%	1%	3%	4%	2%	1%	-1%	-1%	-6%	-4%	9%	ŀ
Sasprla		-1%	2%	1%	3%	-3%	5%	-10%	-2%	-1%	1%	5%	b

Market	(All)
Product	Cola

Avg.Sales	Month											
	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
С		3%	1%	4%	1%	4%	10%	-11%	-14%	-3%	5%	11%
[E		-3%	3%	4%	4%	13%	2%	0%	-10%	-13%	-3%	8%
S		2%	-1%	1%	9%	6%	3%	21%	-15%	1%	-5%	4%
C E S W		-2%	2%	2%	4%	12%	1%	1%	-9%	-11%	-4%	6%

#### Summary

- Data Cube Computation: Preliminary Concepts
- Data Cube Computation Methods
  - Multi-Way Array Aggregation
  - BUC
  - High-Dimensional OLAP with Shell-Fragments
- Multidimensional Data Analysis in Cube Space
  - Multi-feature Cubes
  - Discovery-Driven Exploration of Data Cubes

#### References

- S. Agarwal, R. Agrawal, P. M. Deshpande, A. Gupta, J. F. Naughton, R. Ramakrishnan, and S. Sarawagi. On the computation of multidimensional aggregates. VLDB'96
- K. Beyer and R. Ramakrishnan. Bottom-Up Computation of Sparse and Iceberg CUBEs... SIGMOD'99
- J. Han, J. Pei, G. Dong, K. Wang. Efficient Computation of Iceberg Cubes With Complex Measures. SIGMOD'01
- L. V. S. Lakshmanan, J. Pei, and J. Han, Quotient Cube: How to Summarize the Semantics of a Data Cube, VLDB'02
- X. Li, J. Han, and H. Gonzalez, High-Dimensional OLAP: A Minimal Cubing Approach, VLDB'04
- X. Li, J. Han, Z. Yin, J.-G. Lee, Y. Sun, "Sampling Cube: A Framework for Statistical OLAP over Sampling Data", SIGMOD'08
- K. Ross and D. Srivastava. Fast computation of sparse datacubes. VLDB'97
- D. Xin, J. Han, X. Li, B. W. Wah, Star-Cubing: Computing Iceberg Cubes by Top-Down and Bottom-Up Integration, VLDB'03
- Y. Zhao, P. M. Deshpande, and J. F. Naughton. An array-based algorithm for simultaneous multidimensional aggregates. SIGMOD'97
- D. Burdick, P. Deshpande, T. S. Jayram, R. Ramakrishnan, and S. Vaithyanathan. OLAP over uncertain and imprecise data. VLDB'05

#### References (cont.)

- R. Agrawal, A. Gupta, and S. Sarawagi. Modeling multidimensional databases. ICDE'97
- B.-C. Chen, L. Chen, Y. Lin, and R. Ramakrishnan. Prediction cubes. VLDB'05
- B.-C. Chen, R. Ramakrishnan, J.W. Shavlik, and P. Tamma. Bellwether analysis: Predicting global aggregates from local regions. VLDB'06
- Y. Chen, G. Dong, J. Han, B. W. Wah, and J. Wang, Multi-Dimensional Regression Analysis of Time-Series Data Streams, VLDB'02
- R. Fagin, R. V. Guha, R. Kumar, J. Novak, D. Sivakumar, and A. Tomkins. Multi-structural databases. PODS'05
- J. Han. Towards on-line analytical mining in large databases. SIGMOD Record, 27:97–107, 1998
- T. Imielinski, L. Khachiyan, and A. Abdulghani. Cubegrades: Generalizing association rules. Data Mining & Knowledge Discovery, 6:219–258, 2002.
- R. Ramakrishnan and B.-C. Chen. Exploratory mining in cube space. Data Mining and Knowledge Discovery, 15:29–54, 2007.
- K.A. Ross, D. Srivastava, and D. Chatziantoniou. Complex aggregation at multiple granularities. EDBT'98
- S. Sarawagi, R. Agrawal, and N. Megiddo. Discovery-driven exploration of OLAP data cubes. EDBT'98
- G. Sathe and S. Sarawagi. Intelligent Rollups in Multidimensional OLAP Data. *VLDB'01*