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# Chapter 4. NumPy Basics: Arrays and Vectorized Computation

NumPy, short for Numerical Python, is the fundamental package required for high performance scientific computing and data analysis. It is the foundation on which nearly all of the higher-level tools in this book are built. Here are some of the things it provides:

- ndarray, a fast and space-efficient multidimensional array providing vectorized arithmetic operations and sophisticated *broadcasting* capabilities
- Standard mathematical functions for fast operations on entire arrays of data without having to write loops
- Tools for reading / writing array data to disk and working with memory-mapped files
- Linear algebra, random number generation, and Fourier transform capabilities
- Tools for integrating code written in C, C++, and Fortran

The last bullet point is also one of the most important ones from an ecosystem point of view. Because NumPy provides an easy-to-use C API, it is very easy to pass data to external libraries written in a low-level language and also for external libraries to return data to Python as NumPy arrays. This feature has made Python a language of choice for wrapping legacy C/C++/Fortran codebases and giving them a dynamic and easy-to-use interface.

While NumPy by itself does not provide very much high-level data analytical functionality, having an understanding of NumPy arrays and array-oriented computing will help you use tools like pandas much more effectively. If you're new to Python and just looking to get your hands dirty working with data using pandas, feel free to give this chapter a skim. For more on advanced NumPy features like broadcasting, see Chapter 12.

For most data analysis applications, the main areas of functionality I'll focus on are:

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- o Efficient descriptive statistics and aggregating/summarizing data
- Data alignment and relational data manipulations for merging and joining together heterogeneous data sets
- Expressing conditional logic as array expressions instead of loops with if-elif-else branches
- Group-wise data manipulations (aggregation, transformation, function application). Much more on this in Chapter 5

While NumPy provides the computational foundation for these operations, you will likely want to use pandas as your basis for most kinds of data analysis (especially for structured or tabular data) as it provides a rich, high-level interface making most common data tasks very concise and simple. pandas also provides some more domain-specific functionality like time series manipulation, which is not present in NumPy.

#### NOTE

In this chapter and throughout the book, I use the standard NumPy convention of always using import numpy as np. You are, of course, welcome to put from numpy import \* in your code to avoid having to write np., but I would caution you against making a habit of this.

# The NumPy ndarray: A Multidimensional Array Object

One of the key features of NumPy is its N-dimensional array object, or ndarray, which is a fast, flexible container for large data sets in Python. Arrays enable you to perform mathematical operations on whole blocks of data using similar syntax to the equivalent operations between scalar elements:

```
In [8]: data
```

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```
array([[ 9.5256, -2.4601, -8.8565], array([[ 1.9051, -0.492 , -1.7713],
     [ 5.6385, 2.3794, 9.104 ]])
                                             [ 1.1277, 0.4759, 1.8208]])
```

An idarray is a generic multidimensional container for homogeneous data; that is, all of the elements must be the same type. Every array has a shape, a tuple indicating the size of each dimension, and a dtype, an object describing the data type of the array:

```
In [11]: data.shape
Out[11]: (2, 3)
In [12]: data.dtype
Out[12]: dtype('float64')
```

This chapter will introduce you to the basics of using NumPy arrays, and should be sufficient for following along with the rest of the book. While it's not necessary to have a deep understanding of NumPy for many data analytical applications, becoming proficient in array-oriented programming and thinking is a key step along the way to becoming a scientific Python guru.

#### NOTE

Whenever you see "array", "NumPy array", or "ndarray" in the text, with few exceptions they all refer to the same thing: the ndarray object.

## Creating ndarrays

The easiest way to create an array is to use the array function. This accepts any sequencelike object (including other arrays) and produces a new NumPy array containing the passed data. For example, a list is a good candidate for conversion:

```
In [13]: data1 = [6, 7.5, 8, 0, 1]
In [14]: arr1 = np.array(data1)
```

```
In [15]: arr1
```

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```
In [16]: data2 = [[1, 2, 3, 4], [5, 6, 7, 8]]
In [17]: arr2 = np.array(data2)
In [18]: arr2
Out[18]:
array([[1, 2, 3, 4],
       [5, 6, 7, 8]])
In [19]: arr2.ndim
Out[19]: 2
In [20]: arr2.shape
Out[20]: (2, 4)
```

Unless explicitly specified (more on this later), np.array tries to infer a good data type for the array that it creates. The data type is stored in a special dtype object; for example, in the above two examples we have:

```
In [21]: arr1.dtype
Out[21]: dtype('float64')
In [22]: arr2.dtype
Out[22]: dtype('int64')
```

In addition to np.array, there are a number of other functions for creating new arrays. As examples, zeros and ones create arrays of o's or 1's, respectively, with a given length or shape. empty creates an array without initializing its values to any particular value. To create a higher dimensional array with these methods, pass a tuple for the shape:

```
In [23]: np.zeros(10)
Out[23]: array([ 0., 0., 0., 0., 0., 0., 0., 0., 0.])
In [24]: np.zeros((3, 6))
Out[24]:
array([[ 0., 0., 0., 0., 0., 0.],
      [ 0., 0., 0., 0., 0., 0.],
      [ 0., 0., 0., 0., 0., 0.]])
```

```
In [25] • nn emntv//2 3 2))
```

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```
[ -2.33568637e+124, -6.70608105e-012],
 4.42786966e+160, 1.27100354e+025]]])
```

#### **CAUTION**

It's not safe to assume that np.empty will return an array of all zeros. In many cases, as previously shown, it will return uninitialized garbage values.

arange is an array-valued version of the built-in Python range function:

```
In [26]: np.arange(15)
Out[26]: array([ 0,  1,  2,  3,  4,  5,  6,  7,  8,  9, 10, 11, 12, 13, 14])
```

See Table 4-1 for a short list of standard array creation functions. Since NumPy is focused on numerical computing, the data type, if not specified, will in many cases be float64 (floating point).

#### Table 4-1. Array creation functions

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	Copies the input data by default.	
asarray	Convert input to ndarray, but do not copy if the input is already an ndarray	
arange	Like the built-in range but returns an ndarray instead of a list.	
ones, ones_like	Produce an array of all 1's with the given shape and dtype.  ones_like takes another array and produces a ones array of the same shape and dtype.	
zeros, zeros_like	Like ones and ones_like but producing arrays of o's instead	
empty, empty_like	Create new arrays by allocating new memory, but do not populate with any values like ones and zeros	
eye, identity	Create a square N x N identity matrix (1's on the diagonal and o's elsewhere)	

# Data Types for ndarrays

The data type or dtype is a special object containing the information the ndarray needs to interpret a chunk of memory as a particular type of data:

```
In [27]: arr1 = np.array([1, 2, 3], dtype=np.float64)
In [28]: arr2 = np.array([1, 2, 3], dtype=np.int32)
In [29]: arr1.dtype In [30]: arr2.dtype
Out[29]: dtype('float64')
                           Out[30]: dtype('int32')
```

Dtypes are part of what make NumPy so powerful and flexible. In most cases they map

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object) takes up 8 bytes or 64 bits. Thus, this type is known in NumPy as float64. See Table 4-2 for a full listing of NumPy's supported data types.

#### NOTE

Don't worry about memorizing the NumPy dtypes, especially if you're a new user. It's often only necessary to care about the general kind of data you're dealing with, whether floating point, complex, integer, boolean, string, or general Python object. When you need more control over how data are stored in memory and on disk, especially large data sets, it is good to know that you have control over the storage type.

Table 4-2. NumPy data types

Туре	Type Code	Description
int8, uint8	i1, u1	Signed and unsigned 8-bit (1 byte) integer types
int16, uint16	i2, u2	Signed and unsigned 16-bit integer types
int32, uint32	i4, u4	Signed and unsigned 32-bit integer types
int64, uint64	i8, u8	Signed and unsigned 32-bit integer types
float16	f2	Half-precision floating point
float32	f4 or f	Standard single-precision floating point. Compatible with C float
float64	f8 or d	Standard double-precision floating point. Compatible with C double and Python float object

Type	Type	Description

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complex64, complex128, complex256	c8, c16, c32	Complex numbers represented by two 32, 64, or 128 floats, respectively
bool	?	Boolean type storing True and False values
object	О	Python object type
string_	S	Fixed-length string type (1 byte per character). For example, to create a string dtype with length 10, use 'S10'.
unicode_	U	Fixed-length unicode type (number of bytes platform specific). Same specification semantics as string_(e.g. 'U10').

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You can explicitly convert or *cast* an array from one dtype to another using ndarray's astype method:

```
In [31]: arr = np.array([1, 2, 3, 4, 5])
In [32]: arr.dtype
Out[32]: dtype('int64')
In [33]: float arr = arr.astype(np.float64)
In [34]: float arr.dtype
Out[34]: dtype('float64')
```

In this example, integers were cast to floating point. If I cast some floating point numbers to be of integer dtype, the decimal part will be truncated:

```
In [35]: arr = np.array([3.7, -1.2, -2.6, 0.5, 12.9, 10.1])
In [36]: arr
Out[36]: array([ 3.7, -1.2, -2.6, 0.5, 12.9, 10.1])
In [37]: arr.astype(np.int32)
Out[37]: array([3, -1, -2, 0, 12, 10], dtype=int32)
```

Should you have an array of strings representing numbers, you can use astype to convert them to numeric form:

```
In [38]: numeric strings = np.array(['1.25', '-9.6', '42'], dtype=np.string)
In [39]: numeric_strings.astype(float)
Out[39]: array([ 1.25, -9.6, 42. ])
```

If casting were to fail for some reason (like a string that cannot be converted to float64), a TypeError will be raised. See that I was a bit lazy and wrote float instead of

np.float64; NumPy is smart enough to alias the Python types to the equivalent dtypes.

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```
In [41]: calibers = np.array([.22, .270, .357, .380, .44, .50], dtype=np.float64
In [42]: int array.astype(calibers.dtype)
Out[42]: array([ 0., 1., 2., 3., 4., 5., 6., 7., 8., 9.])
```

There are shorthand type code strings you can also use to refer to a dtype:

```
In [43]: empty uint32 = np.empty(8, dtype='u4')
In [44]: empty uint32
Out[44]:
array([ 0,
                    0, 65904672, 0, 64856792,
                                                           0,
      39438163,
                     0], dtype=uint32)
```

#### NOTE

Calling astype *always* creates a new array (a copy of the data), even if the new dtype is the same as the old dtype.

#### **CAUTION**

It's worth keeping in mind that floating point numbers, such as those in float64 and float32 arrays, are only capable of approximating fractional quantities. In complex computations, you may accrue some floating point error, making comparisons only valid up to a certain number of decimal places.

## Operations between Arrays and Scalars

Arrays are important because they enable you to express batch operations on data without writing any for loops. This is usually called *vectorization*. Any arithmetic operations between equal-size arrays applies the operation elementwise:

```
In [45]: arr = np.array([[1., 2., 3.], [4., 5., 6.]])
```

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```
Out[47]:
                            Out[48]:
array([[ 1., 4., 9.],
                            array([[ 0., 0., 0.],
    [ 16., 25., 36.]])
                             [ 0., 0., 0.]])
```

Arithmetic operations with scalars are as you would expect, propagating the value to each element:

```
In [49]: 1 / arr
                                       In [50]: arr ** 0.5
Out[49]:
                                       Out[50]:
array([[ 1. , 0.5 , 0.3333],
                                       array([[ 1. , 1.4142, 1.7321],
                                                    , 2.2361, 2.449511)
      [ 0.25 , 0.2 , 0.1667]])
                                             [ 2.
```

Operations between differently sized arrays is called *broadcasting* and will be discussed in more detail in Chapter 12. Having a deep understanding of broadcasting is not necessary for most of this book.

# **Basic Indexing and Slicing**

NumPy array indexing is a rich topic, as there are many ways you may want to select a subset of your data or individual elements. One-dimensional arrays are simple; on the surface they act similarly to Python lists:

```
In [51]: arr = np.arange(10)
In [52]: arr
Out[52]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
In [53]: arr[5]
Out[53]: 5
In [54]: arr[5:8]
Out[54]: array([5, 6, 7])
In [55]: arr[5:8] = 12
In [56]: arr
```

```
Out[56]: array([ 0, 1, 2, 3, 4, 12, 12, 12, 8, 9])
```

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array:

```
In [57]: arr slice = arr[5:8]
In [58]: arr slice[1] = 12345
In [59]: arr
Out[59]: array([ 0, 1, 2, 3, 4, 12, 12345, 12,
                                                                   8,
In [60]: arr_slice[:] = 64
In [61]: arr
Out[61]: array([ 0, 1, 2, 3, 4, 64, 64, 64, 8, 9])
```

If you are new to NumPy, you might be surprised by this, especially if you have used other array programming languages which copy data more zealously. As NumPy has been designed with large data use cases in mind, you could imagine performance and memory problems if NumPy insisted on copying data left and right.

#### **CAUTION**

If you want a copy of a slice of an idarray instead of a view, you will need to explicitly copy the array; for example arr[5:8].copy().

With higher dimensional arrays, you have many more options. In a two-dimensional array, the elements at each index are no longer scalars but rather one-dimensional arrays:

```
In [62]: arr2d = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
In [63]: arr2d[2]
Out[63]: array([7, 8, 9])
```

Thus, individual elements can be accessed recursively. But that is a bit too much work, so you can pass a comma-separated list of indices to select individual elements. So these are equivalent:

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See Figure 4-1 for an illustration of indexing on a 2D array.

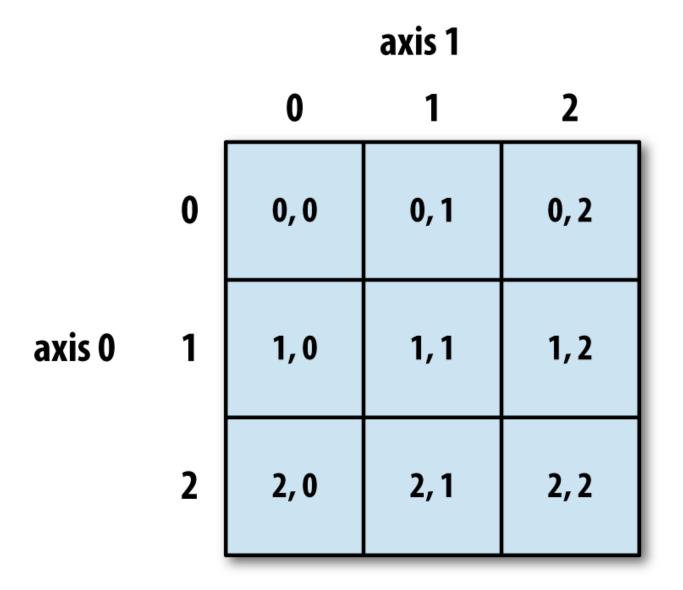


Figure 4-1. Indexing elements in a NumPy array

In multidimensional arrays, if you omit later indices, the returned object will be a lowerdimensional ndarray consisting of all the data along the higher dimensions. So in the  $2 \times 2$ × 3 array arr3d

```
Tn [661: arr3d = np.arrav([[[1. 2. 3]. [4. 5. 6]]. [[7. 8. 9]. [10. 11. 12]]])
                                                                 Sign In
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```

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```
[10, 11, 12]])
```

#### arr3d[0] is a 2 × 3 array:

```
In [68]: arr3d[0]
Out[68]:
array([[1, 2, 3],
       [4, 5, 6]])
```

#### Both scalar values and arrays can be assigned to arr3d[0]:

```
In [69]: old_values = arr3d[0].copy()
In [70]: arr3d[0] = 42
In [71]: arr3d
Out[71]:
array([[[42, 42, 42],
       [42, 42, 42]],
       [[7, 8, 9],
        [10, 11, 12]])
In [72]: arr3d[0] = old values
In [73]: arr3d
Out[73]:
array([[[ 1, 2, 3],
        [ 4, 5, 6]],
       [[7, 8, 9],
        [10, 11, 12]])
```

Similarly, arr3d[1, 0] gives you all of the values whose indices start with (1, 0), forming a 1-dimensional array:

```
In [74]: arr3d[1, 0]
Out[74]: array([7, 8, 9])
```

Note that in all of these cases where subsections of the array have been selected, the

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#### таншаг ѕунцах:

```
In [75]: arr[1:6]
Out[75]: array([ 1, 2, 3, 4, 64])
```

Higher dimensional objects give you more options as you can slice one or more axes and also mix integers. Consider the 2D array above, arr2d. Slicing this array is a bit different:

```
In [76]: arr2d
                         In [77]: arr2d[:2]
                         Out[77]:
Out[76]:
array([[1, 2, 3],
                         array([[1, 2, 3],
      [4, 5, 6],
                               [4, 5, 6]])
      [7, 8, 9]])
```

As you can see, it has sliced along axis o, the first axis. A slice, therefore, selects a range of elements along an axis. You can pass multiple slices just like you can pass multiple indexes:

```
In [78]: arr2d[:2, 1:]
Out[78]:
array([[2, 3],
       [5, 6]])
```

When slicing like this, you always obtain array views of the same number of dimensions. By mixing integer indexes and slices, you get lower dimensional slices:

```
In [80]: arr2d[2, :1]
In [79]: arr2d[1, :2]
Out[79]: array([4, 5])
                            Out[80]: array([7])
```

See Figure 4-2 for an illustration. Note that a colon by itself means to take the entire axis, so you can slice only higher dimensional axes by doing:

```
In [81]: arr2d[:, :1]
Out[81]:
```

```
array([[1],
```

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```
In [82]: arr2d[:2, 1:] = 0
```

# **Boolean Indexing**

Let's consider an example where we have some data in an array and an array of names with duplicates. I'm going to use here the randn function in numpy.random to generate some random normally distributed data:

```
In [83]: names = np.array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'])
In [84]: data = np.random.randn(7, 4)
In [85]: names
Out[85]:
array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'],
     dtype='|S4')
In [86]: data
Out[86]:
array([[-0.048 , 0.5433, -0.2349, 1.2792],
       [-0.268, 0.5465, 0.0939, -2.0445],
       [-0.047, -2.026, 0.7719, 0.3103],
       [ 2.1452, 0.8799, -0.0523, 0.0672],
       [-1.0023, -0.1698, 1.1503, 1.7289],
       [0.1913, 0.4544, 0.4519, 0.5535],
       [0.5994, 0.8174, -0.9297, -1.2564]])
```

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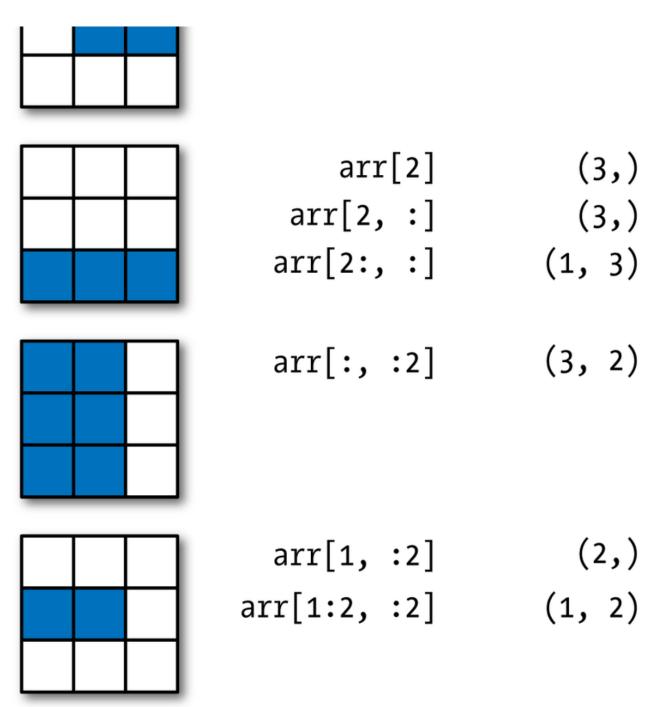


Figure 4-2. Two-dimensional array slicing

Suppose each name corresponds to a row in the data array and we wanted to select all the rows with corresponding name 'Bob'. Like arithmetic operations, comparisons (such as

==) with arrays are also vectorized. Thus, comparing names with the string 'Bob' yields a

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This boolean array can be passed when indexing the array:

```
In [88]: data[names == 'Bob']
Out[88]:
array([[-0.048 , 0.5433, -0.2349, 1.2792],
      [ 2.1452, 0.8799, -0.0523, 0.0672]])
```

The boolean array must be of the same length as the axis it's indexing. You can even mix and match boolean arrays with slices or integers (or sequences of integers, more on this later):

```
In [89]: data[names == 'Bob', 2:]
Out[89]:
array([[-0.2349, 1.2792],
       [-0.0523, 0.0672]]
In [90]: data[names == 'Bob', 3]
Out[90]: array([ 1.2792, 0.0672])
```

To select everything but 'Bob', you can either use != or negate the condition using -:

```
In [91]: names != 'Bob'
Out[91]: array([False, True, True, False, True, True, True], dtype=bool)
In [92]: data[-(names == 'Bob')]
Out[92]:
array([[-0.268, 0.5465, 0.0939, -2.0445],
       [-0.047, -2.026, 0.7719, 0.3103],
       [-1.0023, -0.1698, 1.1503, 1.7289],
       [0.1913, 0.4544, 0.4519, 0.5535],
       [0.5994, 0.8174, -0.9297, -1.2564]])
```

Selecting two of the three names to combine multiple boolean conditions, use boolean arithmetic operators like & (and) and | (or):

```
In [93]: mask = (names == 'Bob') | (names == 'Will')
```

```
In [94]: mask
```

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```
[ 2.1452, 0.8799, -0.0523, 0.0672],
[-1.0023, -0.1698, 1.1503, 1.7289]])
```

Selecting data from an array by boolean indexing always creates a copy of the data, even if the returned array is unchanged.

#### **CAUTION**

The Python keywords and and or do not work with boolean arrays.

Setting values with boolean arrays works in a common-sense way. To set all of the negative values in data to o we need only do:

```
In [96]: data[data < 0] = 0
In [97]: data
Out[97]:
array([[ 0. , 0.5433, 0. , 1.2792],
      [ 0.
            , 0.5465, 0.0939, 0. ],
      [ 0. , 0. , 0.7719,
                              0.3103],
      [ 2.1452, 0.8799, 0. ,
                              0.0672],
      [ 0. , 0. , 1.1503,
                             1.7289],
      [0.1913, 0.4544, 0.4519, 0.5535],
      [0.5994, 0.8174, 0., 0.]
```

Setting whole rows or columns using a 1D boolean array is also easy:

```
In [98]: data[names != 'Joe'] = 7
In [99]: data
Out[99]:
array([[ 7. , 7. , 7. , 7.
             , 0.5465, 0.0939,
      ΓΟ.
                                0.
      [ 7.
               7.
                  , 7.
                                7.
                        7.
                                7.
               7.
               7.
                        7.
                                7.
                                     ],
      [ 7.
      [ 0.1913, 0.4544,
                        0.4519,
                                0.5535],
```

```
[ 0.5994, 0.8174, 0. , 0.
                             ]])
```

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suppose we had a o × 4 array.

```
In [100]: arr = np.empty((8, 4))
In [101]: for i in range(8):
   ....: arr[i] = i
In [102]: arr
Out[102]:
array([[ 0., 0., 0., 0.],
      [ 1., 1., 1., 1.],
      [ 2., 2., 2., 2.],
      [ 3., 3., 3., 3.],
      [ 4., 4., 4., 4.],
      [5., 5., 5., 5.],
      [6., 6., 6., 6.],
      [ 7., 7., 7., 7.]])
```

To select out a subset of the rows in a particular order, you can simply pass a list or ndarray of integers specifying the desired order:

```
In [103]: arr[[4, 3, 0, 6]]
Out[103]:
array([[ 4., 4., 4., 4.],
      [ 3., 3., 3., 3.],
      [ 0., 0., 0., 0.],
      [6., 6., 6., 6.]])
```

Hopefully this code did what you expected! Using negative indices select rows from the end:

```
In [104]: arr[[-3, -5, -7]]
Out[104]:
array([[ 5., 5., 5., 5.],
      [ 3., 3., 3., 3.],
      [ 1., 1., 1., 1.]])
```

Passing multiple index arrays does something slightly different; it selects a 1D array of

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```
in [iub]: arr
Out[106]:
array([[ 0, 1, 2, 3],
       [4, 5, 6, 7],
       [8, 9, 10, 11],
       [12, 13, 14, 15],
       [16, 17, 18, 19],
       [20, 21, 22, 23],
       [24, 25, 26, 27],
       [28, 29, 30, 31]])
In [107]: arr[[1, 5, 7, 2], [0, 3, 1, 2]]
Out[107]: array([ 4, 23, 29, 10])
```

Take a moment to understand what just happened: the elements (1, 0), (5, 3), (7, 1), and (2, 2) were selected. The behavior of fancy indexing in this case is a bit different from what some users might have expected (myself included), which is the rectangular region formed by selecting a subset of the matrix's rows and columns. Here is one way to get that:

```
In [108]: arr[[1, 5, 7, 2]][:, [0, 3, 1, 2]]
Out[108]:
array([[ 4, 7, 5, 6],
      [20, 23, 21, 22],
       [28, 31, 29, 30],
       [8, 11, 9, 10]])
```

Another way is to use the np.ix function, which converts two 1D integer arrays to an indexer that selects the square region:

```
In [109]: arr[np.ix ([1, 5, 7, 2], [0, 3, 1, 2])]
Out[109]:
array([[ 4, 7, 5, 6],
      [20, 23, 21, 22],
       [28, 31, 29, 30],
       [8, 11, 9, 10]])
```

Keep in mind that fancy indexing, unlike slicing, always copies the data into a new array.

## Transposing Arrays and Swapping Axes

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```
In [110]: arr = np.arange(15).reshape((3, 5))
In [111]: arr
                                  In [112]: arr.T
Out[111]:
                                  Out[112]:
array([[ 0, 1, 2, 3, 4],
                                  array([[ 0, 5, 10],
      [5, 6, 7, 8, 9],
                                       [ 1, 6, 11],
      [10, 11, 12, 13, 14]])
                                         [2, 7, 12],
                                         [ 3, 8, 13],
                                         [ 4, 9, 14]])
```

When doing matrix computations, you will do this very often, like for example computing the inner matrix product X<sup>T</sup>X using np.dot:

```
In [113]: arr = np.random.randn(6, 3)
In [114]: np.dot(arr.T, arr)
Out[114]:
array([[ 2.584 , 1.8753, 0.8888],
       [ 1.8753, 6.6636, 0.3884],
       [ 0.8888, 0.3884, 3.9781]])
```

For higher dimensional arrays, transpose will accept a tuple of axis numbers to permute the axes (for extra mind bending):

```
In [115]: arr = np.arange(16).reshape((2, 2, 4))
In [116]: arr
Out[116]:
array([[[ 0, 1, 2, 3],
       [4, 5, 6, 7]],
      [[8, 9, 10, 11],
       [12, 13, 14, 15]])
In [117]: arr.transpose((1, 0, 2))
Out[117]:
array([[[ 0, 1, 2, 3],
       [8, 9, 10, 11]],
      [[4, 5, 6,
```

```
[12, 13, 14, 15]])
```

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```
III [III]. aII.SWapanes(I, 2)
TH [TTO]. GTT
Out[118]:
                                 Out[119]:
array([[[ 0, 1, 2, 3],
                                 array([[[ 0, 4],
      [ 4, 5, 6, 7]],
                                        [ 1, 5],
                                         [2, 6],
      [[8, 9, 10, 11],
                                        [ 3, 7]],
       [12, 13, 14, 15]])
                                        [[8, 12],
                                        [ 9, 13],
                                         [10, 14],
                                         [11, 15]])
```

swapaxes similarly returns a view on the data without making a copy.

# Universal Functions: Fast Element-wise Array **Functions**

A universal function, or *ufunc*, is a function that performs elementwise operations on data in ndarrays. You can think of them as fast vectorized wrappers for simple functions that take one or more scalar values and produce one or more scalar results.

Many ufuncs are simple elementwise transformations, like sqrt or exp:

```
In [120]: arr = np.arange(10)
In [121]: np.sqrt(arr)
Out[121]:
array([ 0. , 1. , 1.4142, 1.7321, 2. , 2.2361, 2.4495,
     2.6458, 2.8284, 3. ])
In [122]: np.exp(arr)
Out[122]:
array([ 1. , 2.7183, 7.3891, 20.0855, 54.5982,
       148.4132, 403.4288, 1096.6332, 2980.958, 8103.0839])
```

These are referred to as *unary* ufuncs. Others, such as add or maximum, take 2 arrays (thus, binary ufuncs) and return a single array as the result:

```
In [1231: x = np.random.randn(8)
```

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```
-0.9337])
In [126]: y
Out[126]:
array([ 0.267 , -1.1131, -0.3361, 0.6117, -1.2323, 0.4788, 0.4315,
      -0.7147])
In [127]: np.maximum(x, y) # element-wise maximum
Out[127]:
array([ 0.267 , 0.0974, 0.2002, 0.6117, 0.4655, 0.9222, 0.446 ,
      -0.71471)
```

While not common, a ufunc can return multiple arrays. modf is one example, a vectorized version of the built-in Python divmod: it returns the fractional and integral parts of a floating point array:

```
In [128]: arr = randn(7) * 5
In [129]: np.modf(arr)
Out[129]:
(array([-0.6808, 0.0636, -0.386, 0.1393, -0.8806, 0.9363, -0.883]),
array([-2., 4., -3., 5., -3., 3., -6.]))
```

See Table 4-3 and Table 4-4 for a listing of available ufuncs.

#### Table 4-3. Unary ufuncs

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	complex-valued data	
sqrt	Compute the square root of each element. Equivalent to arr **  0.5	
square	Compute the square of each element. Equivalent to arr ** 2	
ехр	Compute the exponent e <sup>x</sup> of each element	
log, log10, log2, log1p	Natural logarithm (base $e$ ), log base 10, log base 2, and log(1 + x), respectively	
sign	Compute the sign of each element: 1 (positive), 0 (zero), or -1 (negative)	
ceil	Compute the ceiling of each element, i.e. the smallest integer greater than or equal to each element	
floor	Compute the floor of each element, i.e. the largest integer less than or equal to each element	
rint	Round elements to the nearest integer, preserving the dtype	
modf	Return fractional and integral parts of array as separate array	
isnan	Return boolean array indicating whether each value is NaN (Not a Number)	
isfinite, isinf	Return boolean array indicating whether each element is finite (non-inf, non-NaN) or infinite, respectively	
cos, cosh, sin, tan, tan,	Regular and hyperbolic trigonometric functions	

Function	Description	

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arcsinh, arctan, arctanh	
logical_not	Compute truth value of not x element-wise. Equivalent to -arr.

#### Table 4-4. Binary universal functions

Function	Description
add	Add corresponding elements in arrays
subtract	Subtract elements in second array from first array
multiply	Multiply array elements
divide, floor_divide	Divide or floor divide (truncating the remainder)
power	Raise elements in first array to powers indicated in second array
maximum, fmax	Element-wise maximum. fmax ignores NaN
minimum, fmin	Element-wise minimum. fmin ignores NaN
mod	Element-wise modulus (remainder of division)
copysign	Copy sign of values in second argument to values in first argument

Function Description

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less_equal,	
equal,	
not_equal	
logical_and, logical_or, logical_xor	Compute element-wise truth value of logical operation.  Equivalent to infix operators &  , ^
_	

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concise array expressions that might otherwise require writing loops. This practice of replacing explicit loops with array expressions is commonly referred to as vectorization. In general, vectorized array operations will often be one or two (or more) orders of magnitude faster than their pure Python equivalents, with the biggest impact in any kind of numerical computations. Later, in Chapter 12, I will explain broadcasting, a powerful method for vectorizing computations.

As a simple example, suppose we wished to evaluate the function  $sqrt(x^2 + y^2)$ across a regular grid of values. The np.meshgrid function takes two 1D arrays and produces two 2D matrices corresponding to all pairs of (x, y) in the two arrays:

```
In [130]: points = np.arange(-5, 5, 0.01) # 1000 equally spaced points
In [131]: xs, ys = np.meshgrid(points, points)
In [132]: ys
Out[132]:
array([[-5. , -5. , -5. , ..., -5. , -5. , -5. ],
       [-4.99, -4.99, -4.99, \dots, -4.99, -4.99, -4.99],
       [-4.98, -4.98, -4.98, ..., -4.98, -4.98, -4.98],
       [4.97, 4.97, 4.97, \ldots, 4.97, 4.97, 4.97],
       [4.98, 4.98, 4.98, \ldots, 4.98, 4.98, 4.98],
       [4.99, 4.99, 4.99, \ldots, 4.99, 4.99, 4.99]])
```

Now, evaluating the function is a simple matter of writing the same expression you would write with two points:

```
In [134]: import matplotlib.pyplot as plt
In [135]: z = np.sqrt(xs ** 2 + ys ** 2)
In [136]: z
Out[136]:
array([[ 7.0711, 7.064 , 7.0569, ..., 7.0499, 7.0569, 7.064 ],
      [7.064, 7.0569, 7.0499, \ldots, 7.0428,
                                               7.0499,
                                                        7.0569],
      [7.0569, 7.0499, 7.0428, ..., 7.0357, 7.0428,
                                                        7.0499],
```

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In [138]: plt.title("Image plot of  $\frac{x^2 + y^2}{5}$  for a grid of values") Out[138]: <matplotlib.text.Text at 0x4565790>

See Figure 4-3. Here I used the matplotlib function imshow to create an image plot from a 2D array of function values.

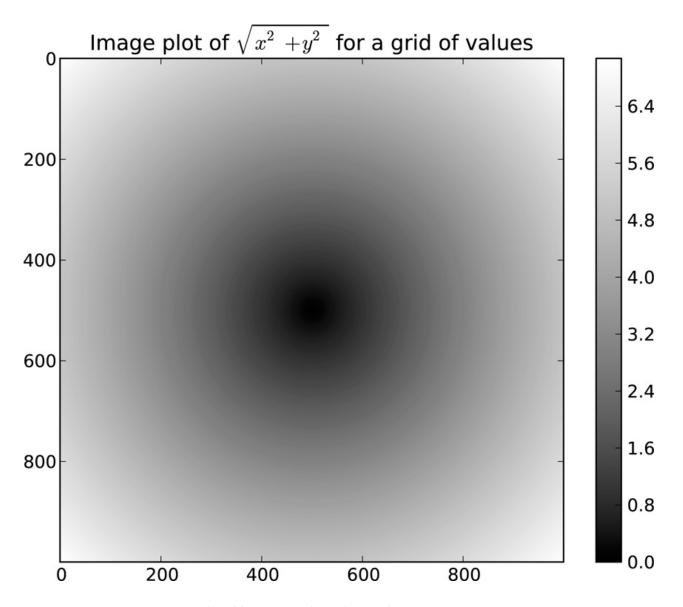


Figure 4-3. Plot of function evaluated on grid

# **Expressing Conditional Logic as Array Operations**

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```
In [141]: yarr = np.array([2.1, 2.2, 2.3, 2.4, 2.5])
In [142]: cond = np.array([True, False, True, True, False])
```

Suppose we wanted to take a value from xarr whenever the corresponding value in cond is True otherwise take the value from yarr. A list comprehension doing this might look like:

```
In [143]: result = [(x \text{ if c else y})]
                    for x, y, c in zip(xarr, yarr, cond)]
In [144]: result
Out[144]: [1.1000000000000001, 2.20000000000000, 1.3, 1.39999999999999, 2.5]
```

This has multiple problems. First, it will not be very fast for large arrays (because all the work is being done in pure Python). Secondly, it will not work with multidimensional arrays. With np. where you can write this very concisely:

```
In [145]: result = np.where(cond, xarr, yarr)
In [146]: result
Out[146]: array([ 1.1, 2.2, 1.3, 1.4, 2.5])
```

The second and third arguments to np. where don't need to be arrays; one or both of them can be scalars. A typical use of where in data analysis is to produce a new array of values based on another array. Suppose you had a matrix of randomly generated data and you wanted to replace all positive values with 2 and all negative values with -2. This is very easy to do with np.where:

```
In [147]: arr = randn(4, 4)
In [148]: arr
Out[148]:
array([[ 0.6372, 2.2043, 1.7904, 0.0752],
      [-1.5926, -1.1536, 0.4413, 0.3483],
```

```
[-0.1798, 0.3299, 0.7827, -0.7585],
          0 1 6 1 0 1 0 5 0 0
```

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```
[ 2, 2, 2, -2]])
In [150]: np.where(arr > 0, 2, arr) # set only positive values to 2
Out[150]:
array([[ 2. , 2. , 2. , 2. ],
     [-1.5926, -1.1536, 2., 2.],
     [-0.1798, 2. , 2. , -0.7585],
     [2., 2., 2., -1.3865]
```

The arrays passed to where can be more than just equal sizes array or scalars.

With some cleverness you can use where to express more complicated logic; consider this example where I have two boolean arrays, cond1 and cond2, and wish to assign a different value for each of the 4 possible pairs of boolean values:

```
result = []
for i in range(n):
    if cond1[i] and cond2[i]:
        result.append(0)
    elif cond1[i]:
        result.append(1)
    elif cond2[i]:
        result.append(2)
    else:
       result.append(3)
```

While perhaps not immediately obvious, this for loop can be converted into a nested where expression:

```
np.where(cond1 & cond2, 0,
         np.where(cond1, 1,
                  np.where(cond2, 2, 3)))
```

In this particular example, we can also take advantage of the fact that boolean values are treated as 0 or 1 in calculations, so this could alternatively be expressed (though a bit more cryptically) as an arithmetic operation:

```
result = 1 * (cond1 \& -cond2) + 2 * (cond2 \& -cond1) + 3 * -(cond1 | cond2)
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```

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the data along an axis are accessible as array methods. Aggregations (often called reductions) like sum, mean, and standard deviation std can either be used by calling the array instance method or using the top level NumPy function:

```
In [151]: arr = np.random.randn(5, 4) # normally-distributed data
In [152]: arr.mean()
Out[152]: 0.062814911084854597
In [153]: np.mean(arr)
Out[153]: 0.062814911084854597
In [154]: arr.sum()
Out[154]: 1.2562982216970919
```

Functions like mean and sum take an optional axis argument which computes the statistic over the given axis, resulting in an array with one fewer dimension:

```
In [155]: arr.mean(axis=1)
Out[155]: array([-1.2833, 0.2844, 0.6574, 0.6743, -0.0187])
In [156]: arr.sum(0)
Out[156]: array([-3.1003, -1.6189, 1.4044, 4.5712])
```

Other methods like cumsum and cumprod do not aggregate, instead producing an array of the intermediate results:

```
In [157]: arr = np.array([[0, 1, 2], [3, 4, 5], [6, 7, 8]])
In [158]: arr.cumsum(0)
                            In [159]: arr.cumprod(1)
Out[158]:
                            Out[159]:
array([[ 0, 1, 2],
                            array([[ 0, 0, 0],
      [ 3, 5, 7],
                                  [ 3, 12, 60],
      [ 9, 12, 15]])
                                  [ 6, 42, 336]])
```

See Table 4-5 for a full listing. We'll see many examples of these methods in action in later

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sum	Sum of all the elements in the array or along an axis. Zero-length arrays have sum o.
mean	Arithmetic mean. Zero-length arrays have NaN mean.
std, var	Standard deviation and variance, respectively, with optional degrees of freedom adjustment (default denominator n).
min,	Minimum and maximum.
argmin,	Indices of minimum and maximum elements, respectively.
cumsum	Cumulative sum of elements starting from o
cumprod	Cumulative product of elements starting from 1

## Methods for Boolean Arrays

Boolean values are coerced to 1 (True) and 0 (False) in the above methods. Thus, sum is often used as a means of counting True values in a boolean array:

```
In [160]: arr = randn(100)
In [161]: (arr > 0).sum() # Number of positive values
Out[161]: 44
```

There are two additional methods, any and all, useful especially for boolean arrays. any tests whether one or more values in an array is True, while all checks if every value is True:

```
In [162]: bools = np.array([False, False, True, False])
```

```
In [163] . hoole anu/)
```

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These methods also work with non-boolean arrays, where non-zero elements evaluate to True.

# Sorting

Like Python's built-in list type, NumPy arrays can be sorted in-place using the sort method:

```
In [165]: arr = randn(8)
In [166]: arr
Out[166]:
array([ 0.6903,  0.4678,  0.0968, -0.1349,  0.9879,  0.0185, -1.3147,
      -0.54251)
In [167]: arr.sort()
In [168]: arr
Out[168]:
array([-1.3147, -0.5425, -0.1349, 0.0185, 0.0968, 0.4678, 0.6903,
       0.98791)
```

Multidimensional arrays can have each 1D section of values sorted in-place along an axis by passing the axis number to sort:

```
In [169]: arr = randn(5, 3)
In [170]: arr
Out[170]:
array([[-0.7139, -1.6331, -0.4959],
       [0.8236, -1.3132, -0.1935],
       [-1.6748, 3.0336, -0.863],
       [-0.3161, 0.5362, -2.468],
       [0.9058, 1.1184, -1.0516]])
In [171]: arr.sort(1)
In [172]: arr
Out[172]:
```

```
array([-1.6331, -0.7139, -0.4959],
       r 1 2120
               0 1005 0 00001
```

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array in place. A quick-and-dirty way to compute the quantiles of an array is to sort it and select the value at a particular rank:

```
In [173]: large arr = randn(1000)
In [174]: large arr.sort()
In [175]: large_arr[int(0.05 * len(large_arr))] # 5% quantile
Out[175]: -1.5791023260896004
```

For more details on using NumPy's sorting methods, and more advanced techniques like indirect sorts, see Chapter 12. Several other kinds of data manipulations related to sorting (for example, sorting a table of data by one or more columns) are also to be found in pandas.

# Unique and Other Set Logic

NumPy has some basic set operations for one-dimensional ndarrays. Probably the most commonly used one is np.unique, which returns the sorted unique values in an array:

```
In [176]: names = np.array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'])
In [177]: np.unique(names)
Out[177]:
array(['Bob', 'Joe', 'Will'],
      dtype='|S4')
In [178]: ints = np.array([3, 3, 3, 2, 2, 1, 1, 4, 4])
In [179]: np.unique(ints)
Out[179]: array([1, 2, 3, 4])
```

Contrast np.unique with the pure Python alternative:

```
In [180]: sorted(set(names))
```

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```
In [181]: values = np.array([6, 0, 0, 3, 2, 5, 6])
In [182]: np.in1d(values, [2, 3, 6])
Out[182]: array([ True, False, False,
                                       True,
                                             True, False, True], dtype=bool)
```

See Table 4-6 for a listing of set functions in NumPy.

Table 4-6. Array set operations

Method	Description	
unique(x)	Compute the sorted, unique elements in x	
<pre>intersect1d(x, y)</pre>	Compute the sorted, common elements in x and y	
union1d(x, y)	Compute the sorted union of elements	
in1d(x, y)	Compute a boolean array indicating whether each element of x is contained in y	
setdiff1d(x, y)	Set difference, elements in x that are not in y	
setxor1d(x, y)	Set symmetric differences; elements that are in either of the arrays, but not both	

# File Input and Output with Arrays

NumPy is able to save and load data to and from disk either in text or binary format. In later chapters you will learn about tools in pandas for reading tabular data into memory.

## Storing Arrays on Disk in Binary Format

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```
In [183]: arr = np.arange(10)
In [184]: np.save('some array', arr)
```

If the file path does not already end in .npy, the extension will be appended. The array on disk can then be loaded using np.load:

```
In [185]: np.load('some array.npy')
Out[185]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

You save multiple arrays in a zip archive using np.savez and passing the arrays as keyword arguments:

```
In [186]: np.savez('array archive.npz', a=arr, b=arr)
```

When loading an .npz file, you get back a dict-like object which loads the individual arrays lazily:

```
In [187]: arch = np.load('array archive.npz')
In [188]: arch['b']
Out[188]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

# Saving and Loading Text Files

Loading text from files is a fairly standard task. The landscape of file reading and writing functions in Python can be a bit confusing for a newcomer, so I will focus mainly on the read\_csv and read\_table functions in pandas. It will at times be useful to load data into vanilla NumPy arrays using np.loadtxt or the more specialized np.genfromtxt.

These functions have many options allowing you to specify different delimiters, converter functions for certain columns, skipping rows, and other things. Take a simple case of a comma-separated file (CSV) like this:

```
In [191]: !cat array ex.txt
```

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This can be loaded into a 2D array like so:

```
In [192]: arr = np.loadtxt('array ex.txt', delimiter=',')
In [193]: arr
Out[193]:
array([[ 0.5801, 0.1867, 1.0407, 1.1344],
       [0.1942, -0.6369, -0.9387, 0.1241],
       [-0.1264, 0.2686, -0.6957, 0.0474],
       [-1.4844, 0.0042, -0.7442, 0.0055],
       [2.3029, 0.2001, 1.6702, -1.8811],
       [-0.1932, 1.0472, 0.4828, 0.9603]])
```

np. savetxt performs the inverse operation: writing an array to a delimited text file. genfromtxt is similar to loadtxt but is geared for structured arrays and missing data handling; see Chapter 12 for more on structured arrays.

```
TIP
```

For more on file reading and writing, especially tabular or spreadsheet-like data, see the later chapters involving pandas and DataFrame objects.

# Linear Algebra

Linear algebra, like matrix multiplication, decompositions, determinants, and other square matrix math, is an important part of any array library. Unlike some languages like MATLAB, multiplying two two-dimensional arrays with \* is an element-wise product instead of a matrix dot product. As such, there is a function dot, both an array method, and a function in the numpy namespace, for matrix multiplication:

```
In [194]: x = np.array([[1., 2., 3.], [4., 5., 6.]])
In [195]: y = np.array([[6., 23.], [-1, 7], [8, 9]])
```

```
In [196]: x
                               In [197]: y
```

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```
Out[198]:
array([[ 28., 64.],
     [ 67., 181.]])
```

A matrix product between a 2D array and a suitably sized 1D array results in a 1D array:

```
In [199]: np.dot(x, np.ones(3))
Out[199]: array([ 6., 15.])
```

numpy.linalg has a standard set of matrix decompositions and things like inverse and determinant. These are implemented under the hood using the same industry-standard Fortran libraries used in other languages like MATLAB and R, such as like BLAS, LAPACK, or possibly (depending on your NumPy build) the Intel MKL:

```
In [201]: from numpy.linalg import inv, qr
In [202]: X = randn(5, 5)
In [203]: mat = X.T.dot(X)
In [204]: inv(mat)
Out[204]:
array([[ 3.0361, -0.1808, -0.6878, -2.8285, -1.1911],
      [-0.1808, 0.5035, 0.1215, 0.6702, 0.0956],
      [-0.6878, 0.1215, 0.2904, 0.8081, 0.3049],
      [-2.8285, 0.6702, 0.8081, 3.4152, 1.1557],
      [-1.1911, 0.0956, 0.3049, 1.1557, 0.6051]])
In [205]: mat.dot(inv(mat))
Out[205]:
array([[ 1., 0., 0., 0., -0.],
      [0., 1., -0., 0., 0.]
      [0., -0., 1., 0., 0.],
      [0., -0., -0., 1., -0.]
      [0., 0., 0., 1.]]
In [206]: q_{r} r = qr(mat)
In [207]: r
Out[207]:
```

```
array([[ -6.9271, 7.389 , 6.1227, -7.1163, -4.9215],
```

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#### NOTE

The scientific Python community is hopeful that there may be a matrix multiplication infix operator implemented someday, providing syntactically nicer alternative to using np.dot. But for now this is the way.

Table 4-7. Commonly-used numpy.linalg functions

Function	Description
diag	Return the diagonal (or off-diagonal) elements of a square matrix as a 1D array, or convert a 1D array into a square matrix with zeros on the off-diagonal
dot	Matrix multiplication
trace	Compute the sum of the diagonal elements
det	Compute the matrix determinant
eig	Compute the eigenvalues and eigenvectors of a square matrix
inv	Compute the inverse of a square matrix
pinv	Compute the Moore-Penrose pseudo-inverse inverse of a matrix
qr	Compute the QR decomposition
svd	Compute the singular value decomposition (SVD)
solve	Solve the linear system $Ax = b$ for x, where A is a square matrix
lstsq	Compute the least-squares solution to $Ax = b$

## Random Number Generation

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```
In [208]: samples = np.random.normal(size=(4, 4))
In [209]: samples
Out[209]:
array([[ 0.1241, 0.3026, 0.5238, 0.0009],
       [1.3438, -0.7135, -0.8312, -2.3702],
       [-1.8608, -0.8608, 0.5601, -1.2659],
       [0.1198, -1.0635, 0.3329, -2.3594]])
```

Python's built-in random module, by contrast, only samples one value at a time. As you can see from this benchmark, numpy.random is well over an order of magnitude faster for generating very large samples:

```
In [210]: from random import normalvariate
In [211]: N = 1000000
In [212]: %timeit samples = [normalvariate(0, 1) for _ in xrange(N)]
1 loops, best of 3: 1.33 s per loop
In [213]: %timeit np.random.normal(size=N)
10 loops, best of 3: 57.7 ms per loop
```

See Table 4-8 for a partial list of functions available in numpy.random. I'll give some examples of leveraging these functions' ability to generate large arrays of samples all at once in the next section.

#### Table 4-8. Partial list of numpy.random functions

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permutation	Return a random permutation of a sequence, or return a permuted range			
shuffle	Randomly permute a sequence in place			
rand	Draw samples from a uniform distribution			
randint	Draw random integers from a given low-to-high range			
randn	Draw samples from a normal distribution with mean o and standard deviation 1 (MATLAB-like interface)			
binomial	Draw samples from a binomial distribution			
normal	Draw samples from a normal (Gaussian) distribution			
beta	Draw samples from a beta distribution			
chisquare	Draw samples from a chi-square distribution			
gamma	Draw samples from a gamma distribution			
uniform	Draw samples from a uniform [0, 1) distribution			

# **Example: Random Walks**

An illustrative application of utilizing array operations is in the simulation of random walks. Let's first consider a simple random walk starting at 0 with steps of 1 and -1 occurring with equal probability. A pure Python way to implement a single random walk with 1,000 steps using the built-in random module:

steps = 1000

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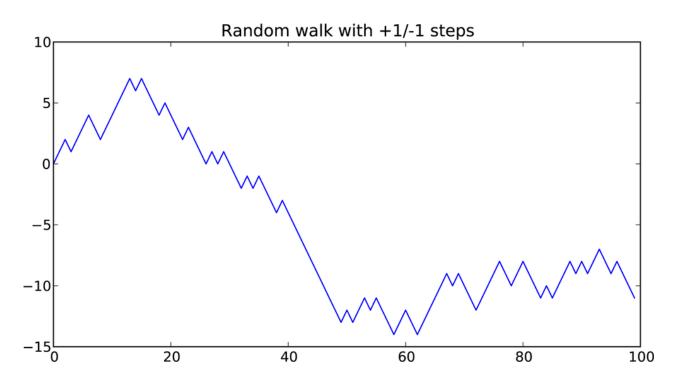


Figure 4-4. A simple random walk

You might make the observation that walk is simply the cumulative sum of the random steps and could be evaluated as an array expression. Thus, I use the np.random module to draw 1,000 coin flips at once, set these to 1 and -1, and compute the cumulative sum:

```
In [215]: nsteps = 1000
In [216]: draws = np.random.randint(0, 2, size=nsteps)
In [217]: steps = np.where(draws > 0, 1, -1)
In [218]: walk = steps.cumsum()
```

From this we can begin to extract statistics like the minimum and maximum value along the walk's trajectory:

```
In [219]: walk.min()
                                  In [220]: walk.max()
O_{11} + [219] \cdot -3
                                  011+[220] • 31
```

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want the index of the first 10 or -10. Turns out this can be computed using argmax, which returns the first index of the maximum value in the boolean array (True is the maximum value):

```
In [221]: (np.abs(walk) >= 10).argmax()
Out[221]: 37
```

Note that using argmax here is not always efficient because it always makes a full scan of the array. In this special case once a True is observed we know it to be the maximum value.

# Simulating Many Random Walks at Once

If your goal was to simulate many random walks, say 5,000 of them, you can generate all of the random walks with minor modifications to the above code. The numpy.random functions if passed a 2-tuple will generate a 2D array of draws, and we can compute the cumulative sum across the rows to compute all 5,000 random walks in one shot:

```
In [222]: nwalks = 5000
In [223]: nsteps = 1000
In [224]: draws = np.random.randint(0, 2, size=(nwalks, nsteps)) # 0 or 1
In [225]: steps = np.where(draws > 0, 1, -1)
In [226]: walks = steps.cumsum(1)
In [227]: walks
Out[227]:
            0, 1, ..., 8, 7, 8],
array([[ 1,
      [ 1, 0, -1, ..., 34, 33, 32],
      [ 1, 0, -1, \ldots, 4, 
                                     4],
            2, 1, ..., 24, 25,
                                    26],
            2, 3, ..., 14, 13,
            -2, -3, ..., -24, -23, -22]])
```

Now, we can compute the maximum and minimum values obtained over all of the walks:

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Out of these warks, let's compute the minimum crossing time to 30 or -30. This is siightly tricky because not all 5,000 of them reach 30. We can check this using the any method:

```
In [230]: hits30 = (np.abs(walks) >= 30).any(1)
In [231]: hits30
Out[231]: array([False, True, False, ..., False, True, False], dtype=bool)
In [232]: hits30.sum() # Number that hit 30 or -30
Out[232]: 3410
```

We can use this boolean array to select out the rows of walks that actually cross the absolute 30 level and call argmax across axis 1 to get the crossing times:

```
In [233]: crossing times = (np.abs(walks[hits30]) >= 30).argmax(1)
In [234]: crossing times.mean()
Out[234]: 498.88973607038122
```

Feel free to experiment with other distributions for the steps other than equal sized coin flips. You need only use a different random number generation function, like normal to generate normally distributed steps with some mean and standard deviation:

```
In [235]: steps = np.random.normal(loc=0, scale=0.25,
                                   size=(nwalks, nsteps))
```

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