Problem Statement

In [6]:

df.info()

Jamboree, a higher education consulting firm, has provided a list of students' performance metrics such as GRE test score (out of 340), TOEFL test score (out of 120), university rating (out of 5.0), undergrad GPA (out of 10), score of recommendation letters and Statement of Purpose (out of 5), research experience (0 or 1), and their chance of getting admit (0 to 1 range). We need to analyze which performance metrics were more important in predicting the chances of getting an admit, to help in predicting the admit chances for future students.

```
In [1]:
         # useful imports
         import numpy as np, seaborn as sns, pandas as pd, matplotlib.pyplot as plt
In [2]:
         # import warnings
         # warnings.filterwarnings("ignore")
In [3]: df = pd.read_csv('Jamboree_Admission.csv')
         df.head()
             Serial No. GRE Score TOEFL Score University Rating
                                                                SOP
                                                                      LOR CGPA Research Chance of Admit
Out[3]:
         0
                    1
                                                                                         1
                             337
                                          118
                                                             4
                                                                  4.5
                                                                       4.5
                                                                             9.65
                                                                                                        0.92
                    2
                             324
                                          107
                                                                  4.0
                                                                       4.5
                                                                             8.87
                                                                                                        0.76
         2
                    3
                                                                                         1
                                          104
                                                                             8.00
                                                                                                        0.72
                             316
                                                             3
                                                                  3.0
                                                                       3.5
         3
                    4
                             322
                                                                                         1
                                                                                                        0.80
                                          110
                                                                  3.5
                                                                       2.5
                                                                             8.67
                    5
                                                                                         0
         4
                             314
                                          103
                                                             2
                                                                  2.0
                                                                       3.0
                                                                             8.21
                                                                                                        0.65
         df.drop(['Serial No.'],axis=1,inplace=True) # deleting the serial no. column as it is not require
In [5]:
         df['Research'].replace([0,1],["no","yes"],inplace=True)
         df.head()
             GRE Score TOEFL Score University Rating
                                                           LOR CGPA Research Chance of Admit
Out[5]:
                                                      SOP
         0
                   337
                                                       4.5
                                                             4.5
                                                                  9.65
                                                                                             0.92
                               118
                                                                             yes
                   324
                               107
                                                       4.0
                                                            4.5
                                                                  8.87
                                                                             yes
                                                                                             0.76
         2
                                                                  8.00
                                                                                             0.72
                   316
                               104
                                                   3
                                                       3.0
                                                             3.5
                                                                             yes
         3
                                                                                             0.80
                   322
                               110
                                                   3
                                                       3.5
                                                             2.5
                                                                  8.67
                                                                             yes
                               103
                                                   2
          4
                  314
                                                       2.0
                                                             3.0
                                                                  8.21
                                                                                             0.65
                                                                             no
```

<class 'pandas.core.frame.DataFrame'> RangeIndex: 500 entries, 0 to 499 Data columns (total 8 columns): Column Non-Null Count Dtype -------------0 GRE Score 500 non-null int64 TOEFL Score 500 non-null int64 1 2 University Rating 500 non-null int64 3 SOP 500 non-null float64 4 LOR 500 non-null float64 5 CGPA 500 non-null float64 6 Research 500 non-null object Chance of Admit float64 500 non-null dtypes: float64(4), int64(3), object(1) memory usage: 31.4+ KB

Shape is 500 rows and 8 columns all except research experience are numerical data types. There are no missing values in any column.

checking for null values

```
In [7]: df.isna().sum()
                               0
Out[7]: GRE Score
         TOEFL Score
                               0
         University Rating
                               0
         SOP
                               0
         LOR
                               0
         CGPA
                               0
         Research
                               0
         Chance of Admit
                               0
         dtype: int64
```

checking for duplicated values

```
In [8]: df.duplicated().sum()
```

Out[8]: 0

Out[9]:

In [9]: df.describe() # numerical features

	GRE Score	TOEFL Score	University Rating	SOP	LOR	CGPA	Chance of Admit
count	500.000000	500.000000	500.000000	500.000000	500.00000	500.000000	500.00000
mean	316.472000	107.192000	3.114000	3.374000	3.48400	8.576440	0.72174
std	11.295148	6.081868	1.143512	0.991004	0.92545	0.604813	0.14114
min	290.000000	92.000000	1.000000	1.000000	1.00000	6.800000	0.34000
25%	308.000000	103.000000	2.000000	2.500000	3.00000	8.127500	0.63000
50%	317.000000	107.000000	3.000000	3.500000	3.50000	8.560000	0.72000
75%	325.000000	112.000000	4.000000	4.000000	4.00000	9.040000	0.82000
max	340.000000	120.000000	5.000000	5.000000	5.00000	9.920000	0.97000

Mean GRE score is 316.47. Ranges from 290 to 340. Median is close to mean at 317.

Mean TOEFL score is 107.2 and median is 107. Ranges from 92 to 120.

Mean university rating is 3.11, median 3 and ranges from 1 to 5.

Mean SOP score is 3.37, median 3.5, and scores range from 1 to 5.

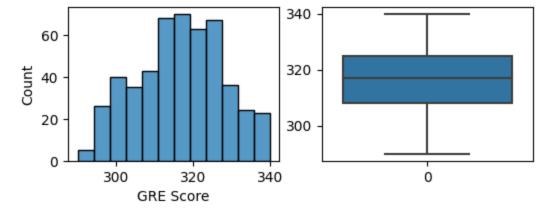
Mean LOR score is 3.48, median 3.5, and scores range from 1 to 5.

Mean CGPA is 8.58, median is 8.56, and range is from 6.8 to 9.92.

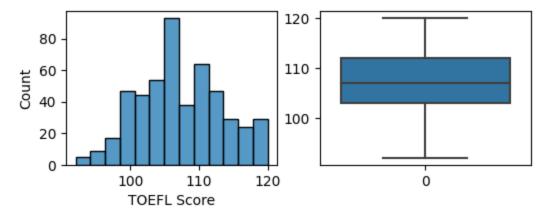
Mean of chances of admit is 0.7217 or 72.17%, median is 72%, and range is from 34% to 97%.

Univariate analysis

```
In [10]: f = plt.figure()
    f.set_figwidth(6)
    f.set_figheight(2)
    plt.subplot(121)
    sns.histplot(data=df, x='GRE Score') # looks close to a bell-shaped curve.
    plt.subplot(122)
    sns.boxplot(df['GRE Score'])
    plt.show() # there are no outliers here.
```

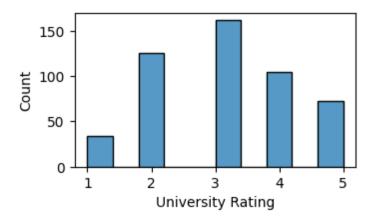


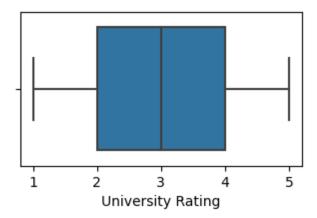
```
In [11]: f = plt.figure()
    f.set_figwidth(6)
    f.set_figheight(2)
    plt.subplot(121)
    sns.histplot(data=df, x='TOEFL Score') # looks close to a bell-shaped curve
    plt.subplot(122)
    sns.boxplot(df['TOEFL Score'])
    plt.show() # no outliers in the boxplot
```



```
In [12]: f = plt.figure()
    f.set_figwidth(8)
    f.set_figheight(2)
    plt.subplot(121)
    sns.histplot(df["University Rating"]) # looks like bell-shaped curve
    plt.subplot(122)
    sns.boxplot(data=df, x='University Rating') # no outliers
```

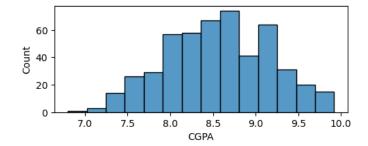
Out[12]: <AxesSubplot: xlabel='University Rating'>

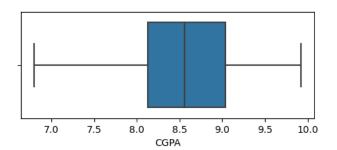




```
In [13]: f = plt.figure()
    f.set_figwidth(12)
    f.set_figheight(2)
    plt.subplot(121)
    sns.histplot(df['CGPA']) #looks like a normal distribution
    plt.subplot(122)
    sns.boxplot(data=df, x='CGPA') # no outliers
```

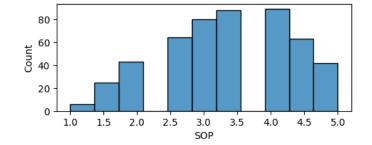
Out[13]: <AxesSubplot: xlabel='CGPA'>

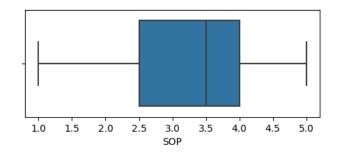




```
In [14]: f = plt.figure()
    f.set_figwidth(12)
    f.set_figheight(2)
    plt.subplot(121)
    sns.histplot(df['SOP']) #looks like a left skewed distribution
    plt.subplot(122)
    sns.boxplot(data=df, x='SOP') # no outliers
```

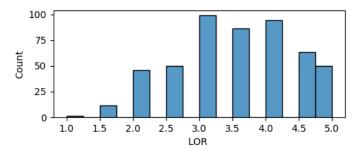
Out[14]: <AxesSubplot: xlabel='SOP'>

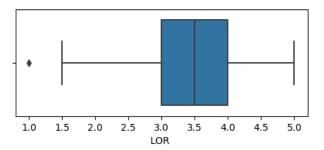




```
In [15]: f = plt.figure()
f.set_figwidth(12)
f.set_figheight(2)
plt.subplot(121)
sns.histplot(df['LOR ']) #looks like a left skewed distribution
plt.subplot(122)
sns.boxplot(data=df, x='LOR ') # there are some outliers
```

Out[15]: <AxesSubplot: xlabel='LOR '>



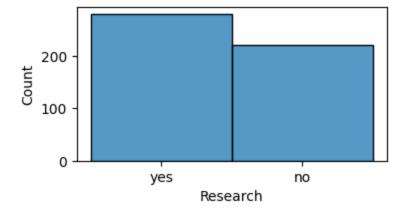


```
In [16]: import scipy
    iqr = scipy.stats.iqr(df['LOR '])
    q1 = np.percentile(df['LOR '],25)
    print(q1)
    df['LOR '][df['LOR '] < (q1 - iqr*1.5)]
    3.0
Out[16]: 347    1.0</pre>
```

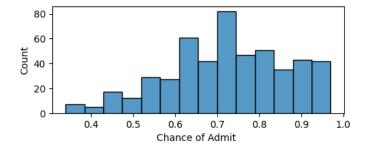
There is only 1 outlier at 1.0 which is not an error, but a valid score so we will keep it.

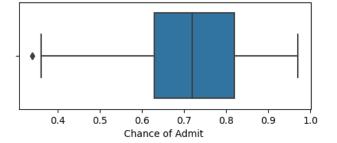
```
In [17]: f = plt.figure()
    f.set_figwidth(4)
    f.set_figheight(2)
    sns.histplot(df['Research']) #there are more students with research experience that those without
```

Out[17]: <AxesSubplot: xlabel='Research', ylabel='Count'>



```
In [18]: f = plt.figure()
    f.set_figwidth(12)
    f.set_figheight(2)
    plt.subplot(121)
    sns.histplot(df['Chance of Admit ']) #looks like a left skewed distribution
    plt.subplot(122)
    sns.boxplot(data=df, x='Chance of Admit ') # there are some outliers
```





Since, these outliers have a valid percentage for chance of admit, we will not remove them.

Now that we have checked the various merits with which students have applied for universities, let's look at their relationship with each other.

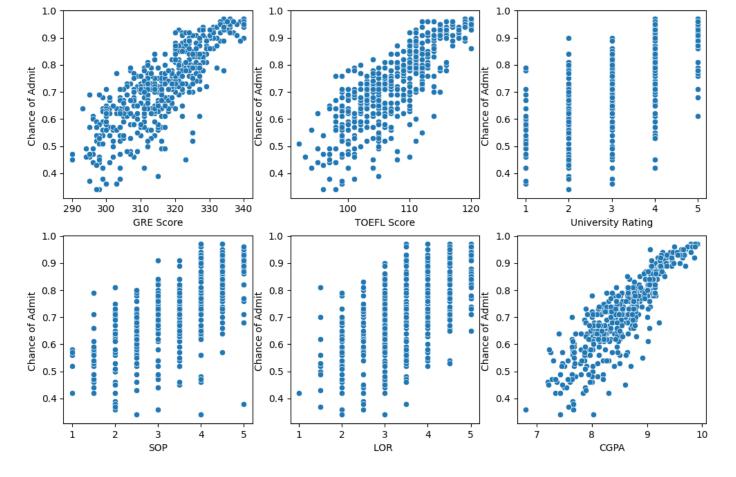
Bivariate analysis

```
In [20]: continuous_cols = df.columns[df.dtypes != 'object'][:-1]
continuous_cols

Out[20]: Index(['GRE Score', 'TOEFL Score', 'University Rating', 'SOP', 'LOR', 'CGPA'], dtype='object')

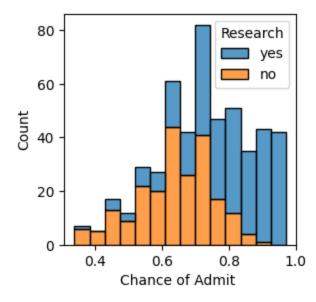
In [21]: f = plt.figure()
f.set_figwidth(12)
f.set_figheight(12)
n = len(continuous_cols)

for i in range(n):
    plt.subplot(n//2,n-(n//2),i+1)
    sns.scatterplot(data=df, x=continuous_cols[i],y='Chance of Admit')
plt.show()
```



All the numerical scores are positively correlated with chance of getting an admit. Most have a linear trend of increase with increase in chance of admit.

```
fig = plt.figure()
    fig.set_figwidth(3)
    fig.set_figheight(3)
    sns.histplot(data=df,x='Chance of Admit ', hue='Research',multiple='stack')
    plt.show()
```



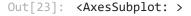
The students with research experience have higher chances of admit. But can we say that for the entire population or just for this sample of data? We would need to get statistical significance for this.

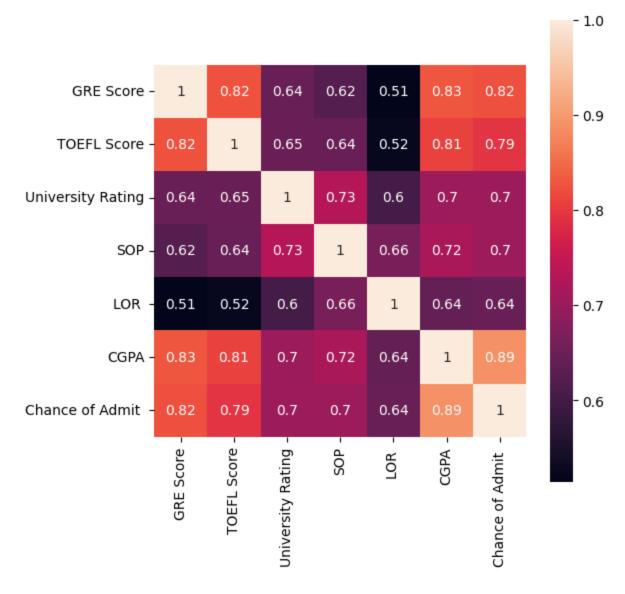
Multivariate analysis

```
In [23]: # Spearman's Rank Correlation Coefficient
plt.figure(figsize=(6,6))
sns.heatmap(df.corr(method='spearman'), square=True,annot=True)
```

C:\Users\Admin\AppData\Local\Temp\ipykernel_15260\3748891021.py:3: FutureWarning: The default value of numeric_only in DataFrame.corr is deprecated. In a future version, it will default to False. Select only valid columns or specify the value of numeric_only to silence this warning.

sns.heatmap(df.corr(method='spearman'), square=True,annot=True)





- 1. The GRE score and undergrad CGPA are highest indicator of chance of admit with correlation of 0.82 and 0.89.
- 2. The TOEFL score, university rating, SOP scores, and LOR scores are also correlated with chance of getting an admit with correlation coefficients at 0.79, 0.7, 0.7 and 0.64 respectively.

Let's find out a way to mathematically model this correlation of admit chances with numerical scores, so that we can do future chance of admit prediction.

Linear Regression

Column Standarization

As the different test scores are in different units, we cannot fairly compare them in terms of importance. We need to scale them to a standard range called standardization.

```
In [24]: # Mean centering and Variance scaling (Standard Scaling)
    from sklearn.preprocessing import StandardScaler
    scaler = StandardScaler()
    std_data = scaler.fit_transform(df[continuous_cols])
    std_data = pd.DataFrame(std_data, columns=continuous_cols)
    std_data.head()
```

Out[24]:		GRE Score	TOEFL Score	University Rating	SOP	LOR	CGPA
	0	1.819238	1.778865	0.775582	1.137360	1.098944	1.776806
	1	0.667148	-0.031601	0.775582	0.632315	1.098944	0.485859
	2	-0.041830	-0.525364	-0.099793	-0.377773	0.017306	-0.954043
	3	0.489904	0.462163	-0.099793	0.127271	-1.064332	0.154847
	4	-0.219074	-0.689952	-0.975168	-1.387862	-0.523513	-0.606480

```
In [25]: Y = np.array(df["Chance of Admit "]).reshape(-1,1)
```

Statsmodel implementation of Linear Regression

```
In [26]: # Statmodels implementation of Linear regression
import statsmodels.api as sm

# Lets define X and Y for Linear regression model fitting
X = std_data

X_sm = sm.add_constant(X) #Statmodels default is without intercept, to add intercept we need to
sm_model = sm.OLS(Y, X_sm).fit() # fitting the model
print(sm_model.summary())
```

OLS Regression Results

		=========	======================================				
Dep. Variable:		у	R-squared:		0.817		
Model:		OLS	Adj. R-squared:		0.815		
Method:	Least		F-statistic:		366	8.8	
Date:	Thu, 19	Thu, 19 Jan 2023 Prob (F-s		istic):	3.22e-1	.78	
Time:		23:50:11	Log-Likelihoo	od:	694.60		
No. Observations:		500	AIC:		-1375.		
Df Residuals:		493	BIC:		-134	6.	
Df Model:		6					
Covariance Type:	n	onrobust					
=======================================	coef		t		_	0.975]	
const	0.7217		265.681		0.716	0.727	
GRE Score	0.0269	0.006	4.897	0.000	0.016	0.038	
TOEFL Score	0.0159	0.005	2.974	0.003	0.005	0.026	
University Rating	0.0077	0.004	1.747	0.081	-0.001	0.016	
SOP	0.0019	0.005	0.417	0.677	-0.007	0.011	
LOR	0.0164	0.004	4.231	0.000	0.009	0.024	
CGPA		0.006					
Omnibus:	=======	119.023	 Durbin-Watson:				
Prob(Omnibus):		0.000	Jarque-Bera (JB):		299.923		
Skew:		-1.187	Prob(JB):		7.46e-66		
Kurtosis:		5.959	Cond. No.		5.	35	

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

The Ordinary Least Squares regression R-squared value is moderately good at 0.817, and adjusted Rsquared at 0.815. The coefficients are as shown below:

```
In [27]: sm_model.params
Out[27]: const
                            0.721740
        GRE Score
                           0.026933
        TOEFL Score
                          0.015946
        University Rating 0.007672
        SOP
                           0.001906
        LOR
                           0.016364
        CGPA
                            0.072051
        dtype: float64
```

Using Scipy package modules for simple Linear regression,

```
Lasso and Ridge regression
In [28]: from sklearn.linear_model import LinearRegression, Lasso, Ridge
         from sklearn.model_selection import train_test_split
         # Create training and test split
         X_train, X_test, y_train, y_test = train_test_split(X, Y, test_size=0.3, random_state=42)
In [29]: from sklearn.metrics import mean_absolute_error, mean_squared_error
In [30]: # Initialize Linear Regression implementation
         model = LinearRegression()
         model.fit(X_train, y_train)
         y_pred = model.predict(X_test)
```

Since the error for test and training data are closeby, this is a good fit model not underfit or overfit.

The coefficients, intercept and R-squared value at 0.817 and adjusted R-squared value of 0.81 is similar to that of statsmodel library model a section above.

Mean absolute error was 0.04 and mean squared error 0.004.

Lasso regression

It performs 'L1 regularization', i.e. it adds a factor of absolute value of sum of coefficients in the optimization objective

Here Lasso regression performed badly as it regularized all the less useful features to 0 value leaving an intercept. And the R-squared value is very low at -0.003. So it means that the Lasso Regression is not

suitable for this dataset.

Ridge regression

It performs 'L2 regularization', i.e. it adds a factor of sum of squares of coefficients in the optimization objective.

```
In [38]: # Initialize Ridge Regression implementation
    ridge = Ridge(alpha=0.1)
        ridge.fit(X_train, y_train)
        y_ridge_pred = ridge.predict(X_test)
        print(ridge.coef_, ridge.intercept_)
        ridge.score(X_test, y_test), ridge.score(X_train, y_train)

        [[0.03106375 0.02014044 0.00474291 0.00136894 0.01457059 0.06967325]] [0.72350203]

Out[38]: (0.817769459660824, 0.8145688752253836)

In [39]: # adjusted R-squared
        1 - (1-ridge.score(X_test, y_test))*(len(y_test)-1)/(len(y_test)-X_test.shape[1]-1)

Out[39]: 0.8101234230032363

In [40]: mean_absolute_error(y_test,y_ridge_pred), mean_squared_error(y_test, y_ridge_pred)

Out[40]: (0.04328161222316256, 0.00379806026053828)

In [41]: mean_absolute_error(y_train,ridge.predict(X_train)), mean_squared_error(y_train, ridge.predict(X_train))
```

The coefficients, intercept of Ridge regression and R-squared value at 0.817 and adj R2 of 0.81 is similar to that of statsmodel library model and simple linear regression model. It is because it regularized all less useful features close to 0. Mean squared error is 0.004 and mean absolute error is 0.04 which are low and good values.

Since the error for test and training data are closeby, this is a good fit model not underfit or overfit.

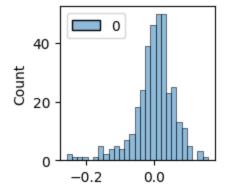
Assumptions of linear regression:

- 1. There is linearity between the independent and dependent variables.
- 2. The residual errors are normally distributed.
- 3. The mean of residuals is close to 0.
- 4. There is homoskedasticity.
- 5. The independent variables are assumed to be independent of each other or have low correlation or are not multi-collinear, i.e. VIF (Variance Inflation Factor) < 10.

```
In [42]: # 1. linearity
sns.pairplot(df, x_vars= continuous_cols, y_vars='Chance of Admit ') # all have linear trend
```

Out[42]: <seaborn.axisgrid.PairGrid at 0x1f87d5065d0>

```
In [54]: # 2. residual errors are normally distributed
    y_pred = model.predict(X_train)
    residuals = y_train - y_pred
    f = plt.figure()
    f.set_figwidth(2)
    f.set_figheight(2)
    sns.histplot(residuals)
    plt.show()
```

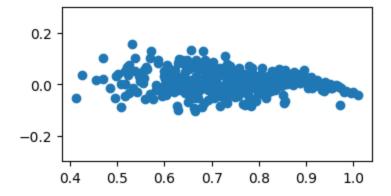


The residuals look similar to normally distributed data but have left-skew. We can remove these outliers to fulfil this assumption.

```
In [44]: iqr = scipy.stats.iqr(residuals)
         q1 = np.percentile(residuals, 25)
         out = residuals < (q1 - iqr*1.5)</pre>
In [45]:
         resid = residuals[~out] # without outliers
In [46]: y_pred_out = y_pred[~out]
In [47]:
         # 3. residual errors are close to 0
         np.mean(resid)
Out[47]: 0.010288532267214564
In [48]: # 4. Homoskedasticity
         f = plt.figure()
         f.set_figwidth(4)
         f.set_figheight(2)
         # print(len(y_pred_out),len(resid))
         plt.scatter(y_pred_out, resid)
```

Out[48]: (-0.3, 0.3)

plt.ylim(-0.3,0.3)



The residuals are not having equal variance, so there is heteroskedasticity.

```
In [49]: # 5. VIF
    from statsmodels.stats.outliers_influence import variance_inflation_factor

In [50]: vif = pd.DataFrame()
    # X_t = X
    vif['Features'] = X.columns
    vif['VIF'] = [variance_inflation_factor(X.values, i) for i in range(X.shape[1])]
    vif['VIF'] = round(vif['VIF'], 2)
    vif = vif.sort_values(by = "VIF", ascending = False)
    vif
```

Out[50]:		Features	VIF
	5	CGPA	4.78
	0	GRE Score	4.10
	1	TOEFL Score	3.90
	3	SOP	2.83
	2	University Rating	2.61
	4	LOR	2.03

Any variable with a VIF of 10 or above is considered strongly correlated with other variables. There are none above 10 so there is no multi-collinearity.

Compare chances of admit for students with and without research experience

Since we are comparing a numerical score for two categories we will be using Mann-Whitney U test which is a non-parametric alternative for two-tailed independent samples t-test.

Ho: their means are equal

Ha: the mean chances of admit for research experienced students is higher than that of students without research experience.

```
import scipy
from scipy.stats import norm, chi2, chi2_contingency, mannwhitneyu, f_oneway, shapiro, levene

a = df['Chance of Admit '][df['Research'] == 'yes']
b = df['Chance of Admit '][df['Research'] == 'no']
```

```
print(len(a),len(b))
print(np.array(a).var(), np.array(b).var()) # variances are unequal
print(shapiro(a)) # test for normality for a , p value is large so a is not normal
print(shapiro(b)) # pvalue is small so b is normal
print(levene(a,b)) # test for equal variances- they are are unequal
mannwhitneyu(a,b,alternative='greater') # we continue to perform t test as the number of data po

280 220
0.015126070153061225 0.012468628099173554
ShapiroResult(statistic=0.9504043459892273, pvalue=3.8728980911173494e-08)
ShapiroResult(statistic=0.9822517037391663, pvalue=0.007273990195244551)
LeveneResult(statistic=2.291641098174848, pvalue=0.130706702224074)

Out[51]: MannwhitneyuResult(statistic=51060.0, pvalue=6.615275731076634e-37)
```

The p-value is small (6.6e-37) so we reject the null hypothesis and say that students with research experience have significantly greater chance of admit than students without.

Business Insights

Mean GRE score is 316.47. Ranges from 290 to 340. Median is close to mean at 317.

Mean TOEFL score is 107.2 and median is 107. Ranges from 92 to 120.

Mean university rating is 3.11, median 3 and ranges from 1 to 5.

Mean SOP score is 3.37, median 3.5, and scores range from 1 to 5.

Mean LOR score is 3.48, median 3.5, and scores range from 1 to 5.

Mean CGPA is 8.58, median is 8.56, and range is from 6.8 to 9.92.

Mean of chances of admit is 0.7217 or 72.17%, median is 72%, and range is from 34% to 97%.

- 1. The GRE score and undergrad CGPA are highest indicator of chance of admit with correlation of 0.82 and 0.89.
- 2. The TOEFL score, university rating, SOP scores, and LOR scores are also correlated with chance of getting an admit with correlation coefficients at 0.79, 0.7, 0.7 and 0.64 respectively.
- 3. The students with research experience have higher chances of admit.

For the categorical column on research, the Mann Whitney U p-value is small (6.6e-37) so we reject the null hypothesis and say that students with research experience have significantly greater chance of admit than students without.

For the numerical test scores, the Ordinary Least Squares regression R-squared value is moderately good at 0.817, and asjusted R-squared at 0.815. The coefficients are as shown below:

Out[52]: const 0.721740 GRE Score 0.026933 TOEFL Score 0.015946 University Rating 0.007672 SOP 0.001906 LOR 0.016364 CGPA 0.072051

dtype: float64

Here Lasso regression performed badly as it regularized all the less useful features to 0 value leaving an intercept. And the R-squared value is very low at -0.003. So it means that the Lasso Regression is not suitable for this dataset.

The coefficients, intercept of Ridge regression and R-squared value at 0.817 and adj R2 of 0.81 is similar to that of statsmodel library model and simple linear regression model. It is because it regularized all less useful features close to 0. Mean squared error is 0.004 and mean absolute error is 0.04 which are low and good values.

Since the error for test and training data are closeby, this is a good fit model not underfit or overfit.

The residuals are not having equal variance, so there is heteroskedasticity. We would need to use weighted regression to improve performance.

Any variable with a VIF of 10 or above is considered strongly correlated with other variables. There are none above 10 so there is no multi-collinearity.

Recommendations

The CGPA and GRE scores have higher effect on chance of admit than other scores. So students should focus more on their undergrad CGPA and GRE test performance.

Next come the TOEFL test scores having high significance and LOR scores, so students with good TOEFL and LOR scores have high chance of admit.

University rating and SOP scores are not as important as other scores, nevertheless they have an impact on admit chances. So Jamboree can accordingly advise students from lower university ratings too.

There was no data present about the students' projects scores or the quality of their resume as that also is significant in showing universities about a student's practical knowledge and skills.

There was no data on any prior work experience if some students worked for a few years after undergrad. Work experience can also help us predict chances of admit and improve model performance.