



# Data-Driven Behavioral Analytics: Observations, Representations and Models

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<http://www.meng-jiang.com/tutorial-cikm16.html>



# I. Mining behavior networks with social and spatiotemporal contexts

## I.1. Behavior prediction and recommendation



# Behavior in Social Networks

## ❑ Facebook: Post, Like, Comment, Share

Update Status | Add Photos/Videos | Create Photo Album

What's on your mind?

Public Post

132 Likes 20 Comments

Like

Comment

Share

## ❑ Twitter: Post, Reply, Retweet, Favorite

What's happening?

Media Location 140 Tweet

5

7

## ❑ YouTube: Upload, Subscribe, Download, Share, Comment



Top 10 NBA Plays: October 18

NBA Subscribed 6,434,753 Download 720 126,540

Add to Share More

2,468 24

# Behavior in Social Networks



Like  
Reply  
Share  
Favorite  
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# Social Recommender Systems

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## Recommended



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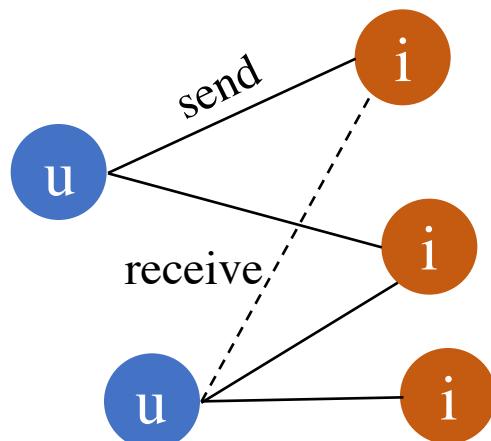


Facebook

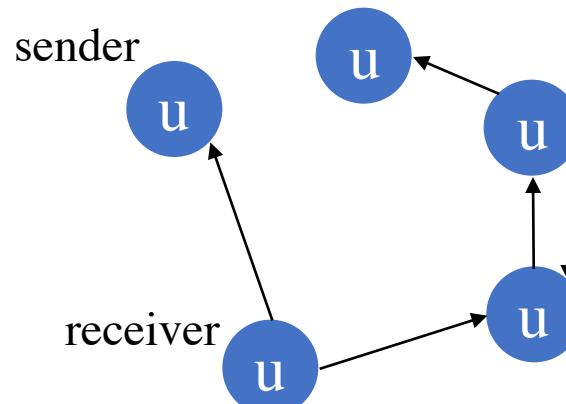
# Social Recommender Systems

- ❑ April 20, 2011: Tencent Weibo visited Tsinghua University
  - ❑ Low *conversion rate* (< 6%): #retweets per feed request
  - ❑ Can we build a *social recommender system*?
  - ❑ Given

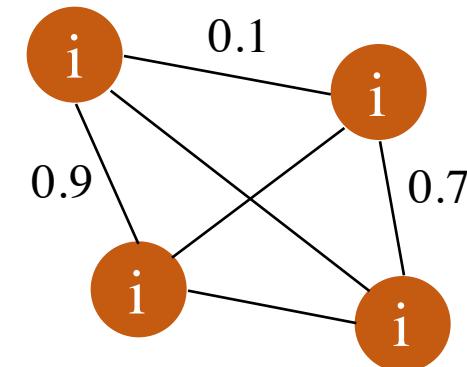
User-item behavior network



User-user social network



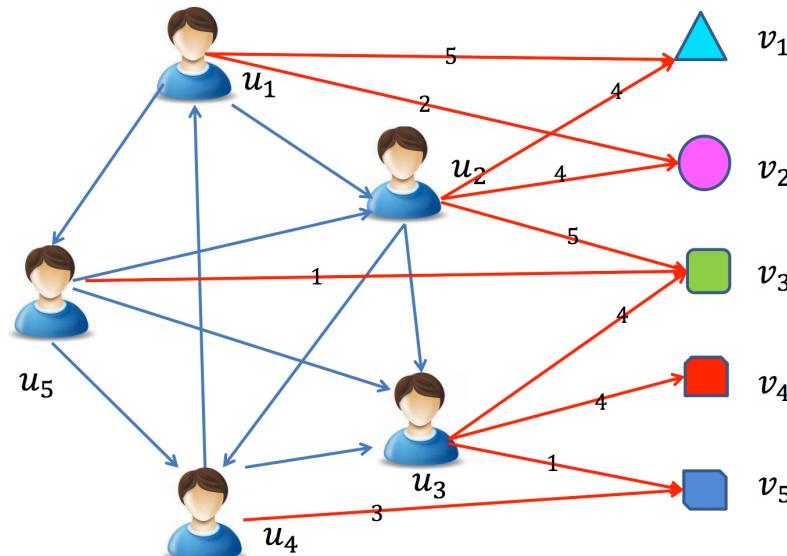
Content similarity  
(topic level) [Blei *et al.*]



- ❑ Predict which tweet/item a user will retweet.

# Traditional Recommender Systems

- ❑ Assumed that users are independent and identically distributed (user-movie, user-book, *etc.*)



	$v_1$	$v_2$	$v_3$	$v_4$	$v_5$
$u_1$	5	?	2	?	?
$u_2$	4	4	5	?	?
$u_3$	?	?	4	4	1
$u_4$	?	?	?	?	3
$u_5$	?	?	1	?	?

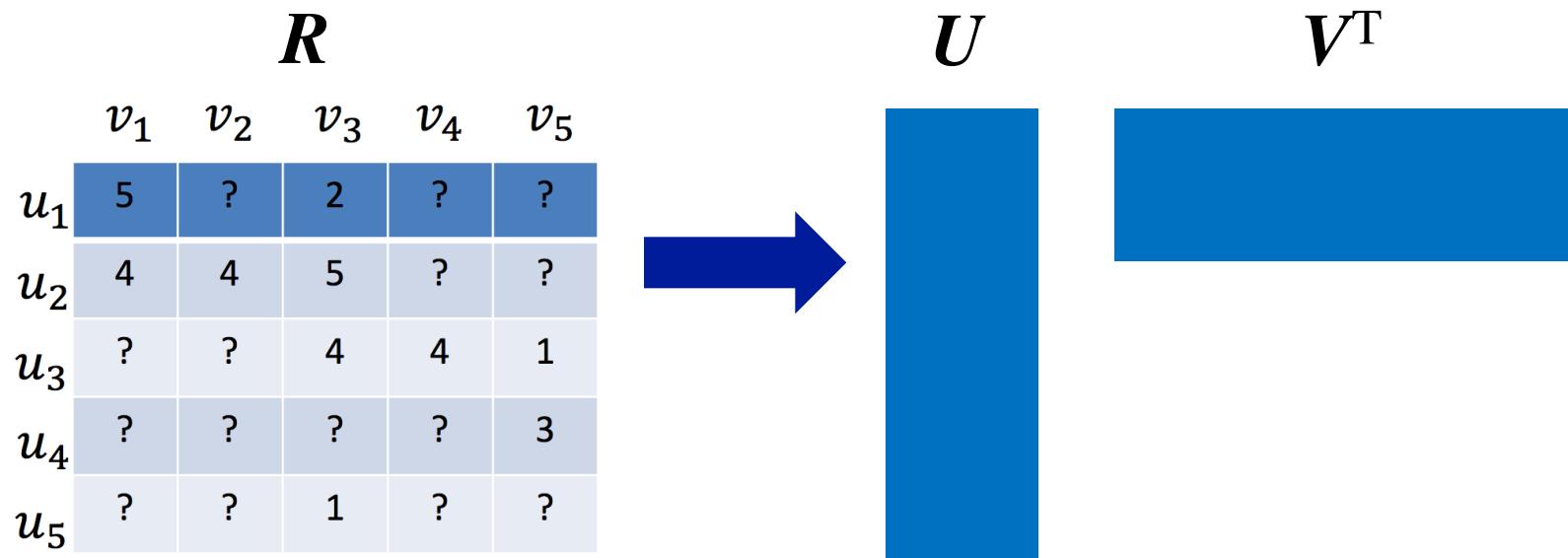


# Traditional Recommender Systems

- ❑ Content-based recommender (e.g., TF-IDF)
  - ❑ For textual information (e.g., news, documents)
  - ❑ *Limitation: limited content analysis, over-specialization*
- ❑ Collaborative filtering based recommender
  - ❑ Memory-based CF (e.g., PCC, similarity)
  - ❑ Model-based CF (e.g., factorization based)
  - ❑ *Limitation: data sparsity, cold-start problem*
- ❑ Hybrid recommender system

# Matrix Factorization (MF) based CF

- Low-rank MF on the user-item rating matrix  $R$
- User preference vector  $U$
- Item characteristic vector  $V$



# Matrix Factorization (MF) based CF

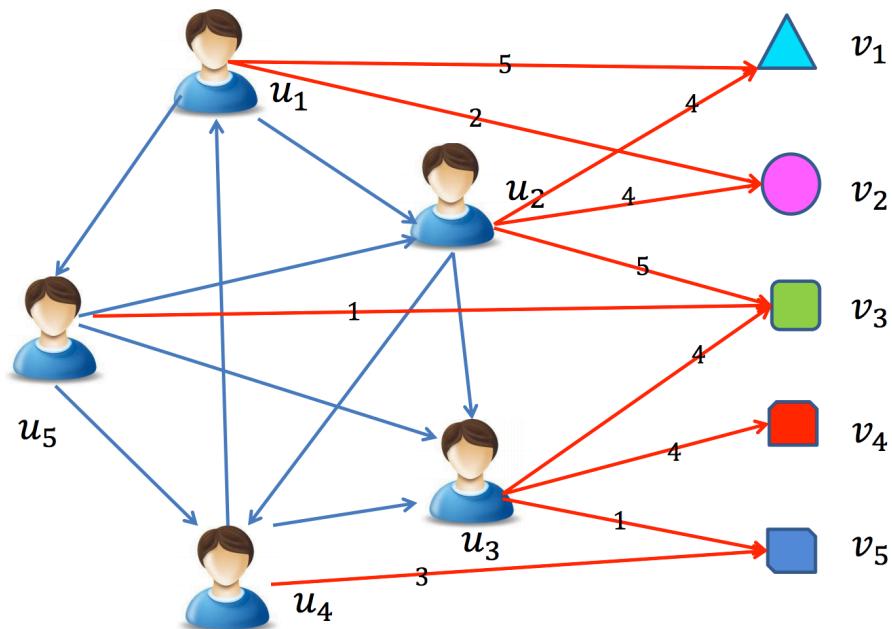
- Low-rank MF on the user-item rating matrix  $R$
- User preference vector  $U$
- Item characteristic vector  $V$
- Observed weight matrix  $W$

$$\min_{\mathbf{U}, \mathbf{V}} \sum_{i=1}^n \sum_{j=1}^m \boxed{\mathbf{W}_{ij}} (\mathbf{R}_{ij} - \mathbf{U}_i \mathbf{V}_j^\top)^2 + \boxed{\alpha(\|\mathbf{U}\|_F^2 + \|\mathbf{V}\|_F^2)}$$

avoid **over-fitting**,  
controlled by the **parameter**

# Social Recommendation

Social relations



	$u_1$	$u_2$	$u_3$	$u_4$	$u_5$
$u_1$	0	1	0	0	1
$u_2$	0	0	1	1	0
$u_3$	0	0	0	0	0
$u_4$	1	0	1	0	0
$u_5$	0	1	1	1	0

	$v_1$	$v_2$	$v_3$	$v_4$	$v_5$
$u_1$	5	?	2	?	?
$u_2$	4	4	5	?	?
$u_3$	?	?	4	4	1
$u_4$	?	?	?	?	3
$u_5$	?	?	1	?	?

# Memory based Social Recommender

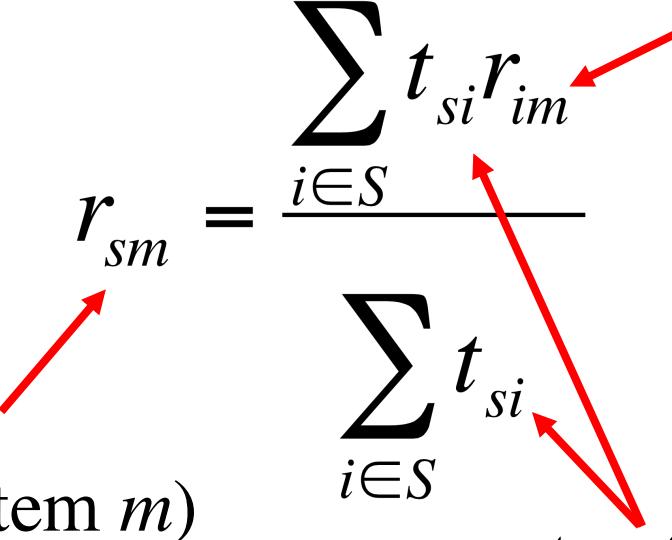
## □ TidalTrust

$$r_{sm} = \frac{\sum_{i \in S} t_{si} r_{im}}{\sum_{i \in S} t_{si}}$$

rating (user  $i$ , item  $m$ )

rating (user  $s$ , item  $m$ )

trust from social relation (user  $s$ , user  $i$ )



# Memory based Social Recommender

## □ MoleTrust

$$p_{a,i} = \bar{r}_a + \frac{\sum_{u=1}^k w_{a,u}(r_{u,i} - \bar{r}_u)}{\sum_{u=1}^k w_{a,u}}$$

average rating (user  $a$ )

rating (user  $u$ , item  $i$ )

predicted rating (user  $a$ , item  $i$ )

trust from social relation (user  $a$ , user  $u$ )

average rating (user  $u$ )

The diagram illustrates the MoleTrust formula with red arrows indicating the flow of information from the labels to the terms in the equation. The labels are: 'average rating (user  $a$ )', 'rating (user  $u$ , item  $i$ )', 'predicted rating (user  $a$ , item  $i$ )', and 'trust from social relation (user  $a$ , user  $u$ )'. The first two labels point to the terms  $\bar{r}_a$  and  $r_{u,i}$  respectively. The third label points to the entire fraction. The fourth label points to the term  $w_{a,u}$ .

# Memory based Social Recommender

## □ TrustWalker

probability of  
user  $u$ 's random walk  
from item  $i$  to item  $j$

$$P(Y_{u,i} = j) = \frac{sim(i, j)}{\sum_{l \in RI_u} sim(i, l)}$$

similarity measure  
(item  $i$ , item  $j$ )

Pearson correlation  
of (item  $i$ , item  $j$ )

$$sim(i, j) = \frac{1}{1 + e^{-\frac{|UC_{i,j}|}{2}}} \times corr(i, j)$$

common user set  
of (item  $i$ , item  $j$ )



# Model based Social Recommender

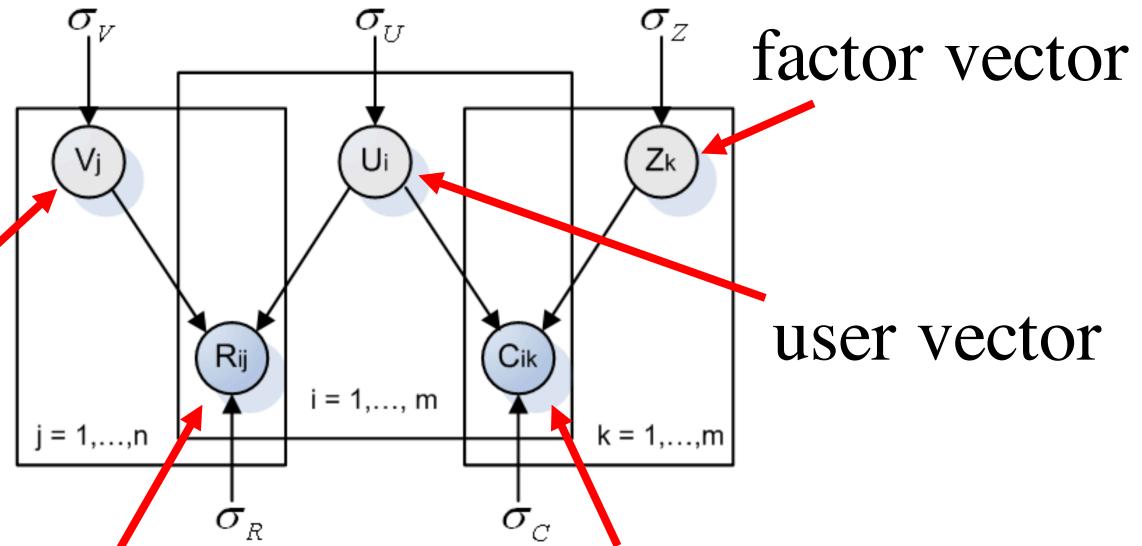
- Optimization methods such as gradient based methods can be applied to find a well-worked optimal solution.
- MF has a nice probabilistic interpretation with Gaussian noise.
- MF is very flexible and allows us to include prior knowledge.

$$\begin{aligned} & \textit{Social Recommendation CF} \\ &= \textit{Basic CF} + \textit{Social Information Model} \end{aligned}$$

# Model based Social Recommender

□ SoRec

item vector



factor vector

user vector

$R$ : user-item  
rating matrix

	$v_1$	$v_2$	$v_3$	$v_4$	$v_5$
$u_1$	5	?	2	?	?
$u_2$	4	4	5	?	?
$u_3$	?	?	4	4	1
$u_4$	?	?	?	?	3
$u_5$	?	?	1	?	?

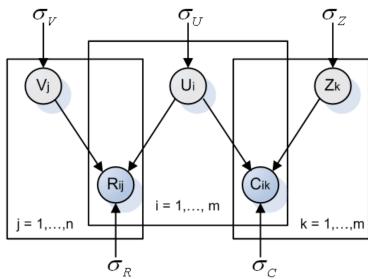
$C$ : user-user  
social matrix

	$u_1$	$u_2$	$u_3$	$u_4$	$u_5$
$u_1$	0	1	0	0	1
$u_2$	0	0	1	1	0
$u_3$	0	0	0	0	0
$u_4$	1	0	1	0	0
$u_5$	0	1	1	1	0

# Model based Social Recommender

## □ SoRec

$$p(\mathcal{C}|U, V, \sigma_R^2) = \prod_{i=1}^m \prod_{j=1}^n \mathcal{N} \left[ \left( r_{ij} | g(U_i^T V_j), \sigma_R^2 \right) \right]^{I_{ij}^R}$$



Gaussian distribution

Logistic function      Observed

$$p(C|U, Z, \sigma_C^2) = \prod_{i=1}^m \prod_{k=1}^m \mathcal{N} \left[ \left( c_{ik} | g(U_i^T Z_k), \sigma_C^2 \right) \right]^{I_{ik}^C}$$

# Model based Social Recommender

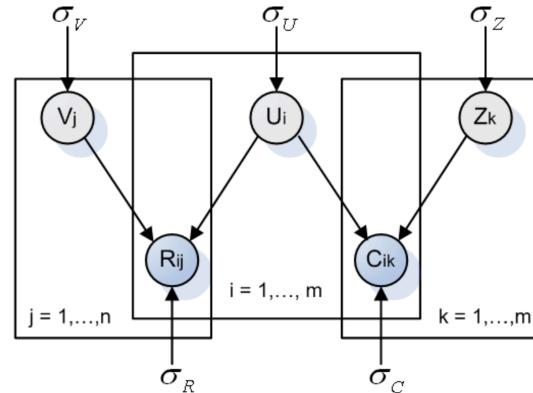
## □ SoRec

*behavioral term*

$$\mathcal{L}(R, C, U, V, Z) =$$

$$\frac{1}{2} \sum_{i=1}^m \sum_{j=1}^n I_{ij}^R \underbrace{(r_{ij} - g(U_i^T V_j))^2}_{social\ term} + \frac{\lambda_C}{2} \sum_{i=1}^m \sum_{k=1}^m I_{ik}^C \underbrace{(c_{ik}^* - g(U_i^T Z_k))^2}_{regularization\ terms}$$

$$+ \frac{\lambda_U}{2} \|U\|_F^2 + \frac{\lambda_V}{2} \|V\|_F^2 + \frac{\lambda_Z}{2} \|Z\|_F^2, \quad (9)$$



# Model based Social Recommender

## □ SoRec

### *Gradient Descent Methods*

$$\frac{\partial \mathcal{L}}{\partial U_i} = \sum_{j=1}^n I_{ij}^R g'(U_i^T V_j) \underline{(g(U_i^T V_j) - r_{ij}) V_j}$$

deviate of  
Logistic  
function

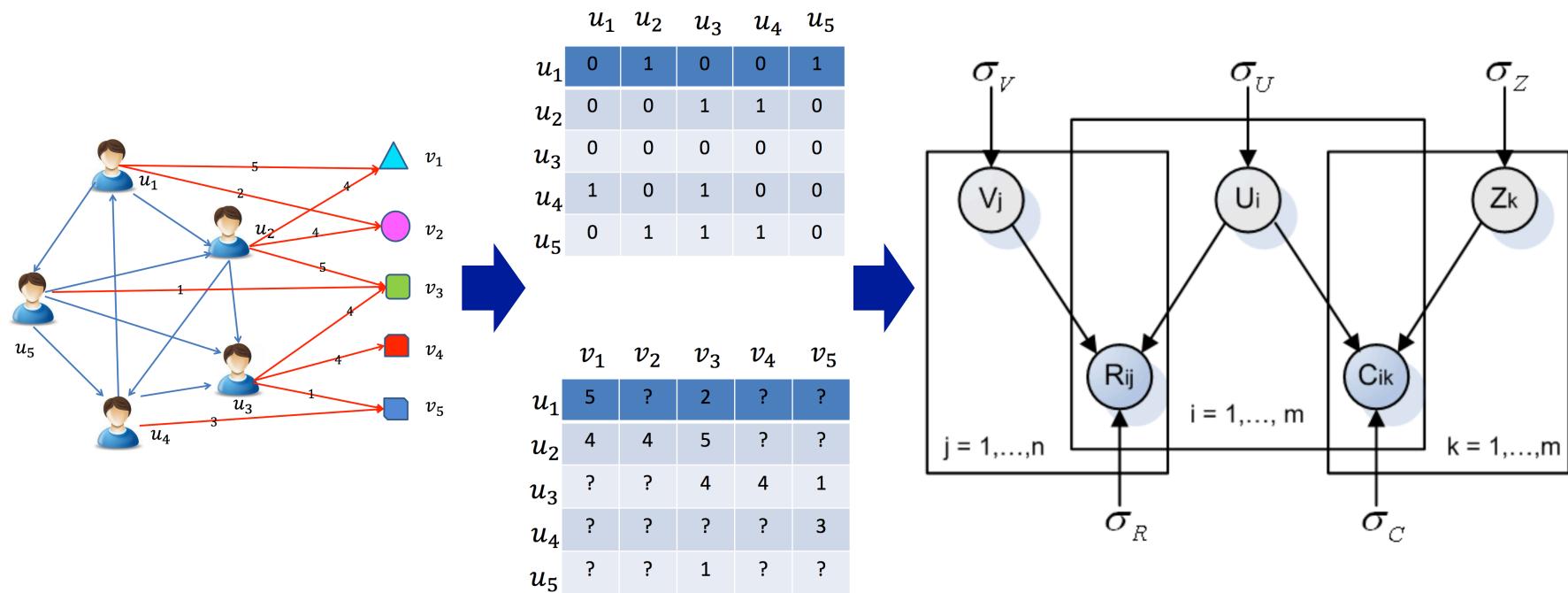
$$+ \lambda_C \sum_{k=1}^m I_{ik}^C g'(U_i^T Z_k) \underline{(g(U_i^T Z_k) - c_{ik}^*) Z_k} + \lambda_U U_i,$$

$$\frac{\partial \mathcal{L}}{\partial V_j} = \sum_{i=1}^m I_{ij}^R g'(U_i^T V_j) \underline{(g(U_i^T V_j) - r_{ij}) U_i} + \lambda_V V_j,$$

$$\frac{\partial \mathcal{L}}{\partial Z_k} = \lambda_C \sum_{i=1}^m I_{ik}^C g'(U_i^T Z_k) \underline{(g(U_i^T Z_k) - c_{ik}^*) U_i} + \lambda_Z Z_k, (10)$$

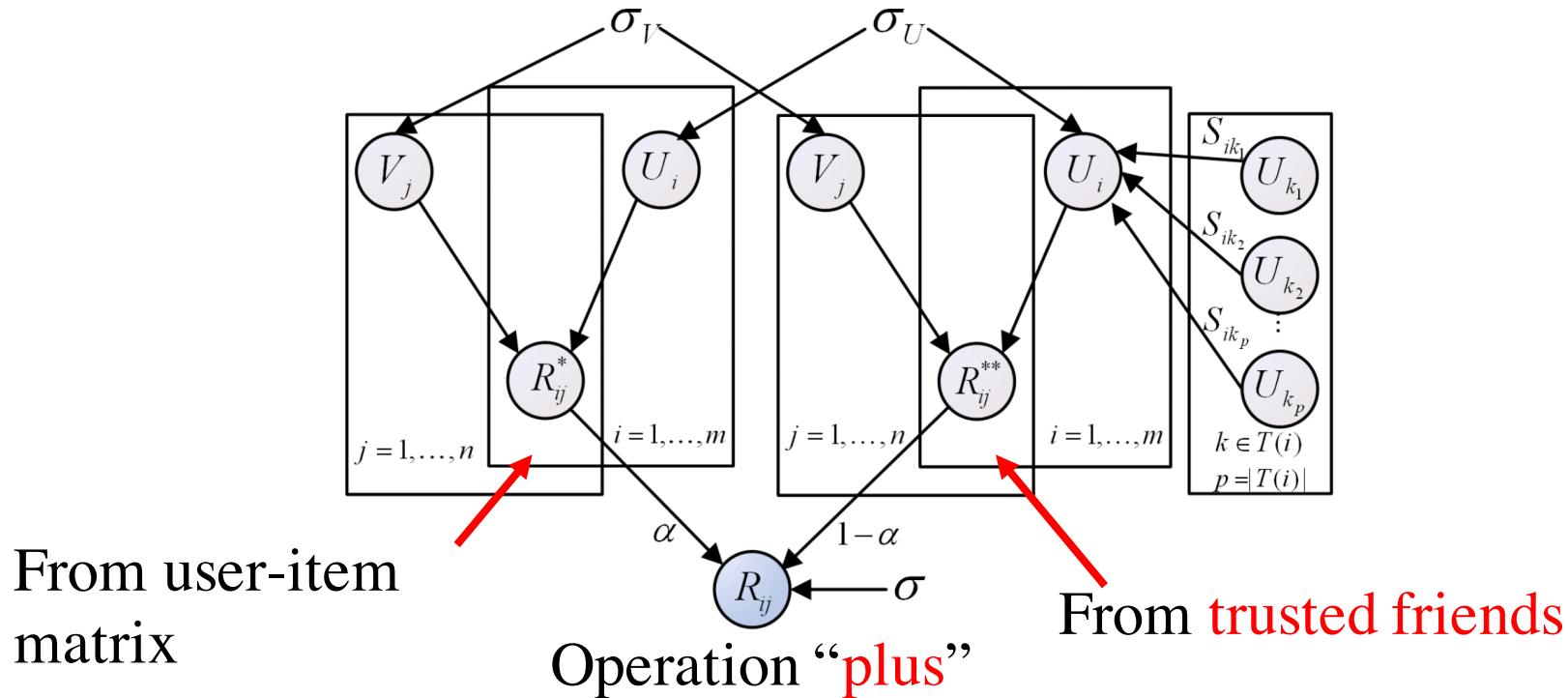
# Model based Social Recommender

## □ SoRec



# Model based Social Recommender

- Replacing social with trust
- “Social Trust” Ensemble for Epinion data



# Model based Social Recommender

## □ “Social Trust” Ensemble

$$\begin{aligned} \mathcal{L}(R, S, U, V) & \quad \text{From user-item matrix} \\ &= \frac{1}{2} \sum_{i=1}^m \sum_{j=1}^n I_{ij}^R (R_{ij} - g(\underline{\alpha U_i^T V_j} + \underline{(1-\alpha) \sum_{k \in \mathcal{T}(i)} S_{ik} U_k^T V_j}))^2 \\ &+ \frac{\lambda_U}{2} \|U\|_F^2 + \frac{\lambda_V}{2} \|V\|_F^2, \end{aligned} \tag{13}$$

# Model based Social Recommender

## □ “Social Trust” Ensemble

*Gradient  
Descent  
Methods*

$$\begin{aligned}
 \frac{\partial \mathcal{L}}{\partial U_i} = & \alpha \sum_{j=1}^n I_{ij}^R g'(\alpha U_i^T V_j + (1 - \alpha) \sum_{k \in \mathcal{T}(i)} S_{ik} U_k^T V_j) V_j \\
 & \times (g(\alpha U_i^T V_j + (1 - \alpha) \sum_{k \in \mathcal{T}(i)} S_{ik} U_k^T V_j) - R_{ij}) \\
 & + (1 - \alpha) \sum_{p \in \mathcal{B}(i)} \sum_{j=1}^n I_{pj}^R g'(\alpha U_p^T V_j + (1 - \alpha) \sum_{k \in \mathcal{T}(p)} S_{pk} U_k^T V_j) \\
 & \times (g(\alpha U_p^T V_j + (1 - \alpha) \sum_{k \in \mathcal{T}(p)} S_{pk} U_k^T V_j) - R_{pj}) S_{pi} V_j + \lambda_U U_i, \\
 \frac{\partial \mathcal{L}}{\partial V_j} = & \sum_{i=1}^m I_{ij}^R g'(\alpha U_i^T V_j + (1 - \alpha) \sum_{k \in \mathcal{T}(i)} S_{ik} U_k^T V_j) \\
 & \times (g(\alpha U_i^T V_j + (1 - \alpha) \sum_{k \in \mathcal{T}(i)} S_{ik} U_k^T V_j) - R_{ij}) \\
 & \times (\alpha U_i + (1 - \alpha) \sum_{k \in \mathcal{T}(i)} S_{ik} U_k^T) + \lambda_V V_j, \tag{14}
 \end{aligned}$$

# Model based Social Recommender

## □ SoReg

**Average-based regularization:**

Regularize with the average of friends' tastes

$$\min_{U, V} \mathcal{L}_1(R, U, V) = \frac{1}{2} \sum_{i=1}^m \sum_{j=1}^n I_{ij} (R_{ij} - U_i^T V_j)^2$$



$$+ \frac{\alpha}{2} \sum_{i=1}^m \|U_i - \frac{\sum_{f \in \mathcal{F}^+(i)} \text{Sim}(i, f) \times U_f}{\sum_{f \in \mathcal{F}^+(i)} \text{Sim}(i, f)}\|_F^2,$$

$$+ \frac{\lambda_1}{2} \|U\|_F^2 + \frac{\lambda_2}{2} \|V\|_F^2. \quad (8)$$

**Information loss:** Friends may have diverse tastes!!!

# Model based Social Recommender

## □ SoReg

**Individual-based regularization:**

Regularize with friends individually

$$\begin{aligned} \min_{U, V} \mathcal{L}_2(R, U, V) &= \frac{1}{2} \sum_{i=1}^m \sum_{j=1}^n I_{ij} (R_{ij} - U_i^T V_j)^2 \\ &+ \frac{\beta}{2} \sum_{i=1}^m \sum_{f \in \mathcal{F}^+(i)} Sim(i, f) \|U_i - U_f\|_F^2 \\ &+ \lambda_1 \|U\|_F^2 + \lambda_2 \|V\|_F^2. \end{aligned} \tag{11}$$


# Related Work

	Behavior	Content	Social	Trust
Collaborative filtering (CF) [Herlocker <i>et al.</i> . TOIS; Koren KDD]	✓			
Content-based filtering with CF [Balabanovic <i>et al.</i> ; Liu <i>et al.</i> . CIKM;]	✓	✓		
SoRec [Ma <i>et al.</i> . CIKM, TIS] SoReg [Ma <i>et al.</i> . WSDM]	✓		✓	
Trust-based methods [Massa <i>et al.</i> . RecSys; Jamali <i>et al.</i> . KDD; Ma <i>et al.</i> . SIGIR, TIST]	✓			✓

❑ **Q:** What are the **factors** of users' decisions on retweeting?  
Can we **observe** them from the data? How to **integrate** the information for accurate prediction?

# Observation: Social Contextual Factors

- Will Michelle Obama share this message?
- Please list your reasons.



**Barack Obama**

Happy birthday, Michelle Obama!

[Like](#) · [Comment](#) · [Share](#) · January 18, 2013

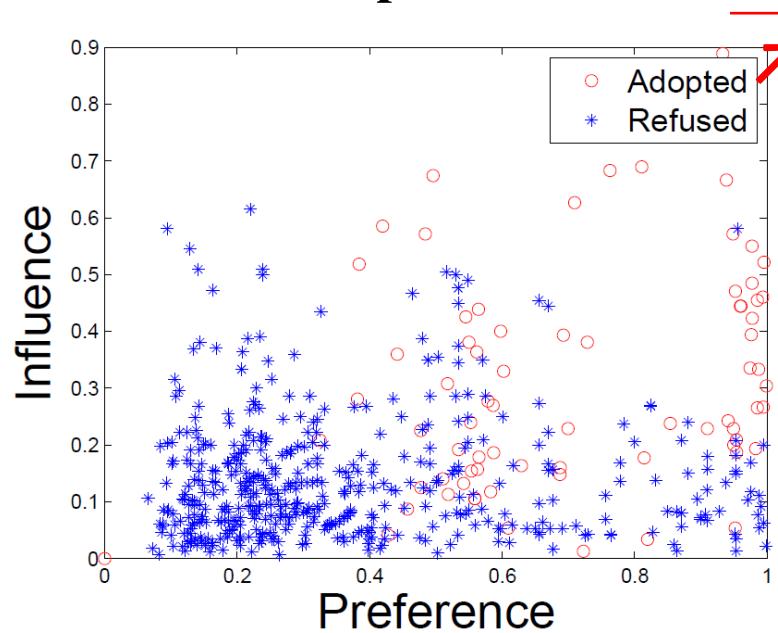
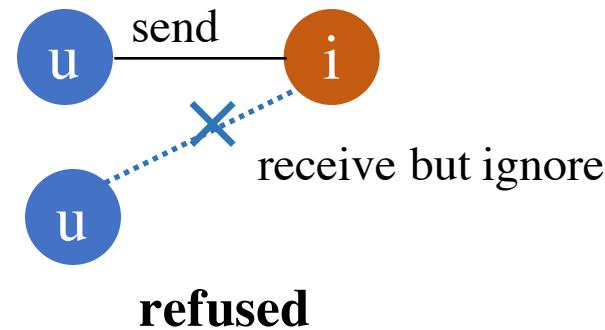
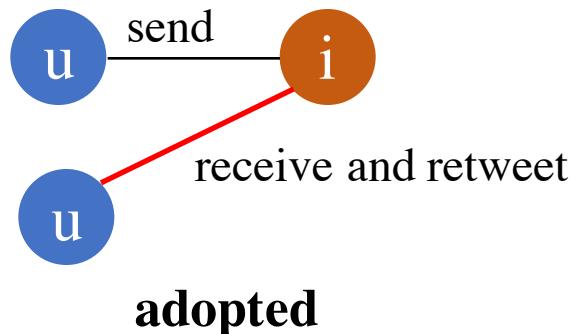


**Michelle Obama** shared Barack Obama's photo.

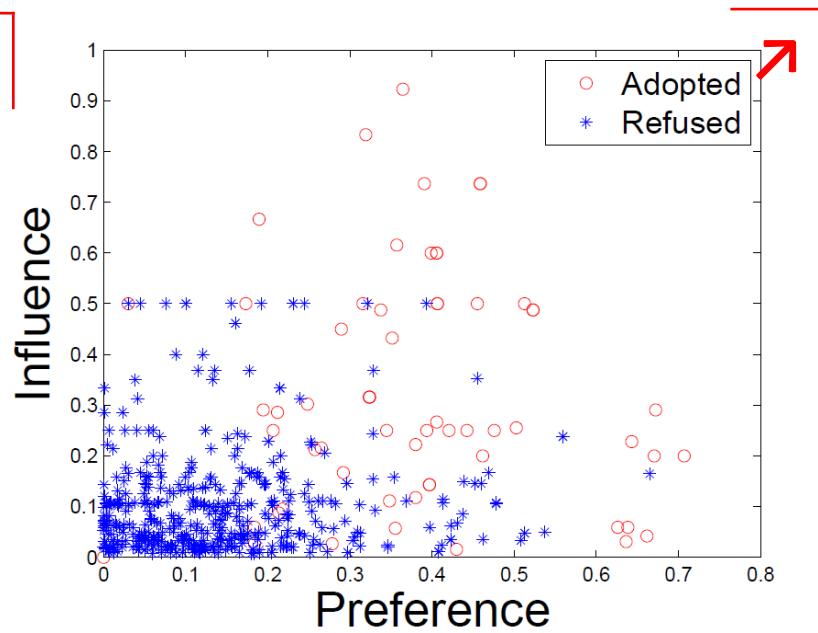
January 18, 2013 ·



# Observation: Social Contextual Factors



China's Facebook: Renren



China's Twitter: Tencent Weibo

# Representation: From Contextual Information to Contextual Factors

## Content

Item-item similarity

Item latent features  $V$

## Behavior

User-item interaction

User latent features  $U$

## Social

User-user social relation

Item sender  $G$

## Interaction frequency

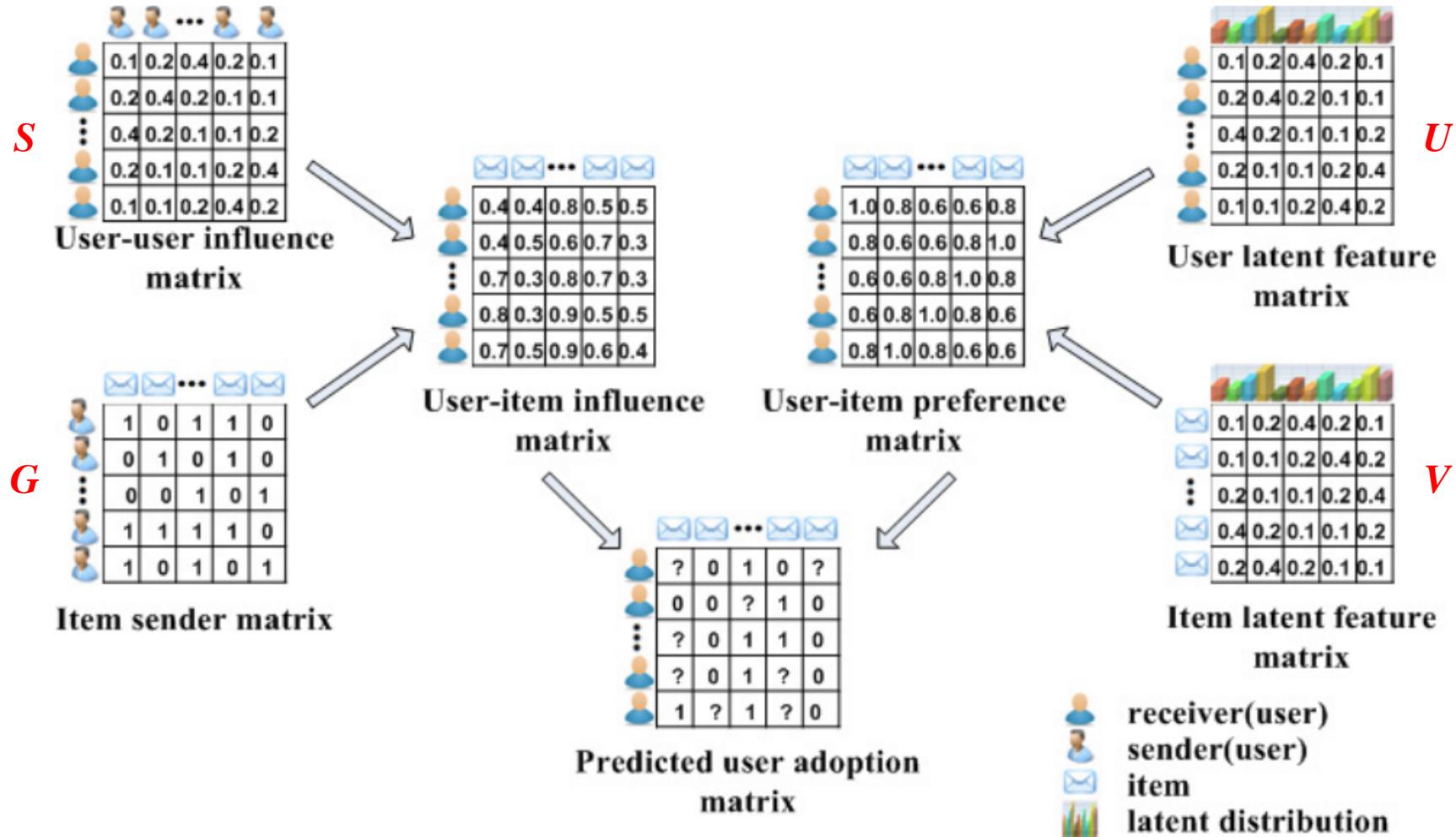
User-user interaction

User-user influence  $S$

Personal preference  
on the given item

Interpersonal influence  
from the item's sender

# Model: ContextMF



# Model: ContextMF

behavior      influence      preference

$$P(\mathbf{R}|\mathbf{S}, \mathbf{U}, \mathbf{V}, \sigma_R^2) = \prod_{i=1}^M \prod_{j=1}^N \mathcal{N}(\underline{\mathbf{R}_{ij}} | \underline{\mathbf{S}_i \mathbf{G}_j^\top} \odot \underline{\mathbf{U}_i^\top \mathbf{V}_j}, \sigma_R^2)$$

behavior      interaction frequency/trust

item content

$$\begin{aligned} \mathcal{J} = & ||\mathbf{R} - \mathbf{S}\mathbf{G}^\top \odot \mathbf{U}^\top \mathbf{V}||_F^2 + \alpha ||\mathbf{W} - \mathbf{U}^\top \mathbf{U}||_F^2 \\ & + \beta ||\mathbf{C} - \mathbf{V}^\top \mathbf{V}||_F^2 + \gamma ||\mathbf{S} - \mathbf{F}||_F^2 \\ & + \delta ||\mathbf{S}||_F^2 + \eta ||\mathbf{U}||_F^2 + \lambda ||\mathbf{V}||_F^2 \end{aligned}$$

social relation

# Model: ContextMF

- Gradient descent method

$$\frac{\partial \mathcal{J}}{\partial \mathbf{S}} = 2 \left( -\mathbf{R}(\mathbf{G} \odot \mathbf{V}^\top \mathbf{U}) + (\mathbf{S}\mathbf{G}^\top \odot \mathbf{U}^\top \mathbf{V})\mathbf{G} \right. \\ \left. + \gamma(\mathbf{S} - \mathbf{F}) + \delta\mathbf{S} \right)$$

$$\frac{\partial \mathcal{J}}{\partial \mathbf{U}} = 2 \left( -\mathbf{V}\mathbf{R}^\top + \mathbf{V}(\mathbf{G}\mathbf{S}^\top \odot \mathbf{V}^\top \mathbf{U}) - 2\alpha\mathbf{U}\mathbf{W} \right. \\ \left. + 2\alpha\mathbf{U}\mathbf{U}^\top \mathbf{U} + \eta\mathbf{U} \right)$$

$$\frac{\partial \mathcal{J}}{\partial \mathbf{V}} = 2 \left( -\mathbf{U}\mathbf{R} + \mathbf{U}(\mathbf{S}\mathbf{G}^\top \odot \mathbf{U}^\top \mathbf{V}) - 2\beta\mathbf{V}\mathbf{C} \right. \\ \left. + 2\beta\mathbf{V}\mathbf{V}^\top \mathbf{V} + \lambda\mathbf{V} \right)$$



# Experimental Results

Method	MAE	RMSE	$\hat{\tau}$	$\hat{\rho}$
Renren Dataset				
Content-based [1]	0.3842	0.4769	0.5409	0.5404
Item CF [25]	0.3601	0.4513	0.5896	0.5988
FeedbackTrust [22]	0.3764	0.4684	0.5433	0.5469
Influence-based [9]	0.3859	0.4686	0.5394	0.5446
SoRec [19]	0.3276	0.4127	0.6168	0.6204
SoReg [20]	0.2985	0.3537	0.7086	0.7140
Influence MF	0.3102	0.3771	0.6861	0.7006
Preference MF	0.3032	0.3762	0.6937	0.7036
Context MF	<b>0.2416</b>	<b>0.3086</b>	<b>0.7782</b>	<b>0.7896</b>

Tencent Weibo Dataset

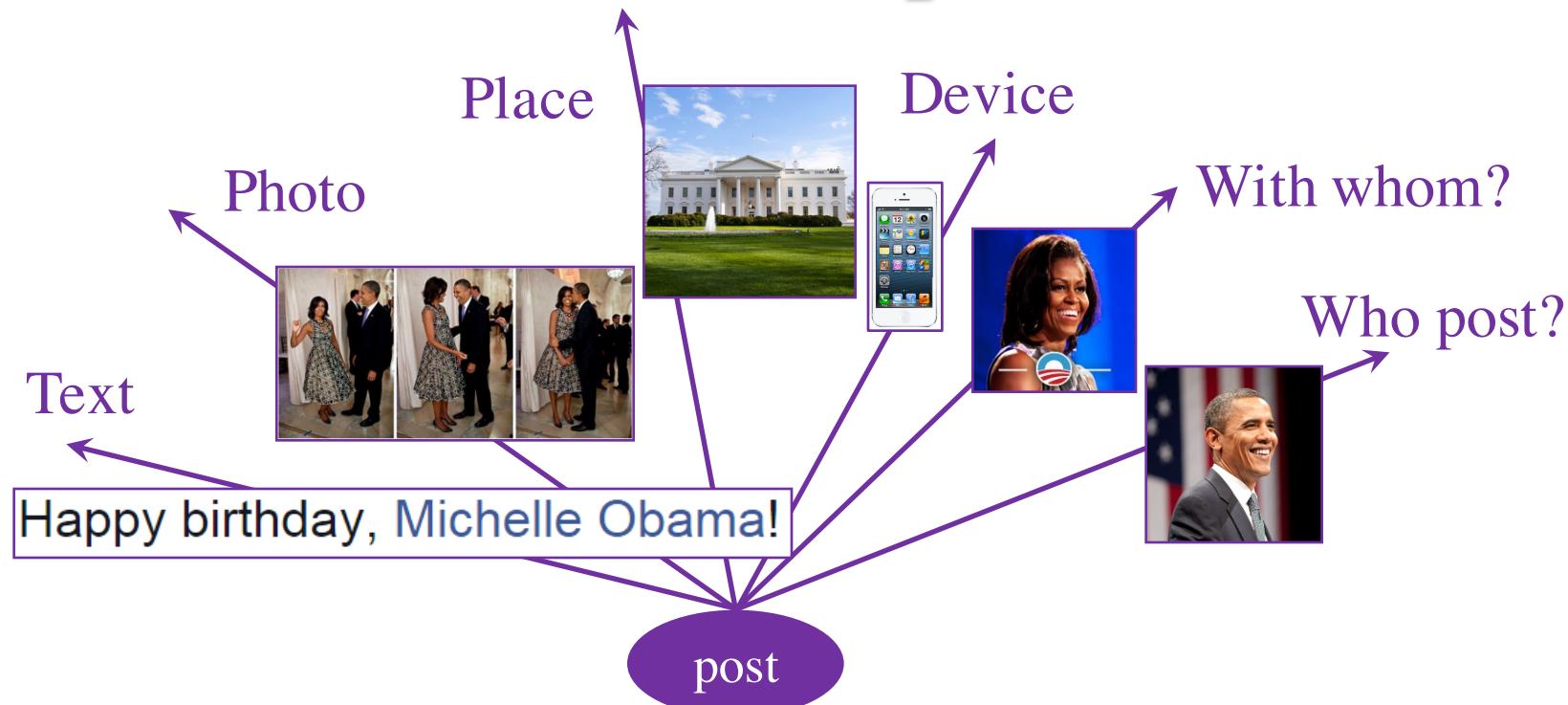
Content-based [1]	0.2576	0.3643	0.7728	<b>0.7777</b>
Item CF [25]	0.2375	0.3372	0.7867	0.8049
FeedbackTrust [22]	0.2830	0.3887	0.7094	<b>0.7115</b>
Influence-based [9]	0.2651	0.3813	0.7163	<b>0.7275</b>
SoRec [19]	0.2256	0.3325	0.7973	0.8064
SoReg [20]	0.1997	0.2962	0.8390	0.8423
Influence MF	0.2183	0.3206	0.8179	<b>0.8258</b>
Preference MF	0.2111	0.3088	0.8384	0.8453
Context MF	<b>0.1514</b>	<b>0.2348</b>	<b>0.8570</b>	<b>0.8685</b>

vs. SoReg [TIST'11]	Renren	Tencent Weibo
MAE	$\downarrow 19.1\%$	$\downarrow 24.2\%$
RMSE	$\downarrow 12.8\%$	$\downarrow 20.7\%$
Kendall's	$\uparrow 9.82\%$	$\uparrow 2.1\%$
Spearman's	$\uparrow 10.6\%$	$\uparrow 3.1\%$

□ **Deployed in Weibo News Feed.** Improved conversion rate from 5.78% to 8.27% (relatively **43%**).

□ #citations = **149**

# Observation: Spatial Context

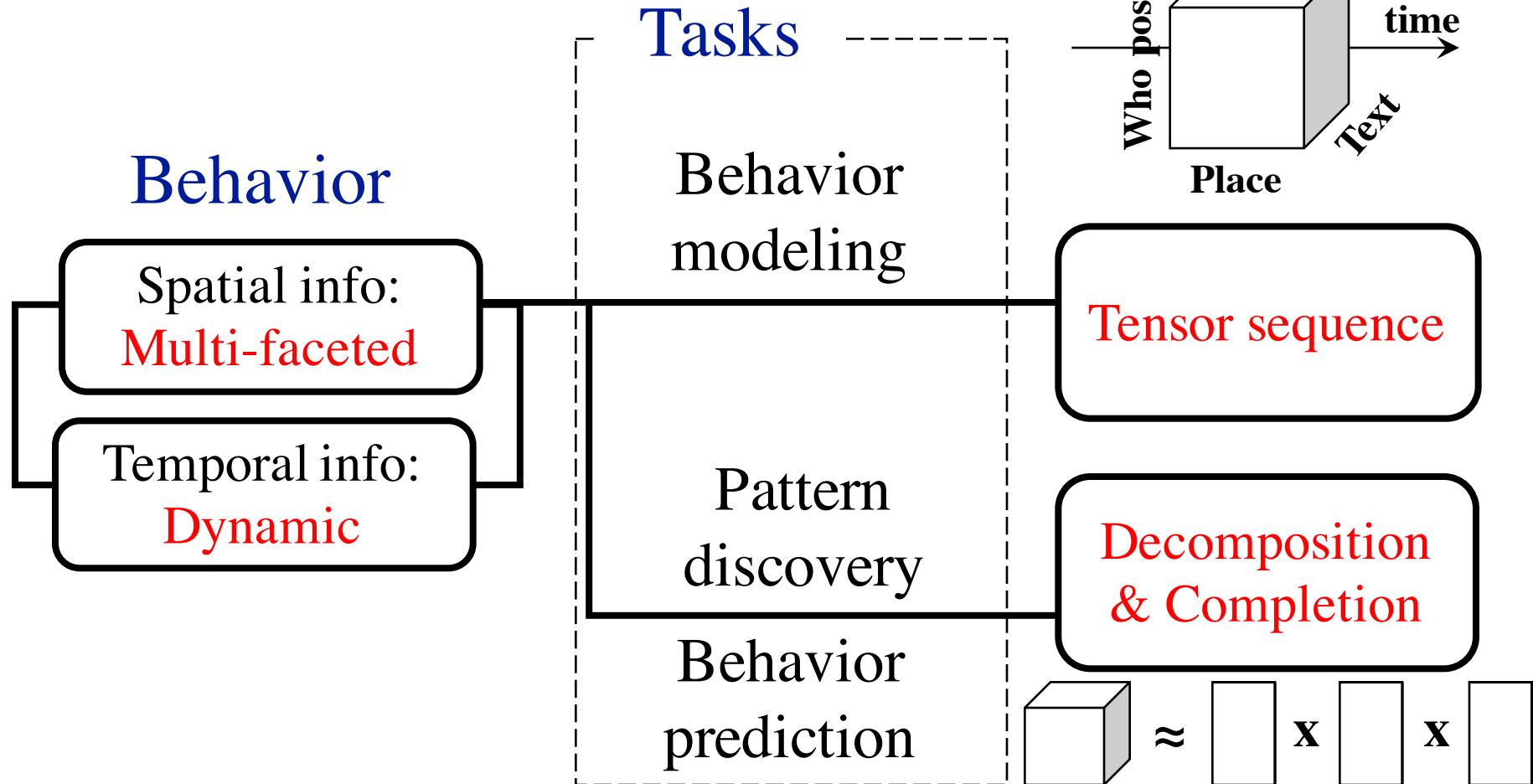


Jan. 18  
Birthday party  
@ White house

# Observation: Temporal Context

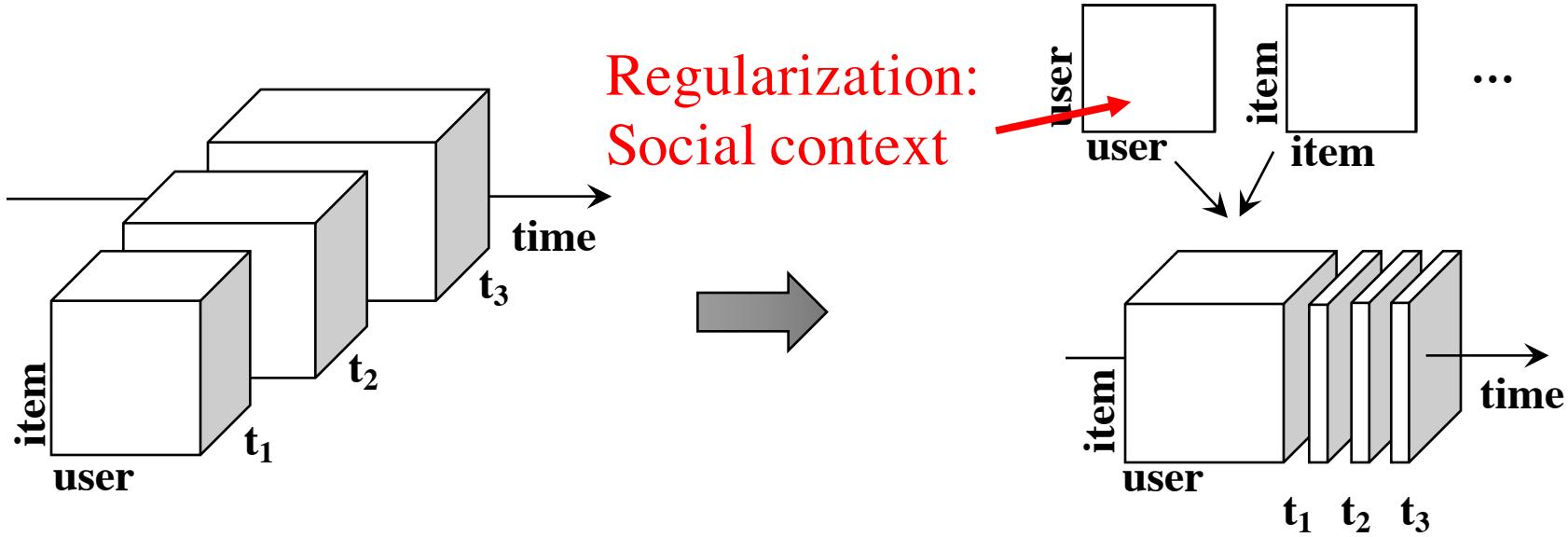


# Representation: Tensor Sequence



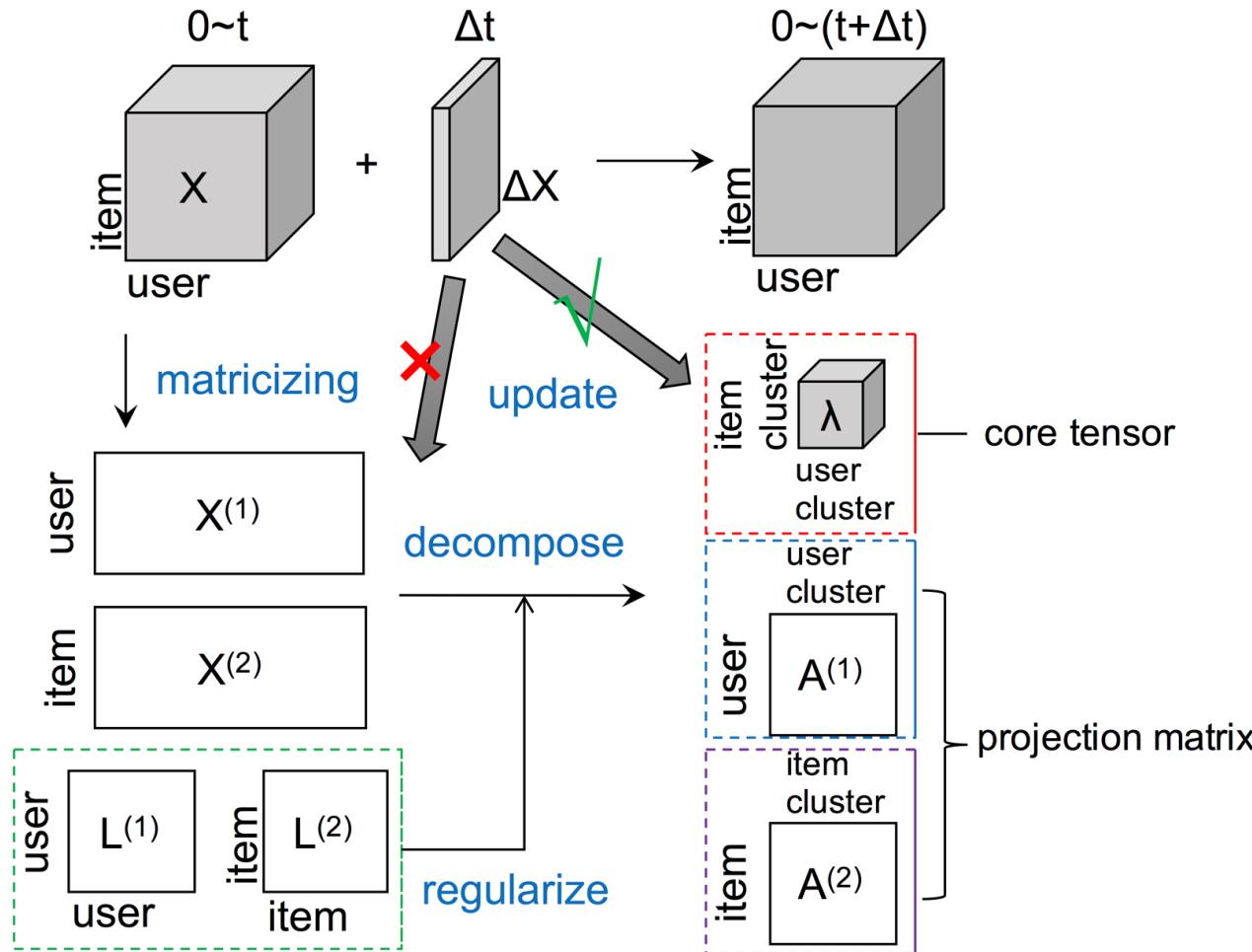
# Challenges: Sparsity and Complexity

- Addressing **sparsity**: *Flexible regularization with auxiliary data*
- Addressing **high complexity**: *Incremental updates for projection matrix*



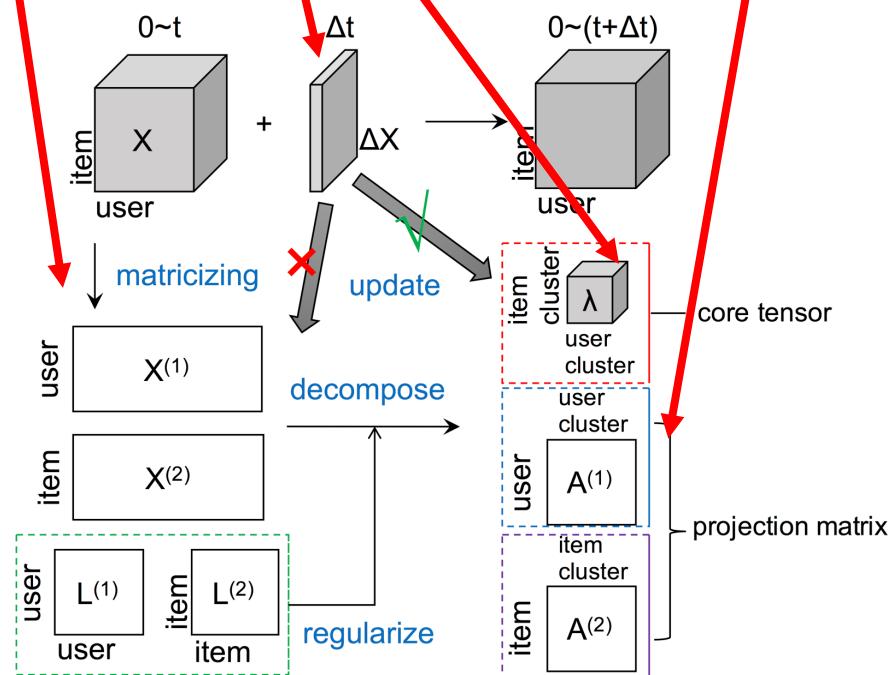
# Model: FEMA

## Flexible Evolutionary Multi-faceted Analysis



# Tensor Perturbation Theory

$$[(\mathbf{X}^{(m)} + \Delta\mathbf{X}^{(m)})(\mathbf{X}^{(m)} + \Delta\mathbf{X}^{(m)})^\top + \mu^{(m)} \mathbf{L}^{(m)}] \cdot (\mathbf{a}_i^{(m)} + \Delta\mathbf{a}_i^{(m)}) = (\lambda_i^{(m)} + \Delta\lambda_i^{(m)}) (\mathbf{a}_i^{(m)} + \Delta\mathbf{a}_i^{(m)})$$



# Algorithm: FEMA

## Approximation

**Require:**  $\mathcal{X}_t, \Delta\mathcal{X}_t, \mathbf{A}_t^{(m)}|_{m=1}^M, \lambda_t^{(m)}|_{m=1}^M$

**for**  $m = 1, \dots, M$  **do**

**for**  $i = 1, \dots, r^{(m)}$  **do**

        Compute  $\Delta\lambda_{t,i}^{(m)}$  using

$$\Delta\lambda_i^{(m)} = \mathbf{a}_i^{(m)\top} (\mathbf{X}^{(m)} \Delta\mathbf{X}^{(m)\top} + \Delta\mathbf{X}^{(m)} \mathbf{X}^{(m)\top}) \mathbf{a}_i^{(m)}$$

        and compute

$$\lambda_{t+1,i}^{(m)} = \lambda_{t,i}^{(m)} + \Delta\lambda_{t,i}^{(m)};$$

        Compute  $\Delta\mathbf{a}_{t,i}^{(m)}$  using

$$\Delta\mathbf{a}_i^{(m)} = \sum_{j \neq i} \frac{\mathbf{a}_j^{(m)\top} (\mathbf{X}^{(m)} \Delta\mathbf{X}^{(m)\top} + \Delta\mathbf{X}^{(m)} \mathbf{X}^{(m)\top}) \mathbf{a}_i^{(m)}}{\lambda_i^{(m)} - \lambda_j^{(m)}} \mathbf{a}_j^{(m)}$$

        and compute

$$\mathbf{a}_{t+1,i}^{(m)} = \mathbf{a}_{t,i}^{(m)} + \Delta\mathbf{a}_{t,i}^{(m)} \text{ and } \mathbf{A}_{t+1}^{(m)} = \{\mathbf{a}_{t+1,i}^{(m)}\};$$

**end for**

**end for**

$$\mathcal{Y}_{t+1} = (\mathcal{X}_t + \Delta\mathcal{X}_t) \prod_{m=1}^M \times_{(m)} \mathbf{A}_{t+1}^{(m)\top};$$

**return**  $\mathbf{A}_{t+1}^{(m)}|_{m=1}^M, \lambda_{t+1}^{(m)}|_{m=1}^M, \mathcal{Y}_{t+1}$

## Bound Guarantee

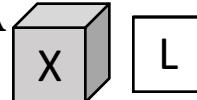
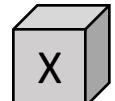
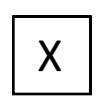
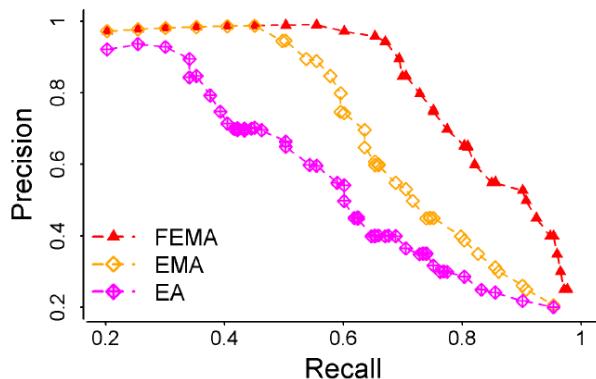
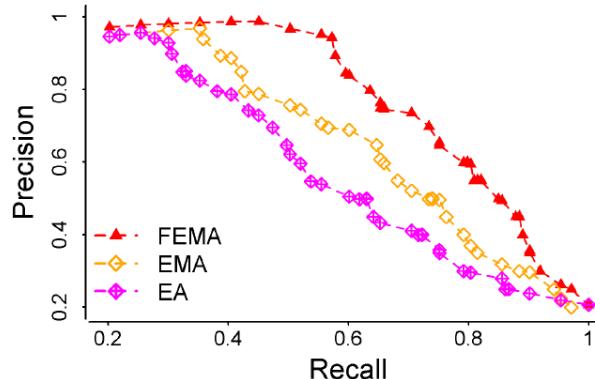
core tensor

$$|\Delta\lambda_i^{(m)}| \leq 2(\lambda_{\mathbf{X}^{(m)\top} \mathbf{X}^{(m)}}^{\max})^{\frac{1}{2}} \|\Delta\mathbf{X}^{(m)}\|_2$$

$$|\Delta\mathbf{a}_i^{(m)}| \leq 2\|\Delta\mathbf{X}^{(m)}\|_2 \sum_{j \neq i} \frac{(\lambda_{\mathbf{X}^{(m)\top} \mathbf{X}^{(m)}}^{\max})^{\frac{1}{2}}}{|\lambda_i^{(m)} - \lambda_j^{(m)}|}$$

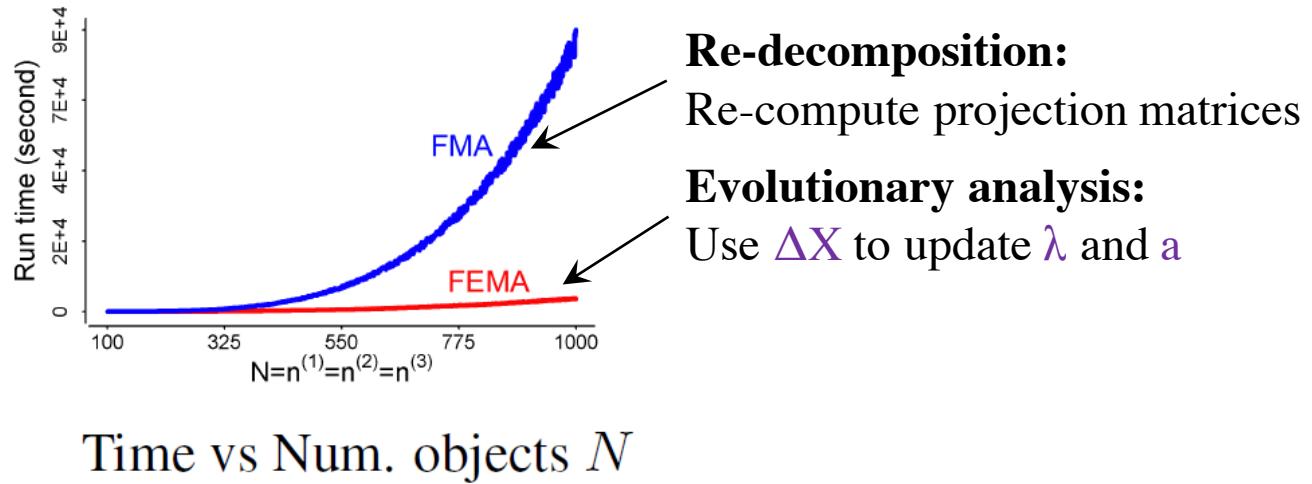
projection matrix

# Results: FEMA > EMA > EA

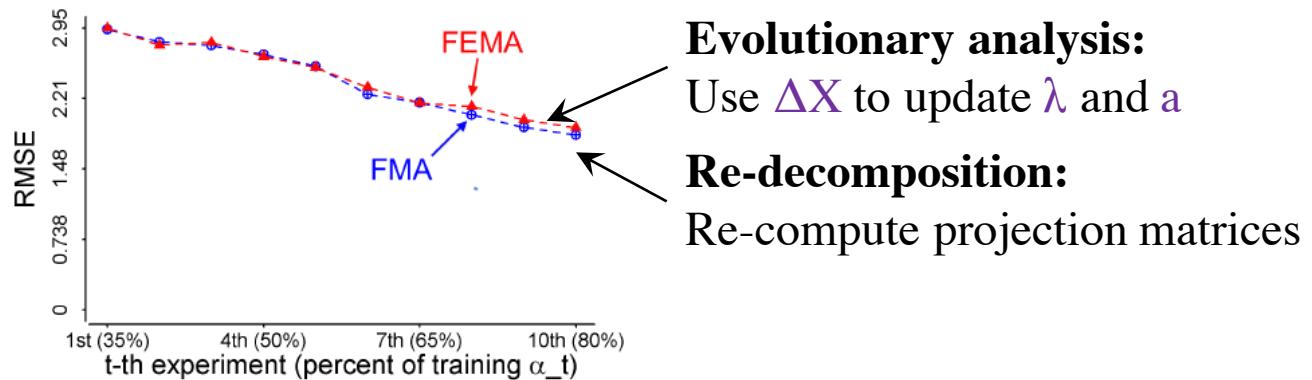
	Microsoft Academic Search		Tencent Weibo mentions “@”	
	MAE	RMSE	MAE	RMSE
FEMA 	<b>0.735</b>	<b>0.944</b>	<b>0.894</b>	<b>1.312</b>
EMA 	0.794	1.130	0.932	1.556
EA 	0.979	1.364	1.120	1.873
Precision vs Recall				



# Results: Efficiency



- Re-decomposition:**  
Re-compute projection matrices
- Evolutionary analysis:**  
Use  $\Delta X$  to update  $\lambda$  and  $a$

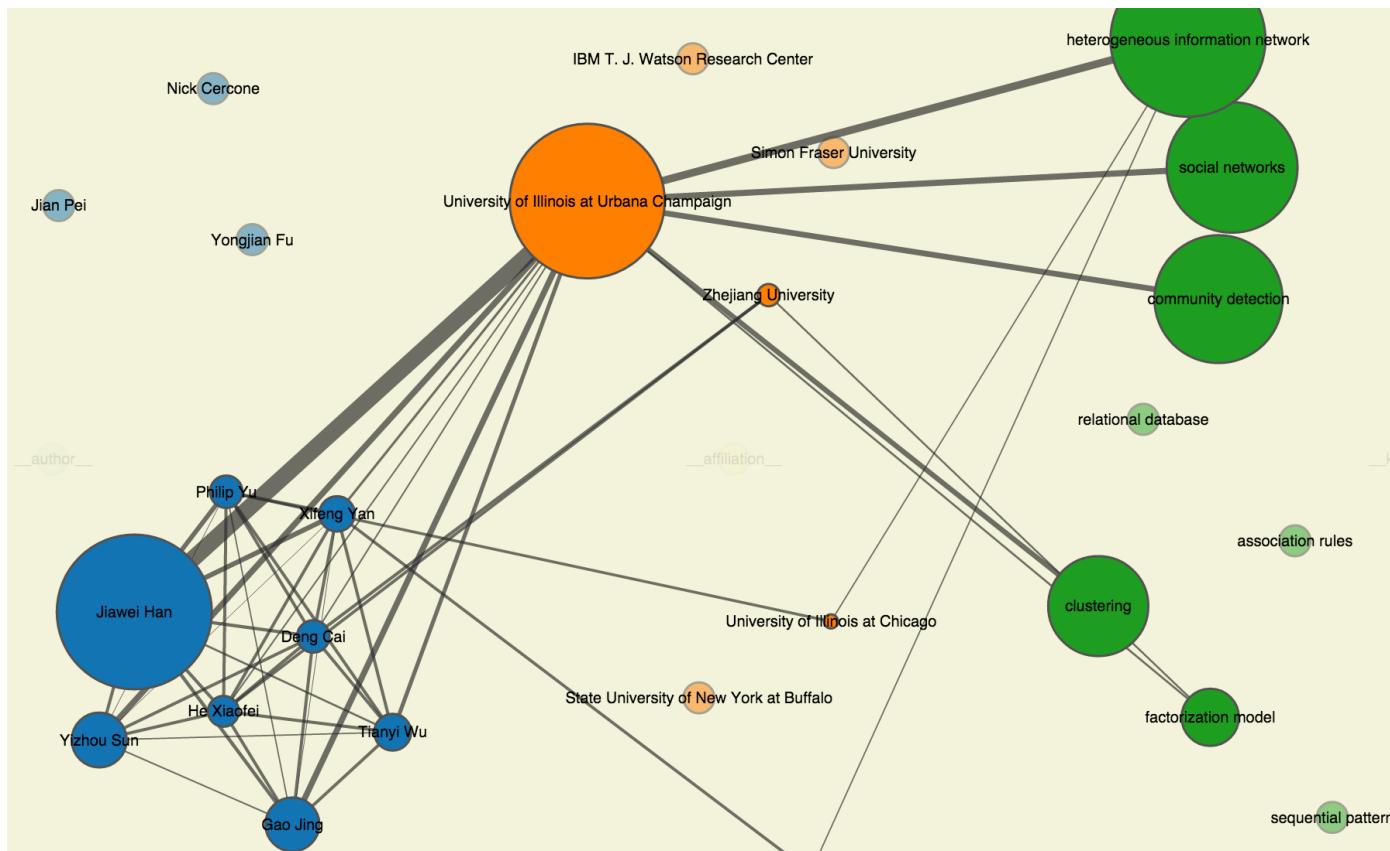


- Evolutionary analysis:**  
Use  $\Delta X$  to update  $\lambda$  and  $a$
- Re-decomposition:**  
Re-compute projection matrices

The loss is small.

# Demo: Author@Affiliation#Keyword

<http://www.meng-jiang.com/demos/fema/mas/>



# Observation: Multiple Domains



**Osmar Zaiane**

20 hrs · Twitter · 

#DataScientists need ability to tell the story about #data and convey #business value <https://t.co/VNN2rXaLuV> #BigData #datascience #dataviz

 Like     Comment     Share

The Globe and Mail shared Globe Politics's video.  
19 hrs · 

Watch highlights from Stephen Harper's concession speech





Philip Bohannon shared a link.  
5 hrs · 



British Library offers over 1 million free vintage images for download

9#  
Closed Group

Joined  Share  ...

Discussion Members Events Photos Files Search this group

Write Post Add Photo / Video Ask Question Add File

Write something...

RECENT ACTIVITY

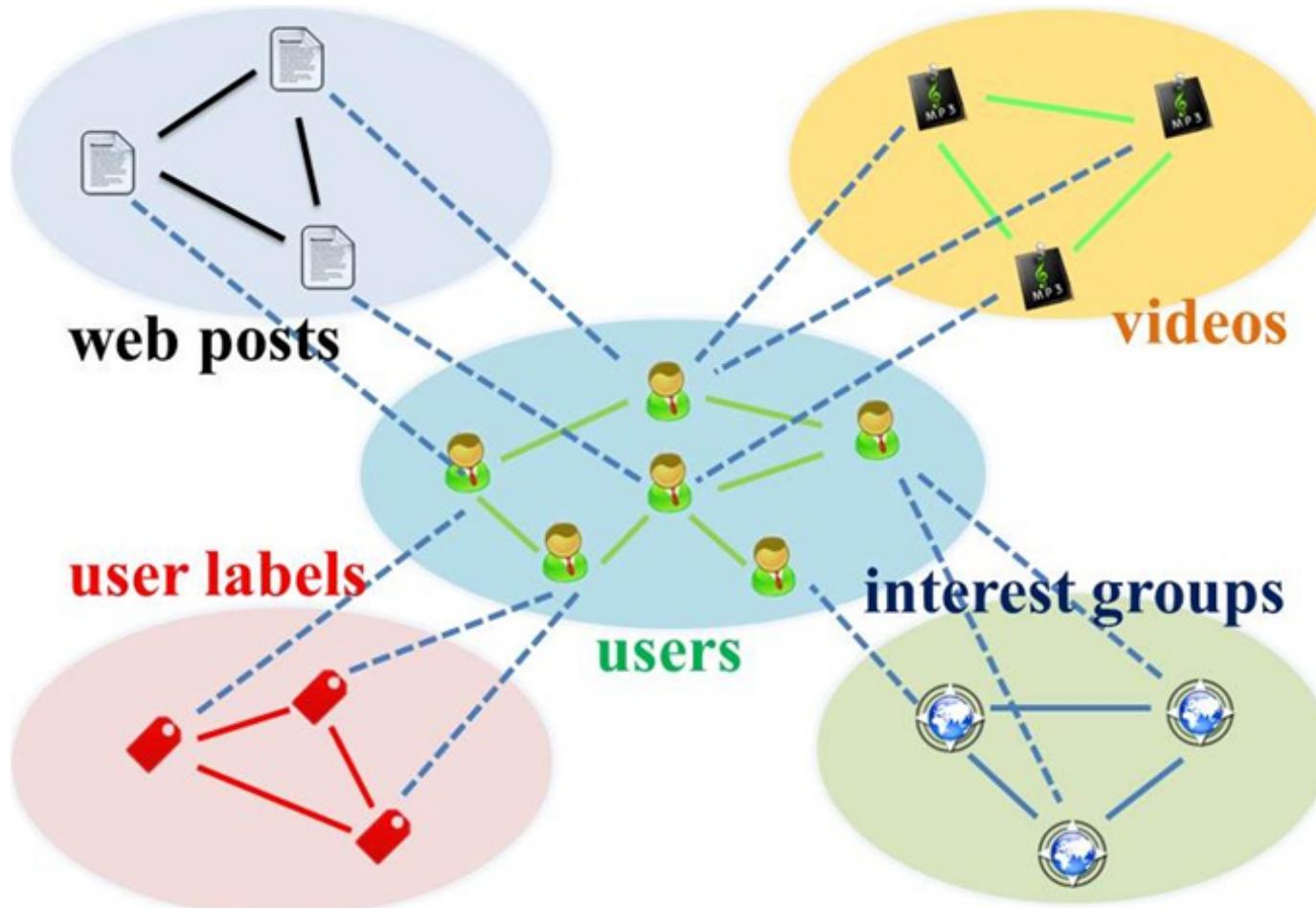
MEMBERS 1,049 Members (4 new)  
+ Add People to Group



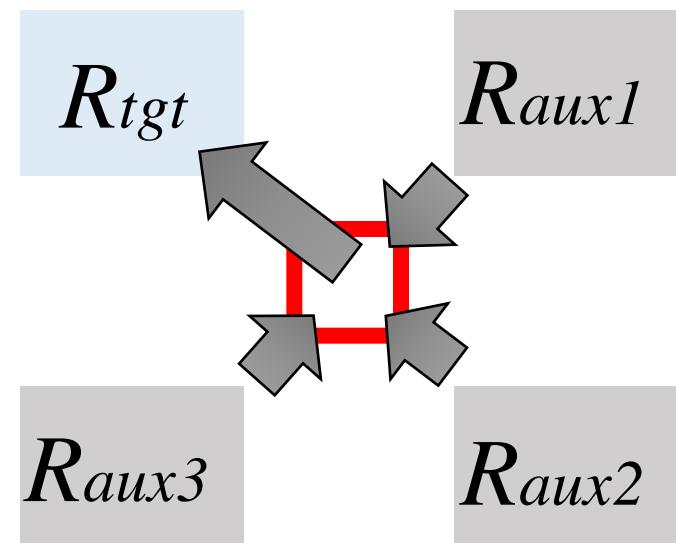
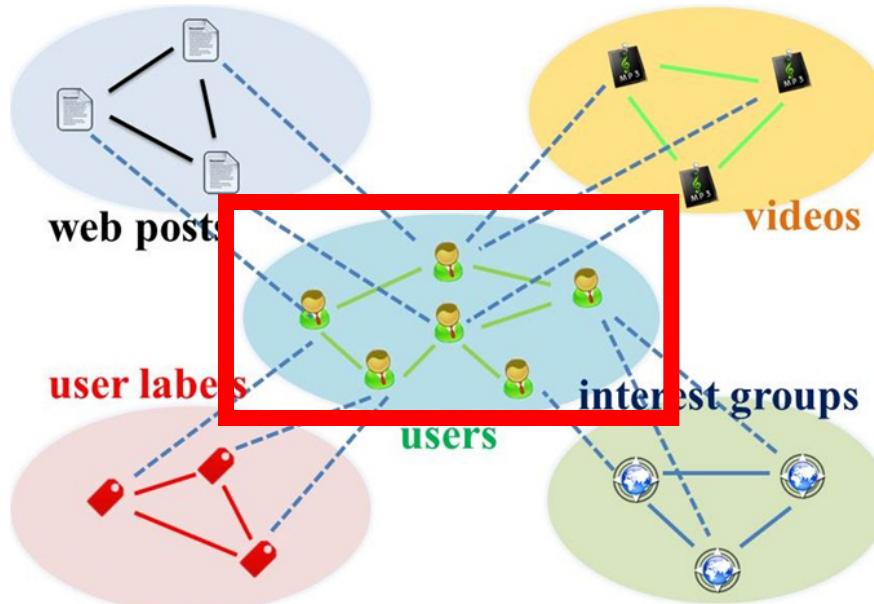
Invite by Email

Religious Views	Christian
Interests	Basketball, writing, spending time w/ kids
Favorite Music	Miles Davis, John Coltrane, Bob Dylan, Stevie Wonder, Johann Sebastian Bach (cello suites), and The Fugees
Favorite Movies	Casablanca, Godfather I & II, Lawrence of Arabia and One Flew Over the Cuckoo's Nest
Favorite TV Shows	Sportscenter
Favorite Quotations	"The Arc of the moral universe is long, but it bends towards justice." (MLK)

# Representation: Star-Structured Graph



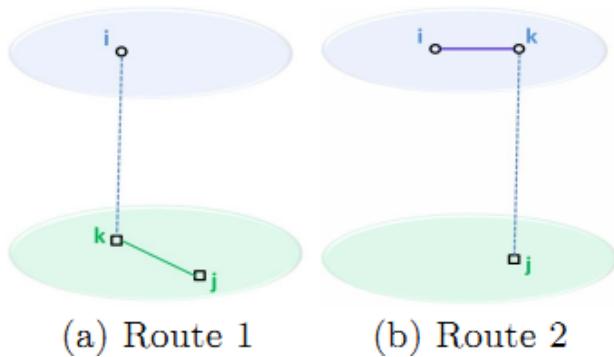
# Representation: Social Bridge



Bridge: Tie strength

# Algorithm: Hybrid Random Walk

## □ Updating cross-domain links



$$p_{ij}^{(\mathcal{UP})+} = \delta \sum_{u_k \in \mathcal{U}} r_{ik}^{(\mathcal{U})} p_{kj}^{(\mathcal{UP})+} + (1 - \delta) \sum_{p_k \in \mathcal{P}} p_{ik}^{(\mathcal{UP})+} r_{kj}^{(\mathcal{P})}$$

$$p_{ij}^{(\mathcal{UP})-} = \delta \sum_{u_k \in \mathcal{U}} r_{ik}^{(\mathcal{U})} p_{kj}^{(\mathcal{UP})-} + (1 - \delta) \sum_{p_k \in \mathcal{P}} p_{ik}^{(\mathcal{UP})-} r_{kj}^{(\mathcal{P})}$$

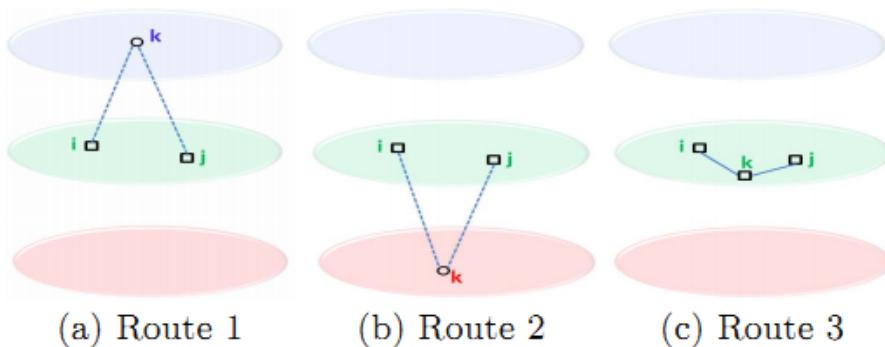
$$p_{ij}^{(\mathcal{UT})+} = \eta \sum_{u_k \in \mathcal{U}} r_{ik}^{(\mathcal{U})} p_{kj}^{(\mathcal{UT})+} + (1 - \eta) \sum_{t_k \in \mathcal{T}} p_{ik}^{(\mathcal{UT})+} r_{kj}^{(\mathcal{T})}$$

$$\mathbf{P}^{(\mathcal{UP})+}(t+1) = \delta \mathbf{R}^{(\mathcal{U})}(t) \mathbf{P}^{(\mathcal{UP})+}(t) + (1 - \delta) \mathbf{P}^{(\mathcal{UP})+}(t) \mathbf{R}^{(\mathcal{P})}$$

$$\mathbf{P}^{(\mathcal{UP})-}(t+1) = \delta \mathbf{R}^{(\mathcal{U})}(t) \mathbf{P}^{(\mathcal{UP})-}(t) + (1 - \delta) \mathbf{P}^{(\mathcal{UP})-}(t) \mathbf{R}^{(\mathcal{P})}$$

$$\mathbf{P}^{(\mathcal{UT})+}(t+1) = \eta \mathbf{R}^{(\mathcal{U})}(t) \mathbf{P}^{(\mathcal{UT})+}(t) + (1 - \eta) \mathbf{P}^{(\mathcal{UT})+}(t) \mathbf{R}^{(\mathcal{T})}$$

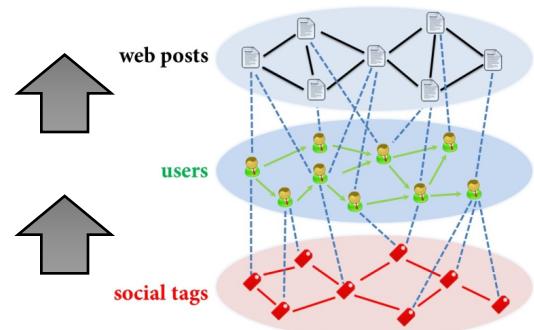
## □ Updating within-domain links



$$r_{ij}^{(\mathcal{U})} = \tau^{(\mathcal{P})} (\mu \sum_{p_k \in \mathcal{P}} p_{ik}^{(\mathcal{UP})+} p_{jk}^{(\mathcal{UP})+} + (1 - \mu) \sum_{p_k \in \mathcal{P}} p_{ik}^{(\mathcal{UP})-} p_{jk}^{(\mathcal{UP})-}) \\ + \tau^{(\mathcal{T})} \sum_{t_k \in \mathcal{T}} p_{ik}^{(\mathcal{UT})+} p_{jk}^{(\mathcal{UT})+} + \tau^{(\mathcal{U})} \sum_{u_k \in \mathcal{U}} r_{ik}^{(\mathcal{U})} r_{kj}^{(\mathcal{U})} \quad (12)$$

$$\mathbf{R}^{(\mathcal{U})}(t+1) = \tau^{(\mathcal{P})} (\mu \mathbf{P}^{(\mathcal{UP})+}(t) \mathbf{P}^{(\mathcal{UP})+}(t)^T + (1 - \mu) \mathbf{P}^{(\mathcal{UP})-}(t) \mathbf{P}^{(\mathcal{UP})-}(t)^T) \\ + \tau^{(\mathcal{T})} \mathbf{P}^{(\mathcal{UT})+}(t) \mathbf{P}^{(\mathcal{UT})+}(t)^T + \tau^{(\mathcal{U})} \mathbf{R}^{(\mathcal{U})}(t) \mathbf{R}^{(\mathcal{U})}(t)^T \quad (13)$$

# Results



## Comparing with Random Walk with Restarts Models

Algorithm	MAE	Precision	Recall	F1	Kendall's $\hat{\tau}$
HRW	<b>0.227±1.5e-3</b>	<b>0.711±1.3e-3</b>	0.921±1.4e-3	<b>0.802±1.1e-3</b>	<b>0.792±2.5e-3</b>
BRW- $R_U$ -P (TrustWalker)	0.276±1.1e-3	0.657±7.6e-4	<b>0.935±9.8e-4</b>	0.772±7.6e-4	0.774±1.6e-3
BRW- $R_U$	0.282±5.3e-3	0.655±4.0e-3	0.921±1.2e-2	0.765±7.7e-3	0.725±2.8e-3
BRW- $W_U$ -P	0.292±1.1e-3	0.666±7.0e-4	0.900±5.2e-4	0.765±6.6e-4	0.725±8.5e-4
BRW- $W_U$ (ItemRank)	0.318±1.4e-3	0.671±1.5e-3	0.713±2.4e-3	0.691±1.2e-3	0.661±2.2e-3
BRW-P	0.438±2.6e-4	0.571±3.4e-4	0.499±4.2e-4	0.532±3.2e-4	0.606±2.3e-4

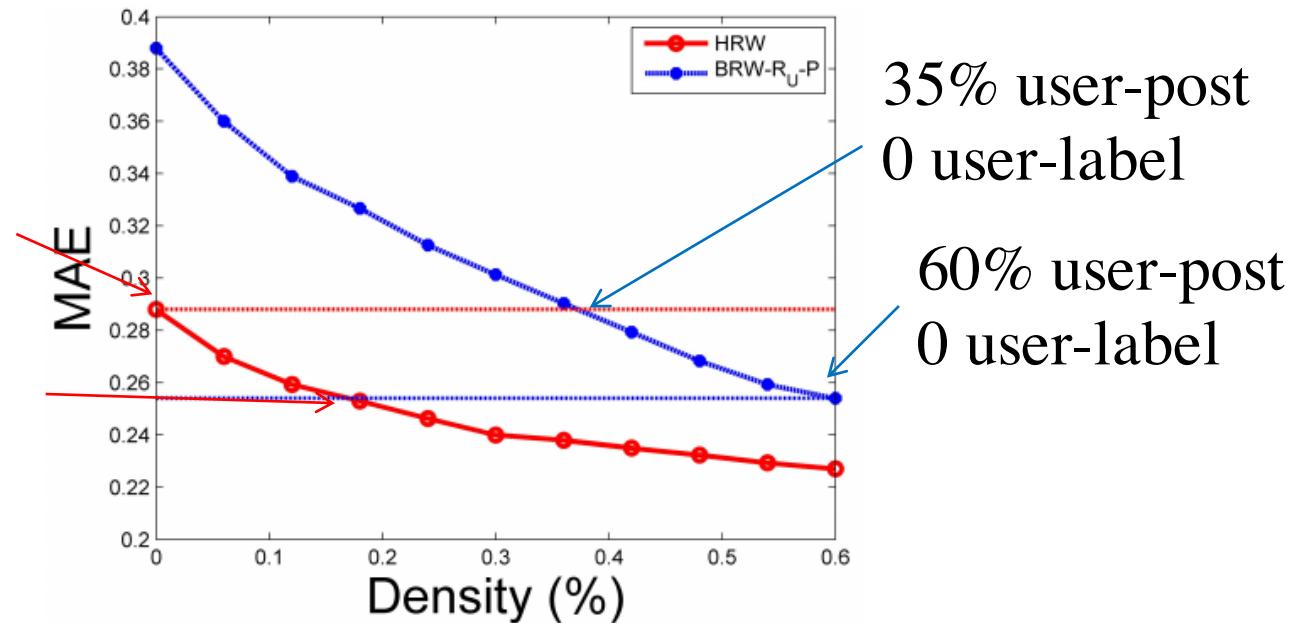
## Comparing with Social Recommendation Baselines

Algorithm	MAE	Precision	Recall	F1	Kendall's $\hat{\tau}$
HRW	<b>0.227±1.5e-3</b>	<b>0.711±1.3e-3</b>	0.921±1.4e-3	<b>0.802±1.1e-3</b>	<b>0.792±2.5e-3</b>
BRW- $R_U$ -P (TrustWalker) [10]	0.276±1.1e-3	0.657±7.6e-4	0.935±9.8e-4	0.772±7.6e-4	0.774±1.6e-3
BRW- $W_U$ (ItemRank) [8]	0.318±1.4e-3	0.671±1.5e-3	0.713±2.4e-3	0.691±1.2e-3	0.661±2.2e-3
MCF [5]	0.352±2.3e-4	0.592±1.8e-3	<b>0.951±6.0e-4</b>	0.730±1.3e-3	0.582±4.3e-4
CF [22]	0.506±3.4e-4	0.552±1.5e-3	0.589±7.2e-4	0.570±1.0e-3	0.540±5.2e-4

# Results: Insight

- ❑ Knowledge transfer from auxiliary domains improves cold-start users' behavior prediction
  - ❑ Using aux. (label) data, saving **60-70%** tgt. (post) data

0 user-post  
100% user-label  
  
18% user-post  
100% user-label



# Observation: Multiple Platforms



# Observation: Cross-Platform

## Add Facebook Login to Your App or Website

Facebook Login for Apps is a secure, fast and convenient way for people to log into your app or website.



iOS



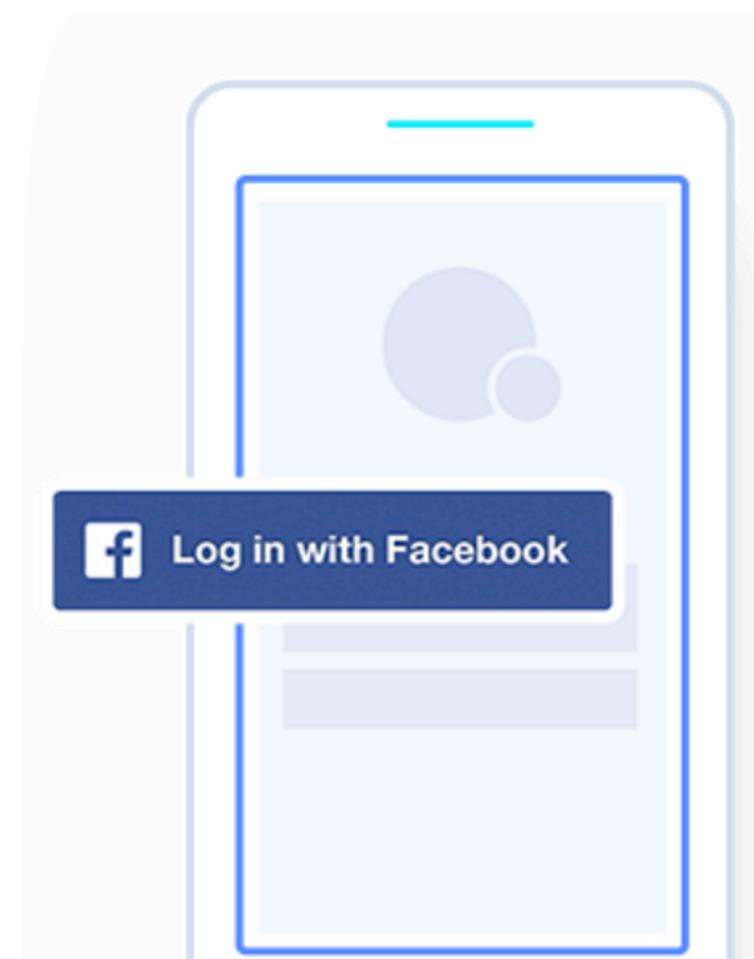
Android



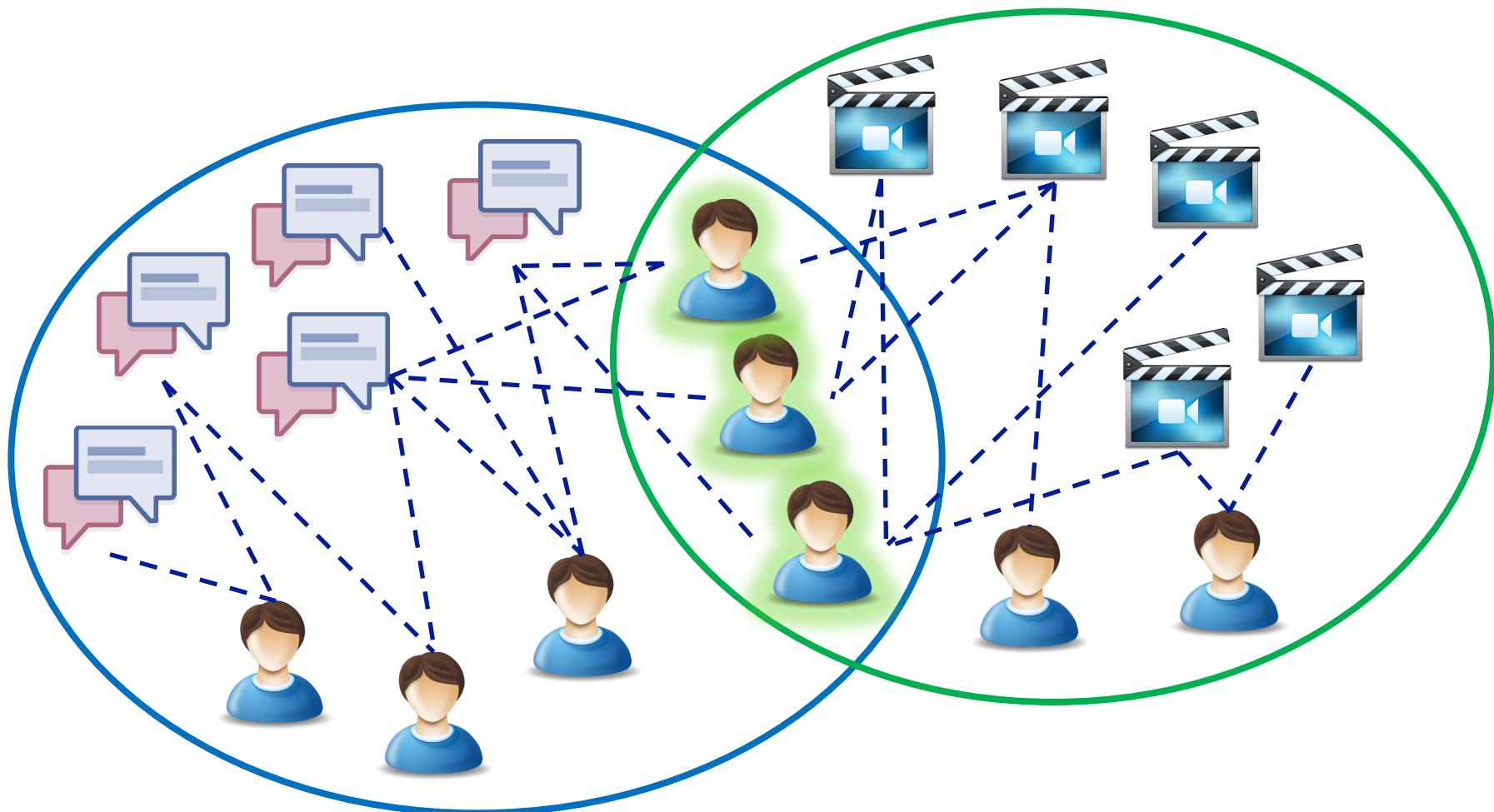
Websites or mobile websites



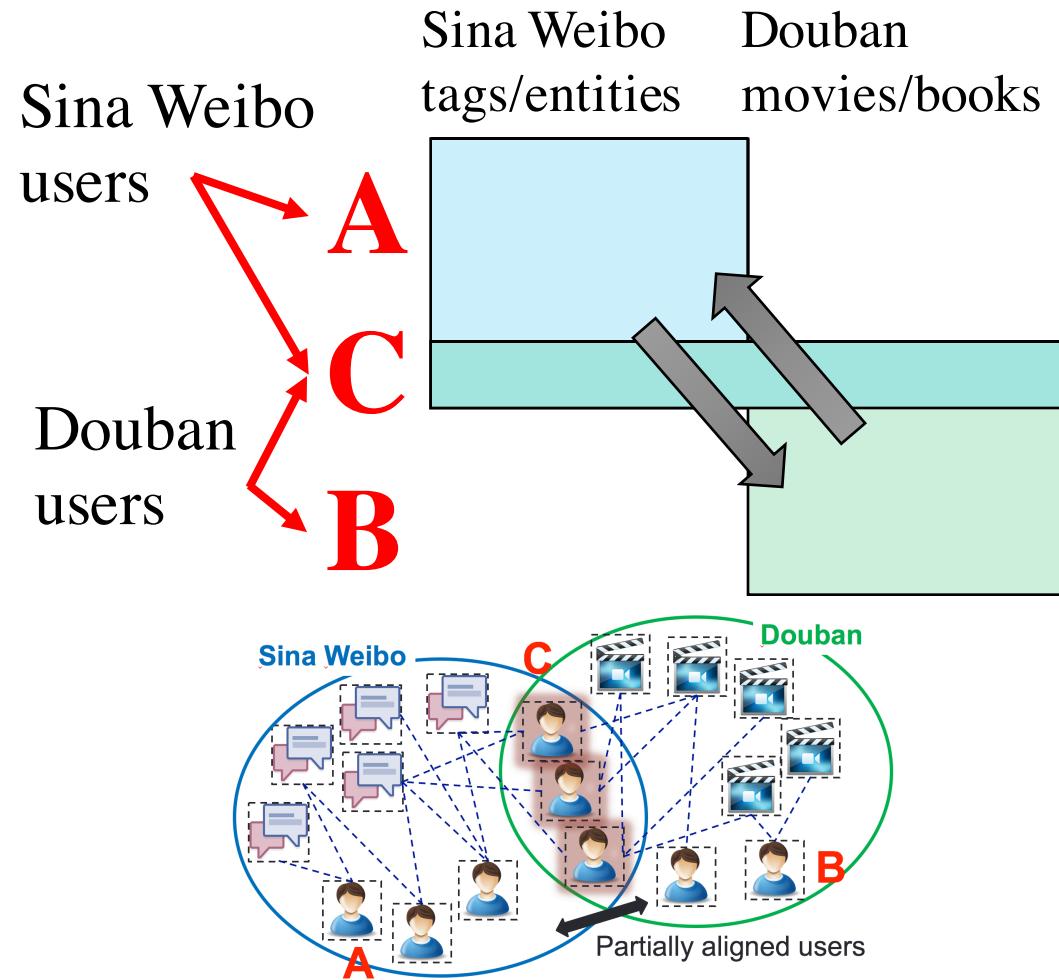
More platforms



# Observation: Partially Overlapped Crowds



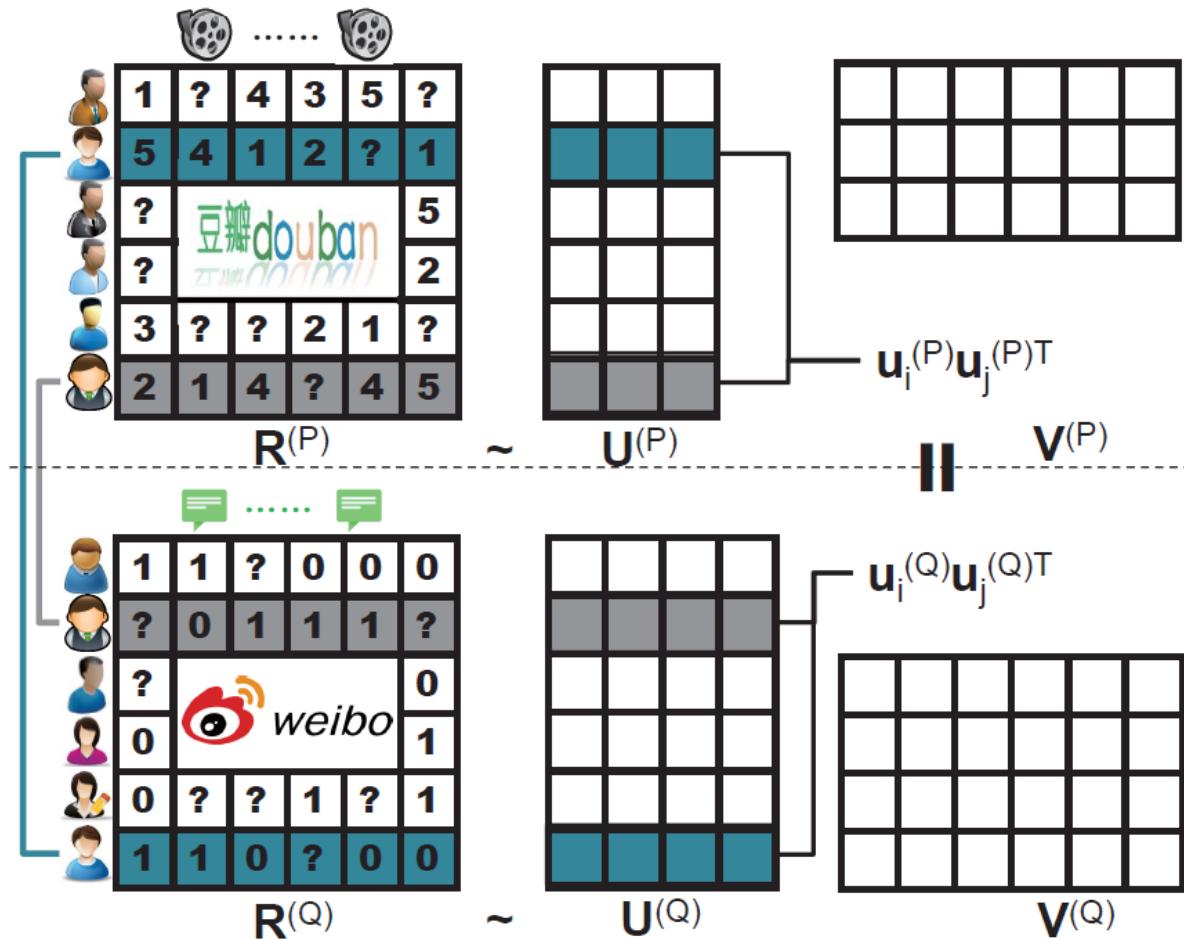
# Representation: When NO Transfer



User set	Weibo tweet entity to Douban movie	RMSE	MAP
A	Auxiliary platform data!		
C	<b>0.779</b>	<b>0.805</b>	
B	<b>1.439</b>		0.640

User set	Douban book to Weibo social tag	RMSE	MAP
A		<b>0.429</b>	0.464
C	<b>0.267</b>	<b>0.666</b>	
B	Auxiliary platform data!		

# Algorithm: XPTTrans



# Algorithm: XPTTrans

## □ Input

- Tgt./Aux. platform P/Q;
- Behavior data R(P)/R(Q);
- Observation W(P)/W(Q);
- Overlapping indicator W(P,Q),

## □ Output

- User latent representation U(P)/U(Q);
- Item latent representation V(P)/V(Q);
- Missing values in R(P)

## □ Objective function

Target platform      Auxiliary platform

$$\mathcal{J} = \sum_{i,j} W_{i,j}^{(P)} \left( R_{i,j}^{(P)} - \sum_r U_{i,r}^{(P)} V_{r,j}^{(P)} \right)^2 + \lambda \sum_{i,j} W_{i,j}^{(Q)} \left( R_{i,j}^{(Q)} - \sum_r U_{i,r}^{(Q)} V_{r,j}^{(Q)} \right)^2 + \mu \sum_{i_1,j_1,i_2,j_2} W_{i_1,j_1}^{(P,Q)} W_{i_2,j_2}^{(P,Q)} \left( A_{i_1,i_2}^{(P)} - A_{j_1,j_2}^{(Q)} \right)^2$$

Overlapping user similarity  
(Pair-wise regularization)

# Results: Leveraging Auxiliary Platform Data

## NO Transfer

User set	Weibo tweet entity to Douban movie	
	RMSE	MAP
A	Auxiliary platform data!	
C	0.779	0.805
B	<b>1.439</b>	<b>0.640</b>

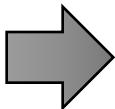
User set	Douban book to Weibo social tag	
	RMSE	MAP
A	<b>0.429</b>	<b>0.464</b>
C	0.267	0.666
B	Auxiliary platform data!	

## Transfer via the Same Latent Space

User set	Weibo tweet entity to Douban movie	
	RMSE	MAP
A		
C	0.757	0.811
B	<b>1.164 (-19%)</b>	<b>0.702 (+9.7%)</b>

User set	Douban book to Weibo social tag	
	RMSE	MAP
A	<b>0.411 (-4.2%)</b>	<b>0.487 (+5.0%)</b>
C	0.256	0.681
B		

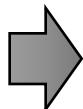




# Results: Leveraging Different Latent Spaces

## Transfer via the Same Latent Space

User set	Weibo tweet entity to Douban movie	
	RMSE	MAP
A		
C	0.757	0.811
B	<b>1.164</b>	<b>0.702</b>
User set	Douban book to Weibo social tag	
	RMSE	MAP
A	<b>0.411</b>	<b>0.487</b>
C	0.256	0.681
B		



## Transfer via Different Latent Spaces

User set	Weibo tweet entity to Douban movie	
	RMSE	MAP
A		
C	0.715	0.821
B	<b>0.722 (-38%)</b>	<b>0.820 (+17%)</b>
User set	Douban book to Weibo social tag	
	RMSE	MAP
A	<b>0.374 (-11 %)</b>	<b>0.533 (+12 %)</b>
C	0.236	0.705
B		

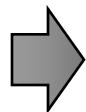
# Results: Where Amazing Happens

## NO Transfer

User set	Weibo tweet entity to Douban movie	
	RMSE	MAP
A	Auxiliary platform data!	
C	0.779	0.805
B	1.439	0.640

User set	Douban book to Weibo social tag	
	RMSE	MAP
A	0.429	0.464
C	0.267	0.666
B	Auxiliary platform data!	



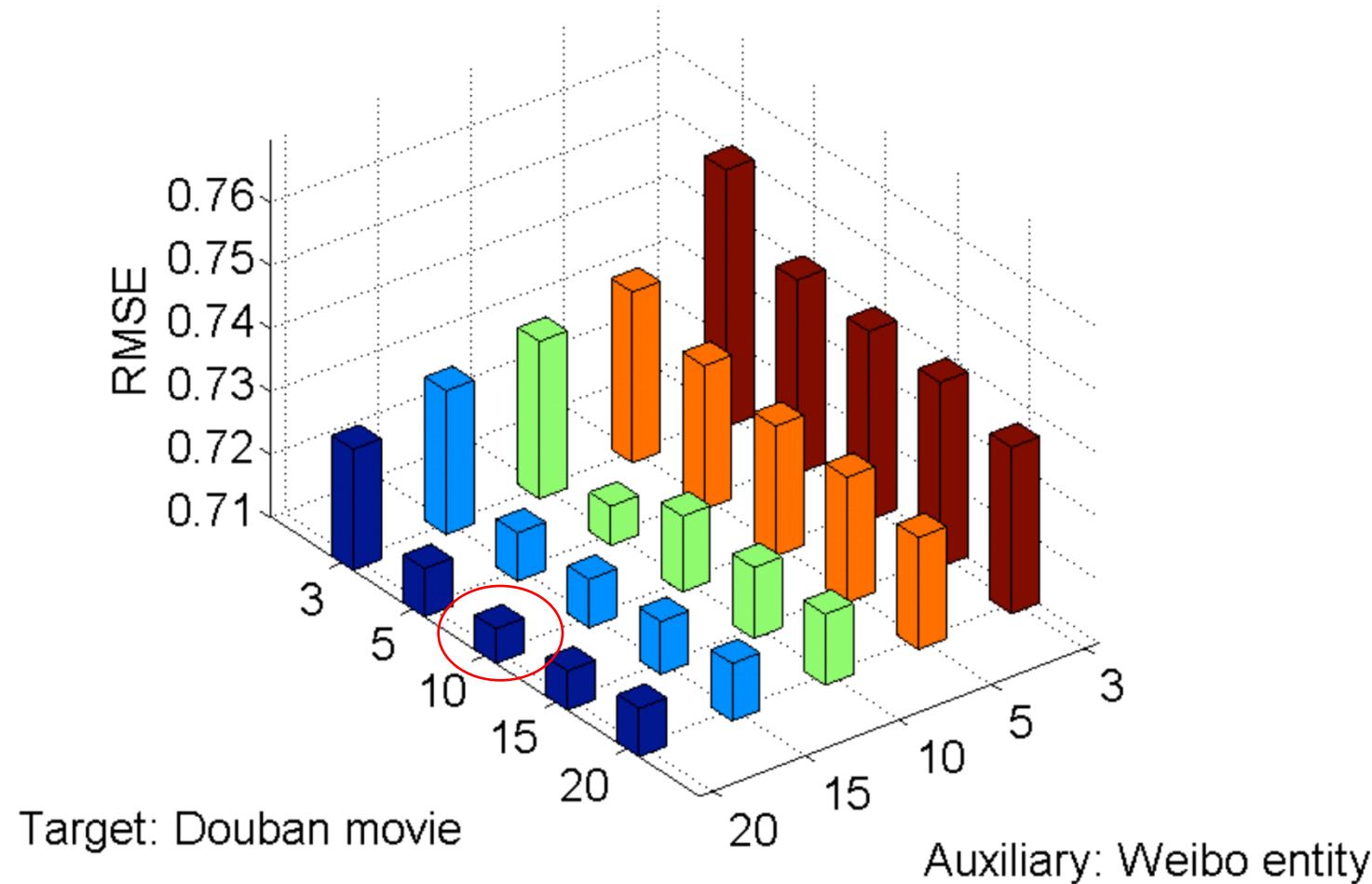
## Transfer via Different Latent Spaces

User set	Weibo tweet entity to Douban movie	
	RMSE	MAP
A		
C	0.715	0.821
B	0.722	0.820

User set	Douban book to Weibo social tag	
	RMSE	MAP
A	0.374	0.533
C	0.236	0.705
B		

# Results: Different Sizes of Latent Spaces





# Summary

- ❑ Like, Reply, Share, Retweet, Favorite, Comment ...
- ❑ Memory based social recommenders
  - ❑ TidalTrust, MoleTrust, TrustWalker
- ❑ Model based social recommenders
  - ❑ SoRec, “Social Trust” Ensemble, SoReg
- ❑ **Observations, Representations, Models**
  - ❑ **ContextMF**: Social contexts (preference & influence)
  - ❑ **FEMA**: Spatiotemporal contexts (multidimensional)
  - ❑ **HybridRW**: Cross-domain behavior modeling
  - ❑ **XPTrans**: Cross-platform behavior modeling



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微软亚洲研究院



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# Thank you!

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