

$$E_{0,e} = 0.510\,998\,95\,\text{MeV}$$

$$m_{0,e} = 0.510\,998\,95\,\text{MeV}/c^2$$

$$k = \frac{g}{p/q}$$

$$k[\text{m}^{-2}] = 299.792458 \frac{g[\text{T/m}]}{p/q[\text{MeV}/c/e]}$$

$$E_{\text{ges}}(E_{\text{kin}}) = E_{\text{kin}} + E_0$$

$$E_{\text{ges}}(p) = \sqrt{(pc)^2 + E_0^2}$$

$$E_{\text{ges}}(\gamma) = \gamma \cdot E_0$$

$$E_{\text{ges}}(\beta) = \frac{E_0}{\sqrt{1 - \beta^2}}$$

$$E_{\text{kin}}(E_{\text{ges}}) = E_{\text{ges}} - E_0$$

$$E_{\text{kin}}(p) = \sqrt{(pc)^2 + E_0^2} - E_0$$

$$E_{\text{kin}}(\gamma) = (\gamma - 1) \cdot E_0$$

$$E_{\text{kin}}(\beta) = \left(\frac{1}{\sqrt{1 - \beta^2}} - 1 \right) \cdot E_0$$

$$p(E_{\text{ges}}) = \frac{1}{c} \sqrt{E_{\text{ges}}^2 - E_0^2}$$

$$p(E_{\text{kin}}) = \frac{1}{c} \sqrt{(E_{\text{kin}} + E_0)^2 - E_0^2} = \frac{1}{c} \sqrt{E_{\text{kin}}^2 + 2E_{\text{kin}}E_0}$$

$$p(\beta, \gamma) = \beta \cdot \gamma \cdot E_0 / c$$

$$p(\gamma) = \sqrt{\gamma^2 - 1} \cdot E_0 / c$$

$$p(\beta) = \frac{\beta}{\sqrt{1 - \beta^2}} \cdot E_0 / c$$

$$\gamma(E_{\text{ges}}) = \frac{E_{\text{ges}}}{E_0}$$

$$\gamma(E_{\text{kin}}) = \frac{E_{\text{kin}}}{E_0} + 1$$

$$\gamma(p) = \frac{\sqrt{(pc)^2 + E_0^2}}{E_0}$$

$$\gamma(\beta) = \frac{1}{\sqrt{1 - \beta^2}}$$

$$\beta(E_{\text{ges}}) = \sqrt{1 - \frac{E_0^2}{E_{\text{ges}}^2}}$$

$$\beta(E_{\text{kin}}) = \sqrt{1 - \frac{E_0^2}{(E_{\text{kin}} + E_0)^2}}$$

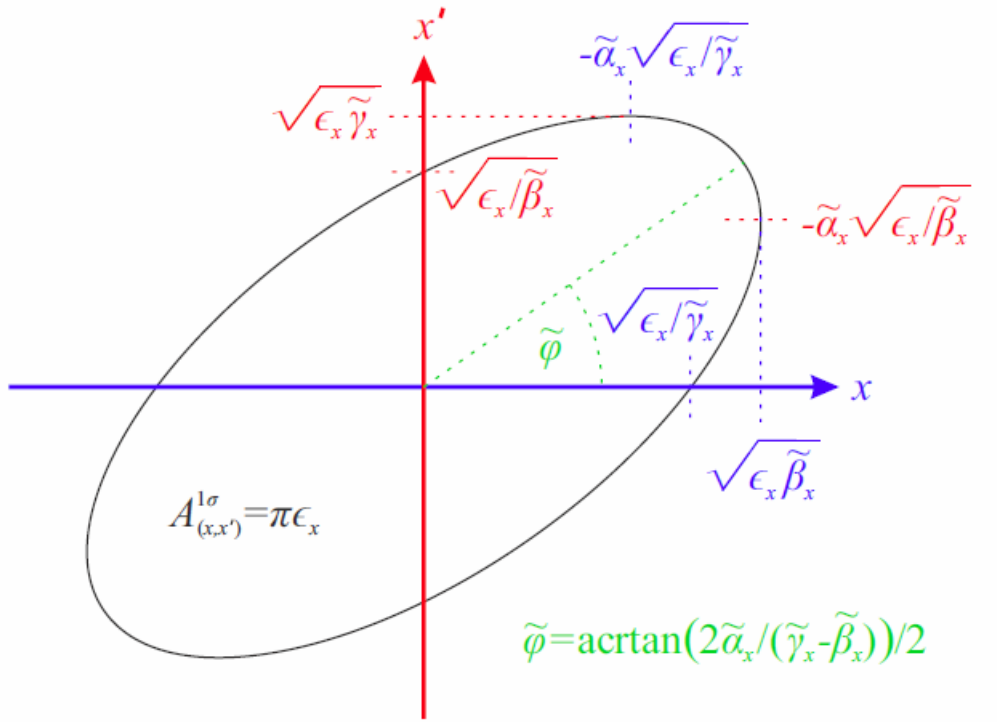
$$\beta(p) = \sqrt{1 - \frac{E_0^2}{(pc)^2 + E_0^2}}$$

$$\beta(\gamma) = \sqrt{1 - \frac{1}{\gamma^2}}$$

$$\begin{aligned}
pc &= \beta E_{\text{ges}} \\
p &= \beta \gamma m_0 c \\
\gamma^2 &= 1 + \beta^2 \gamma^2 \\
\gamma &= \sqrt{(\beta \gamma)^2 + 1} = \sqrt{(p/(m_0 c))^2 + 1} \\
\beta^2 \gamma^2 &= \gamma^2 - 1 = \left(\gamma - \frac{1}{\gamma} \right)^2 + \beta^2 \\
\beta \gamma &= \sqrt{\gamma^2 - 1} \\
1 &= \beta^2 + \frac{1}{\gamma^2} \\
\frac{\partial \beta}{\partial \gamma} &= \frac{1}{\beta \gamma^3} \\
\frac{\partial \gamma}{\partial \beta} &= \frac{\beta}{(1 - \beta^2)^{3/2}} = \beta \gamma^3 = (\gamma^2 - 1) \frac{\gamma}{\beta} \\
\frac{\partial(cp)}{\partial \beta} &= E_0 \gamma^3 \\
\frac{\partial p}{\partial E_{\text{kin}}} &= \frac{\gamma}{\gamma + 1} \frac{p}{E_{\text{kin}}} \\
\frac{\partial E_{\text{ges}}}{\partial p} &= \beta^2 \frac{E_{\text{ges}}}{p} \\
\frac{\partial \beta}{\partial p} &= \frac{\beta}{\gamma^2 p}
\end{aligned}$$

$$\begin{aligned}\epsilon_n &= \epsilon\beta\gamma \\ \epsilon &= \gamma x^2 + 2\alpha x x' + \beta x'^2 \\ \alpha(s) &= -\frac{1}{2} \frac{\partial \beta(s)}{\partial s} \\ \gamma &= \frac{1+\alpha^2}{\beta} \\ 1 &= \beta\gamma - \alpha^2\end{aligned}$$

$$\beta(s) = \beta^* + \frac{s^2}{\beta^*}$$



$$\begin{pmatrix} \beta & -\alpha \\ -\alpha & \gamma \end{pmatrix}_2 = R \cdot \begin{pmatrix} \beta & -\alpha \\ -\alpha & \gamma \end{pmatrix}_1 \cdot R^T$$

R_{56} -Definition:

<https://www3.aps.anl.gov/forums/elegant/viewtopic.php?f=17&t=987>

<https://www3.aps.anl.gov/forums/elegant/viewtopic.php?f=17&t=966&p=4024&hilit=r56#p4024>

Es gilt in linearer Näherung erster Ordnung in elegant:

$$\begin{aligned}
 \sigma_{56} &= \langle s\delta \rangle = \langle (R_{55}s_0 + R_{56}\delta_0) \cdot (R_{66}\delta_0 + R_{65}s_0) \rangle \\
 &= \langle R_{55}R_{66}s_0\delta_0 + R_{56}R_{66}\delta_0^2 + R_{55}R_{65}s_0^2 + R_{56}R_{65}s_0\delta_0 \rangle \\
 &\stackrel{\text{no acc.}}{=} \langle s_0\delta_0 + R_{56}\delta_0^2 \rangle \\
 &= \underbrace{\langle s_0\delta_0 \rangle}_{\sigma_{560}} + R_{56} \langle \delta_0^2 \rangle
 \end{aligned}$$

Index 0 ist der Startpunkt. Falls am Ursprung ($s = 0$), folgt:

$$\begin{aligned}
 \sigma_{56} &= \langle s\delta \rangle = R_{56} \langle \delta_0^2 \rangle \\
 \Leftrightarrow R_{56} &= \frac{\sigma_{56}}{\langle \delta_0^2 \rangle} = \frac{\langle s\delta \rangle}{\langle \delta_0^2 \rangle}
 \end{aligned}$$

$R_{56} = ds/d\delta$, where $\delta = (p - p_0)/p_0$, p_0 being the initial momentum (i.e., prior to acceleration).

Wenn nicht beschleunigt wird, gilt ferner $\delta = \delta_0$. If there is no acceleration, $R_{55}=R_{66}=1$ and $R_{65}=0$. A cavity with phase=0 has a non-zero R_{65} element, which can interact with the R_{56} in the chicane. You'll also see R_{55} change.

<https://www3.aps.anl.gov/forums/elegant/viewtopic.php?f=12&t=581&p=2336&hilit=r56#p2336>

$$\eta_x = e\tau\alpha x = \sigma_{16}/\sqrt{\sigma_{66}}$$

wobei $e\tau\alpha x$ abhängig von der „lokalen“ energy deviation, not the energy deviation at the start of the beamline. R_{16} in contrast is a transport matrix coefficient from the beginning of the beamline. $e\tau\alpha x$ and R_{16} are different when you have acceleration.

Offene Frage: wann wird der bezug resettet? wenn energie sich ändert?

<https://www3.aps.anl.gov/forums/elegant/viewtopic.php?f=17&t=818&p=3379&hilit=r56#p3379>

The default for `twiss_output` is to compute the local dispersion. This can be changed by setting the `local_dispersion` parameter to 0. Because `local_dispersion=1` in `twiss_output`, you'll see apparent inconsistencies with the transport matrix elements, which are always referenced to the initial coordinates. The local dispersion should be consistent with the

effective dispersion computed from the beam moments, unless there is strong nonlinearity (e.g., if x and delta have a strong nonlinear correlation).

<https://www3.aps.anl.gov/forums/elegant/viewtopic.php?f=11&t=804&p=3333&hilit=r56#p3333>

In elegant, R56 is defined as ds/dp_{Initial} , where p_{Initial} is the momentum at the start of the beamline. In many cases, people compute $ds/dp_{\text{ChicaneInput}}$, which is a different number when there is acceleration. Sorry, that should be $R56 = ds/dp_{\text{Initial}} \cdot p_{\text{Initial0}}$, etc.

\Rightarrow

$$R_{56,\text{elegant},\text{lokal}} = \frac{ds}{\frac{dp_{\text{Initial}}}{p_{\text{Initial},0}}} = \frac{ds}{\frac{dp_{\text{Initial}}}{p_{\text{Final},0}}} \cdot \frac{p_{\text{Initial},0}}{p_{\text{Final},0}}$$

\Rightarrow

$$R_{56,\text{elegant},\text{Start2End}} = R_{56,\text{xbeam},\text{Sektion}_1} + R_{56,\text{xbeam},\text{Sektion}_2} \cdot \frac{p_{\text{Initial},0}}{p_{\text{Final},0}}$$

\Rightarrow

$$R_{56,\text{elegant},(\text{I1})2(\text{S})} = R_{56,\text{xbeam},\text{I1}} + R_{56,\text{xbeam},\text{F}} \cdot \frac{p_{\text{I1},0}}{p_{\text{F},0}} + R_{56,\text{xbeam},\text{S}} \cdot \frac{p_{\text{I1},0}}{p_{\text{S},0}}$$

\Rightarrow

$$R_{56,\text{elegant},(\text{I0})2(\text{S})} = R_{56,\text{xbeam},\text{I1}} \cdot \frac{p_{\text{I0},0}}{p_{\text{I1},0}} + R_{56,\text{xbeam},\text{F}} \cdot \frac{p_{\text{I0},0}}{p_{\text{F},0}} + R_{56,\text{xbeam},\text{S}} \cdot \frac{p_{\text{I0},0}}{p_{\text{S},0}}$$

<https://www3.aps.anl.gov/forums/elegant/viewtopic.php?f=9&t=343&p=1432&hilit=r56#p1432>

$$R_{76} = d\delta/dt$$

<https://www3.aps.anl.gov/forums/elegant/viewtopic.php?f=12&t=577&p=2312&hilit=r56#p2312>

You might try using the `analyze_map` command, which also determines the matrix from tracking.