A model data analysis: Ego depletion

MK

December 13, 2019

Contents

1	Ego	depletion	2
2	Imp	ort and tidy	4
	2.1	e task	4
		2.1.1 Read in	4
		2.1.2 Tidy	5
	2.2	MSIT task	6
		2.2.1 Read in	6
		2.2.2 Tidy	7
	2.3	Subject info and ratings	8
	2.0	2.3.1 Read in	8
		2.0.1 1000d III	8
		2.3.2 Tidy	O
3	Pre	iminary description	10
	3.1	eTask data	10
			10
		3	12
			13
	3.2		14
	0.2		14
		- 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	14 18
	2.2		_
	3.3	Linear mixed-effects model	22

1 Ego depletion

Ego depletion is widely-debated topic in the psychological literature. It refers to the claim that people have less self-control in one domain after having to control themselves in another domain of their lives. Thus, one might expect that a person who performs a task that requires self-control (such as the suppression of thoughts, emotions, behavioral impulses, and habits) may not be able to exercise as much self-control in a subsequent task as a person who had not been required to engage in self-control. For example, people who had resisted tempting food, subsequently ate a larger amount of palatable (but unhealthy) food. Because it has been difficult to replicate studies of ego depletion, a group of psychologists in 23 labs independently conducted experiments using an agreed-upon standardized experimental method.

Method of the multilab replication of the ego-depletion effect

Data Collection

Participants were randomly allocated to experimental (ego-depletion) or control (no depletion) groups.

Procedure

They were told that the experiment was a study of speeded recognition of words and numbers. It consisted of two tasks: the "e" task, and the MSIT, both of which we will describe in a moment. Participants first practiced 20 trials from each tasks. Then they did the "e" task, after which they rated how effortful, fatiguing, difficult, and frustrating it had been. They then did the second task.

Materials

The "e" task. There were two conditions: depletion and no depletion, in which participants responded to each word as it appeared on the screen. In the depletion condition, they pressed a button when the word contained the letter "e," and refrained from pressing if the "e" was next to or one letter away from a vowel (an example might be the word done). In the nodepletion version they pressed a button whenever the word contained "e" (for example, done). The main session consisted of 150 trials and lasted 7.5 minutes.

Multi-source interference task (MSIT). The MSIT requires response inhibition. The stimuli were sets of three digits (the numerals 1, 2, 3, or 0). Participants placed their right index, middle, and ring fingers on three keys on the keyboard. On each trial, one of the digits (the target; 1, 2, or 3) differed from the two identical distractors. They pressed the key corresponding to the target digit. On congruent trials, the target matched its position on the keyboard, the distractors were 0s, and the size of the target differed from the distractors (for example: 020). On incongruent trials, the target did not match its position, the distractors were potential targets,

and the different-size digit was not always the target (for example: 233). The session consisted of 200 trials (100 congruent and 100 incongruent), which took about 10 minutes.

The data herein were collected by the lab of Mark J. Brandt, Tilburg University, the Netherlands (OSF: https://osf.io/x3y9b/).

2 Import and tidy

Contents

2.1 e task

2.1.1 Read in

```
mkable <- function(data) {
  knitr::kable(data, booktabs = TRUE, digits = 2) %>%
   kable_styling(position = "center")
}
mkables <- function(data) {
  knitr::kable(data, booktabs = TRUE, digits = 2) %>%
  kable_styling(position = "center", latex_options = "scale_down")
}
```

```
letE <-
 read.delim("~/Dropbox/StatsBook/Book5/EgoDepletion/LetterE_EData.txt",
   fileEncoding = "UTF-16"
# letE should be in package
glimpse(letE)
Observations: 24,750
Variables: 35
$ ExperimentName
                       <fct> LetterETaskt_150_3_easy_NL, LetterETaskt_15...
$ Subject
                       $ Session
                       $ Clock.Information
                       <fct> <?xml version=1.0?>\n<Clock xmlns:dt=urn:sc...
                       <fct> LetterETaskt_150_3_easy_NL-1-1, LetterETask...
$ DataFile.Basename
$ Display.RefreshRate
                       <dbl> 60.001, 60.001, 60.001, 60.001, 60.001, 60....
                       <fct> 1.0.0.63, 1.0.0.63, 1.0.0.63, 1.0.0.63, 1.0...
$ ExperimentVersion
$ Group
                       $ RandomSeed
                       <int> 985805828, 985805828, 985805828, 985805828,...
$ RuntimeVersion
                       <fct> 2.0.10.353, 2.0.10.353, 2.0.10.353, 2.0.10....
$ RuntimeVersionExpected <fct> 2.0.10.242, 2.0.10.242, 2.0.10.242, 2.0.10....
                       <fct> 03-30-2015, 03-30-2015, 03-30-2015, 03-30-2...
$ SessionDate
$ SessionStartDateTimeUtc <fct> 30-3-2015 7:07:29, 30-3-2015 7:07:29, 30-3-...
                       <fct> 09:07:29, 09:07:29, 09:07:29, 09:07:29, 09:...
$ SessionTime
$ StudioVersion
                       <fct> 2.0.10.147, 2.0.10.147, 2.0.10.147, 2.0.10....
$ Block
                       <int> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, ...
$ Procedure
                       <fct> ShowStim, ShowStim, ShowStim, ShowStim, Sho...
$ Running
                       <fct> WordList, WordList, WordList, Wor...
$ target
                       <int> 1, 1, 1, 1, NA, 1, 1, NA, 1, 1, 1, 1, 1, 1, ...
$ TrialNum
                       \langle 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, ...
                       \langle int \rangle 3, 3, 2, 3, 1, 3, 2, 1, 3, 3, 3, 2, 2, 3, 1...
$ TrialType
```

```
$ TrialTypeC
                     <fct> Lonely, Lonely, Companioned, Lonely, NoE, L...
$ Word
                     <fct> scheppen, gebruikt, omstandigheid, zuster, ...
$ Word.ACC
                     <int> 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 0...
$ Word.CRESP
                     <int> 1, 1, 1, 1, NA, 1, 1, NA, 1, 1, 1, 1, 1, 1, ...
$ Word.DurationError
                     $ Word.OnsetDelay
$ Word.OnsetTime
                     <int> 13449, 16449, 19449, 22449, 25449, 28449, 3...
$ Word.OnsetToOnsetTime
                     <int> 1500, 1500, 1500, 1500, 1500, 1500, 1500, 1...
$ Word.RESP
                     <int> 1, 1, 1, 1, NA, 1, 1, NA, 1, 1, 1, 1, 1, 1, ...
$ Word.RT
                     <int> 625, 425, 729, 537, 0, 457, 417, 0, 336, 38...
$ Word.RTTime
                     <int> 14074, 16874, 20178, 22986, 0, 28906, 31866...
                     <int> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, ...
$ WordList
$ WordList.Cycle
                     $ WordList.Sample
                     <int> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, ...
```

Note: UTF-16 allows us to read a wide range of characters, such as used in text not coded in Latin-script alphabets, and also Greek, Cyrillic, Coptic, Armenian, Hebrew, Arabic, Syriac (roughly equivalent to Aramaic), Thaana (Maldives), and N'Ko (Manding languages). We need it here, because the data were collected in a Dutch-language setting.

2.1.2 Tidy

```
eTask <- as_tibble(letE) %>%
 replace_na(list(Word.RESP = 0, Word.CRESP = 0))
eTask <- eTask %>%
 mutate(
   taskDifficulty = as_factor(
     case_when(
       ExperimentName == "LetterETaskt_150_3_hard_NL" ~ "Hard",
       ExperimentName == "LetterETaskt_150_3_easy_NL" ~ "Easy"
   ),
   goNoGo = as_factor(
     case_when(
       taskDifficulty == "Easy" & TrialType %in% c(2, 3) ~ "Go",
        taskDifficulty == "Hard" & TrialType %in% c(3) ~ "Go",
       taskDifficulty == "Easy" & TrialType %in% c(1) ~ "NoGo",
        taskDifficulty == "Hard" & TrialType %in% c(1, 2) ~ "NoGo"
   displayType = as_factor(
     case_when(
       TrialTypeC == "Lonely" ~ "NoFlankers",
       TrialTypeC == "Companioned" ~ "Flankers",
       TrialTypeC == "Lonely" ~ "NoE"
   ),
   sigDet = as_factor(
     case_when(
        Word.RESP == 1 & Word.CRESP == 1 ~ "Hit",
       Word.RESP == 0 & Word.CRESP == 1 ~ "Miss",
       Word.RESP == 1 & Word.CRESP == 0 ~ "FA",
       Word.RESP == 0 & Word.CRESP == 0 ~ "CR"
```

```
),
            signalNoise = as_factor(
                   case_when(
                         Word.CRESP == 1 ~ "Signal",
                         Word.CRESP == 0 ~ "Noise"
                  )
            ),
             subject = as_factor(Subject),
            reactionTime = Word.RT,
             trialNumber = TrialNum
      ) %>%
      select(
            c(
                  taskDifficulty,
                  subject,
                   goNoGo,
                  displayType,
                   sigDet,
                   signalNoise,
                   reactionTime
glimpse(eTask)
Observations: 24,750
Variables: 7
\ task
Difficulty <fct> Easy, Eas
$ subject
                                                    $ goNoGo
                                                      <fct> Go, Go, Go, Go, NoGo, Go, NoGo, Go, Go, Go, Go, ...
$ displayType
                                               <fct> NoFlankers, NoFlankers, Flankers, NoFlankers, NA, No...
                                                    <fct> Hit, Hit, Hit, CR, Hit, Hit, CR, Hit, Hit, Hit,...
$ sigDet
$ signalNoise
                                                      <fct> Signal, Signal, Signal, Noise, Signal, Signa...
$ reactionTime <int> 625, 425, 729, 537, 0, 457, 417, 0, 336, 384, 344, 5...
```

2.2 MSIT task

2.2.1 Read in

```
msit <-
 read.delim(
  file = "~/Dropbox/StatsBook/Book5/EgoDepletion/MSIT200_EData.txt",
   fileEncoding = "UTF-16"
glimpse(msit)
Observations: 33,000
Variables: 41
$ ExperimentName
                    <fct> MAS_MSIT_event_200_3_NL, MAS_MSIT_event_200...
                    $ Subject
                    $ Session
$ Clock.Information
                    <fct> <?xml version=1.0?>\n<Clock xmlns:dt=urn:sc...
$ DataFile.Basename
                    <fct> MAS_MSIT_event_200_3_NL-1-1, MAS_MSIT_event...
$ Display.RefreshRate
                  <dbl> 60.001, 60.001, 60.001, 60.001, 60.001, 60....
```

```
$ ExperimentVersion
                       <fct> 1.0.0.43, 1.0.0.43, 1.0.0.43, 1.0.0.43, 1.0...
$ Group
                       $ RandomSeed
                       <int> -1687224442, -1687224442, -1687224442, -168...
$ RuntimeVersion
                       <fct> 2.0.10.353, 2.0.10.353, 2.0.10.353, 2.0.10....
$ RuntimeVersionExpected <fct> 2.0.10.242, 2.0.10.242, 2.0.10.242, 2.0.10....
                       <fct> 03-30-2015, 03-30-2015, 03-30-2015, 03-30-2...
$ SessionDate
$ SessionStartDateTimeUtc <fct> 30-3-2015 7:16:57, 30-3-2015 7:16:57, 30-3-...
$ SessionTime
                      <fct> 09:16:57, 09:16:57, 09:16:57, 09:16:57, 09:...
$ StudioVersion
                       <fct> 2.0.10.147, 2.0.10.147, 2.0.10.147, 2.0.10....
$ Block
                      <int> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, ...
                      <int> 100, 3, 311, 212, 322, 331, 3, 100, 3, 211,...
$ content
$ Digits.ACC
                      <int> 1, 1, 0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 1, 1, 1...
$ Digits.CRESP
                       <int> 1, 3, 3, 1, 3, 1, 3, 1, 3, 2, 2, 2, 2, 3, 1...
$ Digits.DurationError
                       \langle int \rangle -6, -6, -6, -6, -6, -6, -6, -6, -6, ...
$ Digits.OnsetDelay
                      $ Digits.OnsetTime
                       <int> 24021, 27021, 30021, 33021, 36021, 39021, 4...
$ Digits.RESP
                       <int> 1, 3, 1, 2, 1, 3, 3, 1, 3, 1, 3, 1, 2, 3, 1...
                       <int> 530, 538, 426, 962, 882, 625, 489, 529, 553...
$ Digits.RT
$ Digits.RTTime
                      <int> 24551, 27559, 30447, 33983, 36903, 39646, 4...
$ Left
                       <int> 1, 0, 3, 2, 3, 3, 0, 1, 0, 2, 1, 2, 0, 0, 1...
$ LeftSize
                      <int> 28, 20, 28, 28, 20, 20, 20, 28, 20, 20, 20,...
$ Middle
                       <int> 0, 0, 1, 1, 2, 3, 0, 0, 0, 1, 1, 3, 2, 0, 0...
$ MiddleSize
                       $ Procedure
                       <fct> ShowStim, ShowStim, ShowStim, ShowStim, Sho...
$ Right
                       <int> 0, 3, 1, 2, 2, 1, 3, 0, 3, 1, 2, 3, 0, 3, 0...
$ RightSize
                       <int> 20, 28, 20, 20, 28, 28, 28, 20, 28, 28, 28,...
$ Running
                       <fct> StimList, StimList, StimList, StimList, Sti...
$ StimList
                       <int> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, ...
                       $ StimList.Cycle
                      <int> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, ...
$ StimList.Sample
$ target
                      <int> 1, 3, 3, 1, 3, 1, 3, 1, 3, 2, 2, 2, 2, 3, 1...
$ TrialNum
                       <int> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, ...
                      <int> 1, 1, 2, 2, 2, 2, 1, 1, 1, 2, 2, 2, 1, 1, 1...
$ TrialType
$ TrialTypeC
                       <fct> C, C, I, I, I, C, C, C, I, I, I, C, C, C...
```

2.2.2 Tidy

```
mTask <- as_tibble(msit) %>%
  transmute(
  response = Digits.RESP,
  stimulus = Digits.CRESP,
  sigDet = as_factor(
    case_when(
      stimulus == response ~ "Hit",
      abs(stimulus - response) == 1 ~ "FA1",
      abs(stimulus - response) == 2 ~ "FA2"
    )
  ),
  reactionTime = Digits.RT,
  subject = factor(Subject),
  trialType = as_factor(
    case_when(
      TrialTypeC == "C" ~ "Congruent",
```

2.3 Subject info and ratings

2.3.1 Read in

```
subs <- read_csv(file = "~/Dropbox/StatsBook/Book5/EgoDepletion/SubjectStatus.csv")</pre>
glimpse(subs)
Observations: 165
Variables: 11
$ SubjectID <dbl> 1, 2, 3, 5, 6, 8, 9, 10, 11, 14, 16, 17, 21, 22, 23, 25,...
      $ Task
$ gender <dbl> 2, 1, 2, 2, 2, 2, 1, 2, 2, 2, 2, 2, 2, 2, 1, 2, 2, 2, ...
$ age
        <dbl> 19, 19, 19, 19, 18, 22, 18, 19, 23, 19, 19, 18, 18, 19, ...
$ lang
        $ effort <dbl> 2, 5, 5, 2, 3, 2, 2, 4, 2, 2, 3, 2, 6, 3, 3, 3, 3, 5, 2,...
$ difficult <dbl> 1, 3, 1, 3, 2, 2, 3, 3, 4, 2, 1, 3, 2, 3, 3, 1, 1, 2, 2,...
$ tired <dbl> 6, 4, 2, 5, 3, 3, 5, 2, 2, 6, 4, 4, 6, 5, 2, 1, 4, 4, 4,...
$ frustrated <dbl> 1, 2, 1, 1, 1, 2, 1, 1, 3, 4, 2, 2, 4, 2, 2, 1, 1, 1, 4,...
```

2.3.2 Tidy

```
subjectInfo <- subs %>%
select(-c(langother, condition)) %>%
rename(
   subject = SubjectID,
   effortRating = effort,
   difficultyRating = difficult,
   fatigueRating = tired,
   firstLanguage = lang,
   frustrationRating = frustrated
) %>%
mutate(
   subject = factor(subject),
   taskDifficulty = factor(
```

```
case_when(
         Task == "E" ~ "Easy",
         Task == "H" ~ "Hard"
    ),
    gender = factor(
      case_when(
       gender == 1 ~ "Male",
gender == 2 ~ "Female"
    ),
  ) %>%
  select(
    c(
      taskDifficulty,
      gender,
       subject,
       effortRating,
      difficultyRating,
      frustrationRating,
       fatigueRating
glimpse(subjectInfo)
Observations: 165
Variables: 7
                       <fct> Easy, Easy, Easy, Easy, Easy, Easy, Easy, Easy, E...
fct> Female, Male, Female, Female, Female, Female, Mal...
$ taskDifficulty
$ gender
$ subject
                       <fct> 1, 2, 3, 5, 6, 8, 9, 10, 11, 14, 16, 17, 21, 22, ...
$ effortRating
                       <dbl> 2, 5, 5, 2, 3, 2, 2, 4, 2, 2, 3, 2, 6, 3, 3, 3, 3...
$ difficultyRating <dbl> 1, 3, 1, 3, 2, 2, 3, 3, 4, 2, 1, 3, 2, 3, 3, 1, 1...
$ frustrationRating <dbl> 1, 2, 1, 1, 1, 2, 1, 1, 3, 4, 2, 2, 4, 2, 2, 1, 1...
$ fatigueRating <dbl> 6, 4, 2, 5, 3, 3, 5, 2, 2, 6, 4, 4, 6, 5, 2, 1, 4...
```

3 Preliminary description

Contents

3.1	eTask data	10
3.2	MSIT task data	14
3.3	Linear mixed-effects model	22

3.1 eTask data

3.1.1 Disregarding subjects

RT

Transform RT? Now we would like to get a sense of the mean RTs in these conditions. This cannot be done reasonably unless we assume that these are distributed symmetrically (and preferably normally). But the distribution of RTs is meaningful *only relative to a model*. So we model these data with a linear model. (By doing so, we are — incorrectly — treating the data as if they came from one subject.)

```
eTaskH.FA <- eTask %>%
    filter(sigDet != "CR")
lmETaskH.FA <- lm(reactionTime ~ taskDifficulty * sigDet, data = eTaskH.FA)
```

Rather than examining the distribution of the residuals from lmETaskHit, we look for the value of λ (the power of the transformation) that will maximize the MLE of the model.

```
library(car)
summary(powerTransform(lmETaskH.FA))
bcPower Transformation to Normality
  Est Power Rounded Pwr Wald Lwr Bnd Wald Upr Bnd
Y1 -0.0595
              -0.06
                            -0.0797
                                        -0.0393
Likelihood ratio test that transformation parameter is equal to 0
 (log transformation)
                         LRT df
LR test, lambda = (0) 31.94887 1 1.5828e-08
Likelihood ratio test that no transformation is needed
                                   pval
                        LRT df
LR test, lambda = (1) 7376.75 1 < 2.22e-16
```

So, should we transform reactionTime? Yes. Since $\lambda = -0.06 \approx 0$, and in the ladder of powers $\lambda = 0$ means $y \to \log y$. We can also show this graphically (Figure 1):

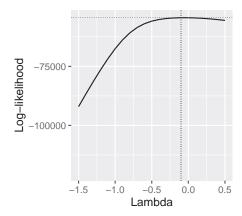


Figure 1: Plot profile log-likelihoods for the parameter of the Box-Cox power family for lmETaskHit.

```
library(lindia)
gg_boxcox(lmETaskH.FA)
```

So we transform reactionTime, and rerun the lm():

```
eTaskH.FA <- eTaskH.FA %>%
    mutate(reactionTimeLog = log(reactionTime))
lmeTaskH.FA.Log <- update(object = lmETaskH.FA, formula. = reactionTimeLog ~ .)</pre>
```

(Note that we use update().)

```
AIC(lmETaskH.FA, lmeTaskH.FA.Log) %>%

as_tibble() %>%

kable(digits = 0, booktabs = TRUE) %>%

kable_styling(position = "center")
```

df	AIC
5 5	210791
Э	6901

We made a point *not* to look at the linear models before determining the difference in AIC, and finding that lmeTaskHitLog is overwhelmingly better than lmeTaskHit. We do not have to do this again when we run LME models on these data. (Nevertheless, it's always prudent to double-check by using powerTransform() on our final model, and confirming that $\lambda \approx 1$, which means that the fit of the model cannot be improved by transforming the response variable.)

Summarize Detection & RT

```
eTaskSum <- eTask %>%
group_by(taskDifficulty, signalNoise, sigDet) %>%
mutate(reactionTimeLog = log(reactionTime)) %>%
summarize(meanRTlog = mean(reactionTimeLog), n = n()) %>%
mutate(prop = n / sum(n), geomMean.eTask.RT = exp(meanRTlog)) %>%
filter(sigDet != "CR") %>%
select(-c(n, meanRTlog)) %>%
select(taskDifficulty, sigDet, prop, geomMean.eTask.RT)
eTaskSum %>%
kable(digits = c(0, 0, 0, 3, 0), booktabs = TRUE) %>%
kable_styling(position = "center")
```

signalNoise	taskDifficulty	sigDet	prop	${\tt geomMean.eTask.RT}$
Signal	Easy	Hit	1.000	542
Noise	Easy	FA	0.064	450
Signal	Hard	Hit	1.000	1080
Noise	Hard	FA	0.138	1072

Clearly none of the subjects made errors when they responded to a word that contained e, but made more than twice as many inhibition errors in the Hard condition (13.8%) than in the Easy condition (6.4%).

Now we do this by subject:

```
eTaskBySub <- eTask %>%
  group_by(taskDifficulty, subject, signalNoise, sigDet) %>%
 mutate(reactionTimeLog = log(reactionTime)) %>%
 summarize(meanRTlog = mean(reactionTimeLog), n = n()) %>%
 mutate(prop = n / sum(n), geomMean.eTask.RT = exp(meanRTlog)) %>%
 filter(sigDet != "CR") %>%
 select(-c(n, meanRTlog)) %>%
 select(taskDifficulty, subject, sigDet, prop, geomMean.eTask.RT)
glimpse(eTaskBySub)
Observations: 308
Variables: 6
Groups: taskDifficulty, subject, signalNoise [308]
$ signalNoise <fct> Signal, Noise, Signal, Noise, Signal, Noi...
$ taskDifficulty
                   <fct> Easy, Easy, Easy, Easy, Easy, Easy, Easy, Easy, E...
$ subject
                   <fct> 1, 1, 2, 3, 3, 5, 5, 6, 8, 8, 9, 9, 10, 10, 11, 1...
$ sigDet
                   <fct> Hit, FA, Hit, Hit, FA, Hit, FA, Hit, FA, Hit...
                   <dbl> 1.00000000, 0.03225806, 1.00000000, 1.00000000, 0...
$ prop
$ geomMean.eTask.RT <dbl> 520.2102, 488.0000, 572.2292, 514.5156, 398.8283,...
```

3.1.2 Join tibbles

Now let's join the eTaskBySub, and subjectInfo tibbles by a common column, subject. We do this using the function full_join()

```
eTaskSub <- subjectInfo %>%
 full_join(eTaskBySub)
dim(eTaskSub)
Γ17 308 11
eTaskSub <- eTaskSub %>%
 drop_na()
dim(eTaskSub)
[1] 302 11
glimpse(eTaskSub)
Observations: 302
Variables: 11
$ taskDifficulty
                   <fct> Easy, Easy, Easy, Easy, Easy, Easy, Easy, Easy, E...
$ gender
                   <fct> Female, Female, Male, Female, Female, Female, Fem...
$ subject
                   <fct> 1, 1, 2, 3, 3, 5, 5, 6, 8, 8, 9, 9, 10, 10, 11, 1...
                   <dbl> 2, 2, 5, 5, 5, 2, 2, 3, 2, 2, 2, 2, 4, 4, 2, 2, 2...
$ effortRating
$ difficultyRating <dbl> 1, 1, 3, 1, 1, 3, 3, 2, 2, 2, 3, 3, 3, 3, 4, 4, 2...
$ frustrationRating <dbl> 1, 1, 2, 1, 1, 1, 1, 1, 2, 2, 1, 1, 1, 1, 3, 3, 4...
$ fatigueRating <dbl> 6, 6, 4, 2, 2, 5, 5, 3, 3, 3, 5, 5, 2, 2, 2, 2, 6...
$ signalNoise
                   <fct> Signal, Noise, Signal, Signal, Noise, Signal, Noi...
$ sigDet
                   <fct> Hit, FA, Hit, Hit, FA, Hit, FA, Hit, FA, Hit...
$ prop
                   <dbl> 1.00000000, 0.03225806, 1.00000000, 1.00000000, 0...
$ geomMean.eTask.RT <dbl> 520.2102, 488.0000, 572.2292, 514.5156, 398.8283,...
```

3.1.3 A quick look at the e task data

Effect of task difficulty on ratings (Figure 2)

```
eTaskSub <- eTaskSub %>%
  mutate(rating = effortRating + difficultyRating + frustrationRating)
ggplot(data = eTaskSub, aes(
  x = taskDifficulty,
  y = rating,
  group = taskDifficulty
)) +
  geom_violin(draw_quantiles = c(0.25, 0.5, 0.75)) +
  labs(x = "task difficulty", y = "composite rating")
```

Effect of task difficulty on false-alarm rate (Figure 3)

```
eTaskSubFA <- eTaskSub %>%
  filter(sigDet == "FA")
ggplot(
  data = eTaskSubFA,
  aes(
    x = taskDifficulty,
    y = prop,
    group = taskDifficulty
)
```

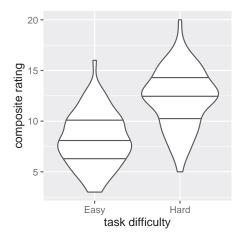


Figure 2: Violin plots of the effort + difficulty + frustration ratings, as a function of task difficulty.

```
) +
  geom_violin(draw_quantiles = c(0.25, 0.5, 0.75)) +
labs(x = "task difficulty", y = "false-alarm rate")
```

Effect of task difficulty on RT (Figure 4)

```
ggplot(
  data = eTaskSub,
  aes(
    x = taskDifficulty,
    y = geomMean.eTask.RT,
    color = sigDet
)
) +
  geom_violin(draw_quantiles = c(0.25, 0.5, 0.75)) +
  labs(x = "task difficulty", y = "RT (geometric mean)") +
  theme(
    legend.position = c(0.05, 0.95),
    legend.justification = c(0.05, 0.95)
)
```

3.2 MSIT task data

3.2.1 Disregarding subjects

RT Transform RT?

```
lmMTask <- lm(reactionTime ~ sigDet * trialType, data = mTask)</pre>
```

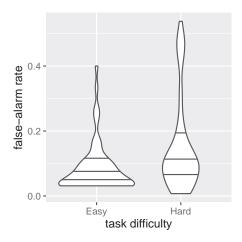


Figure 3: Violin plots of the false-alarm rate, as a function of task difficulty.

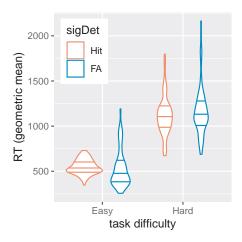


Figure 4: Violin plots of geometric mean RT, as a function of task difficulty and signal detection.

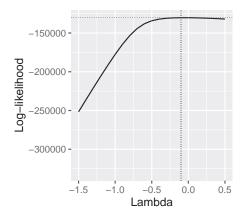


Figure 5: Plot profile log-likelihoods for the parameter of the Box-Cox power family for lmMTask.

We should transform reactionTime because $\lambda=-0.06\approx0.$ We also show this graphically in Figure 5:

```
gg_boxcox(lmMTask)
```

Transform RT, and compare models.

```
mTask <- mTask %>%
  mutate(reactionTimeLog = log(reactionTime))
lmMTaskLog <- lm(reactionTimeLog ~ sigDet * trialType, data = mTask)
AIC(lmMTask, lmMTaskLog) %>%
  as_tibble() %>%
  kable(digits = 0, booktabs = TRUE) %>%
  kable_styling(position = "center")
```

df	AIC
7	449639
7	13896

Here too, there is no doubt that taking the log is the right thing to do.

Measures of accuracy Measures of association for ordinal factors (stimulus, response) in a two-way table:

```
mTaskTab <- with(mTask, table(response, stimulus))</pre>
library(questionr)
cv <- cramer.v(mTaskTab)</pre>
library(DescTools)
gkg <- GoodmanKruskalGamma(mTaskTab)</pre>
gkt <- GoodmanKruskalTau(mTaskTab)</pre>
1 <- Lambda(mTaskTab)</pre>
tribble(
  ~measure, ~value,
  "Cramer's V", cv,
  "Goodman-Kruskal Gamma", gkg,
  "Goodman-Kruskal Tau", gkt,
  "Lambda", 1
) %>%
  kable(digits = 2, booktabs = TRUE) %>%
  kable_styling(position = "center")
```

measure	value
Cramer's V	0.82
Goodman-Kruskal Gamma	0.92
Goodman-Kruskal Tau	0.67
Lambda	0.81

These measures represent how well the subjects responded to each stimulus with the corresponding correct response.

Using Lambda (as an example) we summarize accuracy as a function of trial type and signal detection category:

```
library(questionr)
mTaskC <- mTask %>%
  filter(trialType == "Congruent") %>%
  select(stimulus, response) %>%
  table() %>%
  cramer.v() %>%
  print()

[1] 0.9823959

mTaskI <- mTask %>%
  filter(trialType == "Incongruent") %>%
  select(stimulus, response) %>%
  table() %>%
  cramer.v() %>%
  print()

[1] 0.6559378
```

```
mTaskCramerS <- mTask %>%
 group_by(trialType, subject) %>%
 nest() %>%
 mutate(cv = map(data, ~
 select(.x, c(stimulus, response)) %>%
   table() %>%
   cramer.v() %>%
   as.list() %>%
   as_tibble(.name_repair = ~ c("Cramer_V")))) %>%
 select(-data) %>%
 unnest(cv) %>%
 ungroup()
glimpse(mTaskCramerS)
Observations: 330
Variables: 3
\ trialType <fct> Congruent, Incongruent, Congruent, Incongruent, Congruent...
$ Cramer_V <dbl> 0.98373875, 0.38283932, 1.00000000, 0.72519159, 1.00000000...
```

Effect of trial type on accuracy (Figure 6)

```
mTaskCramerS <- mTaskCramerS %>%
    spread(key = trialType, value = Cramer_V) %>%
    mutate(diff = Congruent - Incongruent)
mTaskDiff <- tibble(bySubject = mTaskCramerS$diff)
ggplot(data = mTaskDiff, aes(
    x = "",
    y = bySubject
)) +
    geom_violin(draw_quantiles = c(0.25, 0.5, 0.75)) +
    labs(x = "", y = "difference in Cramer's V")</pre>
```

The median difference between Cramer's V for congruent and incongruent trials is 0.18.

3.2.2 Join tibbles

```
eTaskmTaskSub <- eTaskSub %>%
full_join(mTaskCramerS)
dim(eTaskmTaskSub)

[1] 305 15

eTaskSub <- eTaskSub %>%
drop_na()
dim(eTaskmTaskSub)

[1] 305 15

glimpse(eTaskmTaskSub)
```

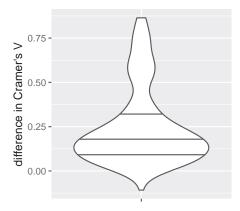


Figure 6: Violin plots of the difference between Cramer's V for congruent and incongruent trials.

```
Observations: 305
Variables: 15
$ taskDifficulty
                    <fct> Easy, Easy, Easy, Easy, Easy, Easy, Easy, Easy, E...
$ gender
                    <fct> Female, Female, Male, Female, Female, Female, Fem...
                    <fct> 1, 1, 2, 3, 3, 5, 5, 6, 8, 8, 9, 9, 10, 10, 11, 1...
$ subject
$ effortRating
                    <dbl> 2, 2, 5, 5, 5, 2, 2, 3, 2, 2, 2, 2, 4, 4, 2, 2, 2...
$ difficultyRating <dbl> 1, 1, 3, 1, 1, 3, 3, 2, 2, 2, 3, 3, 3, 3, 4, 4, 2...
\ frustrationRating \dbl> 1, 1, 2, 1, 1, 1, 1, 1, 2, 2, 1, 1, 1, 1, 3, 3, 4...
$ fatigueRating
                    <dbl> 6, 6, 4, 2, 2, 5, 5, 3, 3, 3, 5, 5, 2, 2, 2, 2, 6...
$ signalNoise
                    <fct> Signal, Noise, Signal, Signal, Noise, Signal, Noi...
$ sigDet
                    <fct> Hit, FA, Hit, Hit, FA, Hit, FA, Hit, Hit, FA, Hit...
                    <dbl> 1.00000000, 0.03225806, 1.00000000, 1.00000000, 0...
$ prop
$ geomMean.eTask.RT <dbl> 520.2102, 488.0000, 572.2292, 514.5156, 398.8283,...
                    <dbl> 4, 4, 10, 7, 7, 6, 6, 6, 6, 6, 6, 6, 8, 8, 9, 9, ...
$ rating
$ Congruent
                    <dbl> 0.9837388, 0.9837388, 0.9856697, 1.0000000, 1.000...
$ Incongruent
                    <dbl> 0.3828393, 0.3828393, 0.8083788, 0.7994993, 0.799...
$ diff
                    <dbl> 0.6008994, 0.6008994, 0.1772909, 0.2005007, 0.200...
eTaskmTaskSubT <- eTaskmTaskSub %>%
  gather(congruence, CramerV, Congruent:Incongruent, factor_key = TRUE)
glimpse(eTaskmTaskSubT)
Observations: 610
Variables: 15
$ taskDifficulty
                    <fct> Easy, Easy, Easy, Easy, Easy, Easy, Easy, Easy, E...
$ gender
                    <fct> Female, Female, Male, Female, Female, Female, Fem...
                    <fct> 1, 1, 2, 3, 3, 5, 5, 6, 8, 8, 9, 9, 10, 10, 11, 1...
$ subject
$ effortRating
                    <dbl> 2, 2, 5, 5, 5, 2, 2, 3, 2, 2, 2, 2, 4, 4, 2, 2, 2...
$ difficultyRating <dbl> 1, 1, 3, 1, 1, 3, 3, 2, 2, 2, 3, 3, 3, 3, 4, 4, 2...
$ frustrationRating <dbl> 1, 1, 2, 1, 1, 1, 1, 1, 2, 2, 1, 1, 1, 1, 3, 3, 4...
                    <dbl> 6, 6, 4, 2, 2, 5, 5, 3, 3, 3, 5, 5, 2, 2, 2, 2, 6...
$ fatigueRating
$ signalNoise
                    <fct> Signal, Noise, Signal, Signal, Noise, Signal, Noi...
$ sigDet
                    <fct> Hit, FA, Hit, Hit, FA, Hit, FA, Hit, FA, Hit...
```

Warning: Factor 'taskDifficulty' contains implicit NA, consider using 'forcats::fct_explicit_na'

taskDifficulty	n	prop
Easy	278	0.46
Hard	326	0.53
NA	6	0.01

```
eTaskmTaskSubT <- eTaskmTaskSubT %>%
  drop_na()
eTaskmTaskSubT %>%
  count(taskDifficulty) %>%
  mutate(prop = prop.table(n)) %>%
  mkable()
```

taskDifficulty	n	prop
Easy Hard	278 326	$0.46 \\ 0.54$

```
ggplot(data = eTaskmTaskSubT, aes(
    x = taskDifficulty,
    y = CramerV, color = congruence
)) +
    geom_boxplot() +
    labs(x = "task difficulty", y = "Cramer's V")
```

```
ggplot(data = eTaskmTaskSubT, aes(
    x = rating,
    y = CramerV, color = congruence
)) +
    geom_point() +
    labs(x = "rating", y = "Cramer's V")
```

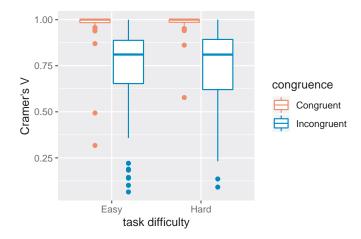


Figure 7: Boxplots of Cramer's V as a function of e task difficulty and congruence in the MSIT task.

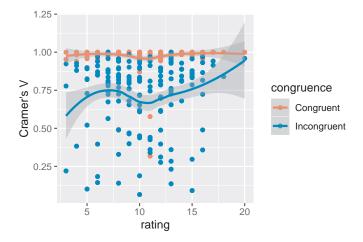


Figure 8: Cramer's V as a function of e rating and congruence in the MSIT task.

```
all <- eTaskmTaskSub %>%
   full_join(mTask)
Warning: Column 'sigDet' joining factors with different levels, coercing to character
vector
dim(all)
[1] 33143
                       20
all <- all %>%
   drop na()
dim(all)
[1] 28219
                       20
glimpse(all)
Observations: 28,219
Variables: 20
$ taskDifficulty
                                    <fct> Easy, Easy, Easy, Easy, Easy, Easy, Easy, Easy, E...
$ gender
                                    <fct> Female, Female, Female, Female, Female, Female, F...
$ subject
                                    $ effortRating
                                    $ fatigueRating
                                    $ signalNoise
                                    <fct> Signal, Signal, Signal, Signal, Signal, S...
                                    $ sigDet
$ prop
$ geomMean.eTask.RT <dbl> 520.2102, 520.2102, 520.2102, 520.2102, 520.2102, 520.2102,...
$ rating
                                   <dbl> 0.9837388, 0.9837388, 0.9837388, 0.983...
$ Congruent
$ Incongruent
                                   <dbl> 0.3828393, 0.3828393, 0.3828393, 0.3828393, 0.382...
$ diff
                                   <dbl> 0.6008994, 0.6008994, 0.6008994, 0.6008994, 0.600...
$ response
                                   <int> 1, 3, 3, 1, 3, 2, 3, 1, 1, 2, 3, 1, 2, 2, 1, 3, 1...
$ stimulus
                                    <int> 1, 3, 3, 1, 3, 2, 3, 1, 1, 2, 3, 1, 2, 2, 1, 3, 1...
$ reactionTime
                                    <int> 530, 538, 489, 529, 553, 593, 457, 417, 449, 762,...
$ trialType
                                    <fct> Congruent, Congr
ggplot(data = all, aes(
   x = taskDifficulty,
   y = reactionTimeLog, color = trialType
)) +
   geom_violin() +
   labs(x = "e task difficult", y = "m task log(RT)")
```

3.3 Linear mixed-effects model

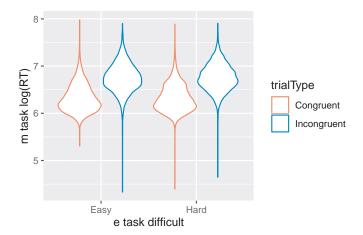


Figure 9: Log(RT) as a function of e task difficulty and congruence in the MSIT task.

More complex random effects

```
lmeMTaskLog2 <-
lmer(reactionTimeLog ~ sigDet * trialType +
        (sigDet * trialType | subject),
        data = mTask
)

Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control$checkConv, : Model
failed to converge with max|grad| = 0.117414 (tol = 0.002, component 1)

AIC(lmeMTaskLog, lmeMTaskLog2) %>%
        as_tibble() %>%
        kable(digits = 0, booktabs = TRUE) %>%
        kable_styling(position = "center")
```

```
df AIC
8 131
28 -1814
```

```
tidy(lmeMTaskLog2, effects = "ran_pars") %>%
    mkables()
```

effect	group	term	estimate
ran_pars	subject	sd(Intercept)	0.19
ran_pars	subject	$sd_sigDetFA2$	0.13
ran_pars	subject	$sd_sigDetFA1$	0.33
ran_pars	subject	sd_trialTypeIncongruent	0.13
ran_pars	$\operatorname{subject}$	$sd_sigDetFA2: trial Type In congruent$	0.27
ran_pars	subject	$sd_sigDetFA1:trialTypeIncongruent$	0.33
ran_pars	subject	$cor_(Intercept).sigDetFA2$	0.40
ran_pars	subject	$cor_(Intercept).sigDetFA1$	0.18
ran_pars	subject	$cor_(Intercept).trialTypeIncongruent$	-0.16
ran_pars	$\operatorname{subject}$	$cor_(Intercept). sigDetFA2: trial TypeIncongruent$	-0.12
ran_pars	subject	$cor_(Intercept). sigDetFA1: trialTypeIncongruent$	-0.14
ran_pars	subject	$cor_sigDetFA2.sigDetFA1$	0.05
ran_pars	subject	$cor_sigDetFA2.trialTypeIncongruent$	0.52
ran_pars	subject	$cor_sigDetFA2.sigDetFA2:trialTypeIncongruent$	-0.19
ran_pars	$\operatorname{subject}$	$cor_sigDetFA2.sigDetFA1: trialTypeIncongruent$	0.08
ran_pars	subject	cor_sigDetFA1.trialTypeIncongruent	-0.14
ran_pars	subject	cor_sigDetFA1.sigDetFA2:trialTypeIncongruent	0.14
ran_pars	subject	$cor_sigDetFA1.sigDetFA1:trialTypeIncongruent$	-0.93
ran_pars	subject	$cor_trial Type Incongruent. sig Det FA2: trial Type Incongruent$	-0.61
ran_pars	$\operatorname{subject}$	$cor_trial Type Incongruent. sig Det FA1: trial Type Incongruent$	-0.02
ran_pars	subject	$cor_sigDetFA2: trialTypeIncongruent.sigDetFA1: trialTypeIncongruent$	-0.05
ran_pars	Residual	$sd_Observation$	0.23

```
library(brms)
library(dotwhisker)
tidy(lmeMTaskLog2, effects = "fixed") %>%
  dwplot(vline = geom_vline(
    xintercept = 0,
    colour = "grey50",
    linetype = 2
))
```

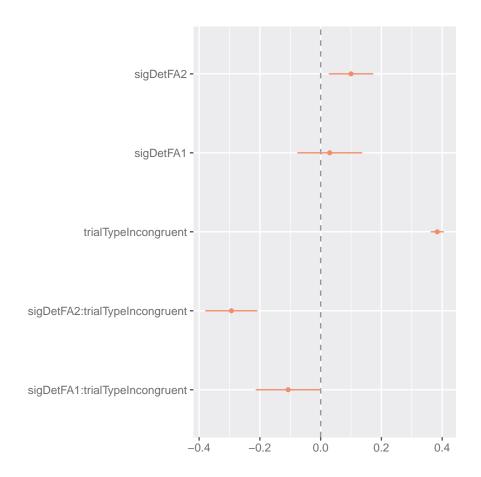


Figure 10: Dot-and-whisker plot of fixed effects of lmeMTaskLog2 model.

R session information

```
sessionInfo()
R version 3.6.1 (2019-07-05)
Platform: x86_64-apple-darwin15.6.0 (64-bit)
Running under: macOS Catalina 10.15.2
Matrix products: default
BLAS: /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRblas.0.dylib
LAPACK: /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRlapack.dylib
locale:
[1] C
attached base packages:
[1] splines parallel stats
                                graphics grDevices utils
                                                             datasets
[8] methods
             base
other attached packages:
 [1] DescTools_0.99.31
                         questionr_0.7.0
                                               janitor_1.2.0
 [4] xtable_1.8-4
                         WWGbook_1.0.1
                                              texreg_1.36.23
 [7] styler_1.2.0
                        stargazer_5.2.2
                                              R.utils_2.9.2
                     R.methodsS3_1.7.1
[10] R.oo_1.23.0
                                              qqplotr_0.0.3
[13] prob_1.0-1
                       fAsianOptions_3042.82 fOptions_3042.86
[16] fBasics_3042.89
                        timeSeries_3042.102 timeDate_3043.102
[19] combinat_0.0-8
                                        merTools_0.5.0
                         printr_0.1
                                              predictmeans_1.0.1
[22] mgcv_1.8-31
                        nlme_3.1-142
[25] arm_1.10-1
                       MASS_7.3-51.4
                                             lme4_1.1-21
                     lintr_2.0.0 lindia_0.9 languageR_1.5.0 kableExtra_1.1.0
[28] Matrix_1.2-18
[31] latex2exp_0.4.0
[34] haven_2.2.0
                         gridExtra_2.3
                                              ggfortify_0.4.8
                                            foreach_1.4.7
[37] formattable_0.2.0.1 foreign_0.8-72
[40] extrafontdb_1.0 extrafont_0.17
                                            effects_4.1-4
[43] dotwhisker_0.5.0
                         car_3.0-5
                                              carData_3.0-3
[46] brms_2.10.0
                         Rcpp_1.0.3
                                              broom.mixed_0.2.4
[49] yardstick_0.0.4
                         rsample_0.0.5
                                              recipes_0.1.7
[52] parsnip_0.0.4
                        infer_0.5.1
                                              dials_0.0.4
                       broom_0.5.2
[55] scales_1.1.0
                                              tidymodels_0.0.3
                       stringr_1.4.0
[58] forcats_0.4.0
                                              dplyr_0.8.3
[61] purrr_0.3.3
                         readr_1.3.1
                                               tidyr_1.0.0
[64] tibble_2.1.3
                         ggplot2_3.2.1
                                               tidyverse_1.3.0
[67] knitr_1.26
loaded via a namespace (and not attached):
  [1] SnowballC_0.6.0 coda_0.19-3
                                              dygraphs_1.1.1.6
                       rpart_4.1-15
 [4] data.table_1.12.6
                                             inline_0.3.15
 [7] generics_0.0.2 callr_3.3.2
                                           future_1.15.1
                                           xml2_1.2.2
 [10] tokenizers_0.2.1 webshot_0.5.2
                      httpuv_1.5.2
 [13] lubridate_1.7.4
                                             StanHeaders_2.19.0
 [16] assertthat_0.2.1
                         gower_0.2.1
                                             xfun_0.11
 [19] hms_0.5.2
                         bayesplot_1.7.1
                                            evaluate_0.14
 [22] promises_1.1.0 fansi_0.4.0 [25] dbplyr_1.4.2 readxl_1.3.1
                                            DEoptimR_1.0-8
                       readxl_1.3.1
                                             igraph_1.2.4.2
 [28] DBI_1.0.0
                                              stats4_3.6.1
                         htmlwidgets_1.5.1
 [31] ellipsis_0.3.0 crosstalk_1.0.0
                                             backports_1.1.5
```

```
[34] survey_3.36
                          markdown_1.1
                                              vctrs_0.2.0
 [37] remotes_2.1.0
                          abind_1.4-5
                                              withr_2.1.2
 [40] robustbase_0.93-5
                          xts_0.11-2
                                              prettyunits_1.0.2
 [43] cyclocomp_1.1.0
                          lazyeval_0.2.2
                                              crayon_1.3.4
 [46] labeling_0.3
                          pkgconfig_2.0.3
                                              blme_1.0-4
 [49] nnet_7.3-12
                          rlang_0.4.2
                                              spatial_7.3-11
 [52] globals_0.12.5
                          lifecycle_0.1.0
                                              miniUI_0.1.1.1
 [55] colourpicker_1.0
                          rex_1.1.2
                                              modelr_0.1.5
 [58] tidytext_0.2.2
                          cellranger_1.1.0
                                              rprojroot_1.3-2
 [61] matrixStats_0.55.0
                         loo_2.1.0
                                              boot_1.3-23
 [64] zoo_1.8-6
                          reprex_0.3.0
                                              base64enc_0.1-3
 [67] ggridges_0.5.1
                          processx_3.4.1
                                              viridisLite_0.3.0
 [70] pROC_1.15.3
                          shinystan_2.5.0
                                              magrittr_1.5
 [73] plyr_1.8.4
                          threejs_0.3.1
                                              compiler_3.6.1
 [76] rstantools_2.0.0
                         cli_1.1.0
                                              DiceDesign_1.8-1
 [79] listenv_0.8.0
                          janeaustenr_0.1.5
                                             ps_1.3.0
 [82] TMB_1.7.15
                          Brobdingnag_1.2-6
                                             tidyselect_0.2.5
 [85] stringi_1.4.3
                         highr_0.8
                                              mitools_2.4
 [88] bridgesampling_0.7-2 grid_3.6.1
                                              tidypredict_0.4.3
 [91] tools_3.6.1
                         rio_0.5.16
                                              rstudioapi_0.10
 [94] prodlim_2019.11.13
                        farver_2.0.1
                                              digest_0.6.23
 [97] shiny_1.4.0
                         lava_1.6.6
                                              later_1.0.0
[100] httr_1.4.1
                          rsconnect_0.8.15
                                              ggstance_0.3.3
                         rvest_0.3.5
[103] colorspace_1.4-1
                                              fs_1.3.1
[106] expm_0.999-4
                         shinythemes_1.1.2 rstanarm_2.19.2
[109] jsonlite_1.6
                          nloptr_1.2.1
                                              rstan_2.19.2
[112] zeallot_0.1.0
                          ipred_0.9-9
                                              R6_2.4.1
[115] pillar_1.4.2
                          htmltools_0.4.0
                                              mime_0.7
[118] glue_1.3.1
                                              minqa_1.2.4
                         fastmap_1.0.1
[121] DT_0.10
                         class_7.3-15
                                              codetools_0.2-16
[124] utf8_1.1.4
                          pkgbuild_1.0.6
                                              mvtnorm_1.0-11
[127] furrr_0.1.0
                         lattice_0.20-38
                                              numDeriv_2016.8-1.1
[130] pbkrtest_0.4-7
                          curl_4.3
                                              gtools_3.8.1
[133] tidyposterior_0.0.2 zip_2.0.4
                                              shinyjs_1.0
[136] openxlsx_4.1.4
                          Rttf2pt1_1.3.7
                                              survival_3.1-8
[139] rmarkdown_1.18
                          desc_1.2.0
                                              munsell_0.5.0
[142] iterators_1.0.12
                         reshape2_1.4.3
                                              gtable_0.3.0
Sys.time()
[1] "2019-12-13 20:54:49 EST"
```