

Pattern Discovery: Definition

- What are patterns?
 - Patterns: A set of items, subsequences, or substructures that occur frequently together (or strongly correlated) in a data set
 - Patterns represent intrinsic and important properties of datasets
- Pattern discovery: Uncovering patterns from massive data
- Motivation examples:
 - What products were often purchased together?
 - What are the subsequent purchases after buying an iPad?
 - What code segments likely contain copy-and-paste bugs?
 - What word sequences likely form phrases in this corpus?

Pattern Discovery: Why Is It Important?

- Finding inherent regularities in a data set
- Foundation for many essential data mining tasks
 - Association, correlation, and causality analysis
 - Mining sequential, structural (e.g., sub-graph) patterns
 - Pattern analysis in spatiotemporal, multimedia, timeseries, and stream data
 - Classification: Discriminative pattern-based analysis
 - Cluster analysis: Pattern-based subspace clustering
- Broad applications
 - Market basket analysis, cross-marketing, catalog design, sale campaign analysis, Web log analysis, biological sequence analysis

Frequent Patterns (Itemsets)

- Itemset: A set of one or more items
- k-itemset: $X = \{x_1, ..., x_k\}$
- (absolute) support (count) of X: Frequency or the number of occurrences of an itemset X
- (relative) support, s: The fraction of transactions that contains X (i.e., the probability that a transaction L contains X)
- An itemset X is frequent if the support of X is no less than a minsup threshold

Tid	Items bought	
10	Beer, Nuts, Diaper	
20	Beer, Coffee, Diaper	
30	Beer, Diaper, Eggs	
40	Nuts, Eggs, Milk	
50	Nuts, Coffee, Diaper, Eggs, Milk	

Let minsup = 50%

Freq. 1-itemsets:

Beer: 3 (60%); Nuts: 3 (60%)

Diaper: 4 (80%); Eggs: 3 (60%)

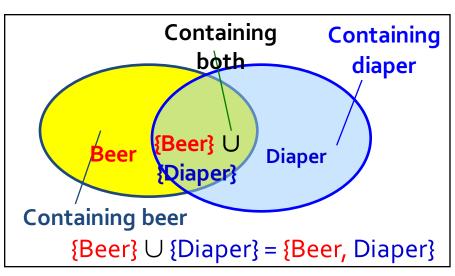
Freq. 2-itemsets:

{Beer, Diaper}: 3 (60%)

From Frequent Itemsets to Association Rules

- Association rules: $X \rightarrow Y$ (s, c)
 - Support, s: The probability that a transaction contains X ∪ Y
 - Confidence, c: The conditional probability that a transaction containing X also contains Y
 - $-c = \sup(X \cup Y) / \sup(X)$
- Association rule mining: Find all of the rules, X → Y, with minimum support and confidence
- Frequent itemsets: Let *minsup* = 50%
 - Freq. 1-itemsets: Beer: 3, Nuts: 3,
 Diaper: 4, Eggs: 3
 - Freq. 2-itemsets: {Beer, Diaper}: 3
- Association rules: Let minconf = 50%
 - − Beer → Diaper (60%, 100%)
 - Diaper → Beer (60%, 75%)

Tid	Items bought	
10	Beer, Nuts, Diaper	
20	Beer, Coffee, Diaper	
30	Beer, Diaper, Eggs	
40	Nuts, Eggs, Milk	
50	Nuts, Coffee, Diaper, Eggs, Milk	



Note: Itemset: $X \cup Y$, a subtle notation!

Challenge: There Are Too Many Frequent Patterns!

- A long pattern contains a combinatorial number of sub-patterns
- How many frequent itemsets does the following TDB₁ contain?

```
- TDB_1: T_1: \{a_1, ..., a_{50}\}; T_2: \{a_1, ..., a_{100}\}
```

- Assuming (absolute) minsup = 1
- Let's have a try

```
1-itemsets: \{a_1\}: 2, \{a_2\}: 2, ..., \{a_{50}\}: 2, \{a_{51}\}: 1, ..., \{a_{100}\}: 1, 2-itemsets: \{a_1, a_2\}: 2, ..., \{a_1, a_{50}\}: 2, \{a_1, a_{51}\}: 1 ..., ..., \{a_{99}, a_{100}\}: 1, ... 99-itemsets: \{a_1, a_2, ..., a_{99}\}: 1, ..., \{a_2, a_3, ..., a_{100}\}: 1 100-itemset: \{a_1, a_2, ..., a_{100}\}: 1 - In total: \binom{100}{1} + \binom{100}{2} + ... + \binom{100}{100} = 2^{100} - 1 sub-patterns!
```

A too huge set for any computer to compute or store!

Expressing Patterns in Compressed Form: Closed Patterns

- How to handle such a challenge?
- Solution 1: Closed patterns: A pattern (itemset) X is closed if X is frequent, and there exists no super-pattern Y > X, with the same support as X
 - Let Transaction DBTDB₁: T_1 : {a₁, ..., a₅₀}; T_2 : {a₁, ..., a₁₀₀}
 - Suppose minsup = 1. How many closed patterns does TDB₁ contain?
 - Two: P₁: "{a₁, ..., a₅₀}: 2"; P₂: "{a₁, ..., a₁₀₀}: 1"
- Closed pattern is a lossless compression of frequent patterns
 - Reduces the # of patterns but does not lose the support information!
 - You will still be able to say: " $\{a_2, ..., a_{40}\}$: 2", " $\{a_5, a_{51}\}$: 1"

Expressing Patterns in Compressed Form: Max-Patterns

- Solution 2: Max-patterns: A pattern X is a max-pattern if X is frequent and there exists no frequent super-pattern Y > X, with the same support as X
- Difference from close-patterns?
 - Do not care the real support of the sub-patterns of a max-pattern
 - Let Transaction DB TDB₁: T_1 : {a₁, ..., a₅₀}; T_2 : {a₁, ..., a₁₀₀}
 - Suppose minsup = 1. How many max-patterns does TDB₁ contain?
 - One: P: "{a₁, ..., a₁₀₀}: 1"
- Max-pattern is a lossy compression!
 - We only know {a₁, ..., a₄₀} is frequent
 - But we do not know the real support of $\{a_1, ..., a_{40}\}, ...,$ any more!
- Thus in many applications, mining closed-patterns is more desirable than mining max-patterns

The Downward Closure Property of Frequent Patterns: Apriori

- Observation: From TDB₁: T₁: {a₁, ..., a₅₀}; T₂: {a₁, ..., a₁₀₀}
 - We get a frequent itemset: {a₁, ..., a₅₀}
 - Also, its subsets are all frequent: $\{a_1\}$, $\{a_2\}$, ..., $\{a_{50}\}$, $\{a_1, a_2\}$, ..., $\{a_1, ..., a_{49}\}$, ...
 - There must be some hidden relationships among frequent patterns!
- The downward closure (also called "Apriori") property of frequent patterns
 - If {beer, diaper, nuts} is frequent, so is {beer, diaper}
 - Every transaction containing {beer, diaper, nuts} also contains {beer, diaper}
 - Apriori: Any subset of a frequent itemset must be frequent
- Efficient mining methodology
 - If any subset of an itemset S is infrequent, then there is no chance for S to be frequent—why do we even have to consider S!?

Apriori Pruning and Scalable Mining Methods

- Apriori pruning principle: If there is any itemset which is infrequent, its superset should not even be generated! (Agrawal & Srikant @VLDB'94, Mannila, et al. @ KDD' 94)
- Scalable mining Methods: Three major approaches
 - Level-wise, join-based approach: Apriori (Agrawal & Srikant@VLDB'94)
 - Vertical data format approach: Eclat (Zaki, Parthasarathy, Ogihara, Li@KDD'97)
 - Frequent pattern projection and growth: FPgrowth (Han, Pei, Yin @SIGMOD'00)

Apriori: A Candidate Generation & Test Approach

- Outline of Apriori (level-wise, candidate generation and test)
 - Initially, scan DB once to get frequent 1-itemset
 - Repeat
 - Generate length-(k+1) candidate itemsets from length-k frequent itemsets
 - Test the candidates against DB to find **frequent** (k+1)-itemsets
 - Set k := k +1
 - Until no frequent or candidate set can be generated
 - Return all the frequent itemsets derived

The Apriori Algorithm (Pseudo-Code)

```
C_k: Candidate itemset of size k
F_k: Frequent itemset of size k
K := 1;
F_{\nu} := \{ \text{frequent items} \}; // \text{ frequent 1-itemset } \}
While (F_k!=\emptyset) do \{ // when F_k is non-empty
  C_{k+1} := candidates generated from F_{k}; // candidate generation
  Derive F_{k+1} by counting candidates in C_{k+1} with respect to TDB at
   minsup;
  k := k + 1
return \bigcup_k F_k // return F_k generated at each level
```

The Apriori Algorithm: An Example



Tid	Items
10	A, C, D
20	В, С, Е
30	A, B, C, E
40	B, E



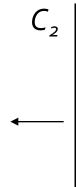
1st scan

Itemset	sup
{A}	2
{B}	3
{C}	3
{D}	1
{E}	3

F	<u>-</u> 1
•	1

ltemset	sup
{A}	2
{B}	3
{C}	3
{E}	3

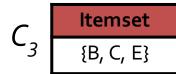
F_{2}	ltemset	sup
	{A, C}	2
	{B, C}	2
	{B, E}	3
	{C, E}	2



Itemset	sup
{A, B}	1
{A, C}	2
{A, E}	1
{B, C}	2
{B, E}	3
{C, E}	2

2nd scan

Itemset	
{A, B}	
{A, C}	
{A, E}	
{B, C}	
{B, E}	
{C, E}	



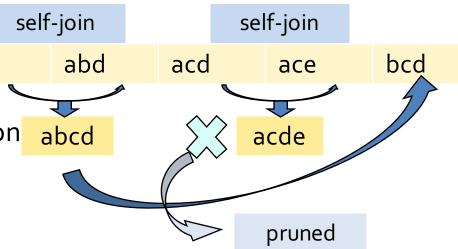
3 rd scan	F

Itemset	sup
{B, C, E}	2

Apriori: Implementation Tricks

abc

- How to generate candidates?
 - Step 1: self-joining F_k
 - Step 2: pruning
- Example of candidate-generation
 - $-F_3 = \{abc, abd, acd, ace, bcd\}$
 - Self-joining: $F_3 * F_3$
 - abcd from abc and abd
 - acde from acd and ace
 - Pruning:
 - acde is removed because ade is not in F₃
 - $C_4 = \{abcd\}$



Candidate Generation: An SQL Implementation

Suppose the items in F_{k-1} are self-join listed self-join in an order abc abd bcd acd ace • Step 1: self-joining F_{k-1} acde abcd insert into C_k select *p.item*₁, *p.item*₂, ..., *p.item*_k. 1, q.item_{k-1} pruned from F_{k-1} as p, F_{k-1} as qwhere $p.item_1 = q.item_1, ..., p.item_k$ $_{2}$ = $q.item_{k-2}$, $p.item_{k-1}$ < $q.item_{k-1}$ Step 2: pruning for all *itemsets c in C_k* do for all (k-1)-subsets s of c do

if (s is not in F_{k-1}) then delete c

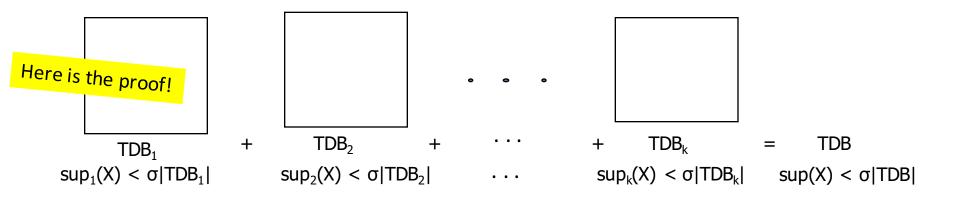
from C_k

Apriori: Improvements and Alternatives

- Reduce passes of transaction database scans
 - Partitioning (e.g., Savasere, et al., 1995)
 - Dynamic itemset counting (Brin, et al., 1997)
- Shrink the number of candidates
 - Hashing (e.g., DHP: Park, et al., 1995)
 - Pruning by support lower bounding (e.g., Bayardo 1998)
 - Sampling (e.g., Toivonen, 1996)
- Exploring special data structures
 - Tree projection (Agarwal, et al., 2001)
 - H-miner (Pei, et al., 2001)
 - Hypecube decomposition (e.g., LCM: Uno, et al., 2004)

Partitioning for Parallelization

 Theorem: Any itemset that is potentially frequent in TDB must be frequent in at least one of the partitions of TDB



- Method: (A. Savasere, E. Omiecinski and S. Navathe, VLDB'95)
 - Scan 1: Partition database and find local frequent patterns
 - Scan 2: Consolidate global frequent patterns

Discussion

- How do you define frequent patterns in scientific knowledge discovery and technology exploration?
 - {"social spam detection", "matrix factorization"}
 - {"social spam detection", "Twitter"}
 - **—** ...
- Do you believe in the association: Diapers -> Beer?

References

- R. Agrawal, T. Imielinski, and A. Swami, "Mining association rules between sets of items in large databases", in Proc. of SIGMOD'93
- R. J. Bayardo, "Efficiently mining long patterns from databases", in Proc. of SIGMOD'98
- N. Pasquier, Y. Bastide, R. Taouil, and L. Lakhal, "Discovering frequent closed itemsets for association rules", in Proc. of ICDT'99
- J. Han, H. Cheng, D. Xin, and X. Yan, "Frequent Pattern Mining: Current Status and Future Directions", Data Mining and Knowledge Discovery, 15(1): 55-86, 2007
- R. Agrawal and R. Srikant, "Fast algorithms for mining association rules", VLDB'94
- A. Savasere, E. Omiecinski, and S. Navathe, "An efficient algorithm for mining association rules in large databases", VLDB'95
- J. S. Park, M. S. Chen, and P. S. Yu, "An effective hash-based algorithm for mining association rules", SIGMOD'95
- S. Sarawagi, S. Thomas, and R. Agrawal, "Integrating association rule mining with relational database systems: Alternatives and implications", SIGMOD'98
- M. J. Zaki, S. Parthasarathy, M. Ogihara, and W. Li, "Parallel algorithm for discovery of association rules", Data Mining and Knowledge Discovery, 1997
- J. Han, J. Pei, and Y. Yin, "Mining frequent patterns without candidate generation", SIGMOD'00

References (cont.)

- M. J. Zaki and Hsiao, "CHARM: An Efficient Algorithm for Closed Itemset Mining", SDM'02
- J. Wang, J. Han, and J. Pei, "CLOSET+: Searching for the Best Strategies for Mining Frequent Closed Itemsets", KDD'03
- C. C. Aggarwal, M.A., Bhuiyan, M. A. Hasan, "Frequent Pattern Mining Algorithms: A Survey", in Aggarwal and Han (eds.): Frequent Pattern Mining, Springer, 2014
- C. C. Aggarwal and P. S. Yu. A New Framework for Itemset Generation. PODS'98
- S. Brin, R. Motwani, and C. Silverstein. Beyond market basket: Generalizing association rules to correlations. SIGMOD'97
- M. Klemettinen, H. Mannila, P. Ronkainen, H. Toivonen, and A. I. Verkamo. Finding interesting rules from large sets of discovered association rules. CIKM'94
- E. Omiecinski. Alternative Interest Measures for Mining Associations. TKDE'03
- P.-N. Tan, V. Kumar, and J. Srivastava. Selecting the Right Interestingness Measure for Association Patterns. KDD'02
- T. Wu, Y. Chen and J. Han, Re-Examination of Interestingness Measures in Pattern Mining: A Unified Framework, Data Mining and Knowledge Discovery, 21(3):371-397, 2010