

**Exercise Number: 3.6.1**

1.  $\mathcal{F}$  is a collection of subsets of  $\Omega$ .
2.  $\mathbb{P}(A)$  is a well-defined element of  $\mathbb{R}$  provided that  $A$  is an element of  $\mathcal{F}$ .
3.  $\{X \leq 5\}$  is shorthand notation for the particular subset of  $\Omega$  which is defined by:  $\{\omega \in \Omega \mid X(\omega) \leq 5\}$ .
4. If  $S$  is a subset of  $\mathbb{R}$ , then  $\{X \in S\}$  is a subset of  $\Omega$ .
5. If  $S$  is a Borel subset of  $\mathbb{R}$ , then  $\{X \in S\}$  must be an element of  $\mathcal{F}$ .