ZGOUBI USERS' GUIDE

ZGOUBI ON WEB:

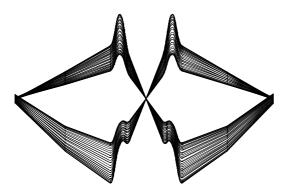
http://sourceforge.net/projects/zgoubi/

François Méot

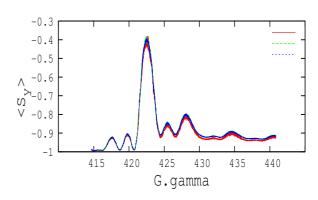
Brookhaven National Laboratory Collider-Accelerator Department Upton, NY, 11973

June 25, 2015

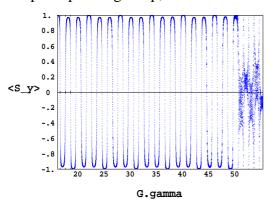
ATLAS & CMS IRs, LHC



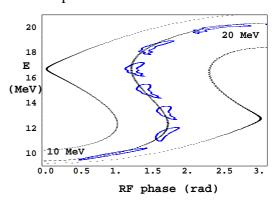
Snake Resonance Crossing in RHIC



Spin flip during ramp, AGS with snakes



Serpentine acceleration in EMMA



Cover figures:

upper left: collision optics at ATLAS and CMS [62],

upper right : evolution of the polarization upon crossing of the 393+ Q_y spin resonance in RHIC [14],

lower left: spin-flipping over an acceleration cycle in the AGS, in presence of the helical snakes [13],

lower right: serpentine acceleration in the prototype linear FFAG EMMA [46, 48].

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PART A Description of software contents

Glossary of Keywords, Part A

Available procedures. Where to find it in Part A

AGSMM	AGS main magnet	85
AGSQUAD	AGS quadrupole	86
AIMANT	Generation of dipole mid-plane 2-D map, polar frame	87
AUTOREF	Transport beam into a new reference frame	92
BEAMBEAM	Beam-beam lens	
BEND	Bending magnet, Cartesian frame	94
BINARY	BINARY/FORMATTED data converter	
BREVOL	1-D uniform mesh magnetic field map	95
CARTEMES	2-D Cartesian uniform mesh magnetic field map	96
CAVITE	Accelerating cavity	
CHAMBR	Long transverse aperture limitation	101
CHANGREF	Transformation to a new reference frame	102
CIBLE	Generate a secondary beam following target interaction	104
COLLIMA	Collimator	
DECAPOLE	Decapole magnet	106
DIPOLE	Dipole magnet, polar frame	107
DIPOLE-M	Generation of dipole mid-plane 2-D map, polar frame	109
DIPOLES	Dipole magnet N-tuple, polar frame	111
DODECAPO	Dodecapole magnet	115
DRIFT	Field free drift space	116
EBMULT	Electro-magnetic multipole	117
EL2TUB	Two-tube electrostatic lens	118
ELMIR	Electrostatic N-electrode mirror/lens, straight slits	119
ELMIRC	Electrostatic N-electrode mirror/lens, circular slits	120
ELMULT	Electric multipole	
ELREVOL	1-D uniform mesh electric field map	123
EMMA	2-D Cartesian or cylindrical mesh field map for EMMA FFAG	124
END	End of input data list	56
ERRORS	Injecting errors	57
ESL	Field free drift space	
FAISCEAU	Print particle coordinates	154
FAISCNL	Store particle coordinates in file FNAME	
FAISTORE	Store coordinates every <i>IP</i> other pass at labeled elements	154
FFAG	FFAG magnet, N-tuple	
FFAG-SPI	Spiral FFAG magnet, N-tuple	
FIN	End of input data list	
FIT	Fitting procedure	
FOCALE	Particle coordinates and horizontal beam size at distance XL	
FOCALEZ	Particle coordinates and vertical beam size at distance XL	
GASCAT	Gas scattering	
GETFITVAL	Get values of variables as saved from former FIT[2] run	
HISTO	1-D histogram	
IMAGE	Localization and size of horizontal waist	
IMAGES	Localization and size of horizontal waists	
IMAGESZ	Localization and size of vertical waists	
IMAGEZ	Localization and size of vertical waist	
MAP2D	2-D Cartesian uniform mesh field map - arbitrary magnetic field	
MAP2D-E	2-D Cartesian uniform mesh field map - arbitrary electric field	130

MADIZED	M. 1	101
MARKER	Marker	
MATRIX	Calculation of transfer coefficients, periodic parameters	
MCDESINT	Monte-Carlo simulation of in-flight decay	
MCOBJET	Monte-Carlo generation of a 6-D object	
MULTIPOL	Magnetic multipole	
OBJET	Generation of an object	
OBJETA	Object from Monte-Carlo simulation of decay reaction	
OCTUPOLE	Octupole magnet	
OPTICS	Write out optical functions	
OPTIONS	Global options	
ORDRE	Taylor expansions order	
PARTICUL	Particle characteristics	
PICKUPS	Bunch centroid path; orbit	
PLOTDATA	Intermediate output for the PLOTDATA graphic software	
POISSON	Read magnetic field data from <i>POISSON</i> output	
POLARMES	2-D polar mesh magnetic field map	
PS170	Simulation of a round shape dipole magnet	
QUADISEX	Sharp edge magnetic multipoles	
QUADRUPO	Quadrupole magnet	
REBELOTE	'Do it again'	
RESET	Reset counters and flags	
SCALING	Power supplies and R.F. function generator	
SEPARA	Wien Filter - analytical simulation	
SEXQUAD	Sharp edge magnetic multipole	
SEXTUPOL	Sextupole magnet	
SOLENOID	Solenoid	
SPINR	Spin rotation	
SPNPRNL	Store spin coordinates into file FNAME	
SPNPRT	Print spin coordinates	
SPNSTORE	Store spin coordinates every <i>IP</i> other pass at labeled elements	164
SPNTRK	Spin tracking	
SRLOSS	Synchrotron radiation energy loss	
SRPRNT	Print SR loss statistics	
SYNRAD	Synchrotron radiation spectral-angular densities	
SYSTEM	System call	
TARGET	Generate a secondary beam following target interaction	
TOSCA	2-D and 3-D Cartesian or cylindrical mesh field map	
TRANSMAT	Matrix transfer	
TRAROT	Translation-Rotation of the reference frame	. 147
TWISS	Calculation of periodic optical parameters	
UNDULATOR	Undulator magnet	
UNIPOT	Unipotential cylindrical electrostatic lens	
VENUS	Simulation of a rectangular shape dipole magnet	150
WIENFILT	Wien filter	
YMY	Reverse signs of Y and Z reference axes	152

Optical elements versus keywords

What can be simulated What keyword(s) can be used for that

This glossary gives a list of keywords suitable for the simulation of common optical elements. These are classified in three categories: magnetic, electric and combined electro-magnetic elements.

Field map procedures are also listed; they provide a means for ray-tracing through measured or simulated electric and/or magnetic fields.

MAGNETIC ELEMENTS

AGS main magnet AGSMM

Cyclotron magnet or sector DIPOLE[S], DIPOLE-M, FFAG, FFAG-SPI

Decapole DECAPOLE, MULTIPOL

Dipole[s], spectrometer dipole AIMANT, BEND, DIPOLE[S][-M], MULTIPOL, QUADISEX

Dodecapole DODECAPO, MULTIPOL

FFAG magnet DIPOLES, FFAG, FFAG-SPI, MULTIPOL

Helical dipole HELIX

Multipole MULTIPOL, QUADISEX, SEXQUAD

Octupole OCTUPOLE, MULTIPOL, QUADISEX, SEXQUAD Quadrupole QUADRUPO, MULTIPOL, SEXQUAD, AGSQUAD Sextupole SEXTUPOL, MULTIPOL, QUADISEX, SEXQUAD

Skew multipoles MULTIPOL Solenoid SOLENOID

Spectrometer dipole DIPOLE, DIPOLE-M, DIPOLES

Undulator UNDULATOR

Using field maps

1-D, cylindrical symmetry BREVOL

2-D, mid-plane symmetry CARTEMES, POISSON, TOSCA

2-D, no symmetry
2-D, polar mesh, mid-plane symmetry
3-D, no symmetry
TOSCA
EMMA FFAG quadrupole doublet
linear composition of field maps
TOSCA

ELECTRIC ELEMENTS

2-tube (bipotential) lens EL2TUB 3-tube (unipotential) lens **UNIPOT** Decapole **ELMULT** Dipole **ELMULT** Dodecapole **ELMULT** Multipole **ELMULT** N-electrode mirror/lens, straight slits **ELMIR** N-electrode mirror/lens, circular slits **ELMIRC** Octupole **ELMULT** Quadrupole **ELMULT** R.F. (kick) cavity

Sextupole

Skew multipoles

CAVITE

ELMULT

ELMULT

Using field maps

1-D, cylindrical symmetry ELREVOL 2-D, no symmetry MAP2D-E

ELECTRO-MAGNETIC ELEMENTS

Decapole **EBMULT** Dipole **EBMULT** Dodecapole **EBMULT** Multipole **EBMULT** Octupole **EBMULT** Quadrupole **EBMULT** Sextupole **EBMULT** Skew multipoles **EBMULT**

Wien filter SEPARA, WIENFILT

PREFACE TO THE BNL EDITION, 2012

The previous release of the Zgoubi Users' Guide as a Lab. report dates from 1997, making the present one the latest in a series of five [1]-[4].

zgoubi has undergone substantial developments since the 4th edition of the Users' Guide, in the frame of a number of projects and of beam dynamics studies, as the Neutrino Factory, lepton and hadron colliders, spin dynamics investigations at SuperB, RHIC, etc. As well the list of optical elements has grown, and so did the "Glossary of Keywords" list, pp. 7 and 177, including new simulation and computing procedures, which range from constraint-matching to overlapping magnetic fields capabilities to spin manipulations and other synchrotron radiation damping recipes.

The code has been installed on SourceForge with the collaboration of J. S. Berg, in Sept. 2007, there it is fully and freely available [5]. The SourceForge package evolves and is maintained at the pace of on-going projects and design studies. It includes the source files, the post-processor program **zpop**, as well as many examples with their input data files ("zgoubi.dat") and output result files ("zgoubi.res").

A series of auxiliary computing tools have been developed in addition, aimed at making the designer's life easier, as, search for closed orbits in periodic machines, computation of optical functions and parameters, tune scans, dynamic aperture scans, spin dynamics data treatment, graphic scripts, etc., and including dedicated ones regarding, *e.g.*, FFAG and cyclotron design, AGS and RHIC studies, synchrotron radiation losses and their effects. In addition "python" interfaces are being developed by several users, possibly made available on web by their authors.

The Users' Guide is intended to describe the contents of the most recent version of **zgoubi**. The code and its Guide are both far from being "finished products".

J. S. Berg and N. Tsoupas, BNL, have reviewed the final proof of the present document.

INTRODUCTION TO THE 4th EDITION, 1997

The initial version of **zgoubi**, dedicated to ray-tracing in magnetic fields, was developed by D. Garreta and J.C. Faivre at CEN-Saclay in the early 1970s. It was perfected for the purpose of studying the four spectrometers SPES I, II, III, IV at the Laboratoire National SATURNE (CEA-Saclay, France), and SPEG at GANIL (Caen, France). It is being used since long in several national and foreign laboratories.

The first manual was in French [1]. Accounting for many developments and improvements, and in order to facilitate access to the program an English version of the manual was written at TRIUMF with the assistance of J. Doornbos. P. Stewart prepared the manuscript for publication [2]

An updating of the latter was necessary for accompanying the third version of the code which included developments regarding spin tracking and ray-tracing in combined electric and magnetic fields; this was done with the help of D. Bunel (SATURNE Laboratory, Saclay) for the preparation of the document and lead to the third release [3].

In the mid-1990s, the computation of synchrotron radiation electromagnetic impulse and spectra was introduced for the purpose of studying interference effects at the LEP synchrotron radiation based diagnostic mini-wiggler. In the mean time, several new optical elements were added, such as electro-magnetic and other electrostatic lenses. Used since several years for special studies in periodic machines (*e.g.*, SATURNE at Saclay, COSY at Julich, LEP and LHC at CERN, Neutrino Factory rings), **zgoubi** has also undergone extensive developments regarding storage ring related features.

These developments of **zgoubi** have strongly benefited of the environment of the Groupe Théorie, Laboratoire National SATURNE, CEA/DSM-Saclay, in the years 1985-1995.

The graphic interface to **zgoubi** (addressed in Part D) has also undergone concomitant extensive developments, which make it a performing tool for the post-processing of **zgoubi** outputs.

The Users' Guide is intended to describe the contents of the most recent version of **zgoubi**, which is far from being a "finished product".

INTRODUCTION

The computer code **zgoubi** calculates trajectories of charged particles in magnetic and electric fields. At the origin specially adapted to the definition and adjustment of beam lines and magnetic spectrometers, it has so evolved that it allows the study of systems including complex sequences of optical elements such as dipoles, quadrupoles, arbitrary multipoles, FFAG magnets and other magnetic or electric devices, and is able as well to handle periodic structures. Compared to other codes, it presents several peculiarities, as follows - a non-exhaustive list:

- a numerical method for integrating the Lorentz equation, based on Taylor series, which optimizes computing time and provides high accuracy and strong symplecticity,
- spin tracking, using the same numerical method as for the Lorentz equation,
- account of stochastic photon emission, and its effects on particle dynamics,
- calculation of the synchrotron radiation electric field and spectra in arbitrary magnetic fields, from the ray-tracing outcomes,
- the possibility of using a mesh, which allows ray-tracing from simulated or measured (1-D, 2-D or 3-D) electric and magnetic field maps,
- a number Monte Carlo procedures : unlimited number of trajectories, in-flight decay, stochastic radiation, etc.,
- built-in fitting procedures allowing arbitrary variables and a large variety of constraints, easily expandable,
- multi-turn tracking in circular accelerators including features proper to machine parameter calculation and survey,
- simulation of time-varying power supplies,
- simulation of arbitrary radio-frequency programs.

The initial version of **zgoubi** was dedicated to ray-tracing in magnetic elements, beam lines, spectrometers. It was perfected for the purpose of studying, and operating, the four spectrometers SPES I, II, III, IV at the Laboratoire National SATURNE (CEA-Saclay, France), and, later, SPEG at GANIL (Caen, France).

Developments regarding spin tracking and ray-tracing in combined electric and magnetic fields were implemented, in the late 1980s and early 1990s respectively.

In the mid-1990s, the computation of synchrotron radiation electromagnetic impulse and spectra was introduced, for the purpose of synchrotron radiation diagnostic R&D at LEP, and further applied to the design of the SR diagnostics installations at LHC in the early 2000s. In the mean time, several new optical elements were added, such as electro-magnetic and other electrostatic lenses. Used since several years for special studies in periodic machines (*e.g.*, SATURNE at Saclay, COSY at Julich, LEP and LHC at CERN), **zgoubi** has also undergone extensive developments regarding storage ring related features.

Many developments have been accomplished since the early 2000s in the frame of a number of project design and beam dynamics studies, as the neutrino factory, lepton and hadron colliders, spin studies at AGS and RHIC, etc. As a consequence the list of optical elements and the compendium of numerical methods, so-called "Glossary of Keywords" list, pp. 7 and 177, has stretched with new simulation and computing procedures, ranging from fitting (FIT2 procedure; additional constraints) to overlapping magnetic field capabilities (DIPOLES, FFAG), spin manipulation (SPINR), optical elements (BEAMBEAM), radiation damping tools (SRLOSS) and many others (FAISTORE, MAP2D-E, OPTICS, PICKUPS, TWISS, etc.).

The graphic interface to **zgoubi** (**zpop**, Part D) has undergone extensive developments, making it a convenient companion tool to the use of **zgoubi**.

1 NUMERICAL CALCULATION OF MOTION AND FIELDS

1.1 zgoubi Frame

The reference frame of **zgoubi** is presented in Fig. 1. Its origin is in the median plane on a reference curve which generally (but not always) coincides with the optical axis of optical elements.

1.2 Integration of the Lorentz Equation

The Lorentz equation, which governs the motion of a particle of charge q, relativistic mass m and velocity \vec{v} in electric and magnetic fields \vec{e} and \vec{b} , is written

$$\frac{d(m\vec{v})}{dt} = q\left(\vec{e} + \vec{v} \times \vec{b}\right) \tag{1.2.1}$$

Noting $()' = \frac{d()}{ds}$ and taking

$$\vec{u} = \frac{\vec{v}}{v}, \quad ds = v dt, \quad \vec{u}' = \frac{d\vec{u}}{ds}, \quad m\vec{v} = mv\vec{u} = q B\rho \vec{u}$$
 (1.2.2)

where $B\rho$ is the rigidity of the particle, this equation can be rewritten

$$(B\rho)'\vec{u} + B\rho\vec{u}' = \frac{\vec{e}}{v} + \vec{u} \times \vec{b}$$
 (1.2.3)

From position $\vec{R}(M_0)$ and unit velocity $\vec{u}(M_0)$ at point M_0 , position $\vec{R}(M_1)$ and unit velocity $\vec{u}(M_1)$ at point M_1 following a displacement Δs , are obtained from truncated Taylor expansions (Fig. 2)

$$\vec{R}(M_1) \approx \vec{R}(M_0) + \vec{u}(M_0) \, \Delta s + \vec{u}'(M_0) \, \frac{\Delta s^2}{2!} + \dots + \vec{u}'''''(M_0) \, \frac{\Delta s^6}{6!}$$

$$\vec{u}(M_1) \approx \vec{u}(M_0) + \vec{u}'(M_0) \, \Delta s + \vec{u}''(M_0) \, \frac{\Delta s^2}{2!} + \dots + \vec{u}'''''(M_0) \, \frac{\Delta s^5}{5!}$$
(1.2.4)

The rigidity at M_1 is obtained in the same way from

$$(B\rho)(M_1) \approx (B\rho)(M_0) + (B\rho)'(M_0)\Delta s + \dots + (B\rho)'''''(M_0)\frac{\Delta s^5}{5!}$$
 (1.2.5)

The equation of time of flight is written in a similar manner

$$T(M_1) \approx T(M_0) + T'(M_0) \Delta s + T''(M_0) \frac{\Delta s^2}{2} + \dots + T'''''(M_0) \frac{\Delta s^5}{5!}$$
 (1.2.6)

The derivatives $\vec{u}^{(n)} = \frac{d^n \vec{u}}{ds^n}$ and $(B\rho)^{(n)} = \frac{d^n (B\rho)}{ds^n}$ involved in these expressions are calculated as described in the next sections. For the sake of computing speed, three distinct software procedures are involved, depending on whether \vec{e} or \vec{b} is zero, or \vec{e} and \vec{b} are both non-zero.



Figure 1: Reference frame and coordinates (Y, T, Z, P) in **zgoubi**.

OX: in the direction of motion,

OY: normal to OX,

OZ: orthogonal to the (X, Y) plane,

 \vec{W} : projection of the velocity, \vec{v} , in the (X,Y) plane,

T =angle between \vec{W} and the X-axis,

P =angle between \vec{W} and \vec{v} .



Figure 2: Position and velocity of a particle in the reference frame.

1.2.1 Integration in Magnetic Fields

Considering $\vec{e}=0$ and given $\vec{B}=\frac{\vec{b}}{B\rho}$, eq. (1.2.3) reduces to

$$\vec{u}' = \vec{u} \times \vec{B} \tag{1.2.7}$$

The successive derivatives $\vec{u}^{(n)} = \frac{d^n \vec{u}}{ds^n}$ of \vec{u} needed in the Taylor expansions (eqs. 1.2.4) are calculated by differentiating $\vec{u}' = \vec{u} \times \vec{B}$

$$\vec{u}'' = \vec{u}' \times \vec{B} + \vec{u} \times \vec{B}'$$

$$\vec{u}''' = \vec{u}'' \times \vec{B} + 2\vec{u}' \times \vec{B}' + \vec{u} \times \vec{B}''$$

$$\vec{u}'''' = \vec{u}''' \times \vec{B} + 3\vec{u}'' \times \vec{B}' + 3\vec{u}' \times \vec{B}'' + \vec{u} \times \vec{B}'''$$

$$\vec{u}''''' = \vec{u}'''' \times \vec{B} + 4\vec{u}''' \times \vec{B}' + 6\vec{u}'' \times \vec{B}'' + 4\vec{u}' \times \vec{B}''' + \vec{u} \times \vec{B}''''$$
(1.2.8)

where $\vec{B}^{(n)} = \frac{d^n \vec{B}}{ds^n}$. From

$$d\vec{B} = \frac{\partial \vec{B}}{\partial X} dX + \frac{\partial \vec{B}}{\partial Y} dY + \frac{\partial \vec{B}}{\partial Z} dZ = \sum_{i=1,3} \frac{\partial \vec{B}}{\partial X_i} dX_i$$
 (1.2.9)

and by successive differentiation, we get

$$\vec{B}' = \sum_{i} \frac{\partial \vec{B}}{\partial X_{i}} u_{i}$$

$$\vec{B}'' = \sum_{ij} \frac{\partial^{2} \vec{B}}{\partial X_{i} \partial X_{j}} u_{i} u_{j} + \sum_{i} \frac{\partial \vec{B}}{\partial X_{i}} u'_{i}$$

$$\vec{B}''' = \sum_{ijk} \frac{\partial^{3} \vec{B}}{\partial X_{i} \partial X_{j} \partial X_{k}} u_{i} u_{j} u_{k} + 3 \sum_{ij} \frac{\partial^{2} \vec{B}}{\partial X_{i} \partial X_{j}} u'_{i} u_{j} + \sum_{i} \frac{\partial \vec{B}}{\partial X_{i}} u''_{i}$$

$$\vec{B}'''' = \sum_{ijkl} \frac{\partial^{4} \vec{B}}{\partial X_{i} \partial X_{j} \partial X_{k} \partial X_{l}} u_{i} u_{j} u_{k} u_{l} + 6 \sum_{ijk} \frac{\partial^{3} \vec{B}}{\partial X_{i} \partial X_{j} \partial X_{k}} u'_{i} u_{j} u_{k}$$

$$+ 4 \sum_{ij} \frac{\partial^{2} \vec{B}}{\partial X_{i} \partial X_{j}} u''_{i} u_{j} + 3 \sum_{ij} \frac{\partial^{2} \vec{B}}{\partial X_{i} \partial X_{j}} u'_{i} u'_{j} + \sum_{i} \frac{\partial \vec{B}}{\partial X_{i}} u'''_{i}$$

$$(1.2.10)$$

From the knowledge of $\vec{u}(M_0)$ and $\vec{B}(M_0)$ at point M_0 of the trajectory, we calculate alternately the derivatives of $\vec{u}(M_0)$ and $\vec{B}(M_0)$, by means of eqs. (1.2.8) and (1.2.10), and inject these into eq. (1.2.4) so yielding $\vec{R}(M_1)$ and $\vec{u}(M_1)$.

1.2.2 Integration in Electric Fields [6]

Admitting that $\vec{b} = 0$, eq. (1.2.3) reduces to

$$(B\rho)'\vec{u} + B\rho\vec{u}' = \frac{\vec{e}}{v} \tag{1.2.11}$$

which, by successive differentiations, gives the recursive relations

$$(B\rho)'\vec{u} + B\rho\vec{u}' = \frac{\vec{e}}{v}$$

$$(B\rho)''\vec{u} + 2(B\rho)'\vec{u}' + B\rho\vec{u}'' = \left(\frac{1}{v}\right)'\vec{e} + \frac{\vec{e}'}{v}$$

$$(B\rho)'''\vec{u} + 3(B\rho)''\vec{u}' + 3(B\rho)'\vec{u}'' + B\rho\vec{u}''' = \left(\frac{1}{v}\right)''\vec{e} + 2\left(\frac{1}{v}\right)'\vec{e}'' + \left(\frac{1}{v}\right)\vec{e}''$$

$$(B\rho)''''\vec{u} + 4(B\rho)'''\vec{u}'' + 6(B\rho)''\vec{u}'' + 4(B\rho)'\vec{u}''' + B\rho\vec{u}'''' = \left(\frac{1}{v}\right)'''\vec{e} + 3\left(\frac{1}{v}\right)''\vec{e}' + 3\left(\frac{1}{v}\right)''\vec{e}'' + \frac{1}{v}\vec{e}'''$$

$$(B\rho)'''''\vec{u} + 5(B\rho)''''\vec{u}' + etc.$$
(1.2.12)

that provide the derivatives $\frac{d^n \vec{u}}{ds^n}$ needed in the Taylor expansions (eq. 1.2.4)

$$\vec{u}' = \left(\frac{1}{v}\right) \vec{E} - \frac{(B\rho)'}{B\rho} \vec{u}$$

$$\vec{u}'' = \left(\frac{1}{v}\right)' \vec{E} + \left(\frac{1}{v}\right) \vec{E}' \mid_{B\rho} - 2\frac{(B\rho)'}{B\rho} \vec{u}' - \frac{(B\rho)''}{B\rho} \vec{u}$$

$$\vec{u}''' = \left(\frac{1}{v}\right)'' \vec{E} + 2\left(\frac{1}{v}\right)' \vec{E}' \mid_{B\rho} + \frac{1}{v} \vec{E}'' \mid_{B\rho} - 3\frac{(B\rho)'}{B\rho} \vec{u}'' - 3\frac{(B\rho)''}{B\rho} \vec{u}' - \frac{(B\rho)'''}{B\rho} \vec{u}$$

$$\vec{u}'''' = \left(\frac{1}{v}\right)''' \vec{E} + 3\left(\frac{1}{v}\right)'' \vec{E}' \mid_{B\rho} + 3\left(\frac{1}{v}\right)' \vec{E}'' \mid_{B\rho} + \left(\frac{1}{v}\right) \vec{E}''' \mid_{B\rho}$$

$$-4\frac{(B\rho)'}{B\rho} \vec{u}''' - 6\frac{(B\rho)''}{B\rho} \vec{u}'' - 4\frac{(B\rho)'''}{B\rho} \vec{u}' - \frac{(B\rho)''''}{B\rho} \vec{u}'$$

$$\vec{u}''''' = \left(\frac{1}{v}\right)'''' \vec{E} + 4\left(\frac{1}{v}\right)''' \vec{E}' \mid_{B\rho} + 6\left(\frac{1}{v}\right)'' \vec{E}'' \mid_{B\rho} + 4\left(\frac{1}{v}\right)' \vec{E}''' \mid_{B\rho} + \left(\frac{1}{v}\right) \vec{E}''' \mid_{B\rho}$$

$$-5\frac{(B\rho)'}{B\rho} \vec{u}'''' - 10\frac{(B\rho)''}{B\rho} \vec{u}''' - 10\frac{(B\rho)''''}{B\rho} \vec{u}'' - 5\frac{(B\rho)'''''}{B\rho} \vec{u}' - \frac{(B\rho)'''''}{B\rho} \vec{u}'$$

where $\vec{E} = \frac{\vec{e}}{B\rho}$, and $()^{(n)}|_{B\rho}$ denotes differentiation at constant $B\rho$: $\vec{E}^{(n)}|_{B\rho} = \frac{1}{B\rho} \frac{d^n \vec{e}}{ds^n}$. These derivatives of the electric field are obtained from the total derivative

$$d\vec{E} = \frac{\partial \vec{E}}{\partial X} dX + \frac{\partial \vec{E}}{\partial Y} dY + \frac{\partial \vec{E}}{\partial Z} dZ$$
 (1.2.14)

$$\vec{E}' = \sum_{i} \frac{\partial \vec{E}}{\partial X_{i}} u_{i}$$

$$\vec{E}'' = \sum_{ij} \frac{\partial^{2} \vec{E}}{\partial X_{i} \partial X_{j}} u_{i} u_{j} + \sum_{i} \frac{\partial \vec{E}}{\partial X_{i}} u'_{i}$$

$$\vec{E}''' = \sum_{ijk} \frac{\partial^{3} \vec{E}}{\partial X_{i} \partial X_{j} \partial X_{k}} u_{i} u_{j} u_{k} + 3 \sum_{ij} \frac{\partial^{2} \vec{E}}{\partial X_{i} \partial X_{j}} u'_{i} u_{j} + \sum_{i} \frac{\partial \vec{E}}{\partial X_{i}} u''_{i}$$

$$(1.2.15)$$

etc. as in eq. 1.2.10. The eqs. (1.2.13), as well as the calculation of the rigidity, eq. (1.2.5), involve derivatives $(B\rho)^{(n)} = \frac{d^n(B\rho)}{ds^n}$, which are obtained in the following way. Considering that

$$\frac{dp^2}{dt} = \frac{d\vec{p}^2}{dt} \quad i.e., \quad \frac{dp}{dt}p = \frac{d\vec{p}}{dt}\vec{p}$$
 (1.2.16)

with $\frac{d\vec{p}}{dt} = q (\vec{e} + \vec{v} \times \vec{b})$ (eq. 1.2.1), we obtain

$$\frac{dp}{dt}p = q(\vec{e} + v \times \vec{b}) \cdot \vec{p} = q\vec{e} \cdot \vec{p}$$
(1.2.17)

since $(\vec{v} \times \vec{b}) \cdot \vec{p} = 0$. Normalizing as previously with $\vec{p} = p\vec{u} = qB\rho\vec{u}$ and ds = vdt, and by successive differentiations, eq. (1.2.17) leads to the $(B\rho)^{(n)}$

$$(B\rho)'' = \frac{1}{v} (\vec{e} \cdot \vec{u})$$

$$(B\rho)'' = \left(\frac{1}{v}\right)' (\vec{e} \cdot \vec{u}) + \frac{1}{v} (\vec{e} \cdot \vec{u})'$$

$$(B\rho)''' = \left(\frac{1}{v}\right)'' (\vec{e} \cdot \vec{u}) + 2\left(\frac{1}{v}\right)' (\vec{e} \cdot \vec{u})' + \frac{1}{v} (\vec{e} \cdot \vec{u})''$$

$$(B\rho)'''' = \left(\frac{1}{v}\right)''' (\vec{e} \cdot \vec{u}) + 3\left(\frac{1}{v}\right)'' (\vec{e} \cdot \vec{u})' + 3\left(\frac{1}{v}\right)' (\vec{e} \cdot \vec{u})'' + \frac{1}{v} (\vec{e} \cdot \vec{u})'''$$

$$(B\rho)''''' = etc.$$
(1.2.18)

The derivatives $(\vec{e} \cdot \vec{u})^{(n)} = \frac{d^n(\vec{e} \cdot \vec{u})}{ds^n}$ are obtained by recursive differentiation

$$(\vec{e} \cdot \vec{u})' = \vec{e}' \cdot \vec{u} + \vec{e} \cdot \vec{u}'$$

$$(\vec{e} \cdot \vec{u})'' = \vec{e}'' \cdot \vec{u} + 2 \vec{e}' \cdot \vec{u}' + \vec{e} \cdot \vec{u}''$$
etc. (1.2.19)

Note that they can be related to the derivatives of the kinetic energy W by $dW = \frac{d\vec{p}}{dt} \cdot \vec{v} \, dt = q\vec{e} \cdot \vec{v} \, dt$ which leads to

$$\frac{d^{n+1}W}{ds^{n+1}} = q \frac{d^n(\vec{e} \cdot \vec{u})}{ds^n}$$
 (1.2.20)

Finally, the derivatives $\left(\frac{1}{v}\right)^{(n)} = \frac{d^n\left(\frac{1}{v}\right)}{ds^n}$ involved in eqs. (1.2.13,1.2.18) are obtained from

$$p = \frac{v}{c} \frac{W + m_0 c^2}{c}$$

 (m_0) is the rest mass) by successive differentiations, that give the recursive relations

$$\left(\frac{1}{v}\right) = \frac{1}{c^2} \frac{W + m_0 c^2}{qB\rho}
\left(\frac{1}{v}\right)' = \frac{1}{c^2} \frac{(\vec{e} \cdot \vec{u})}{B\rho} - \frac{1}{v} \frac{(B\rho)'}{B\rho}
\left(\frac{1}{v}\right)'' = \frac{1}{c^2} \frac{(\vec{e} \cdot \vec{u})'}{B\rho} - 2\left(\frac{1}{v}\right)' \frac{(B\rho)'}{B\rho} - \frac{1}{v} \frac{(B\rho)''}{B\rho}
\left(\frac{1}{v}\right)''' = \frac{1}{c^2} \frac{(\vec{e} \cdot \vec{u})''}{B\rho} - 3\left(\frac{1}{v}\right)'' \frac{(B\rho)'}{B\rho} - 3\left(\frac{1}{v}\right)'' \frac{(B\rho)''}{B\rho} - \frac{1}{v} \frac{(B\rho)'''}{B\rho}
\left(\frac{1}{v}\right)'''' = etc.$$
(1.2.21)

1.2.3 Integration in Combined Electric and Magnetic Fields

When both \vec{e} and \vec{b} are non-zero, the complete eq. (1.2.3) must be considered. Recursive differentiations give the following relations

$$(B\rho)'\vec{u} + B\rho\vec{u}' = \frac{\vec{e}}{v} + \vec{u} \times \vec{b}$$

$$(B\rho)''\vec{u} + 2(B\rho)'\vec{u}' + B\rho\vec{u}'' = \left(\frac{1}{v}\right)'\vec{e} + \left(\frac{1}{v}\right)\vec{e}' + (\vec{u} \times \vec{b})'$$

$$(B\rho)'''\vec{u} + 3(B\rho)''\vec{u}' + 3(B\rho)'\vec{u}'' + B\rho\vec{u}''' = \left(\frac{1}{v}\right)''\vec{e} + 2\left(\frac{1}{v}\right)''\vec{e}' + \left(\frac{1}{v}\right)\vec{e}'' + (\vec{u} \times \vec{b})''$$

$$(B\rho)''''\vec{u} + 4(B\rho)'''\vec{u}'' + 6(B\rho)''\vec{u}''' + 4(B\rho)'\vec{u}''' + B\rho\vec{u}'''' = \left(\frac{1}{v}\right)'''\vec{e}' + 3\left(\frac{1}{v}\right)''\vec{e}'' + \frac{1}{v}\vec{e}''' + (\vec{u} \times \vec{b})'''$$

$$(1.2.22)$$

that provide the derivatives $\frac{d^n \vec{u}}{ds^n}$ needed in the Taylor expansions (1.2.4)

$$\vec{u}' = \left(\frac{1}{v}\right) \vec{E} + (\vec{u} \times \vec{B}) - \frac{(B\rho)'}{B\rho} \vec{u}$$

$$\vec{u}'' = \left(\frac{1}{v}\right)' \vec{E} + \left(\frac{1}{v}\right) \vec{E}' \mid_{B\rho} + (\vec{u} \times \vec{B})' \mid_{B\rho} - 2\frac{(B\rho)'}{B\rho} \vec{u}' - \frac{(B\rho)''}{B\rho} \vec{u}$$

$$\vec{u}''' = \left(\frac{1}{v}\right)'' \vec{E} + 2\left(\frac{1}{v}\right)' \vec{E}' \mid_{B\rho} + \frac{1}{v} \vec{E}'' \mid_{B\rho} + (\vec{u} \times \vec{B})'' \mid_{B\rho} - 3\frac{(B\rho)'}{B\rho} \vec{u}'' - 3\frac{(B\rho)''}{B\rho} \vec{u}' - \frac{(B\rho)'''}{B\rho} \vec{u}$$

$$\vec{u}'''' = \left(\frac{1}{v}\right)''' \vec{E} + 3\left(\frac{1}{v}\right)'' \vec{E}' \mid_{B\rho} + 3\left(\frac{1}{v}\right)' \vec{E}'' \mid_{B\rho} + \left(\frac{1}{v}\right) \vec{E}''' \mid_{B\rho}$$

$$+ (\vec{u} \times \vec{B})''' \mid_{B\rho} - 4\frac{(B\rho)'}{B\rho} \vec{u}''' - 6\frac{(B\rho)''}{B\rho} \vec{u}'' - 4\frac{(B\rho)''''}{B\rho} \vec{u}' - \frac{(B\rho)''''}{B\rho} \vec{u}'$$

$$(1.2.23)$$

where $\vec{E} = \frac{\vec{e}}{B\rho}$, $\vec{B} = \frac{\vec{b}}{B\rho}$, and $^{(n)}$ $|_{B\rho}$ denotes differentiation at constant $B\rho$

$$\vec{E}^{(n)} \mid_{B\rho} = \frac{1}{B\rho} \frac{d^n \vec{e}}{ds^n} \quad \text{and} \quad (\vec{u} \times \vec{B})^{(n)} \mid_{B\rho} = \frac{1}{B\rho} (\vec{u} \times \vec{b})^{(n)}.$$
 (1.2.24)

These derivatives $\vec{E}^{(n)}$ and $\vec{B}^{(n)}$ of the electric and magnetic fields are calculated from the vector fields $\vec{E}(X,Y,Z)$, $\vec{B}(X,Y,Z)$ and their derivatives $\frac{\partial^{i+j+k}\vec{E}}{\partial X^i\partial Y^j\partial Z^k}$ and $\frac{\partial^{i+j+k}\vec{B}}{\partial X^i\partial Y^j\partial Z^k}$, following eqs. (1.2.14, 1.2.15) and eqs. (1.2.9, 1.2.10), respectively.

1.2.4 Calculation of the Time of Flight

The time of flight eq. (1.2.6) involves the derivatives dT/ds = 1/v, $d^2T/ds^2 = d(1/v)/ds$, etc. that are obtained from eq. (1.2.21). In the absence of electric field eq. (1.2.8) however reduces to the simple form

$$T(M_1) = T(M_0) + \Delta s/v \tag{1.2.25}$$

1.3 Calculation of \vec{E} and \vec{B} Fields and their Derivatives

In this section, unless otherwise stated, $\vec{B} = (B_X(X,Y,Z), B_Y(X,Y,Z), B_Z(X,Y,Z))$ stands indifferently for electric field \vec{E} or magnetic field \vec{B} .

 $\vec{B}(X,Y,Z)$ and derivatives are calculated in various ways, depending whether field maps or analytic representations of optical elements are used. The basic means are the following.

1.3.1 1-D (Axial) Analytical Field Models and Extrapolation

This procedure assumes cylindrical symmetry with respect to the X-axis. The longitudinal field component B_X or $E_X(X,r=0)$ $(r=(Y^2+Z^2)^{1/2})$, along that axis is derived by differentiation of an appropriate model of the potential V(X) (e.g., magnetic in SOLENOID, electrostatic in EL2TUB, UNIPOT). The longitudinal and radial field components $B_X(X,r)$, $B_r(X,r)$ and their derivatives off-axis $\frac{\partial^{i+j}B_X}{\partial X^i\partial r^j}$ and $\frac{\partial^{i+j}B_r}{\partial X^i\partial r^j}$ are obtained by Taylor expansions to the second to fifth order in r (depending on the optical element) assuming cylindrical symmetry (eq. (1.3.1)), and then transformed to the (X,Y,Z) Cartesian frame of **zgoubi** in order to provide the derivatives $\frac{\partial^{i+j+k}\vec{B}}{\partial X^i\partial Y^j\partial Z^k}$ needed in eq. (1.2.15).

1.3.2 Extrapolation from 1-D axial field map [7]

A cylindrically symmetric field (e.g., using BREVOL, ELREVOL) can be described by an axial 1-D field map of its longitudinal component $B_X(X,r=0)$ ($r=(Y^2+Z^2)^{1/2}$), while the radial component on axis $B_r(X,r=0)$ is assumed to be zero. $B_X(X,r=0)$ is obtained at any point along the X-axis by a polynomial interpolation from the map mesh (see section 1.4.1). Then the field components $B_X(X,r)$, $B_r(X,r)$ at the position of the particle, (X,r) are obtained from Taylor expansions truncated at the fifth order in r (hence, up to the fifth order derivative $\frac{\partial^5 B_X}{\partial X^5}(X,0)$), assuming cylindrical symmetry

$$B_X(X,r) = B_X(X,0) - \frac{r^2}{4} \frac{\partial^2 B_X}{\partial X^2} (X,0) + \frac{r^4}{64} \frac{\partial^4 B_X}{\partial X^4} (X,0)$$

$$B_r(X,r) = -\frac{r}{2} \frac{\partial B_X}{\partial X} (X,0) + \frac{r^3}{16} \frac{\partial^3 B_X}{\partial X^3} (X,0) - \frac{r^5}{384} \frac{\partial^5 B_X}{\partial X^5} (X,0)$$
(1.3.1)

Then, by differentiation with respect to X and r, up to the second order, these expressions provide the derivatives of $\vec{B}(X,r)$. Finally a conversion from the (X,r) coordinates to the (X,Y,Z) Cartesian coordinates of **zgoubi** is performed, thus providing the expressions $\frac{\partial^{i+j+k}\vec{B}}{\partial X^i\partial Y^j\partial Z^k}$ needed in the eq. (1.2.10).

1.3.3 Extrapolation From Median Plane Field Models

In the median plane, $B_Z(X, Y, 0)$ and its derivatives with respect to X or Y may be derived from analytical models (e.g., in Venus magnet - VENUS, and sharp edge multipoles SEXQUAD and QUADISEX) or numerically by polynomial interpolation from 2-D field maps (e.g., CARTEMES, TOSCA). Median plane antisymmetry is assumed, which results in

$$B_X(X, Y, 0) = 0$$

$$B_Y(X, Y, 0) = 0$$

$$B_X(X, Y, Z) = -B_X(X, Y, -Z)$$

$$B_Y(X, Y, Z) = -B_Y(X, Y, -Z)$$

$$B_Z(X, Y, Z) = B_Z(X, Y, -Z)$$
(1.3.2)

Accommodated with Maxwell's equations, this results in Taylor expansions below, for the three components of \vec{B} (here, B stands for $B_Z(X,Y,0)$)

$$B_X(X,Y,Z) = Z \frac{\partial B}{\partial X} - \frac{Z^3}{6} \left(\frac{\partial^3 B}{\partial X^3} + \frac{\partial^3 B}{\partial X \partial Y^2} \right)$$

$$B_Y(X,Y,Z) = Z \frac{\partial B}{\partial Y} - \frac{Z^3}{6} \left(\frac{\partial^3 B}{\partial X^2 \partial Y} + \frac{\partial^3 B}{\partial Y^3} \right)$$

$$B_Z(X,Y,Z) = B - \frac{Z^2}{2} \left(\frac{\partial^2 B}{\partial X^2} + \frac{\partial^2 B}{\partial Y^2} \right) + \frac{Z^4}{24} \left(\frac{\partial^4 B}{\partial X^4} + 2 \frac{\partial^4 B}{\partial X^2 \partial Y^2} + \frac{\partial^4 B}{\partial Y^4} \right)$$
(1.3.3)

which are then differentiated one by one with respect to X, Y, or Z, up to second or fourth order (depending on optical element or IORDRE option, see section 1.4.2) so as to get the expressions involved in eq. (1.2.10).

1.3.4 Extrapolation from Arbitrary 2-D Field Maps

2-D field maps that give the three components $B_X(X,Y,Z_0)$, $B_Y(X,Y,Z_0)$ and $B_Z(X,Y,Z_0)$ at each node (X,Y) of a Z_0 Z-elevation map may be used. \vec{B} and its derivatives at any point (X,Y,Z) are calculated by polynomial interpolation followed by Taylor expansions in Z, without any hypothesis of symmetries (see section 1.4.3 and keywords MAP2D, MAP2D-E).

1.3.5 Interpolation in 3-D Field Maps [8]

In 3-D field maps \vec{B} and its derivatives up to the second order with respect to X, Y or Z are calculated by means of a second order polynomial interpolation, from 3-D $3 \times 3 \times 3$ -point grid (see section 1.4.4).

1.3.6 2-D Analytical Field Models and Extrapolation

Several optical elements such as *BEND*, *WIENFILT* (that uses the *BEND* procedures), *QUADISEX*, *VENUS*, etc., are defined from the expression of the field and derivatives in the median plane. 3-D extrapolation of these off the median plane is drawn from Taylor expansions and Maxwell's equations.

1.3.7 3-D Analytical Models of Fields

In many optical elements such as *QUADRUPO*, *SEXTUPOL*, *MULTIPOL*, *EBMULT*, etc., the three components of \vec{B} and their derivatives with respect to X, Y or Z are obtained at any step along trajectories from analytical expression drawn from the scalar potential V(X,Y,Z), namely

$$B_X = \frac{\partial V}{\partial X}, \quad B_Y = \frac{\partial V}{\partial Y}, \quad B_Z = \frac{\partial V}{\partial Z}, \quad \frac{\partial B_X}{\partial X} = \frac{\partial^2 V}{\partial X^2}, \quad \frac{\partial B_X}{\partial Y} = \frac{\partial^2 V}{\partial X \partial Y}, \quad \text{etc.}$$
 (1.3.4)

and similarly for \vec{E} with opposite sign for the gradients.

Multipoles

The scalar potential used for the calculation of $\frac{\partial^{i+j+k}\vec{B}_n(X,Y,Z)}{\partial X^i\partial Y^i\partial Z^k}$ $(i+j+k=0\ \text{to}\ 4)$ in the case of magnetic and electro-magnetic multipoles with 2n poles (namely, QUADRUPO (n=2) to DODECAPO (n=6), MULTIPOL $(n=1\ \text{to}\ 10)$, EBMULT $(n=1\ \text{to}\ 10)$) is [9]

$$V_n(X,Y,Z) = (n!)^2 \left(\sum_{q=0}^{\infty} (-1)^q \frac{G^{(2q)}(X)(Y^2 + Z^2)^q}{4^q q! (n+q)!} \right) \left(\sum_{m=0}^n \frac{\sin\left(m\frac{\pi}{2}\right) Y^{n-m} Z^m}{m! (n-m)!} \right)$$
(1.3.5)

where G(X) is the longitudinal gradient, defined at the entrance or exit of the optical element by

$$G(s) = \frac{G_0}{1 + \exp(P(s))}, \quad G_0 = \frac{B_0}{R_0^{n-1}}$$
 (1.3.6)

wherein

$$P(s) = C_0 + C_1 \left(\frac{s}{\lambda}\right) + C_2 \left(\frac{s}{\lambda}\right)^2 + C_3 \left(\frac{s}{\lambda}\right)^3 + C_4 \left(\frac{s}{\lambda}\right)^4 + C_5 \left(\frac{s}{\lambda}\right)^5$$

and s is the distance to the EFB.

Skew Multipoles

A multipole component with arbitrary order n can be tilted independently of the others by an arbitrary angle A_n around the X-axis. If so, the calculation of the field and derivatives in the rotated axis (X, Y_R, Z_R) is done in two steps. First, they are calculated at the rotated position (X, Y_R, Z_R) , in the (X, Y, Z) frame, using the expression (1.3.5) above. Second, \vec{B} and its derivatives at (X, Y_R, Z_R) in the (X, Y, Z) frame are transformed into the new, (X, Y_R, Z_R) frame, by a rotation with angle A_n .

In particular a skew 2n-pole component is created by taking $A_n = \pi/2n$.

A Note on Electrostatic Multipoles

A right electric multipole has the same field equations as the like-order skew magnetic multipole. Therefore, calculation of right or skew electric or electro-magnetic multipoles (*ELMULT*, *EBMULT*, *ELMULT*) uses the same eq. (1.3.5) together with the rotation process as described in section 1.3.7. The same method is used for arbitrary rotation of any multipole component around the *X*-axis.

1.4 Calculation of \vec{E} and \vec{B} from Field Maps

In this section, unless otherwise stated, $\vec{B} = (B_X(X,Y,Z), B_Y(X,Y,Z), B_Z(X,Y,Z))$ stands indifferently for electric field \vec{E} or magnetic field \vec{B} .

1.4.1 1-D Axial Map, with Cylindrical Symmetry

Let B_i be the value of the longitudinal component $B_X(X, r=0)$ of the field \vec{B} , at node i of a uniform mesh that defines a 1-D field map along the symmetry X-axis, while $B_r(X, r=0)$ is assumed to be zero $(r=(Y^2+Z^2)^{1/2})$. The field component $B_X(X, r=0)$ is calculated by a polynomial interpolation of the fifth degree in X, using a 5 points grid centered at the node of the 1-D map which is closest to the actual coordinate X of the particle.

The interpolation polynomial is

$$B(X,0) = A_0 + A_1X + A_2X^2 + A_3X^3 + A_4X^4 + A_5X^5$$
(1.4.1)

and the coefficients A_i are calculated by expressions that minimize the quadratic sum

$$S = \sum_{i} (B(X,0) - B_i)^2$$
 (1.4.2)

Namely, the source code contains the explicit analytical expressions of the coefficients A_i solutions of the normal equations $\partial S/\partial A_i=0$.

The derivatives $\frac{\partial^n B}{\partial X^n}(X,0)$ at the actual position X, as involved in eqs. (1.3.1), are then obtained by differentiation of the polynomial (1.4.1), giving

$$\frac{\partial B}{\partial X}(X,0) = A_1 + 2A_2X + 3A_3X^2 + 4A_4X^3 + 5A_5X^4
\frac{\partial^2 B}{\partial X^2}(X,0) = 2A_2 + 6A_3X + 12A_4X^2 + 20A_5X^3
\dots
\frac{\partial^5 B}{\partial X^5}(X,0) = 120A_5$$
(1.4.3)

1.4.2 2-D Median Plane Map, with Median Plane Antisymmetry

Let B_{ij} be the value of $B_Z(X, Y, 0)$ at the nodes of a mesh which defines a 2-D field map in the (X, Y) plane while $B_X(X, Y, 0)$ and $B_Y(X, Y, 0)$ are assumed to be zero. Such a map may have been built or measured in either Cartesian or polar coordinates. Whenever polar coordinates are used, a change to Cartesian coordinates (described below) provides the expression of \vec{B} and its derivatives as involved in eq. (1.2.10).



Figure 3: Mesh in the (X, Y) plane. The grid is centered on the node which is closest to the actual position of the particle.

A: Cartesian mesh, 9-point interpolation grid.

B: Cartesian mesh, 25-point interpolation grid.

C: Polar mesh and moving Cartesian frame.

zgoubi provides three types of polynomial interpolation from the mesh (option *IORDRE*); namely, a second order interpolation, with either a 9- or a 25-point grid, or a fourth order interpolation with a 25-point grid (Fig. 3).

If the 2-D field map is built up from computer simulation, the grid in principle simply aims at interpolating the field and derivatives at a given point from its 9 or 25 neighbors. On the other hand if the map results from field measurements, the grid also has the virtue of smoothing field fluctuations.

The mesh may be defined in Cartesian coordinates, (Figs. 3A and 3B) or in polar coordinates (Fig. 3C).

The interpolation grid is centered on the node which is closest to the projection in the (X, Y) plane of the actual point of the trajectory.

The interpolation polynomial is

$$B(X,Y,0) = A_{00} + A_{10}X + A_{01}Y + A_{20}X^2 + A_{11}XY + A_{02}Y^2$$
(1.4.4)

to the second order, or

$$B(X,Y,0) = A_{00} + A_{10}X + A_{01}Y + A_{20}X^{2} + A_{11}XY + A_{02}Y^{2}$$

$$+ A_{30}X^{3} + A_{21}X^{2}Y + A_{12}XY^{2} + A_{03}Y^{3}$$

$$+ A_{40}X^{4} + A_{31}X^{3}Y + A_{22}X^{2}Y^{2} + A_{13}XY^{3} + A_{04}Y^{4}$$

$$(1.4.5)$$

to the fourth order. The coefficients A_{ij} are calculated by expressions that minimize, with respect to A_{ij} , the quadratic sum

$$S = \sum_{ij} (B(X, Y, 0) - B_{ij})^2$$
(1.4.6)

The source code contains the explicit analytical expressions of the coefficients A_{ij} solutions of the normal equations $\partial S/\partial A_{ij}=0$.

The A_{ij} may then be identified with the derivatives of B(X,Y,0) at the central node of the grid

$$A_{ij} = \frac{1}{i!j!} \frac{\partial^{i+j} B}{\partial X^i \partial Y^j} (0, 0, 0)$$
 (1.4.7)

The derivatives of B(X, Y, 0) with respect to X and Y, at the actual point (X, Y, 0) are obtained by differentiation of the interpolation polynomial, which gives (e.g., from (1.4.4) in the case of second order interpolation)

$$\frac{\partial B}{\partial X}(X, Y, 0) = A_{10} + 2A_{20}X + A_{11}Y
\frac{\partial B}{\partial Y}(X, Y, 0) = A_{01} + A_{11}X + 2A_{02}Y$$
(1.4.8)

This allows stepping to the calculation of $\vec{B}(X,Y,Z)$ and its derivatives as described in subsection 1.3.3 (eq. 1.3.3).

The Special Case of Polar Maps

In some optical elements (e.g., POLARMES, DIPOLE[S]) the field is given in polar coordinates. It is thus necessary to transform the field and derivatives from the polar frame of the map, (R, α, Z) to the Cartesian moving frame (X, Y, Z), Fig. 3C. This is done as follows.

In second order calculations the correspondence is (we note $B \equiv B_Z(Z=0)$)

$$\frac{\partial B}{\partial X} = \frac{1}{R} \frac{\partial B}{\partial \alpha}$$

$$\frac{\partial B}{\partial Y} = \frac{\partial B}{\partial R}$$

$$\frac{\partial^2 B}{\partial X^2} = \frac{1}{R^2} \frac{\partial^2 B}{\partial \alpha^2} + \frac{1}{R} \frac{\partial B}{\partial R}$$

$$\frac{\partial^2 B}{\partial X \partial Y} = \frac{1}{R} \frac{\partial^2 B}{\partial \alpha \partial R} - \frac{1}{R^2} \frac{\partial B}{\partial \alpha}$$

$$\frac{\partial^2 B}{\partial Y^2} = \frac{\partial^2 B}{\partial R^2}$$

$$\frac{\partial^3 B}{\partial X^3} = \frac{3}{R^2} \frac{\partial^2 B}{\partial \alpha \partial R} - \frac{2}{R^3} \frac{\partial B}{\partial \alpha}$$

$$\frac{\partial^3 B}{\partial X^2 \partial Y} = \frac{-2}{R^3} \frac{\partial^2 B}{\partial \alpha^2} - \frac{1}{R^2} \frac{\partial B}{\partial R} + \frac{1}{R} \frac{\partial^2 B}{\partial R^2}$$

$$\frac{\partial^3 B}{\partial X \partial Y^2} = \frac{2}{R^3} \frac{\partial B}{\partial \alpha} - \frac{2}{R^2} \frac{\partial^2 B}{\partial \alpha \partial R}$$

$$\frac{\partial^3 B}{\partial Y^3} = 0$$
(1.4.9)

In fourth order calculations the relations above are pushed to fourth order in X, Y whereas

urth order calculations the relations above are pushed to fourth order in
$$X$$
, Y whereas
$$\frac{\partial^3 B}{\partial X^3} = \frac{1}{R^3} \frac{\partial^3 B}{\partial \alpha^3} + \frac{3}{R^2} \frac{\partial^2 B}{\partial \alpha \partial R} - \frac{2}{R^3} \frac{\partial B}{\partial \alpha}$$

$$\frac{\partial^3 B}{\partial X^2 \partial Y} = \frac{1}{R^2} \frac{\partial^3 B}{\partial \alpha^2 \partial R} - \frac{2}{R^3} \frac{\partial^2 B}{\partial \alpha^2} - \frac{1}{R^2} \frac{\partial B}{\partial R} + \frac{1}{R} \frac{\partial^2 B}{\partial R^2}$$

$$\frac{\partial^3 B}{\partial X^3 \partial Y^2} = \frac{1}{R} \frac{\partial^3 B}{\partial \alpha \partial R^2} + \frac{2}{R^3} \frac{\partial B}{\partial \alpha} - \frac{2}{R^2} \frac{\partial^2 B}{\partial \alpha \partial R}$$

$$\frac{\partial^3 B}{\partial X^3 \partial Y} = \frac{\partial^3 B}{\partial R^3}$$

$$\frac{\partial^4 B}{\partial X^3 \partial Y} = \frac{1}{R^4} \frac{\partial^4 B}{\partial \alpha^4} - \frac{8}{R^4} \frac{\partial^2 B}{\partial \alpha^2} + \frac{6}{R^3} \frac{\partial^3 B}{\partial \alpha^2 \partial R} + \frac{3}{R^2} \frac{\partial^2 B}{\partial \alpha \partial R^2} - \frac{3}{R^3} \frac{\partial B}{\partial R}$$

$$\frac{\partial^4 B}{\partial X^3 \partial Y} = \frac{1}{R^3} \frac{\partial^4 B}{\partial \alpha^3 \partial R} - \frac{3}{R^4} \frac{\partial^3 B}{\partial \alpha^3 \partial R} - \frac{2}{R^2} \frac{\partial^2 B}{\partial \alpha \partial R^2} - \frac{8}{R^3} \frac{\partial^2 B}{\partial \alpha \partial R^2} - \frac{8}{R^3} \frac{\partial^2 B}{\partial \alpha \partial R} + \frac{6}{R^4} \frac{\partial B}{\partial \alpha}$$

$$\frac{\partial^4 B}{\partial X^2 2 Y^2} = \frac{1}{R^4} \frac{\partial^2 B}{\partial \alpha^2} - \frac{4}{R^3} \frac{\partial^3 B}{\partial \alpha^2 \partial R} - \frac{2}{R^2} \frac{\partial^2 B}{\partial R^2} + \frac{2}{R^3} \frac{\partial B}{\partial R} + \frac{1}{R^2} \frac{\partial^4 B}{\partial \alpha^2 \partial R^2} + \frac{1}{R} \frac{\partial^3 B}{\partial R^3}$$

$$\frac{\partial^4 B}{\partial X \partial Y^3} = \frac{1}{R} \frac{\partial^4 B}{\partial \alpha \partial R^3} - \frac{3}{R^2} \frac{\partial^3 B}{\partial \alpha \partial R^2} + \frac{6}{R^3} \frac{\partial^2 B}{\partial \alpha \partial R} - \frac{6}{R^4} \frac{\partial^4 B}{\partial \alpha^4}$$

$$\frac{\partial^4 B}{\partial Y^4} = \frac{\partial^4 B}{\partial R^4}$$

$$\frac{\partial^4 B}{\partial R^4} = \frac{\partial^4 B}{\partial R^4}$$

NOTE: In case a particle goes beyond the limits of the field map, the field and its derivatives are extrapolated using a grid at the border of the map, which is the closest to the actual position of the particle. The flag *IEX* attached to the particle (section 4.6.10, p. 173) is then given the value -1.

1.4.3 Arbitrary 2-D Map, no Symmetry

The map is assumed to describe the field $\vec{B}(B_X, B_Y, B_Z)$ in the (X, Y) plane at elevation Z_0 . It provides the components $B_{X,ij}$, $B_{Y,ij}$, $B_{Z,ij}$ at each node (i,j) of a 2-D mesh.

The value of \vec{B} and its derivatives at the projection (X, Y, Z_0) of the actual position (X, Y, Z) of a particle is obtained by means of (parameter IORDRE in keyword data list - see for instance MAP2D, MAP2D-E) either a second degree polynomial interpolation from a 3×3 points grid (IORDRE=2), or a fourth degree polynomial interpolation from a 5×5 points grid (IORDRE=4), centered at the node (i, j) closest to the position (X,Y).

To second order for instance

$$B_{\ell}(X, Y, Z_0) = A_{00} + A_{10}X + A_{01}Y + A_{20}X^2 + A_{11}XY + A_{02}Y^2$$
(1.4.11)

where B_{ℓ} stands for any of the three components B_X , B_Y or B_Z . Differentiating then gives the derivatives

$$\frac{\partial B_{\ell}}{\partial X}(X, Y, Z_0) = A_{10} + 2A_{20}X + A_{11}Y$$

$$\frac{\partial^2 B_{\ell}}{\partial X \partial Y}(X, Y, Z_0) = A_{11}$$
etc.
$$(1.4.12)$$

Then follows a procedure of extrapolation from (X, Y, Z_0) to the actual position (X, Y, Z), based on Taylor series development.

No special symmetry is assumed, which allows the treatment of arbitrary field distribution (e.g., solenoid, helical snake).



Figure 4: A 3-D 27-point grid is used for interpolation of magnetic or electric fields and derivatives up to second order. The central node of the grid (i=j=k=0) is the closest to the actual position of the particle.

1.4.4 3-D Field Map

When using a 3-D field map, the vector field $\vec{B}(X,Y,Z)$ and its derivatives necessary for the calculation of position and velocity of the particle are obtained via second degree polynomial interpolation,

$$B_{\ell}(X,Y,Z) = A_{000} + A_{100}X + A_{010}Y + A_{001}Z + A_{200}X^2 + A_{020}Y^2 + A_{002}Z^2 + A_{110}XY + A_{101}XZ + A_{011}YZ$$

$$(1.4.13)$$

 B_{ℓ} stands for any of the three components, B_X , B_Y or B_Z . By differentiation of B_{ℓ} one gets

$$\frac{\partial B_{\ell}}{\partial X} = A_{100} + 2A_{200}X + A_{110}Y + A_{101}Z$$

$$\frac{\partial^2 B_{\ell}}{\partial X^2} = 2A_{200}$$
(1.4.14)

and so on up to second order derivatives with respect to X, Y or Z.

The interpolation involves a $3 \times 3 \times 3$ -point parallelepipedic grid (Fig. 4), the origin of which is positioned at the node of the 3-D field map which is closest to the actual position of the particle.

Let B_{ijk}^{ℓ} be the value of the — measured or computed — magnetic field at each one of the 27 nodes of the 3-D grid (B^{ℓ} stands for B_X , B_Y or B_Z), and $B_{\ell}(X,Y,Z)$ be the value at a position (X,Y,Z) with respect to the central node of the 3-D grid. Thus, any coefficient A_i of the polynomial expansion of B_{ℓ} is obtained by means of expressions that minimize, with respect to A_i , the sum

$$S = \sum_{ijk} (B_{\ell}(X, Y, Z) - B_{ijk}^{\ell})^{2}$$
(1.4.15)

where the indices i, j and k take the values -1, 0 or +1 so as to sweep the 3-D grid. The source code contains the explicit analytical expressions of the coefficients A_{ijk} solutions of the normal equations $\partial S/\partial A_{ijk}=0$.

2 SPIN TRACKING

Spin motion tracking was implemented in **zgoubi** in the SATURNE years [10], it has been since used in a number of studies, including the transport of polarized muons in the Neutrino Factory [11], polarization survival in the superB project [12], studies on proton polarization with helical snakes at AGS [13] and RHIC [14], and in the magic-energy electrostatic ring of the proton-EDM project [15].

2.1 Introduction

The precession of the spin \vec{S} of a charged particle in electric and magnetic fields is governed by the Thomas-BMT first order differential equation [16]

$$\frac{d\vec{S}}{dt} = \frac{q}{m}\,\vec{S} \times \vec{\omega} \tag{2.1.1}$$

with, in the laboratory frame,

$$\vec{\omega} = (1 + \gamma G)\vec{b} + G(1 - \gamma)\vec{b}_{/\!/} + \gamma(G + \frac{1}{1 + \gamma})\frac{\vec{e} \times \vec{v}}{c^2}$$
(2.1.2)

 t, q, m, c, γ and G are respectively the time, charge, relativistic mass, speed of light, Lorentz relativistic factor and anomalous magnetic moment of the particle, \vec{b} and \vec{e} are the fields in the laboratory, \vec{b}_{\parallel} is the component of \vec{b} parallel to the velocity \vec{v} of the particle.

Equation (2.1.1) is normalized by introducing the same notation as for the Lorentz equation, page 17, namely $b = \parallel \vec{b} \parallel$, $v = ||\vec{v}||$, $\vec{v} = v\vec{u}$, ds = vdt the differential path, $\frac{\gamma mv}{q} = B\rho$ the rigidity of the particle,

whereas $\vec{S}' = \frac{d\vec{S}}{ds} = \frac{1}{v} \frac{d\vec{S}}{dt}$ is the derivative of the spin with respect to the path. This yields

$$(B\rho) \vec{S}' = \vec{S} \times \vec{\omega} \quad \text{or} \quad \vec{S}' = \vec{S} \times \vec{\Omega}$$
 (2.1.3)

where, noting $\vec{B}=\vec{b}/B\rho$, $\vec{E}=\vec{e}/B\rho$,

$$\vec{\Omega} = \frac{\vec{\omega}}{B\rho} = (1 + \gamma G)\vec{B} + G(1 - \gamma)\vec{B}_{//} + \frac{\beta\gamma}{c}(G + \frac{1}{1 + \gamma})\vec{E} \times \vec{u}$$
 (2.1.4)

This equation is solved in the same way as the reduced Lorentz equation (1.2.3). From the values of the precession factor $\vec{\omega}(M_0)$ and spin $\vec{S}(M_0)$ of the particle at position M_0 , the spin $\vec{S}(M_1)$ at position M_1 , following a displacement Δs (fig. 2), is obtained from truncated Taylor expansion

$$\vec{S}(M_1) \approx \vec{S}(M_0) + \frac{d\vec{S}}{ds}(M_0) \Delta s + \frac{d^2\vec{S}}{ds^2} (M_0) \frac{\Delta s^2}{2} + \frac{d^3\vec{S}}{ds^3} (M_0) \frac{\Delta s^3}{3!} + \frac{d^4\vec{S}}{ds^4} (M_0) \frac{\Delta s^4}{4!} + \frac{d^5\vec{S}}{ds^5} (M_0) \frac{\Delta s^5}{5!}$$
(2.1.5)

2.2 Integration in Magnetic Fields

In purely magnetic fields $\vec{e} = 0$ thus eq. (2.1.4) reduces to

$$\vec{\Omega}_b = (1 + \gamma G)\vec{B} + G(1 - \gamma)\vec{B}_{/\!/}$$
 (2.2.1)

 \vec{S} and its derivatives $\vec{S}^{(n)} = d^n \vec{S}/ds^n$ satisfy the recursive differentiation relations

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$$\vec{S}' = \vec{S} \times \vec{\Omega}_{b}$$

$$\vec{S}'' = \vec{S}' \times \vec{\Omega}_{b} + \vec{S} \times \vec{\Omega}'_{b}$$

$$\vec{S}''' = \vec{S}'' \times \vec{\Omega}_{b} + 2\vec{S}' \times \vec{\Omega}'_{b} + \vec{S} \times \vec{\Omega}''_{b}$$
etc.
$$(2.2.2)$$

with the derivatives $d^n\vec{\Omega}_b/ds^n$ obtained by differentiation of eq. (2.2.1). This requires $\vec{B}_{/\!\!/}$ and derivatives, obtained in the following way,

$$\vec{B}_{/\!/} = (\vec{B} \cdot \vec{u}) \vec{u}$$

$$\vec{B}_{/\!/}' = (\vec{B}' \cdot \vec{u} + \vec{B} \cdot \vec{u}') \vec{u} + (\vec{B} \cdot \vec{u}) \vec{u}'$$

$$\vec{B}_{/\!/}'' = (\vec{B}'' \cdot \vec{u} + 2\vec{B}' \cdot \vec{u}' + \vec{B} \cdot \vec{u}'') \vec{u} + 2(\vec{B}' \cdot \vec{u} + \vec{B} \cdot \vec{u}') \vec{u}' + (\vec{B} \cdot \vec{u}) \vec{u}''$$
etc. (2.2.3)

The quantities \vec{u} , \vec{B} and their derivatives as involved in these equations are known, being sub-products of the integration of the motion of the particle, eqs. (1.2.8, 1.2.10) p. 19.

2.3 Integration in Electric Fields

In purely electric fields $\vec{b} = 0$, thus eq. (2.1.2) reduces to

$$\omega_e = \frac{\beta \gamma}{c} (G + \frac{1}{1+\gamma}) \, \vec{e} \times \vec{u} \tag{2.3.1}$$

 \vec{S} and its derivatives $\vec{S}^{(n)} = d^n \vec{S}/ds^n$ satisfy the recursive differentiation relations

$$B\rho \vec{S}' = \vec{S} \times \vec{\omega}_{e}$$

$$(B\rho)'\vec{S}' + B\rho\vec{S}'' = \vec{S}' \times \vec{\omega}_{e} + \vec{S} \times \vec{\omega}'_{e}$$

$$(B\rho)''\vec{S}' + 2(B\rho)'\vec{S}'' + B\rho\vec{S}''' = \vec{S}'' \times \vec{\omega}_{e} + 2\vec{S}' \times \vec{\omega}'_{e} + \vec{S}' \times \vec{\omega}''_{e}$$
etc. (2.3.2)

that provide the derivatives $d^n\vec{S}/ds^n$ needed in the Taylor expansion (eq. 2.1.5). The derivatives $(B\rho)^{(n)}=d^n(B\rho)/ds^n$ above are a sub-product of the integration of the force law (eq. 1.2.18). The derivatives of ω_e (eq. 2.3.1) are obtained by recursive differentiation,

$$\vec{\omega}_e' = \left(\frac{\beta\gamma}{c}(G + \frac{1}{1+\gamma})\right)'\vec{e} \times \vec{u} + \frac{\beta\gamma}{c}(G + \frac{1}{1+\gamma})(\vec{e} \times \vec{u})'$$

$$\vec{\omega}_e'' = \left(\frac{\beta\gamma}{c}(G + \frac{1}{1+\gamma})\right)''\vec{e} \times \vec{u} + 2\left(\frac{\beta\gamma}{c}(G + \frac{1}{1+\gamma})\right)'(\vec{e} \times \vec{u})' + \frac{\beta\gamma}{c}(G + \frac{1}{1+\gamma})(\vec{e} \times \vec{u})''$$
etc. (2.3.3)

The quantities $\left(\frac{1}{1+\gamma}\right)^{(n)}$ in the $(\omega_e)^{(n)}$ above are obtained as follows.

From $\gamma^2 = 1/(1-\beta^2)$ it comes $(\gamma+1)(\gamma-1)\beta^2/(1-\beta^2)$ and then

$$\frac{1}{1+\gamma} = \left(\frac{1}{\beta} - 1\right) \left(\frac{1}{\beta} + 1\right) (\gamma - 1)$$

which is easily differentiated, recursively,

$$\left(\frac{1}{1+\gamma}\right)' = \left(\frac{1}{\beta}\right)' \left(\frac{1}{\beta}+1\right) (\gamma-1) + \left(\frac{1}{\beta}-1\right) \left(\frac{1}{\beta}\right)' (\gamma-1) + \left(\frac{1}{\beta}-1\right) \left(\frac{1}{\beta}+1\right) \gamma'
\left(\frac{1}{1+\gamma}\right)'' = \left(\frac{1}{\beta}\right)'' \left(\frac{1}{\beta}+1\right) (\gamma-1) + \left(\frac{1}{\beta}-1\right) \left(\frac{1}{\beta}\right)'' (\gamma-1) + \left(\frac{1}{\beta}-1\right) \left(\frac{1}{\beta}+1\right) \gamma'' +
2 \left(\frac{1}{\beta}\right)' \left(\frac{1}{\beta}\right) (\gamma-1) + 2 \left(\frac{1}{\beta}\right)' \left(\frac{1}{\beta}\right)' (\gamma-1) + 2 \left(\frac{1}{\beta}-1\right) \left(\frac{1}{\beta}\right)' \gamma'
etc.$$
(2.3.4)

The interest of that formulation is that the $\left(\frac{1}{\beta}\right)^{(n)}$ are already known from the particle dynamics, eq. (1.2.21), as well as the derivatives

$$\frac{d^{n+1}\gamma}{ds^{n+1}} = \frac{q}{m} \frac{d^n(\vec{e} \cdot \vec{u})}{ds^n}$$

following eq. (1.2.20), whereas the $d^n(\vec{e} \cdot \vec{u})/ds^n$ are given by eq. (1.2.19).

2.4 Integration in Combined Electric and Magnetic Fields

When both \vec{e} and \vec{b} are non-zero, the complete eqs. (2.1.3, 2.1.4) must be considered.

The precession vector (eq. 2.1.4) and its derivatives can be split into independent, magnetic and electric components, namely

$$\vec{\omega} = \vec{\omega}_b + \vec{\omega}_e, \ \vec{\omega}' = \vec{\omega}_b' + \vec{\omega}_e',$$
 etc.

As a consequence, the spin vector $\vec{S}(s)$ and its derivatives at location M_0 prior to a Δs push to location M_1 (fig. 2) can be obtained by linear superposition of the separate solutions for the magnetic case (eq. 2.2.2) and for the electric case (eq. 2.3.2), namely

$$\begin{split} &B\rho\,\vec{S}^{\,\prime} = \\ &\vec{S} \times \vec{\omega}_b \\ &B\rho\vec{S}^{\,\prime\prime} = \\ &\vec{S}^{\,\prime} \times \vec{\omega}_b + \vec{S} \times \vec{\omega}_b^{\,\prime} \\ &B\rho\vec{S}^{\,\prime\prime\prime} = \\ &\underline{\vec{S}^{\,\prime\prime} \times \vec{\omega}_b + 2\vec{S}^{\,\prime} \times \vec{\omega}_b^{\,\prime} + \vec{S} \times \vec{\omega}_b^{\,\prime\prime}}_{\text{Magnetic field component, eq. (2.2.2)}} \\ &\text{etc.} \\ \end{split}$$

The process is then completed by applying the Δs push, eq. (2.1.5).

3 SYNCHROTRON RADIATION

zgoubi provides the simulation of two distinct types of synchrotron radiation (SR) manifestations namely, on the one hand energy loss by stochastic emission of photons and the ensuing perturbation on particle dynamics and, on the other hand the radiated electro-magnetic field impulse and its spectral-angular energy density as observed in the laboratory.

SR loss simulation was first installed in **zgoubi** in view of beam dynamics studies in the beam delivery system of the Next Linear Collider [17], based on a method developed in the frame of the ELFE project ("EU Lab. For Electrons") [18, 19, 20]. It was next used for including damping effects in beam studies regarding various electron-ring and recirculator projects [12, 21].

SR electromagneitc impulse and spectrum computation was first installed in **zgoubi** for the study of interference effects at the LEP beam diagnostics miniwiggler [23]. These simulation tools were next used to design the LHC SR beam diagnostics systems, located in the IR4 RF section [24].

3.1 Energy Loss and Dynamical Effects

Most of the contents of the present section are drawn from Ref. [17].

Given a particle wandering in the magnetic field of an arbitrary optical element or field map, **zgoubi** computes the energy loss undergone, and its effect on the particle motion. The energy loss is calculated in a classical manner, by invoking two random processes that accompany the emission of a photon namely,

- the probability of emission,
- the energy of the photon.

The effects on the dynamics of the emitting particle either account for the sole alteration of its energy, or, if requested, include the angle kick. Particle position is supposed not to change upon emission of a photon. These calculations and ensuing dynamics corrections are performed at each integration step. In a practical manner, this requires centimeters to tens of centimeters steps in smoothly varying magnetic fields (a quantity to be determined before any simulation, from convergence trials).

Main aspects of the method are developed in the following.

Probability of Emission of a Photon

Given that the number of photons emitted within a step Δs can be very small (units or fractions of a unit)¹ a Poisson probability law

$$p(k) = \frac{\lambda^k}{k!} \exp(-\lambda)$$
 (3.1.1)

is considered. k is the number of photons emitted over a $\Delta\theta$ (circular) arc of trajectory such that, the average number of photons per radian expresses as²

 $^{^1}$ For instance, a 1 GeV electron will emit about 20.6 photons per radian ; an integration step size $\Delta s = 0.1$ m upon $\rho = 10$ m bending radius results in 0.2 photon per step.

²This leads for instance, in the case of electrons, to the classical formula $\lambda/\Delta\theta \approx 129.5 \text{E(GeV)}/2\pi \approx \gamma/94.9$.

$$\lambda = \frac{20er_0}{8\hbar\sqrt{3}}\beta^2 B\rho \frac{\Delta s}{\rho} \tag{3.1.2}$$

where $r_0 = e^2/4\pi\epsilon_0 m_0 c^2$ is the classical radius of the particle of rest-mass m_0 , e is the elementary charge, $\hbar = h/2\pi$, h is the Planck constant, $\beta = v/c$, $B\rho$ is the particle stiffness. λ is evaluated at each integration step from the current values β , $B\rho$ and Δs , then a value of k is drawn by a rejection method.

Energy of the Photons

These k photons are assigned energies $\epsilon = h\nu$ at random, in the following way. The cumulative distribution of the energy probability law $p(\epsilon/\epsilon_c)d\epsilon/\epsilon_c$ (i.e., the probability of emission of a photon with energy in $[0,\epsilon]$) writes ³

$$\mathcal{P}(\epsilon/\epsilon_c) = \frac{3}{5\pi} \int_0^{\epsilon/\epsilon_c} \frac{d\epsilon}{\epsilon_c} \int_{\epsilon/\epsilon_c}^{\infty} K_{5/3}(x) dx \tag{3.1.3}$$

where $K_5/3$ is a modified Bessel function and, $\epsilon_c = \hbar \omega_c$, $\omega_c = 2\pi \times 3\gamma^3 c/2\rho$ being the critical frequency in the presence of bending radius ρ ; ω_c is evaluated at each integration step from the current values γ and ρ , in other words, this energy loss calculation assumes constant magnetic field over the trajectory arc Δs . In the low frequency region $(\epsilon/\epsilon_c \ll 1)$ it can be approximated by



$$\mathcal{P}(\epsilon/\epsilon_c) = \frac{12\sqrt{3}}{2^{1/3} \, 5 \, \Gamma(\frac{1}{2})} (\frac{\epsilon}{\epsilon_c})^{1/3} \tag{3.1.4}$$

Cumulative energy distribution $\mathcal{P}(\epsilon/\epsilon_c)$.

About 40 values of $\mathcal{P}(\epsilon/\epsilon_c)$ computed from eq. 3.1.3 [22], honestly spread over a range $\epsilon/\epsilon_c \leq 10$ are tabulated in **zgoubi** source file (see figure). In order to get ϵ/ϵ_c , first a random value $0 < \mathcal{P} < 1$ is generated uniformly, then ϵ/ϵ_c is drawn either by simple inverse linear interpolation of the tabulated values

if $\mathcal{P} > 0.26$ (corresponding to $\epsilon/\epsilon_c > 10^{-2}$), or, if $\mathcal{P} < 0.26$ from eq. 3.1.4 that gives $\epsilon/\epsilon_c = \left(\frac{5 \, 2^{1/3} \Gamma(\frac{1}{3})}{12 \sqrt{3} \mathcal{P}}\right)^3$ with precision no less than 1% at $\mathcal{P} \to 0.26$.

When SR loss tracking is requested, several optical elements that contain a dipole magnetic field component (e.g., MULTIPOL, BEND) provide a printout of various quantities related to SR emission, as drawn from classical theoretical expressions, such as for instance,

- energy loss per particle $\Delta E(eV) = \frac{2}{3} r_0 c \gamma^3 B(T) \Delta \theta$, with B the dipole field exclusive of any other multipole component in the magnet, $\Delta \theta$ the total deviation as calculated from B, from the magnet length, and from the reference rigidity BORO (as defined with, e.g., [MC]OBJET)
- critical energy $\epsilon_c(eV) = \frac{3\gamma^3 c}{2\rho} \frac{\hbar}{e}$, with $\rho = BORO/B$
- average energy of the photons radiated $<\epsilon>=\frac{8}{15\sqrt{3}}\epsilon_c$,
- rms energy of radiated photons $\epsilon_{rms} = 0.5591\epsilon_c$,
- number of radiated photons per particle $N=\Delta E/<\epsilon>$.

This is done in order to facilitate verifications, since on the other hand statistics regarding those values are drawn from the tracking and may be printed using the dedicated keyword *SRPRNT*.

³From a practical viewpoint, the value of the magnetic field first computed for a one-step push of the particle (eqs. 1.2.4, 1.2.8) is next used to obtain ρ and perform SR loss corrections afterwards.

Finally, upon user's request as well, SR loss can be limited to particular classes of optical elements, for instance dipole magnets alone, or dipole + quadrupole magnets, etc. This option is made available in order to allow further inspection, or easier comparison with other codes, for instance.

3.2 Spectral-Angular Radiated Densities

Most of the content in the present section is drawn from Refs. [23, 24, 25].

The ray-tracing procedures provide the ingredients necessary for the determination of the electric field radiated by the particle subject to acceleration, as shown in Fig. 5, this is developed in section 3.2.1. These ingredients further allow calculating the spectral-angular density of the radiation⁴, this is developed in section 3.2.2.



Figure 5: A scheme of the reference frame in **zgoubi** together with the vectors entering in the definition of the electric field radiated by the accelerated particle:

(x,y): horizontal plane; z: vertical axis.

 $\vec{R}(t)$ = particle position in the fixed frame (O, x, y, z);

 \vec{X} (time-independent) = position of the observer in the (O, x, y, z) frame;

 $\vec{r}(t) = \vec{X} - \vec{R}(t)$ = position of the particle with respect to the observer;

 $\vec{n}(t)$ = (normalized) direction of observation = $\vec{r}(t)/|\vec{r}(t)|$;

 $\vec{\beta}$ = normalized velocity vector of the particle $\vec{v}/c = (1/c)d\vec{R}/dt$.

3.2.1 Calculation of the Radiated Electric Field

The expression for the radiated electric field $\vec{\mathcal{E}}(\vec{n},\tau)$ as seen by the observer in the long distance approximation is [26]

$$\vec{\mathcal{E}}(\vec{n},\tau) = \frac{q}{4\pi\varepsilon_0 c} \frac{\vec{n}(t) \times \left[\left(\vec{n}(t) - \vec{\beta}(t) \right) \times d\vec{\beta}/dt \right]}{r(t) \left(1 - \vec{n}(t) \cdot \vec{\beta}(t) \right)^3}$$
(3.2.1)

where t is the time in which the particle motion is described and τ is the observer time. Namely, when at position $\vec{r}(t)$ with respect to the observer (or as well at position $\vec{R}(t) = \vec{X} - \vec{r}(t)$ in the (O, x, y, z) frame) the particle emits a signal which reaches the observer at time τ , such that $\tau = t + r(t)/c$ where r(t)/c is the delay necessary for the signal to travel from the emission point to the observer, which also leads by differentiation to the well-known relation

⁴These calculations have been installed in the post-processor **zpop**.



Figure 6: Left: typical shapes of the $\mathcal{E}_{\sigma}(t)$ and $\mathcal{E}_{\pi}(t)$ components of the electric field impulse (eq. 3.2.1) emitted by a 2.5 GeV electron on a $\rho=53.6$ m circular trajectory in a l=20 cm-long dipole, as observed in the direction of the centre of the dipole, $\phi=0, \gamma\psi=5$ (observation distance r=10 m). Right: the related spectral angular densities $\partial^3 W_{\sigma,\,\pi}/\partial\phi\,\partial\psi\,\partial\omega$ (eq. 3.2.10). After Ref. [25].

$$\frac{d\tau}{dt} = 1 - \vec{n}(t) \cdot \vec{\beta}(t) \tag{3.2.2}$$

The vectors $\vec{R}(t)$ and $\vec{\beta}(t) = \frac{v}{c}\vec{u}$ (eq. 1.2.2) that describe the motion are obtained from the ray-tracing (eqs. 1.2.4). The acceleration is calculated from (a form of eq. 1.2.1 with $\vec{e} = 0$)

$$\frac{d\vec{\beta}}{dt} = \frac{q}{m} \, \vec{\beta}(t) \times \vec{b}(t) \tag{3.2.3}$$

Then, given the observer position \vec{X} in the fixed frame, it is possible to calculate

$$\vec{r}(t) = \vec{X} - \vec{R}(t)$$
 and $\vec{n}(t) = \frac{\vec{r}(t)}{|\vec{r}(t)|}$ (3.2.4)

As an illustration, Fig. 6 has been produced using **zpop**, it shows the typical shape of the electric field impulse at the observer, with central peak width [25]

$$2\tau_c = 2\frac{2\rho}{3\gamma^3 c} (1 + \gamma^2 \psi^2)^{3/2}$$

Computation of $\vec{n} - \vec{\beta}$ and $1 - \vec{n} \cdot \vec{\beta}$

Owing to computer precision the crude computation of $\vec{n} - \vec{\beta}$ and $1 - \vec{n} \cdot \vec{\beta}$ may lead to

$$\vec{n} - \vec{\beta} = 0$$
 and $1 - \vec{n} \cdot \vec{\beta} = 0$

since the preferred direction of observation is generally almost parallel to $\vec{\beta}$ (in that case, parallel in the sense of computer precision), while $\beta \approx 1$ as soon as particle energies of a few hundred times the rest mass are concerned.

It is therefore necessary to express $\vec{n} - \vec{\beta}$ and $1 - \vec{n} \cdot \vec{\beta}$ in an adequate form for achieving accurate software computation.

The expression for \vec{n} is

$$\vec{n} = (n_x, n_y, n_z) = (\cos \psi \cos \phi, \cos \psi \sin \phi, \sin \psi)$$

$$= \left[1 - 2(\sin^2 \phi/2 + \sin^2 \psi/2) + 4\sin^2 \phi/2\sin^2 \psi/2, \sin \phi(1 - 2\sin^2 \psi/2), \sin \psi\right] \quad (3.2.5)$$

where ϕ and ψ are the observation angles, given by

$$\phi = \operatorname{Atg}\left(\frac{r_y}{r_x}\right) \text{ and } \psi = \operatorname{Atg}\left(\frac{r_z}{\sqrt{r_x^2 + r_y^2}}\right)$$
 (3.2.6)

with $\vec{r} = (r_x, r_y, r_z)$, while $\vec{\beta}$ can be written under the form

$$\vec{\beta} = (\beta_x, \beta_y, \beta_z) = \left[\sqrt{(\beta^2 - \beta_y^2 - \beta_z^2)}, \beta_y, \beta_z \right]$$

$$= \left[\sqrt{(1 - 1/\gamma^2 - \beta_y^2 - \beta_z^2)}, \beta_y, \beta_z \right] = (1 - a/2 + a^2/8 - a^3/16 + ..., \beta_y, \beta_z)$$
(3.2.7)

where $a = 1/\gamma^2 + \beta_y^2 + \beta_z^2$. This leads to

$$n_x = 1 - \varepsilon_x$$
 and $\beta_x = 1 - \xi_x$

with

$$\varepsilon_x = 2(\sin^2 \phi/2 + \sin^2 \psi/2) - 4\sin^2 \phi/2\sin^2 \psi/2$$

and

$$\xi_x = a/2 - a^2/8 + a^3/16 + \dots$$

All this provides, on the one hand,

$$\vec{n} - \vec{\beta} = (-\varepsilon_x + \xi_x, n_y - \beta_y, n_z - \beta_z), \qquad (3.2.8)$$

whose components are combinations of terms of the same order of magnitude (ε_x and $\xi_x \sim 1/\gamma^2$ while n_y, β_y, n_z and $\beta_z \sim 1/\gamma$) and, on the other hand,

$$1 - \vec{n} \cdot \vec{\beta} = \varepsilon_x + \xi_x - n_y \beta_y - n_z \beta_z - \varepsilon_x \xi_x , \qquad (3.2.9)$$

that combines terms of the same order of magnitude (ε_x , ξ_x , $n_y\beta_y$ and $n_z\beta_z\sim 1/\gamma^2$), plus $\varepsilon_x\beta_x\sim 1/\gamma^4$. The precision of these expressions is directly related to the order at which the series

$$\xi_x = a/2 - a^2/8 + a^3/16 + \dots$$
 $(a = 1/\gamma^2 + \beta_y^2 + \beta_z^2)$

is pushed, however the convergence is fast since $a \sim 1/\gamma^2 \ll 1$ in situations of concern.

3.2.2 Calculation of the Fourier Transform of the Electric Field

The Fourier transforms

$$FT_{\omega}[\vec{\mathcal{E}}(\tau)] = \int \vec{\mathcal{E}}(\tau) e^{-i\omega\tau} d\tau$$

of the σ and π electric field components provide the spectral angular energy density

$$\frac{\partial^3 W}{\partial \phi \, \partial \psi \, \partial \omega} = \frac{r^2}{\mu_0 c} \left| F T_\omega \left(\vec{\mathcal{E}}(\tau) \right) \right|^2 \tag{3.2.10}$$

Fig. 6-right gives a typical example in the case of a short magnet. These Fourier transforms are computed without resorting to FFT techniques, namely from

$$FT_{\omega}\left[\vec{\mathcal{E}}(\tau)\right] \approx \sum \vec{\mathcal{E}}(\tau_k) e^{-i\omega\tau_k} \Delta \tau_k$$
 (3.2.11)

for two reasons. On the one hand, the number of integration steps Δs that define the trajectory (eqs. 1.2.4), is arbitrary and therefore in general not of order 2^n . On the other hand, the integration step defines a constant time differential element $\Delta t_k = \Delta s/\beta c$ which results in the observer differential time element $\Delta \tau_k$, which is also the differential element of the Fourier transform, being non-constant, since both are related by eq. 3.2.2 in which $\vec{\beta}$ and \vec{n} vary as a function of the integration step number k.

An additional issue is that $\Delta \tau_k$ may reach drastically small values in the region of the central peak of the electric impulse emitted in a dipole, i.e., $1-\vec{n}(t)\cdot\vec{\beta}(t)\to 1/2\gamma^2$, whereas the total integrated time $\sum_{k=1}^N \Delta \tau_k$ may be several orders of magnitude larger. In terms of the physical phenomenon, the total duration of the electric field impulse as seen by the observer corresponds to the time delay $\sum_{k=1}^N \Delta \tau_k$ that separates photons emitted at the entrance of the magnet from photons emitted at the exit, but the significant part of it (in terms of energy density) which can be represented by the width $2\tau_c=2\frac{2\rho}{3\gamma^3}\frac{1}{c}(1+\gamma^2\psi^2)^{3/2}$ of the radiation peak, is a very small fraction of $\sum_{k=1}^N \Delta \tau_k$.

is a very small fraction of $\sum_{k=1}^N \Delta \tau_k$. The consequence is that, again in relation to computer precision, the differential element $\Delta \tau_k$ involved in the computation of eq. 3.2.11 cannot be derived from such relation as $\Delta \tau_k = \sum_{k=1}^n \Delta \tau_k - \sum_{k=1}^{n-1} \Delta \tau_k$ but instead must be stored as is, in the course of the ray-tracing process, for subsequent data treatment.

4 DESCRIPTION OF THE AVAILABLE PROCEDURES

4.1 Introduction

This chapter gives an inventory of the procedures available in **zgoubi**, their associated "keyword", and a brief description of the way they function.

The chapter has been split into several sections. Sections 4.2 to 4.5 explain the underlying content - physics and numerical methods - behind the keywords, they are organized by topics :

- How to defined an object (a set of initial coordinates),
- Available options,
- Optical elements and procedures,
- Output procedures.

Section 4.6 addresses further a series of functionalities that may be accessed by means of special input data or flags.

4.2 Definition of an Object

The description of the object, *i.e.*, initial coordinates of the ensemble of particles, must be the first procedure in the **zgoubi** input data file, zgoubi.dat.

Several types of automatically generated objects are available, they are described in the following pages and include,

- non-random object, with various distributions : individual particles, grids, object for MATRIX, etc.
- Monte Carlo distribution, with various distributions as well: 6-D window, ellipsoids, etc.

A recurrent quantity appearing in these procedures is *IMAX*, the number of particles to be ray-traced. The maximum value allowed for *IMAX* can be changed at leisure in the include file 'MAXTRA.H' where it is defined (that requires re-compiling **zgoubi**).

MCOBJET: Monte-Carlo generation of a 6-D object

MCOBJET generates a set of IMAX random 6-D initial conditions (the maximum value for IMAX is defined in the include file 'MAXTRA.H'). It can be used in conjunction with the keyword REBELOTE which either allows generating an arbitrarily high number of initial conditions, or, in the hypothesis of a periodic structure, allows multi-turn tracking with initial conditions at pass number IPASS identified with conditions at end of pass number IPASS - 1.

The first datum in MCOBJET is the reference rigidity (a negative value is allowed)

$$BORO = \frac{p_0}{q} \text{ (kG.cm)}$$

Depending on the value of the next datum, *KOBJ*, the *IMAX* particles have their initial random conditions Y, T, Z, P, X and D (relative rigidity, $B\rho/BORO$) generated on 3 different types of supports, as described below.

Next come the data

that specify the type of probability density for the 6 coordinates.

KY, KT, KZ, KP, KX can take the following values:

- 1. uniform density, $p(x) = 1/2\delta x$ if $-\delta x \le x \le \delta x$, p(x) = 0 elsewhere,
- 2. Gaussian density, $p(x) = \frac{1}{\delta x \sqrt{2\pi}} e^{-\frac{x^2}{2\delta x^2}}$,
- 3. parabolic density, $p(x) = \frac{3}{4\delta x}(1 \frac{x^2}{\delta x^2})$ if $-\delta x \le x \le \delta x$, p(x) = 0 elsewhere.

KD can take the following values:

- 1. uniform density, $p(D) = 1/2\delta D$ if $-\delta D \le D \le \delta D$, p(D) = 0 elsewhere,
- 2. exponential density, $p(D) = N_0 \exp(C_0 + C_1 l + C_2 l^2 + C_3 l^3)$ with $0 \le l \le 1$ and $-\delta D \le D \le \delta D$,
- 3. p(D) is determined by a kinematic relation, namely, with T = horizontal angle, $D = \delta D * T$.

Next come the central values for the random sorting,

$$Y_0, T_0, Z_0, P_0, X_0, D_0$$

namely, the probability density laws p(x) (x = Y, T, Z, P or X) and p(D) described above apply to the variables $x - x_0$ ($\equiv Y - Y_0, T - T_0, ...$) and $D - D_0$ respectively. Negative value for D_0 is allowed (see section 4.6.11, page 173).

KOBJ = 1 : Random generation of *IMAX* particles in a hyper-window with widths (namely the half-extent for uniform or parabolic distributions (KY, KT, ... = 1 or 3), and the r.m.s. width for Gaussian distributions (KY, KT, ... = 2))

$$\delta Y$$
, δT , δZ , δP , δX , δD

Then follow the cut-off values, in units of the r.m.s. widths δY , δT , ... (used only for Gaussian distributions, KY, KT, ... = 2)

$$N_{\delta Y}$$
, $N_{\delta T}$, $N_{\delta Z}$, $N_{\delta P}$, $N_{\delta X}$, $N_{\delta D}$

The last data are the parameters

$$N_0$$
, C_0 , C_1 , C_2 , C_3

needed for generation of the D coordinate upon option KD=2 (unused if $KD=1,\ 3$) and a set of three integer seeds for initialization of random sequences,

$$IR1$$
, $IR2$, $IR3$ (all $\simeq 10^6$)

All particles generated by MCOBJET are tagged with a (non-S) character, for further statistic purposes (e.g., with HISTO, MCDESINT).

KOBJ = 2 : Random generation of IMAX = IY * IT * IZ * IP * IX * ID particles on a hyper-grid. The input data are the number of bars in each coordinate

the spacing of the bars

the width of each bar

$$\delta Y$$
, δT , δZ , δP , δX , δD

the cut-offs, used with Gaussian densities (in units of the r.m.s. widths)

$$N_{\delta Y}$$
, $N_{\delta T}$, $N_{\delta Z}$, $N_{\delta P}$, $N_{\delta X}$, $N_{\delta D}$

This is illustrated in Fig. 7.

The last two sets of data in this option are the parameters

$$N_0, C_0, C_1, C_2, C_3$$

needed for generation of the D coordinate upon option KD= 2 (unused if KD= 1, 3) and a set of three integer seeds for initialization of random sequences, IR1, IR2, and IR3 (all $\simeq 10^6$).

All particles generated by *MCOBJET* are tagged with a (non-S) character, for further statistic purposes (see *HISTO* and *MCDESINT*).

 $\mathbf{KOBJ} = \mathbf{3}$: Distribution of IMAX particles inside a 6-D ellipsoid defined by the three sets of data (one set per 2-D phase-space)

$$\begin{array}{lll} \alpha_{Y}, & \beta_{Y}, & \frac{\varepsilon_{Y}}{\pi}, & N_{\varepsilon_{Y}} & [, & N'_{\varepsilon_{Y}}, \text{ if } N_{\varepsilon_{Y}} < 0] \\ \alpha_{Z}, & \beta_{Z}, & \frac{\varepsilon_{Z}}{\pi}, & N_{\varepsilon_{Z}} & [, & N'_{\varepsilon_{Z}}, \text{ if } N_{\varepsilon_{Z}} < 0] \\ \alpha_{X}, & \beta_{X}, & \frac{\varepsilon_{X}^{*}}{\pi}, & N_{\varepsilon_{X}} & [, & N'_{\varepsilon_{X}}, \text{ if } N_{\varepsilon_{X}} < 0] \end{array}$$

where α , β are the ellipse parameters and ε/π the rms emittance, corresponding to an elliptical frontier $\frac{1+\alpha_Y^2}{\beta_Y}Y^2+2\alpha_YYT+\beta_YT^2=\varepsilon_Y/\pi$ (idem for the (Z,P) or (X,D) planes). N_{ε_Y} , N_{ε_Z} and N_{ε_X} are the sorting cut-offs (used only for Gaussian distributions, KY,KT,...=2).

The sorting is uniform in surface (for KY = 1 or KZ = 1 or KX = 1) or Gaussian (KY = 2 or KZ = 2), and so on, as described above. A uniform sorting has the ellipse above for support. A Gaussian sorting

has the ellipse above for r.m.s. frontier, leading to $\sigma_Y = \sqrt{\beta_Y \varepsilon_Y / \pi}$, $\sigma_T = \sqrt{\frac{(1 + \alpha_Y^2)}{\beta_Y} \varepsilon_Y / \pi}$, and similar relations for σ_Z , σ_P , σ_X , σ_D .

If N_{ε} is negative, thus the sorting fills the elliptical ring that extends from $|N_{\varepsilon}|$ to N'_{ε} (rather than the inner region determined by the N_{ε} cut-off as discussed above).



Figure 7: A scheme of input parameters to MCOBJET when KOBJ=2. Top: Possible distributions of the Y coordinate. Bottom: A 2-D grid in (Y, Z) space.

OBJET: Generation of an object

OBJET is dedicated to the construction of sets of initial coordinates, in several ways.

The first datum is the reference rigidity (a negative value is allowed)

$$BORO = \frac{p_0}{q}$$

At the object, the beam is defined by a set of IMAX particles (the maximum value for IMAX is defined in the include file 'MAXTRA.H') with the initial conditions $(Y,\,T,\,Z,\,P,\,X,\,D)$ with $D=B\rho/BORO$ the relative rigidity.

Depending on the value of the next datum *KOBJ*, these initial conditions may be generated in eight different ways:

KOBJ = 1 : Defines a grid in the Y, T, Z, P, X, D space. One gives the number of points desired

with $IY \leq n_Y \dots ID \leq n_D$ such that $n_Y \times n_T \times \dots \times n_D \leq \max(IMAX)$. One defines the sampling range in each coordinate

zgoubi then generates IMAX = IY * IT * IZ * IP * IX * ID particles with initial coordinates

In this option relative rigidities will be classified automatically in view of possible further use of $\mathit{IMAGES}[Z]$ for momentum analysis and image formation.

The particles are tagged with an index IREP possibly indicating a symmetry with respect to the (X,Y) plane, as explained in option KOBJ=3. If two trajectories have mid-plane symmetry, only one will be ray-traced, while the other will be deduced using the mid-plane symmetries. This is done for the purpose of saving computing time. It may be incompatible with the use of some procedures (e.g. MCDESINT, which involves random processes).

The last datum is a reference in each coordinate, YR, TR, ZR, PR, XR, DR. For instance the reference rigidity is DR*BORO, resulting in the rigidity of a particle of initial condition I*PD to be (DR+I*PD)*BORO.

0,
$$PZ$$
, $2*PZ$, ..., $(IZ-1)*PZ$, 0, PP , $2*PP$, ..., $(IP-1)*PP$,

This object results in shorter outputs/CPU-time when studying problems with Z symmetry.

KOBJ = 2: Next data: IMAX, IDMAX. Initial coordinates are entered explicitly for each trajectory. IMAX is the total number of particles. These may be classified in groups of equal number for each value of momentum, in order to fulfill the requirements of image calculations by IMAGES[Z]. IDMAX is the number of groups of momenta. The following initial conditions defining a particle are specified for each one of the IMAX particles

$$Y$$
, T , Z , P , X , D , $'A'$

where D * BORO is the rigidity (negative value allowed) and 'A' is a (arbitrary) tagging character.

The last record *IEX* (I=1, *IMAX*) contains *IMAX* times either the character "1" to indicates that the particle has to be tracked, or "-9" to indicates that the particle should not be tracked.

This option *KOBJ*= 2 may be be useful for the definition of objects including kinematic effects.

```
iiiiiii .mine KOBJ = 2.1: Same as KOBJ= 2 except for the units, meter and radian in that case. ====== KOBJ = 2.01: Same as KOBJ= 2 except for the units, meter and radian in that case. ¿¿¿¿¿¿¿ .r499
```

iiiiiii .mine **KOBJ = 3 :** This option allows the reading of initial conditions from an **======= KOBJ = 3 :** This option allows the reading of initial conditions from an ¿¿¿¿¿¿; .r499 external input file *FNAME*. The next three data lines are :

```
IT1, IT2, ITStep
IP1, IP2, IPStep
YF, TF, ZF, PF, SF, DPF, TiF, TAG
YR, TR, ZR, PR, SR, DPR, TiR
InitC
```

followed by the storage file name FNAME.

IT1, IT2, ITStep cause the code to read coordinates of particles number IT1 through IT2 by step ITStep.

IP1, IP2, IPStep cause the code to read coordinates belonging in the passes range IP1 through IP2, step IPStep.

YF, TF, ZF, PF, SF, DPF, TiF are scaling factors whereas YR, TR, ZR, PR, SR, DPR, TiR are references added to the values of respectively Y, T, Z, P, S, DP as read in file FNAME, so that any coordinate C = Y, T, Z... is changed into CF*C + CR. In addition a flag character TAG allows retaining only particles with identical tagging letter LET, unless TAG='* in which case it has no selection effect for instance TAG='S' can be used to retain only secondary particles following in-flight decay simulations.

If InitC= 1 ray-tracing starts from the current coordinates F(J, I),

if InitC= 0 ray-tracing starts from the initial coordinates FO(J, I), as read from file FNAME.

The file *FNAME* must be formatted in the appropriate manner. The following *FORTRAN* sequence is an instance, details and possible updates are to be found in the source file 'obj3.f':

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD')
 DO I = 1, IMAX
   READ (NL,100) LET (I), IEX(I), (FO(J,I),J=1,6), (F(J,I),J=1,6), I, IREP(I),
          LET(I), IEX(I), -1.D0+FO(1,I), (FO(J,I), J=2,MXJ),
            -1.D0+F(1,I),F(2,I),F(3,I),
           (F(J,I),J=4,MXJ),ENEKI,
           ID,I,IREP(I), SORT(I),D,D,D,D,RET(I),DPR(I),
           D, D, D, BORO, IPASS, KLEY, LBL1, LBL2, NOEL
          FORMAT(1X,
100
   LET(IT), KEX, 1.D0-FO(1,IT),(FO(J,IT),J=2,MXJ),
                A1,1X,I2,1P,7E16.8,
    1.D0-F(1,IT), (FO(J,IT),J=2,MXJ),
C2
              /,3E24.16,
    Z,P*1.D3,SAR,
C3
                      TAR,
                                DS,
              /,4E24.16,E16.8,
    KART, IT, IREP(IT), SORT(IT), X, BX, BY, BZ, RET(IT), DPR(IT),
              /,I1,2I6,7E16.8,
         EX, EY, EZ, BORO, IPASS, KLEY, (LABEL(NOEL, I), I=1,2), NOEL
C5
    5 /,4E16.8,
                          I6,1X, A8,1X, 2A10,
 ENDDO
```

where the meaning of the parameters (apart from D=dummy real, ID=dummy integer) is the following

```
LET(I) : one-character string (for tagging)IEX(I) : flag, see KOBJ= 2 and page 173
```

FO(1-6,I): coordinates D, Y, T, Z, P and path length of particle num-

ber I, at the origin. D * BORO = rigidity

F(1-6,I): id, at the current position.

IREP is an index which indicates a symmetry with respect to the median plane. For instance, if Z(I+1) = -Z(I), then normally IREP(I+1) = IREP(I). Consequently the coordinates of particle I+1 will not be obtained from ray-tracing but instead deduced from those of particle I by simple symmetry. This saves on computing time.

KOBJ= 3 can be used for reading files filled by FAISCNL, FAISTORE. If more than IMAX particles are to be read from a file, use REBELOTE.

Note: In this option, one has to make sure that input data do not conflict with possible use of the keyword *PARTICUL* that assigns mass and charge.

iiiiiii .mine KOBJ = 3.1: Same as KOBJ = 3, except for the formatting of trajectory coordinate ====== KOBJ = 3.01: Same as KOBJ = 3, except for the formatting of trajectory coordinate ¿¿¿¿¿¿ .r499 data in FNAME, namely, according to the following FORTRAN sequence

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD')

1 CONTINUE

READ (NL,*,END=10,ERR=99) Y, T, Z, P, S, D

GOTO 1

10 CALL ENDFIL

99 CALL ERREAD
```

iiiiiii .mine KOBJ = 3.2 : As for KOBJ=3.1, except for the different format ======= KOBJ = 3.02 : As for KOBJ=3.01, except for the different format ¿¿¿¿¿¿¿ .r499

where PX, PY, and PZ, are the momenta in MeV/c. Note that DPR will be ignored in this case.

iiiiiii .mine **KOBJ = 3.3**: As for **KOBJ=3.1**, except for the different format : ======= **KOBJ = 3.03**: As for **KOBJ=3.01**, except for the different format : ididitio .r499

where MASS is the mass in MeV/c and CHARGE is the charge in units of the elementary charge.

Note: For details and possible updates in the formatted read of concern in the *FORTRAN*, regarding options 3.01-3.03, see the source file 'obj3.f'.

RECOVERING FROM A CRASH

OBJET with option *KOBJ*=3[.*] can be used to recover from a job crash, when multi-turn tracking - due to computer crash or else. This is discussed in the *SCALING* section, page 76, an example of job resuming is given page 241.

 $\mathbf{KOBJ} = \mathbf{5}$: Mostly dedicated to the calculation of first order transfer matrix and various other optical parameters, using for instance *MATRIX* or *TWISS*. The input data are the coordinate sampling

The code generates 11 particles, with initial coordinates

$$0, \pm PY, \pm PT, \pm PZ, \pm PP, \pm PX, \pm PD$$

These values should be small enough, so that the paraxial ray approximation be valid. The last data line gives the reference

$$YR$$
, TR , ZR , PR , XR , DR

(with DR * BORO the reference rigidity - negative value allowed), which adds to the previous coordinate values.

KOBJ = **5.1**: Same as KOBJ = 5, except for an additional data line giving initial beam ellipse parameters and dispersions, α_Y , β_Y , α_Z , β_Z , α_X , β_X , D_Y , D_Y , D_Z , D_Z , for further transport of these using *MATRIX*, or for possible use by the *FIT*[2] procedure.

iiiiiii .mine **KOBJ** = **5.N**: Like KOBJ = **5**, except for $N \ge 2$ references needed in this case (thus N-I additional input data lines), rather than just one. Zgoubi will generate N sets of 11 particles with initial coordinates in each set taken wrt. one of the N references. ======= **KOBJ** = **5.N**: Like KOBJ = **5**, except for NN = 2 - 99 references needed in this case (thus NN-I additional input data lines), rather than just one. Zgoubi will generate NN sets of 11 particles with initial coordinates in each set taken wrt. one of the NN references. $i \in i \in i$ $i \in i$

A subsequent use of MATRIX would then cause the computation of N transport matrices.

KOBJ = 6: Mostly dedicated to the calculation of first, second and other higher order transfer coefficients and various other optical parameters, using for instance *MATRIX*. The input data are the coordinate sampling (normally taken paraxial)

to allow the building up of an object containing 61 particles (note: their coordinates can be checked by printing out into zgoubi.res using *FAISCEAU*), whereas a last data line gives the reference

$$YR$$
, TR , ZR , PR , XR , DR

(with DR * BORO the reference rigidity - negative value allowed), which adds to the previous coordinate values.

KOBJ = 7: Object with kinematics

The data and functioning are the same as for KOBJ= 1, except for the following

- *ID* is not used,
- PD is the kinematic coefficient, such that for particle number I, the initial relative rigidity D_I is calculated from the initial angle T_I following

$$D_I = DR + PD * T_I$$

while T_I is in the range

$$0, \pm PT, \pm 2 * PT, \ldots, \pm IT/2 * PT$$

as stated under KOBJ= 1

KOBJ = **8**: Generation of phase-space coordinates on ellipses.

The ellipses are defined by the three sets of data (one set per ellipse)

$$\begin{array}{lll} \alpha_Y, & \beta_Y, & \varepsilon_Y/\pi \\ \alpha_Z, & \beta_Z, & \varepsilon_Z/\pi \\ \alpha_X, & \beta_X, & \varepsilon_X/\pi \end{array}$$

where α , β are the ellipse parameters and ε / is the ellipse surface, corresponding to an ellipse with equation

$$\frac{1 + \alpha_Y^2}{\beta_Y} Y^2 + 2\alpha_Y Y T + \beta_Y T^2 = \varepsilon_Y / \pi$$

(idem for the (Z, P) or (X, D) planes).

The ellipses are centered respectively on (Y_0, T_0) , (Z_0, P_0) , (X_0, D_0) .

The number of samples per plane is respectively IX, IY, IZ. If that value is zero, the central value above is assigned.

OBJETA: Object from Monte-Carlo simulation of decay reaction [27]

This generator simulates the reactions

$$M_1 + M_2 \longrightarrow M_3 + M_4$$

and then

$$M_4 \longrightarrow M_5 + M_6$$

where M_1 is the mass of the incoming body; M_2 is the mass of the target; M_3 is an outgoing body; M_4 is the rest mass of the decaying body; M_5 and M_6 are decay products. Example:

$$p + d \longrightarrow^{3} \mathrm{He} + \eta$$
$$\eta \longrightarrow \mu^{+} + \mu^{-}$$

The first input data are the reference rigidity

$$BORO = p_0/q$$

an index IBODY which specifies the particle to be ray-traced, namely M3 (IBODY = 1), M5 (IBODY = 2) or M6 (IBODY = 3). In this last case, initial conditions for M6 must be generated by a first run of OBJETA with IBODY = 2; they are then stored in a buffer array, and restored as initial conditions at the next occurrence of OBJETA with IBODY = 3. Note that **zgoubi** by default assumes positively charged particles.

Another index, KOBJ, specifies the type of distribution for the initial transverse coordinates Y, Z; namely either uniform (KOBJ= 1) or Gaussian (KOBJ= 2). The other three coordinates T, P and D are deduced from the kinematic of the reactions.

The next data are the number of particles to be generated, *IMAX*, the masses involved in the two previous reactions.

$$M_1, M_2, M_3, M_4, M_5, M_6$$

and the kinetic energy T_1 of the incoming body (M_1) .

Then one gives the central value of the distribution for each coordinate

$$Y_0, T_0, Z_0, P_0, D_0$$

and the width of the distribution around the central value

$$\delta Y$$
, δT , δZ , δP , δD

so that only those particles in the range

$$Y_0 - \delta Y \le Y \le Y_0 + \delta Y$$
 ... $D_0 - \delta D \le D \le D_0 + \delta D$

will be retained. The longitudinal initial coordinate is uniformly sorted in the range

$$-XL < X_0 < XL$$

The random sequences involved may be initialized with different values of the two integer seeds IR_1 and IR_2 ($\simeq 10^6$).

Possible use of *PARTICUL* will have no effect: it will not change the mass and charge assumptions as set by *OBJETA*.

A series of options are available which allow the control of various of the procedures and functionalities of the code.

Some of these options are normally declared right after the object definition, for instance

- SPNTRK: switch-on spin tracking,
- *PARTICUL* to declare particle mass and charge, if for instance tracking in electric fields, or tracking spin, or in presence of synchrotron radiation energy loss simulations,

some may appear further down in the structure (in zgoubi.dat), for instance

- MCDESINT: switch-on in-flight decay, could be after a target,
- REBELOTE: for multi-turn tracking, including an extraction line section for instance,

others may normally be declared at the end of zgoubi.dat data pile, for instance

- END: end of a problem,
- FIT: fitting procedure can also appear before REBELOTE

GETFITVAL may appear before the object definition (keyword [MC]OBJET, normally the first in **zgoubi** input data list). This is the case if variables prior saved following a 'FIT[2]' procedure and then read back using GETFITVAL, happen to belong in the [MC]OBJET data list.

SYSTEM as well, may appear anywhere in the data list.

BINARY: BINARY/FORMATTED data converter

This procedure translates field map data files from "BINARY" to "FORMATTED" – in the FORTRAN sense, or the other way.

The keyword is followed by, next data line,

the number of files to be translated [READ format option, a single digit integer, optional], number of data columns in the file, number of header lines in the file.

Fortran READ format, case of formatted input file:

If J is not given, the NCOL arrangement should be consistent with the following FORTRAN READ statement :

```
READ (unit=ln,*) (X7(I),I=1,NCOL) If J=1, NCOL should be consistent with the following FORTRAN READ statement: READ (unit=ln,fmt='(1x,ncol*E11.2)') (X7(I),I=1,NCOL)
```

Fortran READ format, case of formatted input file:

Data are expected to have been recorded under the form of Ncol column rows.

Then follow, line by line, the NF names of the files to be translated.

Iff a file name begins with the prefix "B_" or "b_", it is assumed "binary", and hence converted to "formatted", and given the same name after suppression of the prefix "B_" or "b_". Conversely, iff the file name does not begin with "B_" or "b_", the file is presumed "formatted" and hence translated to "binary", and is given the same name after addition of the prefix "b_".

In its present state, the procedure *BINARY* only supports a limited number of read/write formats. Details concerning I/O formatting can be found in the *FORTRAN* file 'binary.f'.

END or FIN: End of input data list

The end of a problem, or of a set of several problems stacked in the data file, should be stated by means of the keywords *FIN* or *END*.

Any information following these keywords will be ignored.

In some cases, these keywords may cause some information to be printed in zgoubi.res, for instance when the keyword *PICKUPS* is used.

ERRORS: Injecting errors

UNDER DEVELOPMENT

The keyword *ERRORS* allows injecting diverse types of errors in optical elements, including field and positionning defects. Uniform and Gaussian distribution laws are available.

Optical elements concerned can be discriminated using one or both of their labels.

ERRORS is under development, functionalities at the moment are the following:

MULTIPOL can be injected field defects.

FIT, FIT2: Fitting procedure

The keywords FIT, FIT2 allow the automatic adjustment of up to 20 variables, for fitting up to 20 constraints.

FIT was implemented in 1985, drawn from the matrix transport code BETA [28]. FIT2 is a simplex method (Nelder-Mead method), it has been implemented in 2007 [29]. One or the other may converge faster, or may have some advantages/disadvantages, depending on the problem.

Any physical parameter of any element in the zgoubi.dat data list may be varied. Examples of available constraints are, amongst others:

- trajectory coordinates in the F(J, I) array, I = particle number, J = coordinate number = 1 to 7 for respectively D, Y, T, Z, P, S =path length, time;
- spin coordinates;
- any of the 6×6 coefficients of the first order transfer matrix $[R_{ij}]$ as defined in the keyword MATRIX;
- any of the $6 \times 6 \times 6$ coefficients of the second order array $[T_{ijk}]$ as defined in MATRIX;
- any of the 4×4 coefficients of the beam σ -matrix
- transmission efficiency of an optical channel.
- tunes $\nu_{Y,Z}$ and periodic betatron functions $\beta_{Y,Z}$, $\alpha_{Y,Z}$, $\gamma_{Y,Z}$, as computed in the coupled hypothesis [30].

A full list of the constraints available is given in the table page 62.

FIT, FIT2 are compatible with the use of (i.e., can be encompassed in) REBELOTE for successive fitting trials using various sets of parameters (option K = 22 in REBELOTE).

VARIABLES

The first input data in *FIT*[2] is the number of variables *NV*. A variable is defined by a line of data comprised of

IR = number of the varied element in the structure

IP = number of the physical parameter to be varied in this element

XC = coupling parameter. Normally XC = 0. If $XC \neq 0$, coupling will occur (see below)

followed by, either

DV = allowed relative range of variation of the physical parameter IP

or

[Vmin, Vmax] = allowed interval of variation of the physical parameter IP

Numbering of the Elements (IR):

The elements (*i.e.*, keywords *DIPOLE*, *QUADRUPO*, etc.) as read by **zgoubi** in the zgoubi.dat sequence are assigned a number. which follows their sequence in the data file. It is that very number, *IR*, that the *FIT[2]* procedure uses. A simple way to get *IR* once the zgoubi.dat file has been built, is to do a preliminary run, since the first thing **zgoubi** does is copy the sequence from zgoubi.dat into the result file zgoubi.res, with all elements numbered.

Numbering of the Physical Parameters (IP):

All the data that follow a keyword are numbered - except for SCALING, see below.

With most of the keywords, the numbering follows the principle hereafter:

Input data	Numbering for FIT		
'KEYWORD'			
first line	1, 2, 3,, 9		
second line	10, 11, 12, 13,, 19		
this is a comment	a line of comments is skipped		
next line	20, 21, 22,, 29		
and so on			

The examples of QUADRUPO (quadrupole) and TOSCA (Cartesian or cylindrical mesh field map) are as follows.

Input data	Numbering for FIT
'QUADRUPO'	
IL	1
XL, R_0, B	10, 11, 12
X_E, λ_E	20, 21
$NCE, C_0, C_1, C_2, C_3, C_4, C_5$	30, 31, 32, 33, 34, 35, 36
X_S, λ_S	40, 41
$NCS, C_0, C_1, C_2, C_3, C_4, C_5$	50, 51, 52, 53, 54, 55, 56
XPAS	60
KPOS, XCE, YCE, ALE	70, 71, 72, 73
'TOSCA'	
IC, IL	1, 2
BNORM, X- [, Y-, Z-]NORM	10, 11 [, 12, 13]
TIT	This is text
IX, IY, IZ, MOD	20, 21, 22, 23
FNAME	This is text
$ID, A, B, C [A', B', C', \text{ etc. if } ID \ge 2]$	30, 31, 32, 33 [34, 35, 36 [, 37, 38, 39] if $ID \ge 2$]
IORDRE	40
XPAS	50
KPOS, XCE, YCE, ALE	60,61,62,63

A different numbering, fully sequential, has been adopted in the following elements:

AIMANT, DIPOLE, EBMULT, ELMULT, MULTIPOL.

It is illustrated here after in the case of MULTIPOL and DIPOLE-M.

Input data	Numbering for FIT
'MULTIPOL'	
0	1
365.760 10.0 7.5739 1.4939 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0	2, 3, 4, 5,, 13
10.0 4.0 0.80 0.0 0.0 0.0 0.0 0. 0. 0. 0.	14, 15,, 24
$NC, C_0, C_1, C_2, C_3, C_4, C_5$, shift	25, 26, 27, 28, 29, 30, 31, 32
10.0 4.0 0.80 0.0 0.0 0.0 0.0 0. 0. 0. 0.	33, 34,, 43
$NC, C_0, C_1, C_2, C_3, C_4, C_5$, shift	44, 45, 46, 47,, 51
0. 0. 0. 0. 0. 0. 0. 0. 0. 0.	52, 53, 54,, 61
step size	62
KPOS, XCE, YCE, ALE	63, 64, 65, 66

Input data	Numbering for FIT
'DIPOLE-M'	_
NFACE, IC, IL	1, 2, 3
IAMAX, IRMAX	4, 5
B_0, N, B, G	6, 7, 8, 9
AT, ACENT, RM, RMIN, RMAX	10, 11, 12, 13, 14
λ , ξ	15,16
$NC, C_0, C_1, C_2, C_3, C_4, C_5$, shift	17, 18, 19, 20, 21, 22, 23, 24
ω , θ , R_1 , U_1 , U_2 , R_2	25, 26, 27, 28, 29, 30
etc.	

Parameters in SCALING also have a sequential numbering, yet some positions are skipped, this is illustrated in the example hereafter which covers all possible working modes of SCALING (all details regarding the numbering can be found in the FORTRAN subroutine rscal.f):

Input data	Numbering for FIT	Quantities to be varied (see SCALING for details)
'SCALING'		,
1 9	1 2	Non relevant
AGSMM *AF *BF		Keywords concerned, their labels
-1 3 12 1. 13 1. 14 1.	3 4 5	dB1, dB2, dB3 parameters in AGSMM
7.2135	6	Field factor
1	7	Timing
AGSMM *AD *BD	,	······································
-1 3 12 1. 13 1. 14 1.	8 9 10	
7.2135	11	
1	12	
AGSMM *CF	12	
-1 3 12 1. 13 1. 14 1.	13 14 15	
7.2135	16	
1	17	
AGSQUAD QH_*	17	
3		
$\begin{bmatrix} 0.605 & 0.77 & 0.879 \end{bmatrix}$	18 19 20	Field factor
1 2000 10000	21 22 23	Timing
AGSQUAD QV_*	21 22 23	Tilling
3		
0.587 0.83 0.83	24 25 26	
1 2000 10000	27 28 29	
MULTIPOL COH1	21 20 2)	
1.10		No numbering if 1.10 type of option
./Csnk3D/bump_centered.scal		
1 2		
MULTIPOL COH2		
1.10		
./Csnk3D/bump_centered.scal		
14		
MULTIPOL KICKH KICKV		
2	20 21	E' 116 .
0.1 0.3	30 31	Field factor
	32 33	Timing
MULTIPOL -1		
	2.4	
0.72135154291	34	
1	35	

Coupled Variables (XC)

Coupling a variable parameter to any other parameter in the structure is possible. This is done by giving XC a value of the form r.ppp where the integer part r is the number of the coupled element in the structure (equivalent to IR, see above), and the decimal part ppp is the number of its parameter of concern (equivalent to IP, see above) (if the parameter number is in the range 1, 2, ..., 9 (resp. 10, 11, ... 19 or 100, ...), then ppp must take the form 00p (resp. 0pp, ppp)). For example, XC = 20.010 is a request for coupling with the parameter number 10 of element number 20 of the structure, while XC = 20.100 is a request for coupling with the parameter number 100 of element 20.

An element of the structure which is coupled (by means of $XC \neq 0$) to a variable declared in the data list of the FIT[2] keyword, needs not appear as one of the NV variables in that data list (this would be redundant information).

XC can be either positive or negative. If XC > 0, then the coupled parameter will be given the same value as the variable parameter (for example, symmetric quadrupoles in a lens triplet will be given the same field). If XC < 0, then the coupled parameter will be given a variation opposite to that of the variable, so that the sum of the two parameters stays constant (for example, an optical element can be shifted while preserving the length of the structure, by coupling together its upstream and downstream drift spaces).

Variation Range

There are two ways to define the allowed range for a variable, as follows.

- (i) DV : For a variable (parameter number IP under some keyword) with initial value v, the FIT[2] procedure is allowed to explore the range $v \times (1 \pm DV)$.
- (i) $[v_{min}, v_{max}]$: This specifies the allowed interval of variation.

CONSTRAINTS

The next input data in *FIT[2]* is the number of constraints, *NC*. A list of the available constraints is given in the table page 62; adding or changing a constraint resorts to the *FORTRAN* file ff.f.

Each constraint is defined by the following list of data:

```
IC[.IC2] = type of constraint (see table p. 62).
```

 $I, J = \text{constraint } (i.e., R_{ij}, \text{determinant, tune }; T_{ijk}; \sigma_{ij}; \text{trajectory } \#I \text{ and coordinate } \#J)$

IR = number of the keyword at the exit of which the constraint applies

V = desired value of the constraint

W = weight of the constraint (smaller W for higher weight)

NP NP additional parameters, values PR_{1-NP} , defining the constraint

- IC=0: The coefficients σ_{11} (σ_{33}) = horizontal (vertical) beta values and σ_{22} (σ_{44}) = horizontal (vertical) derivatives ($\alpha = -\beta'/2$) are obtained by transport of their initial values at line start as introduced using for instance *OBJET*, KOBJ=5.1.
- IC=0.1: Beam parameters: $\sigma_{11}=\beta_Y, \sigma_{12}=\sigma_{21}=-\alpha_Y, \sigma_{22}=\gamma_Y, \sigma_{33}=\beta_Z, \sigma_{34}=\sigma_{43}=-\alpha_Z, \sigma_{44}=\gamma_Z$; periodic dispersion: $\sigma_{16}=D_Y, \sigma_{26}=D_Y', \sigma_{36}=D_Z, \sigma_{46}=D_Z'$, all quantities derived by assuming periodic structure and identifying the first order transfer matrix with the form $Icos\mu+Jsin\mu$.
- IC=1, 2: The coefficients R_{ij} and T_{ijk} are calculated following the procedures described in MATRIX, option IFOC=0. The fitting of the $[R_{ij}]$ matrix coefficients supposes the tracking of particles with paraxial coordinates, normally defined using OBJET option KOBJ=5 or 6.

T	Parameters defining the constraints			Recommended			
Type of constraint	IC	I	J	Constraint	Additional parameter(s) $NP \mid PR_{1-NP} \text{ value(s)}$		[MC]OBJET, and other comments
σ -matrix	0	1 - 6	1 - 6	σ_{IJ} $(\sigma_{11}=\beta_Y,\sigma_{21,\ 12}=\alpha_Y,\text{etc.})$			OBJET/KOBJ=5,6
Periodic parameters (N=1-9 for MATRIX block 1-9)	0.N	1 - 6 7 8 9 10	1 - 6 any any any any	$\sigma_{IJ} (\sigma_{11} = \cos \mu_Y + \alpha_Y \sin \mu_Y, \text{ etc.})$ $Y\text{-tune} = \mu_Y / 2\pi$ $Z\text{-tune} = \mu_Z / 2\pi$ $\cos(\mu_Y)$ $\cos(\mu_Z)$			OBJET/KOBJ=5.N
First order transport coeffs.	1	$ \begin{array}{c c} 1 - 6 \\ 7 \\ 8 \end{array} $	$egin{array}{c} 1-6 \ & \mathrm{i} \ & \mathrm{j} \end{array}$	Transport coeff. R_{IJ} $i \neq 8$: YY-determinant; i=8: YZ-det. $j \neq 7$: ZZ-determinant; j=7: ZY-det.			OBJET/KOBJ=5
Second order transport coeffs.	2	1-6	11 – 66	Transport coeff. $T_{I,j,k}$ $(j = [J/10], k = J - 10[J/10])$			OBJET/KOBJ=6
Trajectory	3	1 - IMAX	1 - 7	F(J,I)			[MC]OBJET
coordinates		-1	1 - 7	$< F(J,i) >_{i=I1,I2}$	$\{_{2}^{0}$	$ig _{I_1=I_2}$	$\Leftrightarrow 1, IMAX \\ 1 \le I_1 \le I_2 \le IMAX$
(I = particle number; J=1-7 for D,Y,T,Z,P,S,time)		-2 -3 -4	$egin{array}{c} 1 - 7 \ 1 - 7 \ 1 - 7 \end{array}$	$Sup(F(J,i))_{i=1,IMAX}$ $Dist [F(J,I)_{i=11,12}]$ $Dist [PU_i, i=1, N]$	3 2	$I_1, I_2, \Delta I$ $NOEL_A, NOEL_B$	$1 \le I_1 \le I_2 \le IMAX$ PU range
	3.1 3.2 3.4 3.5	$ \begin{array}{c c} 1 - IMAX \\ 1 - IMAX \\ 1 - IMAX \\ 1 - IMAX \end{array} $	1 - 7 $1 - 7$ $1 - 7$ $1 - 7$	F(J,I) - FO(J,I) F(J,I) + FO(J,I) F(J,I) - F(J,K) (F(J,I) - F(J,K))/F(J,K)	1 1	K K	$K \le IMAX$ $K \le IMAX$
Ellipse parameters	4	1 - 6	1 - 6	$\sigma_{IJ} \;\; (\sigma_{11}=eta_Y, \ \sigma_{12}=\sigma_{21}=lpha_Y, ext{etc.})$			OBJET/KOBJ=8 ; MCOBJET/KOBJ=3
Number of particles	5	$ \begin{array}{r} -1 \\ 1 - 3 \\ 4 - 6 \end{array} $	any any any	$N_{survived}/ ext{IMAX} \ N_{in \; \epsilon_{Y,Z,X}}/N_{survived} \ N_{in \; best \; \epsilon_{Y,Z,X,rms}}/N_{survived}$	1	ϵ/π	OBJET MCOBJET MCOBJET
Coordinates & fields, across optical elements	7.1 7.2 7.3	1 - IMAX 1 - IMAX 1 - IMAX	$ \begin{array}{r} 1 - 7 \\ 1 - 7 \\ 1 - 7 \end{array} $	min. (1) or max. (2) of $F(J, I)$ $\max(F(J, I)) - \min F(J, I)$ $\min F(J, I)) + \max(F(J, I))$	1	1-2	[MC]OBJET
$(J=1, 2, 3 \text{ for } B_{X, Y, Z})$	7.6 7.7 7.8 7.9	$ \begin{array}{c c} 1 - IMAX \\ 1 - IMAX \\ 1 - IMAX \\ 1 - IMAX \end{array} $	1 - 3 $1 - 3$ $1 - 3$ $1 - 3$	min. (1) or max. (2) value of B_J $\max(B_J)$ - $\min(B_J)$ $\min(B_J)$ + $\max(B_J)$ $\int B_J ds$	1	1-2	
Spin	10 10.1	$ \begin{vmatrix} 1 - IMAX \\ 1 - IMAX \end{vmatrix} $	1 - 4 $1 - 3$	$ S_{X,Y,Z}(I), \vec{S}(I) S_{X,Y,Z}(I) - SO_{X,Y,Z}(I) $			[MC]OBJET +SPNTRK

IC=3: If $1 \le I \le IMAX$ then the value of coordinate type J (J=1,6 for respectively D, Y, T, Z, P, S) of particle number I ($1 \le I \le IMAX$) is constrained. However I can take special meaning, as follows.

I=-1: the constraint is the average value of coordinate of type J over particles $[I_1,I_2]$,

I = -2: the constraint is the maximum value of coordinate of type J,

I=-3: the constraint is the distance between particles I_1-I_2 (step ΔI).

I=-4: take the average of the F(J,i) coordinate (J=1-7 for D,Y,T,Z,P,S,time) over (I2-I1+1) particles in the range i=I1-I2, get it at N different pickup locations $PU_1,PU_2,...,PU_N$. The constraint is, minimizing the distance between these averages, $Dist\left[< F(J,i)>_{i=I1,I2}\right]_{PU_{1-N}}$ (Ex.: minimize the difference between PU records, for a series of PUs along a beamline). If the number of locations is 997 (i.e., N+2=999) then all PUs upstream of IR are accounted for. This constraint requires declaring pick-ups using PICKUPS keyword, their locations are as numbered in the data list in zgoubi.res.

IC=3.1: Absolute value of the difference between local and initial J-coordinate of particle I (convenient e.g. for closed orbit search).

IC=3.2: Absolute value of the sum of the local and initial J-coordinate of particle number I.

- IC=3.4: Absolute value of the difference between local J-coordinates of particles respectively I and K.
- IC=3.5: Difference between local J-coordinates of particles respectively I and K, relative to J-coordinate of particle K.
- IC=4: The coefficients σ_{11} (σ_{33}) = horizontal (vertical) beta values and σ_{22} (σ_{44}) = horizontal (vertical) derivatives ($\alpha = -\beta'/2$) are derived from an ellipse match of the current particle population (as generated for instance using MCOBJET, KOBJ=3).

The fitting of the $[\sigma_{ij}]$ coefficients supposes the tracking of a relevant population of particles within an appropriate emittance.

- *IC*=5: The constraint value is the ratio of particles (over *IMAX*). Three cases possible:
 - I = -1, ratio of particles still on the run.
- $I=1,\ 2,\ 3$, maximization of the number of particles encompassed within a given I-type (for respectively $Y,\ Z,\ D$) phase-space emittance value. Then, NP=1, followed by the emittance value. The center and shape of the ellipse are determined by a matching to the position and shape of the particle distribution.
- $I=4,\ 5,\ 6,$ same as previous case, except for the ellipse, taken to be the *rms* matched ellipse to the distribution. Thus NP=0.
- IC=7 series: The quantity to be constrained is taken *inside* the optical element with number IR (see page 61).
- IC=7.1: Minimum or maximum value as reached by coordinate J of particle number I.
- IC=7.2: Maximum minus minimum of the value of coordinate J of particle number I.
- IC=7.3: Maximum plus minimum of the value of coordinate J of particle number I.
- IC=7.6: Minimum (PR=1) or maximum (PR=2) value as reached by the X, Y or Z component of the field along the trajectory of particle number I.
- IC=7.7: Maximum minus minimum of the values taken by the X, Y or Z component of the field along the trajectory of particle number I.
- IC=7.8: Maximum plus minimum of the values taken by the X, Y or Z component of the field along the trajectory of particle number I.
- IC=7.9: Integral of the X, Y or Z component of the field as experienced by particle number I, across the optical element.
- IC=10: If $1 \le I \le IMAX$ then the value of coordinate type J (J=1,3 for respectively S_X, S_Y, S_Z) of particle number I is constrained.
- IC=10.1: Difference between final and initial *J*-spin coordinate of particle *I* (convenient *e.g.* for \vec{n}_0 spin vector search).

OBJECT DEFINITION

Depending on the type of constraint (see table p. 62), constraint calculations are performed either from transport coefficient calculation and in such case require OBJET with either KOBJ = 5 or KOBJ = 6, or from particle distributions and in this case need object definition using for instance OBJET with KOBJ = 8, MCOBJET with KOBJ = 3.

THE FITTING METHODS

The FIT procedure was drawn from the matrix transport code BETA [28]. It is a direct sequential minimization of the quadratic sum of all errors (i.e., differences between desired and actual values for the NC constraints), each normalized by its specified weight W (the smaller W, the stronger the constraint).

The step sizes for the variation of the physical parameters depend on their initial values, and cannot be accessed by the user. At each iteration, the optimum value of the step size, as well as the optimum direction of variation, is determined for each one of the *NV* variables. Then follows an iterative global variation of all *NV* variables, until the minimization fails which results in a next iteration on the optimization of the step sizes.

The FIT2 procedure is based on the Nelder-Mead method, it has various specificities, details can be found in Ref. [29].

The optimization process may be stopped by means of a penalty value, or a maximum number of iterations on the step size or on the call to the function.

COMBINING FIT[2] AND REBELOTE

FIT[2] may be followed by the keyword REBELOTE. This allows for instance executing again the fitting procedure, following a change, by REBELOTE, in the value of some parameter in zgoubi.dat data list.

An example is given page 223.

OPTIONS

FIT and FIT2 accept various options, as follows.

- 'nofinal' option: a request to avoid a final run that would normally follow the completion of the fit, allowing for the variable values as just determined by FIT[2]. By default, i.e., if 'nofinal' does not appear in the FIT[2] data list, then that final run does occur.
- 'save' [, FileName] option : a request for the variable values as resulting from FIT[2] to be saved, by default in zgoubi.FITVALS.out, or in FileName file if the latter is specified following the 'save' instruction.
- Penalty: value of the penalty to be reached, following what the *FIT*[2] procedure will be considered completed, and thus stopped.
- ITER: maximum allowed number of "calls to the function" (namely, (recursive) calls to zgoubi). Once that number is reached, *FIT[2]* is stopped, regardless of a possible "penalty" value.

An example using all five options, "nofinal", "save [FileName]", "penalty" and "ITER", is given in page 224.

GASCAT: Gas scattering

Modification of particle momentum and velocity vector, performed at each integration step, under the effect of scattering by residual gas.

Installation is to be completed.

GETFITVAL: Get values of variables as saved from former FIT[2] run

This keyword allows reading, from a file whose name needs be specified, parameter values to be assigned to optical elements in zgoubi.dat.

That file is expected to contain a copy-paste of the data under the FIT[2] procedure as displayed in zgoubi.res, normally under the form

```
STATUS OF VARIABLES (Iteration #
                                                  95)
 LMNT VAR PARAM MINIMUM INITIAL
                                                      FINAL
                                                                      MIMIXAM
                                                                                     STEP
                                                                                                 NAME
                                                                                                                LBL1 LBL2
         1 4 -3.000E+03 762.
                                                     761.9484791 3.000E+03 1.254E-05 MULTIPOL HKIC DHCB02
          2 4 -1.000E+03 -231. -230.9846875 1.000E+03 4.182E-06 MULTIPOL HKIC DHCB02
3 4 -1.000E+03 -320. -319.8554171 1.000E+03 4.182E-06 MULTIPOL VKIC DVCB02
4 4 -1.000E+03 528. 527.7249064 1.000E+03 4.182E-06 MULTIPOL VKIC DVCB08
  182
  146
         5 4 -3.000E+03
6 4 -1.000E+03
7 4 -1.000E+03
                                          308. 307.6860565 3.000E+03 1.254E-05 MULTIPOL -114. -113.8490362 1.000E+03 4.182E-06 MULTIPOL
  615
                                                                                                                  HKIC DHCF02
  651
                                                                                                                  HKIC DHCF08
                                         -78.9 -78.88730937 1.000E+03 4.182E-06 MULTIPOL
  616
                                                                                                                  VKIC DVCF02
                       -1.000E+03
           8 4
                                         212. 211.8789183 1.000E+03 4.182E-06 MULTIPOL
                                                                                                                  VKIC DVCF08
  652
  STATUS OF CONSTRAINTS
  TYPE I J LMNT#
                                  DESIRED
                                                    WEIGHT
                                                                          REACHED
                                                                                                KI2
                                                                                                           * Parameter(s)
    3 1 2 127 0.0000000E+00 1.0000E+00 1.0068088E-08 6.0335E-01 * 0:

3 1 3 127 0.0000000E+00 1.0000E+00 7.0101405E-09 2.9250E-01 * 0:

3 1 4 127 0.0000000E+00 1.0000E+00 2.9184383E-10 5.0696E-04 * 0:
     3 1 5 127 0.0000000E+00 1.0000E+00 3.1142381E-10 5.7727E-04 *
3 1 2 436 0.0000000E+00 1.0000E+00 3.8438378E-09 8.7944E-02 *
3 1 3 436 0.0000000E+00 1.0000E+00 1.5773011E-09 1.4808E-02 *
#
                                                                                                                0:
     3 1 4 436 0.0000000E+00 1.0000E+00 2.2081272E-10 2.9022E-04 *
     3 1 5 436 0.0000000E+00 1.0000E+00 5.7930552E-11 1.9975E-05 * Function called 1859 times
#
#
           1.68006E-16 Busy...
```

A '#' at the beginning of a line means it is commented, thus it will not be taken into account. However a copy-paste from zgoubi.res (which is the case in the present example) would not not need any commenting. Since some of the FIT[2] variables may belong in [MC]OBJET, GETFITVAL may appear upstream of [MC]OBJET in zgoubi.dat, to allow updating the latter.

Note that, if the 'nofinal' option is not set in FIT[2] (see page 64), then, once completed, FIT[2] will be followed by a final run of zgoubi.dat with the variable values as resulting from FIT[2]. In that case, for that final run, GETFITVAL will be inhibited so avoid overridding these updated variable values.

MCDESINT: Monte-Carlo simulation of in-flight decay[31]

As soon as MCDESINT appears in a structure (normally, after OBJET or after CIBLE), in-flight decay simulation starts. It must be preceded by PARTICUL for the definition of mass M_1 and COM lifetime τ_1 . The two-body decay simulated is

$$1 \longrightarrow 2 + 3$$

The decay is isotropic in the center of mass. 1 is the incoming particle, with mass M_1 , momentum $p_1 = \gamma_1 M_1 \beta_1 c$ (relative momentum $D_1 = \frac{p_1}{q} \frac{1}{BORO}$ with BORO = reference rigidity, defined in [MC]OBJET), and position Y_1, Z_1 in the **zgoubi** frame. 2 and 3 are decay products with respective masses and momenta M_2, M_3 and $p_2 = \gamma_2 M_2 \beta_2 c$, $p_3 = \gamma_3 M_3 \beta_3 c$.

The decay length s_1 of particle 1 is related to its center of mass lifetime τ_1 by

$$s_1 = c\tau_1 \sqrt{\gamma_1^2 - 1}$$

The path length s up to the decay point is then calculated from a random number $0 < R_1 \le 1$ by using the exponential decay formula

$$s = -s_1 \ell n R_1$$

After decay, particle 2 will be ray-traced with assumed positive charge, while particle 3 is discarded. Its scattering angles in the center of mass θ^* and ϕ are generated from two other random numbers $0 < R_2 \le 1$ and $0 < R_3 \le 1$ by

$$\theta^* = a\cos(1 - 2R_2) \qquad (0 < \theta^* \le \pi)$$

$$\phi = 2\pi R_3 \qquad (0 < \phi < 2\pi)$$

 ϕ is a relativistic invariant, and θ in the laboratory frame (Fig. 8) is given by

$$\tan \theta = \frac{1}{\gamma_1} \frac{\sin \theta^*}{\frac{\beta_1}{\beta_2^*} + \cos \theta^*}$$

 β_2^* and momentum p_2 are given by

$$\gamma_2^* = \frac{M_1^2 + M_2^2 - M_3^2}{2M_1 M_2}$$

$$\gamma_2 = \gamma_1 \gamma_2^* \left(1 + \beta_1 \beta_2^* \cos \theta^* \right)$$

$$\beta_2 = \left(1 - \frac{1}{\gamma_2^2} \right)^{1/2}$$

$$p_2 = M_2 \sqrt{\gamma_2^2 - 1}$$

Finally, θ and ϕ are transformed into the angles T_2 and P_2 in the **zgoubi** frame, and the relative momentum takes the value $D_2 = \frac{p_2}{q} \frac{1}{BORO}$ (where BORO is the reference rigidity, see OBJET), while the starting position of M_2 is (Y_1, Z_1, s_1) .

The decay simulation by **zgoubi** satisfies the following procedures. In optical elements and field maps, after each integration step *XPAS*, the actual path length of the particle, F(6, I), is compared to its limit path length s. If s is passed, then the particle is considered as having decayed at $F(6, I) - \frac{XPAS}{2}$, at a position obtained by a linear translation from the position at F(6, I). Presumably, the smaller *XPAS*, the smaller the error on position and angles at the decay point.



Figure 8: At position $M(X_1, Y_1, Z_1)$, particle 1 decays into 2 and 3; **zgoubi** then proceeds with the computation of the trajectory of 2, while 3 is discarded. θ and ϕ are the scattering angles of particle 2 relative to the direction of the incoming particle 1; they transform to T_2 and P_2 in **zgoubi** frame.

In ESL and CHANGREF, F(6, I) is compared to s at the end of the element. If the decay occurs inside the element, the particle is considered as having decayed at its actual limit path length s, thus its coordinates at s are recalculated by translation.

The limit path length of all particles (I=1, IMAX) is stored in the array FDES(6,I). For further statistical purposes (e.g., use of HISTO) the daughter particle 2 is tagged with an 'S' standing for "secondary". When a particle decays, its coordinates D, Y, T, Z, P, s, time at the decay point are stored in FDES(J,I), J=1,7.

A note on negative drifts:

The use of negative drifts with MCDESINT is allowed and correct. For instance, negative drifts may occur in a structure for some of the particles when using CHANGREF (due to the Z-axis rotation or a negative XCE), or when using DRIFT with XL < 0. Provision has been made to take it into account during the MCDESINT procedure, as follows.

If, due to a negative drift, a secondary particle reaches back the decay location of its parent particle, then the parent particle is "resurrected" with its original coordinates at that location, the secondary particle is discarded, and ray-tracing resumes in a regular way for the parent particle which is again allowed to decay, after the same path length. This procedure is made possible by prior storage of the coordinates of the parent particles (in array FDES(J, I)) each time a decay occurs.

Negative steps (XPAS < 0) in optical elements are not compatible with MCDESINT.

OPTICS: Write out optical functions

OPTICS normally appears next to object definition, it normally works in conjunction with element label(s). *OPTICS* causes the transport and write out, in zgoubi.res, of the 6×6 beam matrix, following options *KOPT* and 'label', below.

IF KOPT=0: Off

IF KOPT=1: Will transport the optical functions with initial values as specified in OBJET, option KOBJ=5.1.

Note: The initial values in *OBJET[KOBJ=5.1]* may be the periodic ones, as obtained, for instance, from a first run using *MATRIX[IFOC=11]*.

A second argument, 'label', allows

- if *label* = *all* : printing out, into zgoubi.res, after all keywords of the zgoubi.dat structure,
- otherwise, printing out at all keyword featuring $LABEL \equiv label$ as a first label (see section 4.6.5, page 169, regarding the labelling of keywords).

An optional third argument, *IMP*=1, or equivalently the command 'PRINT', will cause saving of the transported optical functions into file zgoubi.OPTICS.out.

About the source code:

The program beamat ensures the transport of the beam matrix along the zgoubi.dat sequence. beamat is called by optics, itself called after each optical element, in the program zgoubi.

The starting beam matrix value is in the array FI, initialized by *OBJET[KOBJ=5.1]*, program obj5. The array F0 contains the running beam matrix.

The program beaimp prints to zgoubi.res, whereas optimp prints to zgoubi.OPTICS.out. Both are called from optics.

OPTIONS: Global options

OPTIONS allows switching various options.

Available, for now:

- Inhibit (most of) write statements to zgoubi.res Form of the statement : "WRITE -1"

Back to normal: "WRITE +1"

ORDRE: Taylor expansions order

The position \vec{R} and velocity \vec{u} of a particle are obtained from Taylor expansions as described in eq. (1.2.4). By default, these expansions are up to the fifth order derivative of \vec{u} ,

$$\vec{R}_1 \approx \vec{R}_0 + \vec{u}\Delta s + \dots + \vec{u}^{(5)} \frac{\Delta s^6}{6!}$$

 $\vec{u}_1 \approx \vec{u} + \vec{u}'\Delta s + \dots + \vec{u}^{(5)} \frac{\Delta s^5}{5!}$

which corresponds to fourth order derivatives of fields \vec{B} , eq. (1.2.8). and of \vec{E} , eq. (1.2.13).

However, third or higher order derivatives of fields may be zero in some optical elements, for instance in a sharp edge quadrupole. Also, in several elements, no more than first and second order field derivatives are implemented in the code. One may also wish to save on computation time by limiting the time-consuming calculation of lengthy (while possibly ineffective in terms of accuracy) Taylor expansions.

In that spirit, the purpose of *ORDRE*, option IO = 2 - 5, is to allow for expansions to the $\vec{u}^{(n)}$ term in eq. 1.2.4. Default functioning is IO = 4, stated in *FORTRAN* file block.f.

Note the following:

As concerns the optical elements

DECAPOLE, DODECAPO, EBMULT, ELMULT, MULTIPOL, OCTUPOLE, QUADRUPO, SEXTUPOL

field derivatives (see eq. 1.2.10 p. 19, eq. 1.2.15 p. 21,) have been installed in the code according to $\vec{u}^{(5)}$ Taylor development order; it may not be as complete for other optical elements. In particular, in electric optical elements field derivatives (eq. 1.2.15) are usually provided to no more than second order, which justifies saving on computing time by means of *ORDRE*, so to avoid pushing Taylor expansions as high as $\vec{u}^{(5)}$.

NOTE: see also the option *IORDRE* in field map declarations (*DIPOLE-M*, *TOSCA*, etc.).

PARTICUL: Particle characteristics

Since **zgoubi** works using the rigidity, (BORO, as declared in [MC]OBJET), PARTICUL only needs be introduced (normally, following [MC]OBJET in the input data file zgoubi.dat) when the definition of some characteristics of the particles (mass, charge, gyromagnetic factor, life-time in the center of mass) is needed, as is the case when using the following procedures:

CAVITE : mass, charge

MCDESINT: mass, COM life-timeSPNTRK: mass, gyromagnetic factor

SRLOSS: mass, chargeSYNRAD: mass, chargeElectric and Electro-Magnetic elements: mass, charge

The declaration of *PARTICUL* must **precede** these keywords.

If *PARTICUL* is omitted, which is in general the case when ray-tracing ions in purely magnetic optical assemblies, then **zgoubi**, since it only knows the rigidity, will skip the computation of such quantities as time of flight.

REBELOTE: 'Do it again'

When REBELOTE is encountered in the input data file, the code execution jumps,

- either back to the beginning of the data file the default behavior,
- or, if option K=99.1 or K=99.2, back to a particular LABEL.

Then NPASS-1 passes (from LABEL to REBELOTE) follow.

As to the last pass, number *NPASS+1*, there are two possibilities :

- either it also encompasses the whole LABEL to REBELOTE range,
- or, upon request (option K=99.2), execution may exit that final pass upstream of *REBELOTE*, at a location defined by a second dedicated *LABEL* placed between the first above mentioned *LABEL*, and *REBELOTE*. In both cases, following the end of this "multiple-pass" procedure, the execution continues from the keyword which follows *REBELOTE*, until 'END' is encountered.

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The two functionalities of *REBELOTE* are the following:

- REBELOTE can be used for Monte Carlo simulations when more than Max(IMAX) particles are to be tracked. Thus, when the following random procedures are used: MCOBJET, OBJETA, MCDESINT, SPNTRK (KSO = 5), their random seeds are not reset and independent statistics will add up.
- This includes **Monte Carlo simulations**, in beam lines: normally K = 0. NPASS runs through the same structure, from MCOBJET to REBELOTE will follow, resulting in the calculation of (1 + NPASS) * IMAX trajectories, with as many random initial coordinates.
- REBELOTE can be used for multi-turn ray-tracing in circular machines **circular machines**: normally K=99 in that case. NPASS turns in the same structure will follow, resulting in the tracking of IMAX particles over 1+NPASS turns. For the simulation of pulsed power supplies, synchrotron motion, and other Q-jump manipulation, see SCALING.

For instance, using option described K=99.2 above, a full "injection line + ring + extraction line" installation can be simulated - kicker firing and other magnet ramping can be simulated using SCALING.

Using the double-*LABEL* method discussed above with option *K*=99.2, it is possible to encompass the ring between an injection line section (namely, with the element sequence of the latter extending from *OBJET* to the first *LABEL*), and an extraction line (its description will then follow *REBELOTE*), whereas the ring description extends from to the first *LABEL* to *REBELOTE*, with possible extraction, at the last pass, at the location of the second *LABEL*, located between the first one and *REBELOTE*,

In addition to what precedes, *REBELOTE* can change the value of arbitrary parameters in zgoubi.dat data list, using the forth argument *IOPT=1* (see page 256). *NPRM* tells the number of parameters to be changed. A series of *NPRM* lists of values, one list per parameter to be changed and each list with *NRBLT* data, tells the values to be taken by each one of these parameters, over the *NRBLT* passes of the *REBELOTE* process.

Output prints over NPASS+1 passes might result in a prohibitively big zgoubi.res file. They may be switched on/off by means of the option KWRIT=i.j, with i=1/0 respectively. The j flag commands printing pass number and some other information onto the video output, every 10^{j-1} turns if j>0; output is switched off if j=0.

REBELOTE also provides information: statistical calculations and related data regarding particle decay (MCDESINT), spin tracking (SPNTRK), stopped particles (CHAMBR, COLLIMA), etc.

COMBINING REBELOTE AND FIT[2]

The keyword *REBELOTE* can follow *FIT[2]*. This allows executing again the fit procedure, after changing the value of some parameter in zgoubi.dat using *REBELOTE* with option *IOPT=1*. That's the interest of the game : *REBELOTE* changes that parameter, and then sends the zgoubi execution pointer back to the top of zgoubi.dat for a new run.

EXAMPLES

An example of the use of the *REBELOTE* procedure is given page 257.

An example combining FIT and REBELOTE is given page 223.

RECOVERING FROM A CRASH

When accelerating a bunch, *REBELOTE* is used to ensure the multi-turn process. Now, if the job is stopped - due to computer crash or else - it is possible to resume the tracking from the latest records (in [b_]zboubi.fai storage file), for instance using *OBJET*, *KOBJ*= 3. *CAVITE* and *SCALING* aspects of the data file modifications necessary to ensure the recovery, in the case of pulsed magnets, are discussed respectively in the *SCALING* section, pp. 76, 78, an example of job resuming is given page 241.

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RESET : Reset counters and flags

Resets counters involved in CHAMBR, COLLIMA, HISTO and INTEG procedures.

Switches off CHAMBR, MCDESINT, SCALING and SPNTRK options.

SCALING: Power supplies and R.F. function generator

SCALING acts as a function generator dedicated to varying fields in optical elements, potentials in electrostatic devices, RF parameters in *CAVITE*. It is normally intended to be declared right after the object definition, and used in conjunction with *REBELOTE*, for the simulation of multi-turn tracking - possibly including acceleration cycles.

SCALING acts on families of elements, a family being designated by its name that coincides with the keyword of the corresponding element. For instance, declaring MULTIPOL as to be varied will result in the same timing law being applied to all MULTIPOLs in the zgoubi optical structure data file. Subsets can be selected by labeling keywords in the data file (section 4.6.5, page 169) and adding the corresponding LABEL(s) in the SCALING declarations (two LABELs maximum). The family name of concern, as well as the scaling function for that family, are given as input data to the keyword SCALING. There is an upper limit, NFMAX, to the number NF of families that can be declared as subject to a scaling law, NFMAX can be changed in the FORTRAN include file MXFS. H. A scaling law can be comprised of up to NT successive timings, between two successive timings, a linear interpolation law is used to determine the scaling factor.

An example of data formatting for the simulation of an acceleration cycle in a circular machine is given in the following.

```
SCALING
                                          - Scaling
                                          Active. NF = 4 families of elements are concerned, as listed below
   4
QUADRUPO QFA QFB
                                          - Quadrupoles labeled 'QFA' and Quadrupoles labeled 'QFB'
                                          NT = 2 \text{ timings}
18131.E-3
                                         The field increases (linearly) from 18131E-3*B_0 to 24176E-3*B_0
                           24176.E-3
                            6379
                                          from turn 1 to turn 6379
MULTIPOL QDA QDB
                                          - Multipoles labeled 'QDA' and Multipoles labeled 'QDB'
                                          NT=2 timings
18131.E-3
                           24176.E-3
                                          Fields increase from 18131E-3*B_i to 24176E-3*B_i (\forall i = 1, 10 poles)
1
                            6379
                                          from turn 1 to turn 6379
BEND
                                          - All BENDs (regardless of any LABEL)
                                          NT = 2 timings
18131.E-3
                           24176.E-3
                                         As above
1
                            6379
CAVITE
                                          - Accelerating cavity
3
                                          NT = 3 timings
                                          The synchronous rigidity (B\rho)_s increases,
1
     1.22
                           1.33352
1
     1200
                           6379
                                          from (B\rho)_{s_o} to 1.22 *(B\rho)_{s_o} from turn 1 to 1200, and
                                          from 1.22 *(B\rho)_{s_o} to 1.33352 (B\rho)_{s_o} from turn 1200 to 6379
```

The timing is in unit of turns. In this example, TIMING = 1 to 6379 (turns). Therefore, at turn number N, B and B_i are updated in the following way. Let SCALE(TIMING = N) be the updating scale factor

$$SCALE(N) = 18.131 \frac{24.176 - 18.131}{1 + 6379 - 1}(N - 1)$$

and then

$$B(N) = SCALE(N)B_0$$

 $B_i(N) = SCALE(N)B_{i0}$

The RF frequency is computed using

$$f_{RF} = \frac{hc}{\mathcal{L}} \frac{q(B\rho)_s}{(q^2(B\rho)_s^2 + (Mc^2)^2)^{1/2}}$$

where the rigidity is updated in the following way. Let $(B\rho)_{s_o}$ be the initial rigidity (namely, $(B\rho)_{s_o} = BORO$ as defined in the keyword OBJET for instance). Then, at turn number N,

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$$\begin{split} &\text{if } 1 \leq N \leq 1200 \ \text{ then, } \textit{SCALE}(N) = 1 + \frac{1.22 - 1}{1 + 1200 - 1} \left(N - 1\right) \\ &\text{if } 1200 \leq N \leq 6379 \ \text{ then, } \textit{SCALE}(N) = 1.22 + \frac{1.33352 - 1.22}{1 + 6379 - 1200} \left(N - 1200\right) \end{split}$$

and then,

$$(B\rho)_s(N) = SCALE(N) \cdot (B\rho)_{s_0}$$

from which value the calculations of $f_{RF}(N)$ follow.

NT can take negative values, then acting as an option switch (rather than giving number of timings), as follows:

• NT = -1: this is convenient for synchrotron acceleration. In this case the next two lines both contain a single data (as for NT = 1), respectively the starting scaling factor value, and 1. The current field scaling factor will then be updated from the energy kick by the cavity if for instance CAVITE/IOPT = 2 is used, namely,

$$SCALE(N) = SCALE(N-1) * \frac{B\rho(N)}{B\rho(N-1)}$$

Note that in the case of the previous example (assuming, though, that the ramping of the magnetic fields strictly follows the *CAVITE* kick, which was not strictly the case), the *SCALING* argument list can be simplified, including by suppressing '*CAVITE*' from the list, as follows:

```
\begin{array}{lll} SCALING & - Scaling \\ 1 & 3 & Active. \ NF = 3 \ families \ of \ elements \ are \ concerned, \ as \ listed \ below \\ - QUADRUPO \ QFA \ QFB & - Quadrupoles \ labeled \ 'QFA' \ and \ Quadrupoles \ labeled \ 'QFB' \\ -1 & 18131.E-3 & - Multipoles \ labeled \ 'QDA' \ and \ Multipoles \ labeled \ 'QDB' \\ -1 & 18131.E-3 & - All \ BEND & - All \ BEND \ (regardless \ of \ any \ LABEL) \\ -1 & 18131.E-3 & 1 & - All \ BEND \ (regardless \ of \ any \ LABEL) \\ \end{array}
```

- NT = -2: this is convenient for reading an RF law for *CAVITE* from an external data file, including usage for acceleration in fixed field accelerators.
- NT = 1.10: allows taking the scaling law from an external data file, as in the following example:

MULTIPOL COH1

1.10

./Csnk3D/bump_centered.scal File name

Column numbers in the file : col. 2 gives the scaling factor at rigidity given by col. 1.

Notes:

1. In causing, via *CAVITE*, a change of the synchronous rigidity, *SCALING* causes a change of the reference rigidity, following (see *CAVITE*)

$$B\rho_{ref} = BORO \longrightarrow B\rho_{ref} = BORO + \delta B\rho_s$$

2. It may happen that some optical elements won't scale, for source code development or updating reasons. This should be paid attention to by preliminary simulation tests.

RECOVERING FROM A CRASH

When accelerating a bunch in a pulsed ring, SCALING is used to ramp magnetic fields, so following the rigidity increase by CAVITE. CAVITE may or may not be part of the SCALING argument list, see the two previous examples. Now, if the job is stopped - due to computer crash or else - it is possible to resume the tracking from the latest records (in [b_]zboubi.fai storage file), for instance using OBJET, KOBJ=3. In the presence of acceleration using CAVITE however, since there is no reference particle in **zgoubi**, CAVITE needs be told the reference rigidity at the corresponding time/turn where tracking is resumed. This is done using SCALING, see example page 241. This has the effect of updating the refrence rigidity $B\rho_{ref}$ to its correct value (see Note 1 above), the one it had when the job stopped.

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SPNTRK: Spin tracking

The keyword *SPNTRK* allows switching spin tracking on (index *KSO*=1) or off (*KSO*=0), or resuming (index *KSO*=-1, following an occurrence *KSO*=0). It also permits the attribution of an initial spin to each one of the *IMAX* particles of the beam, following a distribution that depends on the option index *KSO*. It must be preceded by *PARTICUL* for the definition of mass and gyromagnetic factor.

KSO = 1 (respectively 2, 3): the *IMAX* particles defined with *[MC]OBJET* are given a longitudinal (1,0,0) spin component (respectively transverse horizontal (0,1,0), vertical (0,0,1)).

KSO = **4**: initial spin components are entered explicitly for each one of the *IMAX* particles of the beam.

KSO = **4.1**: three initial spin components S_X , S_Y , S_Z are entered explicitly just once, they are then assigned to each one of the *IMAX* particles of the beam.

KSO = 5: random generation of IMAX initial spin conditions as described in Fig. 9. Given a mean polarization axis (S) defined by its angles T_0 and P_0 , and a cone of angle A with respect to this axis, the IMAX spins are sorted randomly in a Gaussian distribution

$$p(a) = \exp\left[-\frac{(A-a)^2}{2\delta A^2}\right]/\delta A\sqrt{2\pi}$$

and within a cylindrical uniform distribution around the (S) axis. Examples of simple distributions available by this mean are given in Fig. 10.

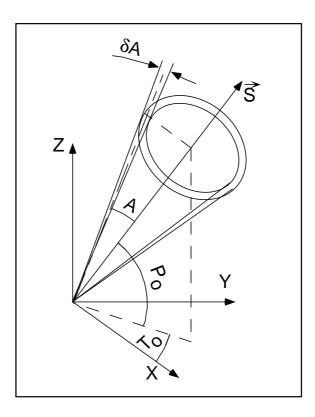


Figure 9: Spin distribution as obtained with option KSO = 5. The spins are distributed within an annular strip δA (standard deviation) at an angle A with respect to the axis of mean polarization (S) defined by T_0 and P_0 .

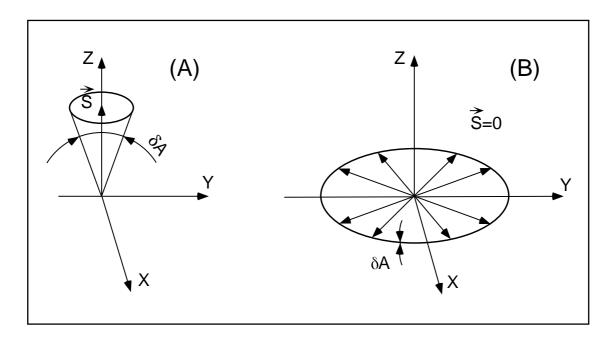


Figure 10: Examples of the use of KSO = 5.

A: Gaussian distribution around a mean vertical polarization axis, obtained with T_0 = arbitrary, $P_0 = \pi/2$, A = 0 and $\delta A \neq 0$. B: Isotropic distribution in the median plane, obtained with $P_0 = \pm \pi/2$,

 $A = \pi/2$, and $\delta A = 0$.

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SRLOSS: Synchrotron radiation energy loss [17]

The keyword SRLOSS allows activating or stopping (option KSR = 1, 0 respectively) stepwise tracking of energy loss by stochastic emission of photons in magnetic fields, following the method described in section 3.1.

It can be chosen to allow radiation in the sole dipole fields, or in all types of fields regardless of their multipole composition. It can also be chosen to allow for the radiation induced transverse kick.

SRLOSS must be preceded by *PARTICUL* for defining mass and charge values as they enter in the definition of SR parameters.

Statistics on SR parameters are computed and updated while tracking, the results of which can be obtained by means of the keyword *SRPRNT*.

SYNRAD: Synchrotron radiation spectral-angular densities

The keyword *SYNRAD* enables (or disables) the calculation of synchrotron radiation (SR) electric field and spectral angular energy density. It must be preceded by *PARTICUL* for defining mass and charge values, as they enter in the definition of SR parameters.

SYNRAD is supposed to appear a first time at the location where SR should start being taken into account, with the first data KSR set to 1. It results in on-line storage of the electric field vector and other relevant quantities in zgoubi.sre, as step by step integration proceeds. The observer position (XO, YO, ZO) is specified next to KSR.

Data stored in zgoubi.sre:

```
(ELx, ELy, ELz): electric field vector \vec{\mathcal{E}} (eq. 3.2.1) (btx, bty, btz) = \vec{\beta} = \frac{1}{c} \times \text{particle velocity} (gx, gy, gz) = \frac{d\vec{\beta}}{dt} = \text{particle acceleration (eq. 3.2.3)} \Delta \tau = \text{observer time increment (eq. 3.2.2)} t' = \tau - r(t')/c = \text{retarded (particle) time} (rtx, rty, rtz) : \vec{R}(t), particle to observer vector (eq. 3.2.4) (x, y, z) = \text{particle coordinates} \Delta s = \text{step size in the magnet (fig. 2)} NS = \text{step number} I = \text{particle number} LET(I) = \text{tagging letter} IEX(I) = \text{stop flag (see section 4.6.10)}
```

SYNRAD is supposed to appear a second time at the location where SR calculations should stop, with KSR set to 2. It results in the output of the angular energy density $\int_{\nu_1}^{\nu_2} \partial^3 W/\partial\phi \,\partial\psi \,\partial\nu$ (eq. 3.2.11) as calculated from the Fourier transform of the electric field (eq. 3.2.11). The spectral range of interest and frequency sampling (ν_1, ν_2, N) are specified next to KSR.

4.3 Declaring Options 83

SYSTEM : System call

The keyword *SYSTEM* allows one or a series of system calls. It can appear anywhere, an arbitrary number of times, in the zgoubi.dat data list. It is effective at the very location where it appears.

SYSTEM keyword is followed by the list of the desired system commands. That can be saving zgoubi output files, calling again **zgoubi** at the end of a run so allowing dependent consecutive jobs, etc.

Examples of the use of SYSTEM are given in pp. 223, 271.

4.4 Optical Elements and Related Numerical Procedures

AGSMM: AGS main magnet

The AGS main magnet is a combined function dipole with straight axis (lines of constant field are straight lines).

The field computation routines for AGSMM are the same as for MULTIPOL (details in section 1.3.7, page 25), however AGSMM has the following four particularities:

- There are only three multipole components present in AGSMM : dipole, quadrupole and sextupole.
- The dipole field B_0 is drawn from the reference rigidity, $B\rho_{ref}$, and follows the latter so to preserve $\rho = B\rho_{ref}/B_0$ and the orbit deviation L/ρ . In particular,
 - in the absence of acceleration, $B\rho_{ref} \equiv BORO$, with BORO the quantity appearing in the object definition using [MC]OBJET,
 - in presence of acceleration using *CAVITE*, $B\rho_{ref}$ is changed to $BORO \times D_{ref}$ at each passage in the cavity, with D_{ref} the relative synchronous momentum increase, a quantity that **zgoubi** updates at cavity traversal.
- The field indices, quadrupole K1 and sextupole K2, are derived from the reference rigidity, $B\rho_{ref}$, via momentum-dependent polynomials, taken from Ref. [32], and following in that the methods found in the MAD model of the AGS [33].
- The AGS main dipole has back-leg windings, used for instance for injection and extraction orbit bumps. The number of winding turns and the number of ampere-turns are part of the data in the input data list. The intensity in the windings is accounted for in the conversion from total ampere-turns in the magnet to momentum and then to magnetic field.

Note: A consequence of items 2 and 3 is that no field value is required in defining the AGS main magnets in the zgoubi.dat input data list.

AGSQUAD: AGS quadrupole

The AGS quadrupoles are regular quadrupoles. The simulation of *AGSQUAD* uses the same field modelling as *MULTIPOL*, section 1.3.7, page 25. However amperes are provided as input to *AGSQUAD* rather than fields, the reason being that some of the AGS quadrupoles have two superimposed coil circuits, with separate power supplies. It has been dealt with this particularity by allowing for an additional set of quadrupole data in *AGSQUAD*, compared to *MULTIPOL*.

The field in *AGSQUAD* is computed using transfer functions, from the specified ampere-turns in the coils to magnetic field at pole-tip, that account for the non-linearity of the magnetic permeability [33].

AIMANT: Generation of dipole mid-plane 2-D map, polar frame

The keyword *AIMANT* provides an automatic generation of a dipole median plane field map in polar coordinates.

A more recent and improved version will be found in *DIPOLE-M*. In addition, a similar modelling, that however skips the stage of an intermediate mid-plane field map, can be found in *DIPOLE[S]*.

The extent of the map is defined by the following parameters, as shown in Figs. 11A and 11B,

AT : total angular aperture

RM: mean radius used for the positioning of field boundaries RMIN, RMAX: minimum and maximum radial boundaries of the map

The 2 or 3 effective field boundaries (EFB) inside the map are defined from geometric boundaries, the shape and position of which are determined by the following parameters,

ACENT: arbitrary angle, used for the positioning of the EFBs.

 ω : azimuth of an EFB with respect to ACENT

 θ : angle of a boundary with respect to its azimuth (wedge angle)

 R_1, R_2 : radius of curvature of an EFB U_1, U_2 : extent of the linear part of the EFB.

At any node of the map mesh, the value of the Z component of the field is calculated as

$$B_Z = \mathcal{F}(R,\theta) * B_0 * \left(1 + N * \left(\frac{R - RM}{RM}\right) + B * \left(\frac{R - RM}{RM}\right)^2 + G * \left(\frac{R - RM}{RM}\right)^3\right)$$
(4.4.1)

where N, B and G are respectively the first, second and third order field indices and $\mathcal{F}(R,\theta)$ is the fringe field coefficient (it determines the "flutter" in periodic structures).

Calculation of the Fringe Field Coefficient

With each EFB a realistic extent of the fringe field, λ , is associated (Figs. 11A and 11B), and a fringe field coefficient F is calculated. In the following λ stands for either λ_E (Entrance), λ_S (Exit) or λ_L (Lateral EFB).

If a node of the map mesh is at a distance of the EFB larger than λ , then F = 0 outside the field map and F = 1 inside. If a node is inside the fringe field zone, then F is calculated as follows.

Two options are available, for the calculation of F, depending on the value of ξ .

If $\xi \geq 0$, F is a second order type fringe field (Fig. 12) given by

$$F = \frac{1}{2} \frac{(\lambda - s)^2}{\lambda^2 - \xi^2} \quad \text{if } \xi \le s \le \lambda$$
 (4.4.2)

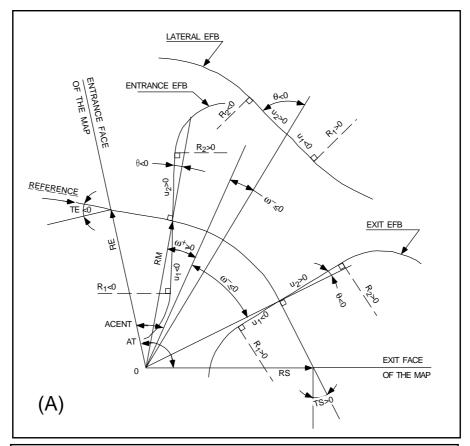
$$F = 1 - \frac{1}{2} \frac{(\lambda - s)^2}{\lambda^2 - \xi^2}$$
 if $-\lambda \le s \le -\xi$ (4.4.3)

where s is the distance to the EFB, and

$$F = \frac{1}{2} + \frac{s}{\lambda + \xi} \quad \text{if } 0 \le s \le \xi \tag{4.4.4}$$

$$F = \frac{1}{2} - \frac{s}{\lambda + \xi}$$
 if $-\xi \le s \le 0$ (4.4.5)

This simple model allows a rapid calculation of the fringe field, but may lead to erratic behavior of the field when extrapolating out of the median plane, due to the discontinuity of d^2B/ds^2 , at $s=\pm\xi$ and $s=\pm\lambda$. For better accuracy it is advised to use the next option.



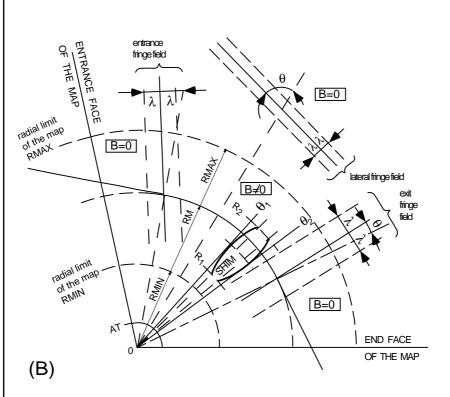


Figure 11: A : Parameters used to define the field map and geometrical boundaries.

B: Parameters used to define the field map and fringe fields.

If $\xi = -1$, F is an exponential type fringe field (Fig. 12) given by [34]

$$F = \frac{1}{1 + \exp P(s)} \tag{4.4.6}$$

where s is the distance to the EFB, and

$$P(s) = C_0 + C_1 \left(\frac{s}{\lambda}\right) + C_2 \left(\frac{s}{\lambda}\right)^2 + C_3 \left(\frac{s}{\lambda}\right)^3 + C_4 \left(\frac{s}{\lambda}\right)^4 + C_5 \left(\frac{s}{\lambda}\right)^5 \tag{4.4.7}$$

The values of the coefficients C_0 to C_5 should be such that the derivatives of B_Z with respect to s be negligible at $s=\pm\lambda$, so as not to perturb the extrapolation of \vec{B} out of the median plane.

It is also possible to simulate a shift of the EFB, by giving a non zero value to the parameter *shift*. s is then changed to s- s-shift in the previous equation. This allows small variations of the total magnetic length.

Let F_E (respectively F_S , F_L) be the fringe field coefficient attached to the entrance (respectively exit, lateral) EFB following the equations above. At any node of the map mesh, the resulting value of the fringe field coefficient (eq. 4.4.1) is (Fig. 13)

$$\mathcal{F}(R,\theta) = F_E * F_S * F_L$$

In particular, $F_L \equiv 1$ if no lateral EFB is requested.

The Mesh of the Field Map

The magnetic field is calculated at the nodes of a mesh with polar coordinates, in the median plane. The radial step is given by

$$\delta R = \frac{RMAX - RMIN}{IRMAX - 1}$$

and the angular step by

$$\delta\theta = \frac{AT}{IAMAX - 1}$$

where, *RMIN* and *RMAX* are the lower and upper radial limits of the field map, and *AT* is its total angular aperture (Fig. 11B). *IRMAX* and *IAMAX* are the total number of nodes in the radial and angular directions.

Simulating Field Defects and Shims

Once the initial map is calculated, it is possible to perturb it by means of the parameter *NBS*, so as to simulate field defects or shims.

If NBS = -2, the map is globally modified by a perturbation proportional to $R - R_0$, where R_0 is an arbitrary radius, with an amplitude $\Delta B_Z/B_0$, so that B_Z at the nodes of the mesh is replaced by

$$B_Z * \left(1 + \frac{\Delta B_Z}{B_0} \frac{R - R_0}{RMAX - RMIN}\right)$$

If NBS = -1, the perturbation is proportional to $\theta - \theta_0$, and B_Z is replaced by

$$B_Z * \left(1 + \frac{\Delta B_Z}{B_0} \frac{\theta - \theta_0}{AT}\right)$$

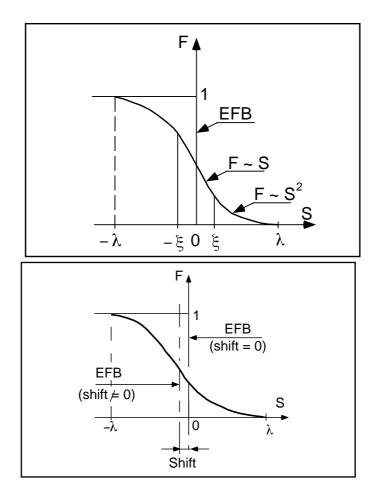


Figure 12: Second order type fringe field (upper plot) and exponential type fringe field (lower plot).



Figure 13: Effective value of $\mathcal{F}(R,\theta)$ for overlapping fringe fields F_1 and F_2 centered at O_1 and O_2 .

If NBS \geq 1, then NBS shims are introduced at positions $\frac{R_1 + R_2}{2}$, $\frac{\theta_1 + \theta_2}{2}$ (Fig. 14) [35] The initial field map is modified by shims with second order profiles given by

$$\theta = \left(\gamma + \frac{\alpha}{\mu}\right) \beta \, \frac{X^2}{\rho^2}$$

where X is shown in Fig. 14, $\rho = \frac{R_1 + R_2}{2}$ is the central radius, α and γ are the angular limits of the shim, β and μ are parameters.

At each shim, the value of B_Z at any node of the initial map is replaced by

$$B_Z * \left(1 + F\theta * FR * \frac{\Delta B_Z}{B_0}\right)$$

where $F\theta=0$ or FR=0 outside the shim, and $F\theta=1$ and FR=1 inside.

Extrapolation Off Median Plane

The vertical field \vec{B} and its derivatives in the median plane are calculated by means of a second or fourth order polynomial interpolation, depending on the value of the parameter IORDRE (IORDRE=2, 25 or 4, see section 1.4.2). The transformation from polar to Cartesian coordinates is performed following eqs. (1.4.9 or 1.4.10). Extrapolation off median plane is then performed by means of Taylor expansions following the procedure described in section 1.3.3.



Figure 14: A second order profile shim. The shim is centered at $\frac{(R_1+R_2)}{2}$ and $\frac{(\theta_1+\theta_2)}{2}$.

AUTOREF: Transport beam into a new reference frame

AUTOREF positions the new reference frame following four different options (apart from I=0 which is just an "off" switch):

If I = 1, AUTOREF is equivalent to

$$CHANGREF[XCE = 0, YCE = Y(1), ALE = T(1)]$$

so that the new reference frame is at the exit of the last element, with particle 1 at the origin with its horizontal angle set to T=0.

If I = 2, it is equivalent to

so that the new reference frame is at the position (XW, YW) of the waist (calculated automatically in the same way as for IMAGE) of the three rays number 1, 4 and 5 (compatible for instance with OBJET, KOBJ = 5, 6, together with the use of MATRIX) while T(1), the horizontal angle of particle number I1, is set to zero.

If I = 3, it is equivalent to

so that the new reference frame is at the position (XW,YW) of the waist (calculated automatically in the same way as for IMAGE) of the three rays number I1, I2 and I3 specified as data, while T(I1) is set to zero.

If I = 4: new horizontal beam centroid positionning XCE, YCE, ALE is provided. The beam is moved by XCE and then centered on YCE, ALE.

If I = 4.1: new beam centroid positionning XCE, YCE, ALE, DCE is provided. The beam is moved by XCE and then centered on YCE, ALE. In addition, the beam is centered on a new relative momentum DCE.

If I = 5: new vertical beam centroid positionning ZCE, PLE (position, angle) is provided. The beam is centered on vertical position and angle ZCE, PLE.

BEAMBEAM: Beam-beam lens

BEAMBEAM is a beam-beam lens simulation, a point transform [36].

Upon option using SPNTRK, BEAMBEAM will include spin kicks, after modelling as described in Ref. [37].

BEND: Bending magnet, Cartesian frame

BEND is one of several keywords available for the simulation of dipole magnets. It presents the interest of easy handling, and is well adapted for the simulation of synchrotron dipoles and such other regular dipoles as sector magnets with wedge angles.

The field in *BEND* is defined in a Cartesian coordinate frame (unlike for instance *DIPOLE[S]* that uses a polar frame). As a consequence, having particle coordinates at entrance or exit of the magnet referring to the curved main direction of motion may require using *KPOS*, in particular *KPOS=3* (in a circular machine cell for instance, see section 4.6.7, p. 170).

The dipole simulation accounts for the magnet geometrical length XL, for a possible skew angle (X-rotation, useful for obtaining vertical deviation magnet), and for the field B1 such that in absence of fringe field the deviation θ satisfies $XL = 2\frac{BORO}{B1}\sin\theta/2$.

Then follows the description of the entrance and exit EFBs and fringe fields. The wedge angles W_E (entrance) and W_S (exit) are defined with respect to the sector angle, with the signs as described in Fig. 15. Within a distance $\pm X_E(\pm X_S)$ on both sides of the entrance (exit) EFB, the fringe field model is used (same as for *QUADRUPO*, Fig. 35, p. 139); elsewhere, the field is supposed to be uniform.

If λ_E (resp. λ_S) is zero sharp edge field model is assumed at entrance (resp. exit) of the magnet and X_E (resp. X_S) is forced to zero. In this case, the wedge angle vertical first order focusing effect (if $\vec{B}1$ is non zero) is simulated at magnet entrance and exit by a kick $P_2 = P_1 - Z_1 \tan(\epsilon/\rho)$ applied to each particle (P_1 , P_2 are the vertical angles upstream and downstream the EFB, Z_1 the vertical particle position at the EFB, ρ the local horizontal bending radius and ϵ the wedge angle experienced by the particle; ϵ depends on the horizontal angle T).

Magnet (mis-)alignment is assured by *KPOS*. *KPOS* also allows some degrees of automatic alignment useful for periodic structures (section 4.6.7).

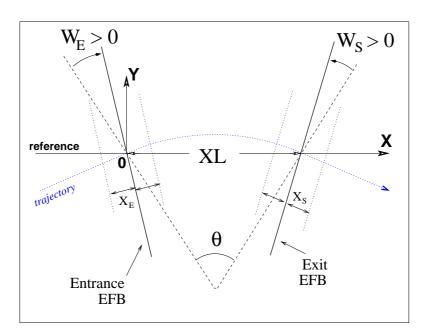


Figure 15: Geometry and parameters of BEND: XL = length, $\theta = deviation$, W_E , W_S are the entrance and exit wedge angles. The motion is computed in the Cartesian frame (O, X, Y, Z)

BREVOL: 1-D uniform mesh magnetic field map

BREVOL reads a 1-D axial field map from a storage data file, whose content must match the following FORTRAN reading sequence (possible FORMAT updates are to be found in fmapw.f).

where IX is the number of nodes along the (symmetry) X-axis, X(I) their coordinates, and BX(I) are the values of the X component of the field. BX is normalized with BNORM factor prior to ray-tracing, as well X is normalized with the coefficient XNORM (useful to convert to centimeters, the working units in zgoubi). For binary files, FNAME must begin with ' B_{-} ' or ' b_{-} ', a flag 'BINARY' will thus be set to '.TRUE.' by the FORTRAN.

X-cylindrical symmetry is assumed, resulting in BY and BZ taken to be zero on axis. $\vec{B}(X,Y,Z)$ and its derivatives along a particle trajectory are calculated by means of a 5-point polynomial interpolation followed by second order off-axis extrapolation (see sections 1.3.2, 1.4.1).

Entrance and/or exit integration boundaries may be defined in the same way as in *CARTEMES* by means of the flag ID and coefficients A, B, C, etc.

CARTEMES: 2-D Cartesian uniform mesh magnetic field map

CARTEMES was originally dedicated to the reading and processing of the measured median plane field maps of the QDD spectrometer SPES2 at Saclay, assuming mid-plane dipole symmetry. However, it can be used for the reading of any 2-D median plane maps, provided that the format of the field data storage file fits the following *FORTRAN* sequence

where, IX and JY are the number of longitudinal and transverse horizontal nodes of the uniform mesh, and X(I), Y(J) their coordinates. *FNAME* is the name of the file containing the field data. For binary files, *FNAME* must begin with 'B₋' or 'b₋', a flag 'BINARY' will thus be set to '.TRUE.' by the *FORTRAN*.

The measured field BMES is normalized with BNORM,

$$B(I, J) = BMES(I, J) \times BNORM$$

As well the longitudinal coordinate X is normalized with a *XNORM* coefficient (useful to convert to centimeters, the working units in **zgoubi**).

The vector field, \vec{B} , and its derivatives out of the median plane are calculated by means of a second or fourth order polynomial interpolation, depending on the value of the parameter IORDRE (IORDRE = 2, 25 or 4, see section 1.4.2).

In case a particle exits the mesh, its IEX flag is set to -1 (see section 4.6.10, p. 173), however it is still tracked with the field being *extrapolated* from the closest nodes of the mesh. Note that such extrapolation process may induce erratic behavior if the distance from the mesh gets too large.

Entrance and/or exit integration boundaries can be defined with the flag ID, as follows (Fig. 16).

If ID = 1: the integration in the field is terminated on a boundary with equation A'X + B'Y + C' = 0, and then the trajectories are extrapolated linearly onto the exit border of the map.

If ID = -1: an entrance boundary is defined, with equation A'X + B'Y + C' = 0, up to which trajectories are first extrapolated linearly from the map entrance border, prior to being integrated in the field.

If ID \geq 2: one entrance boundary, and ID-1 exit boundaries are defined, as above. The integration in the field terminates on the last (ID-1) exit boundary. No extrapolation onto the map exit border is performed in this case.

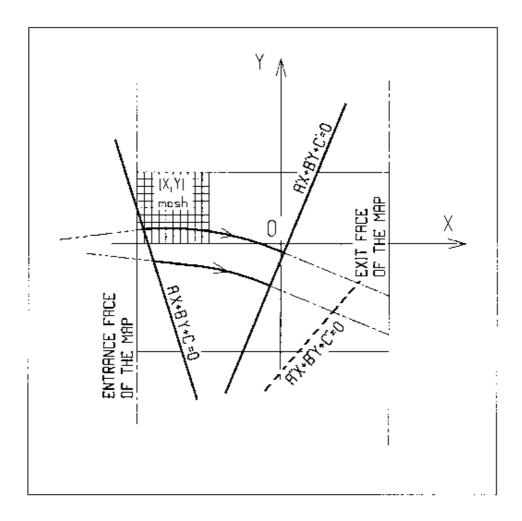


Figure 16: OXY is the coordinate system of the mesh. Integration boundaries may be defined, using $ID \neq 0$: particle coordinates are extrapolated linearly from the entrance face of the map, onto the boundary A'X + B'Y + C' = 0; after ray-tracing inside the map and terminating on the boundary AX + BY + C = 0, coordinates are extrapolated linearly onto the exit face of the map if ID = 2, or terminated on the last (ID - 1) boundary if ID > 2.

CAVITE: Accelerating cavity

CAVITE provides a simulation of a (zero length) accelerating cavity; it can be used in conjunction with keywords REBELOTE and SCALING for the simulation of multi-turn tracking with synchrotron or fixed field (FFAG, cyclotron) acceleration (see section 4.6.9). It must be preceded by PARTICUL for the definition of mass M and charge q.

A major effect of CAVITE on optics settings is the following:

The reference rigidity of a problem, as used when computing optical strengths from field values, sections 1.2.1-1.2.3, is specified in the object definition by [MC]OBJET. However, in many cases – options as described below – that reference rigidity will be updated upon crossing the cavity, by the amount of the synchronous rigidity increase as induced by the cavity, namely,

$$B\rho_{ref} = BORO \longrightarrow B\rho_{ref} = BORO + \delta B\rho_s$$

Note as an illustration of the process, that, in this case, a simple way to have the optical elements have their strengths maintained constant is to use SCALING with the option NTIM = -1.

If IOPT = 0: CAVITE is switched off.

If IOPT = 1: CAVITE simulates the RF cavity of a synchrotron accelerator: the periodic motion over IP = 1, NPASS + 1 turns (passes through the structure) is obtained using the keyword REBELOTE, option K = 99, while RF and optical elements time dependent functions are simulated by means of SCALING – see section 4.6.9. CAVITE may conveniently be located at the end of the optical structure, otherwise its phasing has to be indicated. The synchrotron motion of any of the IMAX particles of a beam is obtained from the following mapping

$$\begin{cases} \phi_2 - \phi_1 = 2\pi f_{RF} \left(\frac{\ell}{\beta c} - \frac{\mathcal{L}}{\beta_s c} \right) \\ W_2 - W_1 = q \hat{V} \sin \phi_1 \end{cases}$$

where

 ϕ = RF phase; $\phi_2 - \phi_1$ = variation of ϕ between two traversals

W = kinetic energy; $W_2 - W_1 = \text{energy gain at a traversal of } \textit{CAVITE}$

 \mathcal{L} = length of the synchronous closed orbit (to be calculated by prior ray-tracing,

see the bottom NOTE)

 ℓ = orbit length of the particle between two traversals

 $\beta_s c$ = velocity of the (virtual) synchronous particle

 βc = velocity of the particle

 \hat{V} = peak RF voltage

q = particle electric charge.

The RF frequency f_{RF} is a multiple of the synchronous revolution frequency, and is obtained from the input data, following

$$f_{RF} = \frac{hc}{\mathcal{L}} \frac{q(B\rho)_s}{\sqrt{q^2(B\rho)_s^2 + (Mc)^2}}$$

where

h = harmonic number of the R.F

M =mass of the particle

c = velocity of light.

The current rigidity $(B\rho)_s$ of the synchronous particle is obtained from the timing law specified by means of SCALING following $(B\rho)_s = BORO \cdot SCALE(TIMING)$ (see SCALING for the meaning and calculation of the scale factor SCALE(TIMING)). If SCALING is not used, $(B\rho)_s$ is assumed to keep the constant value BORO as given in the object description (see OBJET for instance).

The velocity βc of a particle is calculated from its current rigidity

$$\beta = \frac{q(B\rho)}{\sqrt{q^2(B\rho)^2 + (Mc)^2}}$$

The velocity $\beta_s c$ of the synchronous particle is obtained in the same way from

$$\beta_s = \frac{q(B\rho)_s}{\sqrt{q^2(B\rho)_s^2 + (Mc)^2}}$$

The kinetic energies and rigidities involved in these formulae are related by

$$q(B\rho) = \sqrt{W(W + 2Mc^2)}$$

Finally, the initial conditions for the mapping, at the first turn, are the following

- For the (virtual) synchronous particle

$$\phi_1 = \phi_s = ext{synchronous phase}$$
 $(B
ho)_{1s} = BORO$

- For any of the I = 1, IMAX particles of the beam

$$\phi_{1I} = \phi_s = \text{synchronous phase}$$

 $(B\rho)_{1I} = BORO * D_I$

where the quantities BORO and D_I are given in the object description.

Calculation of the Coordinates

Let $p_I = [p_{XI}^2 + p_{YI}^2 + p_{ZI}^2]^{1/2}$ be the momentum of particle I at the exit of the cavity, while $p_{I_0} = [p_{XI_0}^2 + p_{YI_0}^2 + p_{ZI_0}^2]^{1/2}$ is its momentum at the entrance. The kick in momentum is assumed to be fully longitudinal, resulting in the following relations between the coordinates at the entrance (denoted by the index zero) and at the exit

$$\begin{split} p_{XI} &= \left[p_I^2 - (p_{I_0}^2 - p_{XI_0}^2)\right]^{1/2} \\ p_{YI} &= p_{YI_0}, \quad \text{and} \quad p_{ZI} = p_{ZI_0} \quad \text{(longitudinal kick)} \\ X_I &= X_{I_0}, \quad Y_I = Y_{I_0} \quad \text{and} \quad Z_I = Z_{I_0} \quad \text{(zero length cavity)} \end{split}$$

and for the angles (see Fig. 1)

$$T_{I} = \operatorname{Atg}\left(\frac{p_{YI}}{p_{XI}}\right)$$

$$P_{I} = \operatorname{Atg}\left(\frac{P_{ZI}}{(p_{YI}^{2} + p_{YI}^{2})^{1/2}}\right)$$
(damping of the transverse motion)

If IOPT = 2: the same simulation of a synchrotron RF cavity as for IOPT = 1 is performed, except that the keyword SCALING (family CAVITE) is not taken into account in this option: the increase in kinetic energy at each traversal, for the synchronous particle, is

$$\Delta W_s = q\hat{V} \sin \phi_s$$

where the synchronous phase ϕ_s is given in the input data. From this, the calculation of the law $(B\rho)_s$ and the RF frequency f_{RF} follows, according to the formulae given in the IOPT = 1 case.

If IOPT = 3: sine RF law, acceleration without synchrotron motion. Any particle will be given a kick

$$\Delta W = q\hat{V} \sin \phi_s$$

where \hat{V} and ϕ_s are input data.

If IOPT = 6: allows reading the RF frequency and/or phase law from an external file (wih name normally "zgoubi.freqLaw.In"). See routines cavite.f and scalin.f for details Was first used for acceleration in scaling FFAG [45].

If IOPT = **7**: fixed frequency RF, quasi- or isochronous acceleration. Was first used for quasi-isochronous, fixed frequency acceleration in the EMMA prototype linear FFAG [46, 47]. Can be used for cyclotron acceleration.

CLOSED ORBIT COMPUTATION

Due to possible dipole type of optical defects (e.g., fringe fields, straight axis combined function dipoles), the closed orbit may not coincide with the ideal axis of the optical elements (hence it will be almost everywhere non-zero). One way to calculate it at the beginning of the structure (i.e., where the initial particle coordinates are defined) is to ray-trace a single particle over a sufficiently large number of turns, starting with initial conditions taken near the reference orbit, so as to obtain statistically well-defined transverse phase-space ellipses. The local closed orbit coincides with the coordinates Y_c , T_c , Z_c , P_c of the center of the ellipses. A few iterations are usually sufficient (avoid near-integer tunes) to ensure accuracy. Next, ray-tracing over one turn a particle starting with the initial condition (Y_c, T_c, Z_c, P_c) will provide the entire closed orbit, and as a sub-product its length \mathcal{L} (the F(6,1) coordinate in the FORTRAN).

RECOVERING FROM A CRASH

When accelerating a bunch in a pulsed ring, SCALING is used to ramp magnetic fields, so following the rigidity increase by CAVITE. CAVITE may or may not be part of the SCALING argument list, this is discussed in the SCALING section, page 78. Now, if the job is stopped - due to computer crash or else - it is possible to resume the tracking from the latest records (in [b_]zboubi.fai storage file), for instance using OBJET, KOBJ=3. In the presence of acceleration using CAVITE however, since there is no reference particle in **zgoubi**, CAVITE needs be told the reference rigidity at the corresponding time/turn where tracking is resumed. This is done using SCALING. This has the effect of updating the refrence rigidity $B\rho_{ref}$ to its correct value (see Note 1 above), the one it had when the job stopped. See the SCALING section for more (page 76) and the examples there, as well as the example page 241.

CHAMBR: Long transverse aperture limitation

CHAMBR causes the identification, counting and stopping of particles that reach the transverse limits of the vacuum chamber. The chamber can be either rectangular (IFORM = 1) or elliptic (IFORM = 2). The chamber is centered at YC, ZC and has transverse dimensions $\pm YL$ and $\pm ZL$ such that any particle will be stopped if its coordinates Y, Z satisfy

$$(Y - YC)^2 \ge YL^2$$
 or $(Z - ZC)^2 \ge ZL^2$ if $IFORM = 1$
$$\frac{(Y - YC)^2}{YL^2} + \frac{(Z - ZC)^2}{ZL^2} \ge 1$$
 if $IFORM = 2$

The conditions introduced with CHAMBR are valid along the optical structure until the next occurrence of the keyword CHAMBR. Then, if IL=1 the aperture is possibly modified by introducing new values of YC, ZC, YL and ZL, or, if IL=2 the chamber ends and information is printed concerning those particles that have been stopped.

The testing is done in optical elements at each integration step, between the EFBs. For instance, in QUADRUPO there will be no testing from $-X_E$ to 0 and from XL to $XL + X_S$, but only from 0 to XL; in DIPOLE, there is no testing as long as the $ENTRANCE\ EFB$ is not reached, and testing is stopped as soon as the EXIT or $LATERAL\ EFBs$ are passed.

In optical elements defined in polar coordinates, Y stands for the radial coordinate (e.g., DIPOLE, see Figs. 3C, p. 27, and 11, p. 88). Thus, centering CHAMBR at

YC = RM simulates a chamber curved with radius RM, and having a radial acceptance $RM \pm YL$. In DRIFT, the testing is done at the beginning and at the end, and only for positive drifts. There is no testing in CHANGREF.

When a particle is stopped, its index *IEX* (see *OBJET* and section 4.6.10) is set to the value -4, and its actual path length is stored in the array *SORT* for possible further use.

CHANGREF: Transformation to a new reference frame

CHANGREF transports particles from a reference plane (O, Y, Z) at path distance S, to a new one by a combination of translations and/or rotations. It essentially aims at positioning optical elements with respect to one another, as setting a reference frame at the entrance or exit of field maps, or to simulate misalignments (see also KPOS option). CHANGREF can be placed anywhere in a structure.

Spin tracking, particle decay and gas-scattering are taken into account in *CHANGREF*. Energy loss by synchrotron radiation (*SRLOSS* keyword) is not.

There are two "styles" of CHANGREF, as follows.

The "old style" CHANGREF requires the three data XCE, YCE, ALE and then gets the new particle coordinates Y_2 , T_2 , Z_2 , P_2 and path length S_2 from the old ones Y_1 , T_1 , Z_1 , P_1 and S_1 using

$$T_{2} = T_{1} - ALE$$

$$Y_{2} = \frac{(Y_{1} - YCE)\cos T_{1} + XCE\sin T_{1}}{\cos T_{2}}$$

$$DL^{2} = (XCE - Y_{2}\sin ALE)^{2} + (YCE - Y_{1} + Y_{2}\cos ALE)^{2}$$

$$Z_{2} = Z_{1} + DL\operatorname{tg}P_{1}$$

$$S_{2} = S_{1} + \frac{DL}{\cos P_{1}}$$

$$P_{2} = P_{1}$$

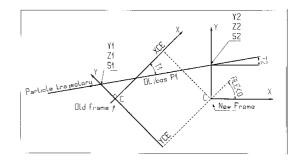


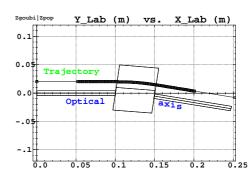
Figure 17: Scheme of the CHANGREF procedure.

where, XCE and YCE are shifts in the horizontal plane along, respectively, X- and Y-axis, and ALE is a rotation around the Z-axis. DL is given the sign of $XCE - Y_2 \sin(ALE)$.

The example below shows the use of *CHANGREF* for the symmetric positioning of a combined function dipole+quadrupole magnet in a drift-bend-drift geometry with 12.691 degrees deviation (obtained upon combined effect of a dipole component and of quadrupole axis shifted 1 cm off optical axis).

Zgoubi data file:

```
Using CHANGREF, "Old style"
'OBJET'
51.71103865921708
                          ! Electron, Ekin=15MeV.
                          ! One particle, with
1 1
2. 0. 0.0 0.0 0.0 1. 'R' ! Y_0=2 cm.
1 1 1 1 1 1 1
'MARKER'
                   .plt
            BEG
                          ! Print into zgoubi.plt.
'DRIFT'
                          ! 10 cm drift.
10.
'CHANGREF'
0. 0. -6.34165
                          ! 1/ half Z-rotation.
'CHANGREF'
0.1.0.
                          ! 2/ Y-shift.
'MULTIPOL'
                 ! Combined function dipole + quadrupole.
                          ! Print into zgoubi.plt.
5 10. 2.064995867082342 2. 0. 0. 0. 0. 0. 0. 0. 0.
0 0 5. 1.1 1.00 1.00 1.00 1.00 1.00 1. 1. 1. 1.
  .1455 2.2670 -.6395 1.1558 0.0.0.
 0 0 5. 1.1 1.00 1.00 1.00 1.00 1.00 1. 1. 1. 1.
  .1455 2.2670 -.6395 1.1558 0.0.
0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0
.1 step size
1 0.0.0.
'CHANGREF'
0. -1. -6.34165
                          ! 1/ Y-shift, 2/ half Z-rotate.
                          ! 10 cm drift.
'DRIFT'
10.
'FAISCEAU'
'END'
```



Note: The square markers scheme the stepwise integration in case of ± 5 cm additional fringe field extent upstream and downstream of the 5 cm long multipole.

The "new style" CHANGREF allows all 6 degrees of freedom rather than just 3, namely, X-, Y-, Z-shift, X-, Y-, Z-rotation. In addition, **CHANGREF** "new style" allows up to 9 successive such elementary transformations, in arbitrary order. The "old style" example above is transposed into "new style", hereafter.

Zgoubi data file:

```
Using CHANGREF, "New Style"
'OBJET'
51.71103865921708
                         ! Electron, Ekin=15MeV.
                     ! One particle, with
1 1
2. 0. 0.0 0.0 0.0 1. 'R' ! Y_0=2 cm.
1 1 1 1 1 1 1
'MARKER' BEG .plt ! Print into zgoubi.plt.
'DRIFT'
                         ! 10 cm drift.
10.
'CHANGREF'
ZR -6.34165 YS 1. ! 1/ half Z-rotate, 2/ Y-shift.
'MULTIPOL' ! Combined function dipole + quadrupole.

2 ! Print into zgoubi plt
! Print into zgoubi.plt.
5 10. 2.064995867082342 2. 0. 0. 0. 0. 0. 0. 0. 0.
0 0 5. 1.1 1.00 1.00 1.00 1.00 1.00 1.1. 1. 1.
4 .1455 2.2670 -.6395 1.1558 0.0.0.
0 0 5. 1.1 1.00 1.00 1.00 1.00 1.00 1. 1. 1. 1.
4 .1455 2.2670 -.6395 1.1558 0.0.0.
0 0 0 0 0 0 0 0 0 0
.1 step size
1 0.0.0.
'CHANGREF'
YS -1. ZR -6.34165 ! 1/ Y-shift, 2/ half Z-rotate.
'DRIFT'
                           ! 10 cm drift.
10.
'FAISCEAU'
'END'
```

CIBLE or TARGET: Generate a secondary beam following target interaction

The reaction is $1+2 \longrightarrow 3+4$ with the following parameters

The geometry of the interaction is shown in Fig. 18.

The angular sampling at the exit of the target consists of the NT coordinates $0, \pm TS, \pm 2*TS... \pm (NT-1)*TS/2$ in the median plane, and the NP coordinates $0, \pm PS, \pm 2*PS... \pm (NP-1)*PS/2$ in the vertical plane.

The position of B downstream is deduced from that of A upstream by a transformation equivalent to two transformations using CHANGREF, namely

$$CHANGREF(XCE = YCE = 0, ALE = \beta)$$

followed by

CHANGREF(
$$XCE = YCE = 0$$
, $ALE = \theta - \beta$).

Particle 4 is discarded, while particle 3 continues. The energy loss Q is related to the variable mass M_4 by

$$Q = M_1 + M_2 - (M_3 + M_4)$$
 and $dQ = -dM_4$

The momentum sampling of particle 3 is derived from conservation of energy and momentum, according to

$$M_1c^2 + W_2 = W_3 + W_4$$

 $p_4^2 = p_2^2 + p_3^2 - 2p_2p_3\cos(\theta - T)$

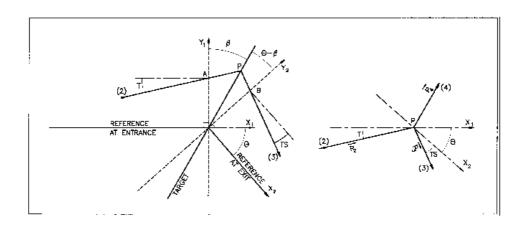


Figure 18: Scheme of the principles of CIBLE (TARGET)

A, T = position, angle of incoming particle 2 in the entrance reference frame

P = position of the interaction

B, T =position, angle of the secondary particle in the exit reference frame

 θ = angle between entrance and exit frames

 β = tilt angle of the target

COLLIMA: Collimator

COLLIMA acts as a mathematical aperture of zero length. It causes the identification, counting and stopping of particles that reach the aperture limits.

Physical Aperture

A physical aperture can be either rectangular (*IFORM* = 1) or elliptic (*IFORM* = 2). The collimator is centered at YC, ZC and has transverse dimensions $\pm YL$ and $\pm ZL$ such that any particle will be stopped if its coordinates Y, Z satisfy

$$(Y - YC)^2 \ge YL^2 \text{ or } (Z - ZC)^2 \ge ZL^2 \text{ if } IFORM = 1$$

$$\frac{(Y - YC)^2}{YL^2} + \frac{(Z - ZC)^2}{ZL^2} \ge 1 \text{ if } IFORM = 2$$

Longitudinal Phase-space Collimation

COLLIMA can act as a longitudinal phase-space aperture, coordinates acted on are selected with *IFORM.J.* Any particle will be stopped if its horizontal (h) and vertical (v) coordinates satisfy

$$(h \le h_{min} \text{ or } h \ge h_{max}) \text{ or } (v \le v_{min} \text{ or } v \ge v_{max})$$

wherein, h is either path length S if IFORM=6 or time if IFORM=7, and v is either 1+DP/P if J=1 or kinetic energy if J=2 (provided mass and charge have been defined using the keyword PARTICUL).

Transverse Phase-space Collimation

COLLIMA can act as a transverse phase-space aperture. Any particle will be stopped if its coordinates satisfy

$$\gamma_Y Y^2 + 2\alpha_Y YT + \beta_Y T^2 \ge \epsilon_Y / \pi$$
 if $IFORM = 11$ or 14 $\gamma_Z Z^2 + 2\alpha_Z ZP + \beta_Z P^2 \ge \epsilon_Z / \pi$ if $IFORM = 12$ or 15

If IFORM=11 (respectively 12) then ϵ_Y/π (respectively ϵ_Z/π) is to be specified by the user as well as $\alpha_{Y,Z}$, $\beta_{Y,Z}$. If IFORM=14 (respectively 15) then α_Y and β_Y (respectively α_Z , β_Z) are determined by **zgoubi** by prior computation of the matched ellipse to the particle population, so only $\epsilon_{Y,Z}/\pi$ need be specified by the user.

When a particle is stopped, its index *IEX* (see *OBJET* and section 4.6.10) is set to the value -4, and its actual path length is stored in the array *SORT* for possible further use with *HISTO*).

DECAPOLE: Decapole magnet (Fig. 19)

The meaning of parameters for DECAPOLE is the same as for QUADRUPO.

In fringe field regions the magnetic field $\vec{B}(X,Y,Z)$ and its derivatives up to fourth order are derived from the scalar potential expressed to the 5th order in Y and Z

$$V(X,Y,Z)=G(X)\left(Y^4Z-2Y^2Z^3+\frac{Z^5}{5}\right)$$
 with $G_0=\frac{B_0}{R_0^4}$

The modelling of the fringe field form factor G(X) is described under $\it QUADRUPO$, p. 138.

Outside fringe field regions, or everywhere in sharp edge decapole ($\lambda_E = \lambda_S = 0$), $\vec{B}(X,Y,Z)$ in the magnet is given by

$$B_X = 0$$

$$B_Y = 4G_0(Y^2 - Z^2)YZ$$

$$B_Z = G_0(Y^4 - 6Y^2Z^2 + Z^4)$$

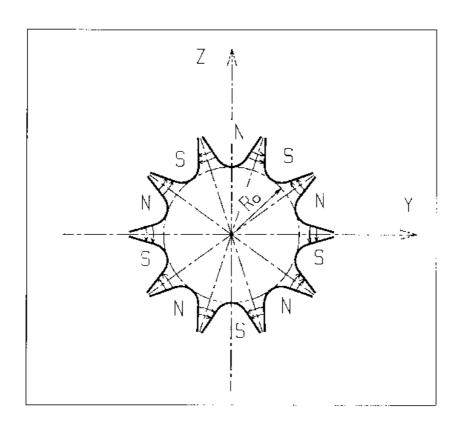


Figure 19: Decapole magnet

DIPOLE: Dipole magnet, polar frame

DIPOLE provides a model of a dipole field, possibly with transverse indices. The field along a particle trajectory is computed as the particle motion proceeds, straightforwardly from the dipole geometrical boundaries. Field simulation in DIPOLE is the same as used in DIPOLE-M and AIMANT for computing a field map; the essential difference in DIPOLE is in its skipping that intermediate stage of field map generation found in DIPOLE-M and AIMANT.

DIPOLE has a version, *DIPOLES*, that allows overlapping of fringe fields in a configuration of neighboring magnets.

The dimensioning of the magnet is defined by (Fig. 11, p. 88)

AT: total angular aperture

RM: mean radius used for the positioning of field boundaries

The 2 or 3 effective field boundaries (EFB), from which the dipole field is drawn, are defined from geometric boundaries, the shape and position of which are determined by the following parameters.

ACENT: arbitrary inner angle, used for EFBs positioning ω : azimuth of an EFB with respect to ACENT

 θ : angle of an EFB with respect to its azimuth (wedge angle)

 R_1, R_2 : radius of curvature of an EFB U_1, U_2 : extent of the linear part of an EFB.

The magnetic field is calculated in polar coordinates. At any position (R, θ) along the particle trajectory the value of the vertical component of the mid-plane field is calculated using

$$B_Z(R,\theta) = \mathcal{F}(R,\theta) * B_0 * \left(1 + N * \left(\frac{R - RM}{RM}\right) + B * \left(\frac{R - RM}{RM}\right)^2 + G * \left(\frac{R - RM}{RM}\right)^3\right)$$
(4.4.8)

where N, B and G are respectively the first, second and third order field indices and $\mathcal{F}(R,\theta)$ is the fringe field coefficient (it determines the "flutter" in periodic structures).

Calculation of the Fringe Field Coefficient

With each EFB a realistic extent of the fringe field, λ (normally equal to the gap size), is associated and a fringe field coefficient F is calculated. In the following λ stands for either λ_E (Entrance), λ_S (Exit) or λ_L (Lateral EFB).

F is an exponential type fringe field (Fig. 12, p. 90) given by [34]

$$F = \frac{1}{1 + \exp P(s)}$$

wherein s is the distance to the EFB and depends on (R, θ) , and

$$P(s) = C_0 + C_1 \left(\frac{s}{\lambda}\right) + C_2 \left(\frac{s}{\lambda}\right)^2 + C_3 \left(\frac{s}{\lambda}\right)^3 + C_4 \left(\frac{s}{\lambda}\right)^4 + C_5 \left(\frac{s}{\lambda}\right)^5$$

It is also possible to simulate a shift of the *EFB*, by giving a non zero value to the parameter *shift*. s is then changed to s-*shift* in the previous equation. This allows small variations of the magnetic length.

Let F_E (respectively F_S , F_L) be the fringe field coefficient attached to the entrance (respectively exit, lateral) EFB. At any position on a trajectory the resulting value of the fringe field coefficient (eq. 4.4.8) is

$$\mathcal{F}(R,\theta) = F_E * F_S * F_L$$

In particular, $F_L \equiv 1$ if no lateral EFB is requested.

Calculation of the Mid-plane Field and Derivatives

 $B_Z(R,\theta)$ in Eq. 4.4.8 is computed at the $n \times n$ nodes (n=3 or 5 in practice) of a "flying" interpolation grid in the median plane centered on the projection m_0 of the actual particle position M_0 as schemed in Fig. 20. A polynomial interpolation is involved, of the form

$$B_Z(R,\theta) = A_{00} + A_{10}\theta + A_{01}R + A_{20}\theta^2 + A_{11}\theta R + A_{02}R^2$$

that yields the requested derivatives, using

$$A_{kl} = \frac{1}{k!l!} \frac{\partial^{k+l} B_Z}{\partial \theta^k \partial r^l}$$

Note that, the source code contains the explicit analytical expressions of the coefficients A_{kl} solutions of the normal equations, so that the operation is not CPU time consuming.

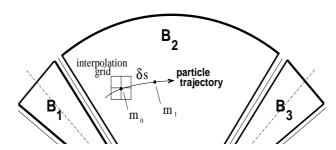


Figure 20: Interpolation method. m_0 and m_1 are the projections in the median plane of particle positions M_0 and M_1 and separated by δs , projection of the integration step.

Extrapolation Off Median Plane

From the vertical field \vec{B} and derivatives in the median plane, first a transformation from polar to Cartesian coordinates is performed, following eqs (1.4.9 or 1.4.10), then, extrapolation off median plane is performed by means of Taylor expansions, following the procedure described in section 1.3.3.

DIPOLE-M: Generation of dipole mid-plane 2-D map, polar frame

DIPOLE-M is a more recent, simpler and improved version of AIMANT.

The keyword *DIPOLE-M* provides an automatic generation of a dipole field map in polar coordinates. The extent of the map is defined by the following parameters, as shown in Figs. 11A and 11B.

AT : total angular aperture

RM : mean radius used for the positioning of field boundaries

RMIN, RMAX: minimum and maximum radii

The 2 or 3 effective field boundaries (EFB) inside the map are defined from geometric boundaries, the shape and position of which are determined by the following parameters.

ACENT: arbitrary inner angle, used for EFBs positioning ω : azimuth of an EFB with respect to ACENT

 θ : angle of an EFB with respect to its azimuth (wedge angle)

 R_1, R_2 : radius of curvature of an EFB U_1, U_2 : extent of the linear part of an EFB.

At any node of the map mesh, the value of the field is calculated as

$$B_Z(R,\theta) = \mathcal{F}(R,\theta) * B_0 * \left(1 + N * \left(\frac{R - RM}{RM}\right) + B * \left(\frac{R - RM}{RM}\right)^2 + G * \left(\frac{R - RM}{RM}\right)^3\right)$$
(4.4.9)

where N, B and G are respectively the first, second and third order field indices and \mathcal{F} is the fringe field coefficient.

Calculation of the Fringe Field Coefficient

With each EFB a realistic extent of the fringe field, λ (normally equal to the gap size), is associated and a fringe field coefficient F is calculated. In the following λ stands for either λ_E (Entrance), λ_S (Exit) or λ_L (Lateral EFB).

F is an exponential type fringe field (Fig. 12) given by [34]

$$F = \frac{1}{1 + \exp P(s)}$$

where s is the distance to the EFB, and

$$P(s) = C_0 + C_1 \left(\frac{s}{\lambda}\right) + C_2 \left(\frac{s}{\lambda}\right)^2 + C_3 \left(\frac{s}{\lambda}\right)^3 + C_4 \left(\frac{s}{\lambda}\right)^4 + C_5 \left(\frac{s}{\lambda}\right)^5$$

It is also possible to simulate a shift of the *EFB*, by giving a non zero value to the parameter *shift*. s is then changed to s-shift in the previous equation. This allows small variations of the total magnetic length.

Let F_E (respectively F_S , F_L) be the fringe field coefficient attached to the entrance (respectively exit, lateral) EFB. At any node of the map mesh, the resulting value of the fringe field coefficient (eq. 4.4.9) is

$$\mathcal{F}(R,\theta) = F_E * F_S * F_L$$

In particular, $F_L \equiv 1$ if no lateral EFB is requested.

The Mesh of the Field Map

The magnetic field is calculated at the nodes of a mesh with polar coordinates, in the median plane. The radial step is given by

$$\delta R = \frac{RMAX - RMIN}{IRMAX - 1}$$

and the angular step by

$$\delta\theta = \frac{AT}{IAMAX - 1}$$

where RMIN and RMAX are the lower and upper radial limits of the field map, and AT is its total angular aperture (Fig. 11B). IRMAX and IAMAX are the total number of nodes in the radial and angular directions.

Simulating Field Defects and Shims

Once the initial map is calculated, it is possible to modify it by means of the parameter *NBS*, so as to simulate field defects or shims.

If NBS = -2, the map is globally modified by a perturbation proportional to $R - R_0$, where R_0 is an arbitrary radius, with an amplitude $\Delta B_Z/B_0$, so that B_Z at the nodes of the mesh is replaced by

$$B_Z * \left(1 + \frac{\Delta B_Z}{B_0} \, \frac{R - R_0}{\text{RMAX-RMIN}}\right)$$

If NBS = -1, the perturbation is proportional to $\theta - \theta_0$, and B_Z is replaced by

$$B_Z * \left(1 + \frac{\Delta B_Z}{B_0} \frac{\theta - \theta_0}{AT} \right)$$

If NBS \geq 1, then NBS shims are introduced at positions $\frac{R_1 + R_2}{2}$, $\frac{\theta_1 + \theta_2}{2}$ (Fig. 14) [35] The initial field map is modified by shims with second order profiles given by

$$\theta = \left(\gamma + \frac{\alpha}{\mu}\right) \beta \, \frac{X^2}{\rho^2}$$

where X is shown in Fig. 12, $\rho = \frac{R_1 + R_2}{2}$ is the central radius, α and γ are the angular limits of the shim, β and μ are parameters.

At each shim, the value of B_Z at any node of the initial map is replaced by

$$B_Z * \left(1 + F\theta * FR * \frac{\Delta B_Z}{B_0} \right)$$

where $F\theta = 0$ or FR = 0 outside the shim, and $F\theta = 1$ and FR = 1 inside.

Extrapolation Off Median Plane

The vector field \vec{B} and its derivatives in the median plane are calculated by means of a second or fourth order polynomial interpolation, depending on the value of the parameter *IORDRE* (*IORDRE*=2, 25 or 4, see section 1.4.2). The transformation from polar to Cartesian coordinates is performed following eqs (1.4.9 or 1.4.10). Extrapolation off median plane is then performed by means of Taylor expansions, following the procedure described in section 1.3.3.

DIPOLES : Dipole magnet N-tuple, polar frame [38, 39]

DIPOLES works much like DIPOLE as to the field modelling, yet with the particularity that it allows positioning up to 5 such dipoles within the angular sector with full aperture AT thus allowing accounting for overlapping fringe fields. This is done in the following way⁵.

The dimensioning of the magnet is defined by

AT: total angular aperture

RM: mean radius used for the positioning of field boundaries

For each one of the N=1 to 5 dipoles of the N-tuple, the 2 effective field boundaries (entrance and exit EFBs) from which the dipole field (eqs. 4.4.10, 4.4.11) is drawn are defined from geometrical boundaries, the shape and position of which are determined by the following parameters (in the same manner as in DIPOLE, DIPOLE-M) (see Fig. 11-A, p. 88, and Fig. 21)

 ACN_i : arbitrary inner angle, used for EFBs positioning

 ω : azimuth of an EFB with respect to ACN

 θ : angle of an EFB with respect to its azimuth (wedge angle)

 R_1, R_2 : radius of curvature of an EFB U_1, U_2 : extent of the linear part of an EFB

Calculation of the Field From a Single Dipole

The magnetic field is calculated in polar coordinates. At all (R, θ) in the median plane (Z = 0), the magnetic field due a single one (index i) of the dipoles of a N-tuple magnet can take either form, upon option,

(i)
$$B_{Zi}(R,\theta) = B_{Z0,i} \mathcal{F}_i(R,\theta) \left(1 + b_{1i}(R - RM_i)/RM_i + b_{2i}(R - RM_i)^2/RM_i^2 + \dots\right) (4.4.10)$$

(ii)
$$B_Z(R,\theta) = B_{Z_{0,i}} + \sum_{i=1}^N \mathcal{F}_i(R,\theta) \left(b_{1_i}(R - RM_i) + b_{2_i}(R - RM_i)^2 + \dots \right)$$
(4.4.11)

wherein $B_{Z_{0,i}}$ is a reference field, at reference radius RM_i , and $\mathcal{F}(R,\theta)$ is the fringe field coefficient, see below. This field model is proper to simulate for instance chicane dipoles, cyclotron or FFAG magnets, etc.



Figure 21: Definition of a dipole triplet using the *DIPOLES* or *FFAG* procedures.

Calculation of the Fringe Field Coefficient

In a dipole, a realistic extent of the fringe field, g, is associated with each EFB, and a fringe field coefficient F is calculated.

⁵FFAG can be referred to as another instance of a procedure based on such method.

F is an exponential type fringe field (Fig. 12, page 90) given by [34]

$$F = \frac{1}{1 + \exp P(d)}$$

wherein d is the distance to the EFB and depends on (R, θ) , and

$$P(d) = C_0 + C_1 \left(\frac{d}{g}\right) + C_2 \left(\frac{d}{g}\right)^2 + C_3 \left(\frac{d}{g}\right)^3 + C_4 \left(\frac{d}{g}\right)^4 + C_5 \left(\frac{d}{g}\right)^5$$

In addition, g is made dependent of R (a way to simulate the effect of variable gap size on fringe field extent), under the form

$$g(R) = g_0 (RM/R)^{\kappa}$$

This dependence is accounted for rigorously if the interpolation method (see below) is used, or else to order zero (derivatives of g(R) are not considered) if the analytic method (below) is used.

Let F_E (respectively F_S) be the fringe field coefficient attached to the entrance (respectively exit) EFB; at any position on a trajectory the resulting value of the fringe field coefficient is taken to be

$$\mathcal{F}_i(R,\theta) = F_E * F_S \tag{4.4.12}$$

Calculation of the Field Resulting From all N Dipoles

Now, accounting for N neighboring dipoles in an N-tuple, the mid-plane field and field derivatives are obtained by addition of the contributions of the N dipoles taken separately, namely

$$B_Z(R,\theta) = \sum_{i=1}^{N} B_{Zi}(R,\theta)$$
 (4.4.13)

$$\frac{\partial^{k+l}\vec{B_Z}(R,\theta)}{\partial\theta^k\partial r^l} = \sum_{i=1,N} \frac{\partial^{k+l}\vec{B_Z_i}(R,\theta)}{\partial\theta^k\partial r^l}$$
(4.4.14)

Note that, in doing so it is not meant that field superposition does apply in reality, it is just meant to provide the possibility of obtaining a realistic field shape, that would for instance closely match (using appropriate $C_0 - C_5$ sets of coefficients) 3-D field simulations obtained from magnet design codes.

Calculation of the Mid-plane Field Derivatives

Two methods have been implemented to calculate the field derivatives in the median plane (Eq. 4.4.13), based on either analytical expressions derived from the magnet geometrical description, or classical numerical interpolation.

The first method has the merit of insuring best symplecticity in principle and fastest tracking. The interest of the second method is in its facilitating possible changes in the mid-plane magnetic field model $B_Z(R, \theta)$, for instance if simulations of shims, defects, or special R, θ field dependence need to be introduced.

Analytical method [40]:

The starting ingredients are, on the one hand distances to the EFBs,

$$d(R,\theta) = \sqrt{(x(R,\theta) - x_0(R,\theta))^2 + (y(R,\theta) - y_0(R,\theta))^2}$$

to be computed for the two cases d_{Entrance} , d_{Exit} , and on the other hand the expressions of the coordinates of particle position M and its projection P on the EFB in terms of the magnet geometrical parameters, namely

$$\begin{array}{rcl} x(R,\theta) & = & \cos(ACN - \theta) - RM \\ y(R,\theta) & = & R\sin(ACN - \theta) \\ x_P(R,\theta) & = & \sin(u) \left(y(R,\theta) - y_b \right) / 2 + x_b \sin^2(u) + x(R,\theta) \cos^2(u) \\ y_P(R,\theta) & = & \sin(u) \left(x(R,\theta) - x_b \right) / 2 + y_b \cos^2(u) + y(R,\theta) \sin^2(u) \end{array}$$

with x_b , y_b , u parameters drawn from the magnet geometry (sector angle, wedge angle, face curvatures, etc.).

These ingredients allow calculating the derivatives $\frac{\partial^{u+v}x(R,\theta)}{\partial\theta^u\partial r^v}, \frac{\partial^{u+v}y(R,\theta)}{\partial\theta^u\partial r^v}, \frac{\partial^{u+v}x_0(R,\theta)}{\partial\theta^u\partial r^v}, \frac{\partial^{u+v}x_0(R,\theta)}{\partial\theta^u\partial r^v}, \frac{\partial^{u+v}y_0(R,\theta)}{\partial\theta^u\partial r^v}, \frac{\partial^{u+v}y_0$

Interpolation method:

The expression $B_Z(R, \theta)$ in Eq. 4.4.13 is, in this case, computed at the $n \times n$ nodes (n = 3 or 5 in practice) of a "flying" interpolation grid in the median plane centered on the projection m_0 of the actual particle position M_0 as schemed in Fig. 22. A polynomial interpolation is involved, of the form

$$B_Z(R,\theta) = A_{00} + A_{10}\theta + A_{01}R + A_{20}\theta^2 + A_{11}\theta R + A_{02}R^2$$

that yields the requested derivatives, using

$$A_{kl} = \frac{1}{k!l!} \frac{\partial^{k+l} B}{\partial \theta^k \partial r^l}$$

Note that, the source code contains the explicit analytical expressions of the coefficients A_{kl} solutions of the normal equations, so that the operation is not CPU time consuming.



Figure 22: Interpolation method. m_0 and m_1 are the projections in the median plane of particle positions M_0 and M_1 and separated by δs , projection of the integration step.

Extrapolation Off Median Plane

From the vertical field \vec{B} and derivatives in the median plane, first a transformation from polar to Cartesian coordinates is performed, following eqs (1.4.9 or 1.4.10), then, extrapolation off median plane is performed by means of Taylor expansions, following the procedure described in section 1.3.3.

Sharp Edge

Sharp edge field fall-off at a field boundary can only be simulated if the following conditions are fulfilled:

- entrance (resp. exit) field boundary coincides with entrance (resp. exit) dipole limit (it means in particular, see Fig. 11, $\omega^+ = ACENT$ (resp. $\omega^- = -(AT ACENT)$), together with $\theta = 0$ at entrance (resp. exit) EFBs),
 - analytical method for calculation of the mid-plane field derivatives is used.

DODECAPO: Dodecapole magnet (Fig. 23)

The meaning of parameters for DODECAPO is the same as for QUADRUPO.

In fringe field regions the magnetic field $\vec{B}(X,Y,Z)$ and its derivatives up to fourth order are derived from the scalar potential approximated to the 6th order in Y and Z

$$V(X,Y,Z)=G(X)\left(Y^4-\frac{10}{3}Y^2Z^2+Z^4\right)YZ$$
 with $G_0=\frac{B_0}{R_0^5}$

The modelling of the fringe field form factor G(X) is described under QUADRUPO, p. 138.

Outside fringe field regions, or everywhere in sharp edge dodecapole ($\lambda_E = \lambda_S = 0$), $\vec{B}(X,Y,Z)$ in the magnet is given by

$$B_X = 0$$

$$B_Y = G_0(5Y^4 - 10Y^2Z^2 + Z^4)Z$$

$$B_Z = G_0(Y^4 - 10Y^2Z^2 + 5Z^4)Y$$

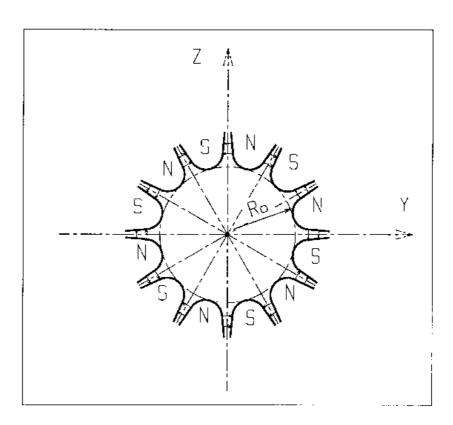


Figure 23: Dodecapole magnet

DRIFT or **ESL**: Field free drift space

DRIFT or ESL allow introduction of a drift space with length XL with positive or negative sign, anywhere in a structure. The associated equations of motion are (Fig. 24)

$$Y_2 = Y_1 + XL * tgT$$

$$Z_2 = Z_1 + \frac{XL}{\cos T} tgP$$

$$SAR_2 = SAR_1 + \frac{XL}{\cos T * \cos P}$$



Figure 24: Transfer of particles in a drift space.

EBMULT: Electro-magnetic multipole

EBMULT simulates an electro-magnetic multipole, by addition of electric (\vec{E}) and magnetic (\vec{B}) multipole components (dipole to 20-pole). \vec{E} and its derivatives $\frac{\partial^{i+j+k}\vec{E}}{\partial X^i\partial Y^j\partial Z^k}$ $(i+j+k\leq 4)$ are derived from the general expression of the multipole scalar potential (eq. 1.3.5), followed by a $\frac{\pi}{2n}$ rotation (n=1,2,3,...) (see also ELMULT). \vec{B} and its derivatives are derived from the same general potential, as described in section 1.3.7 (see also MULTIPOL).

The entrance and exit fringe fields of the \vec{E} and \vec{B} components are treated separately, in the same way as described under *ELMULT* and *MULTIPOL*, for each one of these two fields. Wedge angle correction is applied in sharp edge field model if $\vec{B}1$ is non zero, as in *MULTIPOL*. Any of the \vec{E} or \vec{B} multipole field component can be X-rotated independently of the others.

Use PARTICUL prior to EBMULT, for the definition of particle mass and charge.



Figure 25: An example of \vec{E} , \vec{B} multipole : the achromatic quadrupole (known for its allowing null second order chromatic aberrations [41]).

EL2TUB: Two-tube electrostatic lens

The lens is cylindrically symmetric about the X-axis.

The length and potential of the first (resp. second) electrode are X1 and V1 (X2 and V2). The distance between the two electrodes is D, and their inner radius is R_0 (Fig. 26). The model for the electrostatic potential along the axis is [42]

$$V(X) = \frac{V_2 - V_1}{2} \text{ th } \frac{\omega x}{R_0} \left[+ \frac{V_1 + V_2}{2} \right]$$
 if $D = 0$

$$V(X) = \frac{V_2 - V_1}{2} \frac{1}{2\omega D/R_0} \ln \frac{\operatorname{ch} \omega}{\operatorname{ch} \omega} \frac{x + D}{R_0} \left[+ \frac{V_1 + V_2}{2} \right] \qquad \text{if } D \neq 0$$

(x= distance from half-way between the electrodes; $\omega=1.318$; th = hyperbolic tangent; ch = hyperbolic cosine) from which the field $\vec{E}(X,Y,Z)$ and its derivatives are derived following the procedure described in section 1.3.1 (note that they don't depend on the constant term $\left[\frac{V_1+V_2}{2}\right]$ which disappears when differentiating).

Use PARTICUL prior to EL2TUB, for the definition of particle mass and charge.

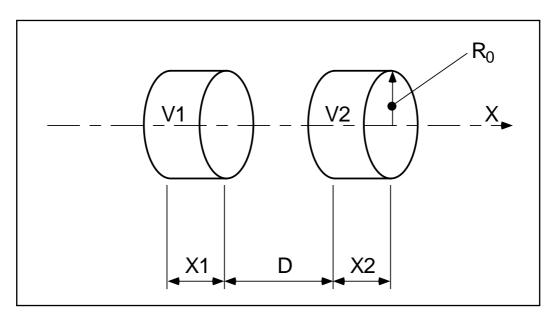


Figure 26: Two-electrode cylindrical electric lens.

ELMIR: Electrostatic N-electrode mirror/lens, straight slits

The device works as mirror or lens, horizontal or vertical. It is made of N 2-plate electrodes and has mid-plane symmetry.

Electrode lengths are L1, L2, ..., LN. D is the mirror/lens gap. The model for the Y-independent electrostatic potential is (after Ref. [43, p.412])

$$V(X,Z) = \sum_{i=2}^{N} \frac{Vi - Vi - 1}{\pi} \arctan \frac{\sinh(\pi(X - Xi - 1)/D)}{\cos(\pi Z/D)}$$

where Vi are the potential at the N electrodes (and normally V1=0 refers to the incident beam energy), Xi are the locations of the zero-length slits, X is the distance from the origin taken at the first slit (located at $X1\equiv 0$ between the first and second electrodes). From V(X,Z) the field $\vec{E}(X,Y,Z)$ and derivatives are deduced following the procedure described in section 1.3.7 (page 25).

The total X-extent of the mirror/lens is $L = \sum_{i=1}^{N} Li$.

In the mirror mode (option MT=11 for vertical mid-plane or MT=12 for horizontal mid-plane) stepwise integration starts at $X=-L\!1$ (entrance of the first electrode) and terminates either when back to $X=-L\!1$ or when reaching $X=L-L\!1$ (end of the N-th electrode). In the latter case particles are stopped with their index $I\!E\!X$ set to -8 (see section 4.6.10 on page 173). Normally $X\!1$ should exceed 3D (enough that $V(X< X\!1)$ have negligible effect in terms of trajectory behavior).

In the lens mode (option flag MT=21 for vertical mid-plane or MT=22 for horizontal mid-plane) stepwise integration starts at X=-L1 (entrance of the first electrode) and terminates either when reaching X=L-L1 (end of the N-th electrode) or when the particle deflection exceeds $\pi/2$. In the latter case the particle is stopped with their index IEX set to -3.

Use PARTICUL prior to ELMIR, for the definition of particle mass and charge.



Figure 27: Electrostatic N-electrode mirror/lens, straight slits, in the case N=3, in horizontal mirror mode (MT=11). Possible non-zero entrance quantities YCE, ALE should be specified using CHANGREF, or using KPOS=3 with YCE and ALE=half-deviation matched to the reference trajectory.

ELMIRC: Electrostatic N-electrode mirror/lens, circular slits [43]

The device works as mirror or lens, horizontal or vertical. It is made of N 2-plate electrodes and has mid-plane symmetry⁶.

Electrode slits are circular, concentric with radii R1, R2, ..., R_{N-1} , D is the mirror/lens gap. The model for the mid-plane (Z=0) radial electrostatic potential is (after Ref. [43, p.443])

$$V(r) = \sum_{i=2}^{N} \frac{Vi - Vi - 1}{\pi} \arctan\left(\sinh\frac{\pi(r - Ri - 1)}{D}\right)$$

where Vi are the potential at the N electrodes (and normally V1 = 0 refers to the incident beam energy). r is the current radius.

The mid-plane field $\vec{E}(r)$ and its r-derivatives are first derived by differentiation, then $\vec{E}(r,Z)$ and derivatives are obtained from Taylor expansions and Maxwell relations. Eventually a transformation to the rotating frame provides $\vec{E}(X,Y,Z)$ and derivatives as involved in eq. 1.2.15.

Stepwise integration starts at entrance (defined by RE, TE) of the first electrode and terminates when rotation of the reference rotating frame (RM, X, Y) has reached the value AT. Normally, R1 - RE and R1 - RS should both exceed 3D (so that potential tails have negligible effect in terms of trajectory behavior).

Positioning of the element is performed by means of KPOS (see section 4.6.7).

Use PARTICUL prior to ELMIRC, for the definition of particle mass and charge.



Figure 28: Electrostatic N-electrode mirror/lens, circular slits, in the case N=3, in horizontal mirror mode.

 $^{^6}$ NOTE: in the present version of the code, the sole horizontal mirror mode is operational, and N is limited to 3.

ELMULT: Electric multipole

The simulation of multipolar electric field \vec{M}_E proceeds by addition of the dipolar $(\vec{E}1)$, quadrupolar $(\vec{E}2)$, sextupolar $(\vec{E}3)$, etc., up to 20-polar $(\vec{E}10)$ components, and of their derivatives up to fourth order, following

$$\begin{split} \vec{M}_E &= \vec{E}1 + \vec{E}2 + \vec{E}3 + \ \dots \ + \vec{E}10 \\ \frac{\partial \vec{M}_E}{\partial X} &= \frac{\partial \vec{E}1}{\partial X} + \frac{\partial \vec{E}2}{\partial X} + \frac{\partial \vec{E}3}{\partial X} + \dots \ + \frac{\partial \vec{E}10}{\partial X} \\ \frac{\partial^2 M_E}{\partial X \partial Z} &= \frac{\partial^2 \vec{E}1}{\partial X \partial Z} + \frac{\partial^2 \vec{E}2}{\partial X \partial Z} + \frac{\partial^2 \vec{E}3}{\partial X \partial Z} + \dots \ + \frac{\partial^2 \vec{E}10}{\partial X \partial Z} \\ \text{etc.} \end{split}$$

The independent components $\vec{E}1$ to $\vec{E}10$ and their derivatives up to the fourth order are calculated by differentiating the general multipole potential given in eq. 1.3.5 (page 25), followed by a $\frac{\pi}{2n}$ rotation about the X-axis, so that the so defined right electric multipole of order n, and of strength [41, 44]

$$K_n = \frac{1}{2} \frac{\gamma}{\gamma^2 - 1} \frac{V_n}{R_0^n}$$

 $(V_n = \text{potential at the electrode}, R_0 = \text{radius at pole tip}, \gamma = \text{relativistic Lorentz factor of the particle})$ has the same focusing effect as the right magnetic multipole of order n and strength $K_n = \frac{B_n}{R_0^{n-1}B\rho}$ ($B_n = \text{field}$ at pole tip, $B\rho = \text{particle rigidity}$, see MULTIPOL).

The entrance and exit fringe fields are treated separately. They are characterized by the integration zone X_E at entrance and X_S at exit, as for *QUADRUPO*, and by the extent λ_E at entrance, λ_S at exit. The fringe field extents for the dipole component are λ_E and λ_S . The fringe field extent for the quadrupolar (sextupolar, ..., 20-polar) component is given by a coefficient E_2 (E_3 , ..., E_{10}) at entrance, and E_2 (E_3 , ..., E_{10}) at exit, such that the fringe field extent is E_3 (E_4) at exit, E_4) at entrance and E_3 (E_4) at exit, E_5 0 at exit.

If $\lambda_E = 0$ ($\lambda_S = 0$) the multipole lens is considered to have a sharp edge field at entrance (exit), and then, $X_E(X_S)$ is forced to zero (for the mere purpose of saving computing time).

If $E_i = 0$ ($S_i = 0$) (i = 2, 10), the entrance (exit) fringe field for multipole component i is considered as a sharp edge field.

Any multipole component $\vec{E}i$ can be rotated independently by an angle RXi around the longitudinal X-axis, for the simulation of positioning defects, as well as skew lenses.

Use PARTICUL prior to ELMULT, for the definition of particle mass and charge.



Figure 29: An electric multipole combining skew-quadrupole $(\vec{E}2 \neq \vec{0}, \vec{R}2 = \pi/4)$ and skew-octupole $(\vec{E}4 \neq \vec{0}, \vec{R}4 = \pi/8)$ components $(\vec{E}1 = \vec{E}3 = \vec{E}5 = ... = \vec{E}10 = \vec{0})$ [44].

ELREVOL: 1-D uniform mesh electric field map

ELREVOL reads a 1-D axial field map from a storage data file, whose content must fit the following FORTRAN reading sequence

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED'])
DO 1 I=1, IX
   IF (BINARY) THEN
      READ(NL) X(I), EX(I)
ELSE
      READ(NL,*) X(I), EX(I)
ENDIF
1 CONTINUE
```

where IX is the number of nodes along the (symmetry) X-axis, X(I) their coordinates, and EX(I) are the values of the X component of the field. EX is normalized with ENORM prior to ray-tracing. As well the longitudinal coordinate X is normalized with a XNORM coefficient (useful to convert to centimeters, the working units in zgoubi).

X-cylindrical symmetry is assumed, resulting in EY and EZ taken to be zero on axis. $\vec{E}(X,Y,Z)$ and its derivatives along a particle trajectory are calculated by means of a 5-points polynomial interpolation followed by second order off-axis extrapolation (see sections 1.3.1 and 1.4.1).

Entrance and/or exit integration boundaries may be defined in the same way as in *CARTEMES* by means of the flag ID and coefficients A, B, C, A', B', C'.

Use PARTICUL prior to ELREVOL, for the definition of particle mass and charge.

EMMA: 2-D Cartesian or cylindrical mesh field map for EMMA FFAG

EMMA is dedicated to the reading and treatment of 2-D or 3-D Cartesian mesh field maps representing the EMMA FFAG cell quadrupole doublet⁷ [47, 48].

EMMA can sum up independent field maps of each of the two quadrupoles, with each its scaling coefficient. The two maps can be radially positioned independently of one another at Y_F , Y_D respectively, just like the actual EMMA quadrupoles. In particular,

MOD: operational and map FORMAT reading mode;

MOD≤19 : Cartesian mesh ; *MOD*>20 : cylindrical mesh.

MOD=0: two 2D maps, one representing QF, one representing QD. A single map, superimposition of both, is built prior to tracking and used for tracking.

MOD=1: two 2D maps, one representing QF, one representing QD, a resulting single map is devised in the following way: QF_new is interpolated from QF with dr=xF, QD_new is interpolated from QD with dr=xD. A single map, superimposition of both, is built prior to tracking and used for tracking.

The parameters that move/position the maps, as (Y_F, Y_D) , are accessible from the FIT, allowing to adjust the cell tunes.

EMMA works much like TOSCA. Refer to that keyword, and to the FORTRAN file emmac.f, for details.

⁷The stepwise ray-tracing code Zgoubi is the on-line model code for the worlds first non-scaling FFAG experiment.

FFAG: FFAG magnet, N-tuple [38, 39]

FFAG works much like DIPOLES as to the field modelling, apart from the radial dependence of the field, $B = B_0(r/r_0)^k$, so-called "scaling". Note that DIPOLES does similar job by using a Taylor r-expansion of $B_0(r/r_0)^k$.

The FFAG procedure allows overlapping of fringe fields of neighboring dipoles, thus simulating in some sort the field in a dipole N-tuple - as for instance in an FFAG doublet or triplet. A detailed application, with five dipoles, can be found in Ref. [38]. This is done in the way described below.

The dimensioning of the magnet is defined by

AT: total angular aperture

RM: mean radius used for the positioning of field boundaries

For each one of the N=1 to (maximum) 5 dipoles of the N-tuple, the two effective field boundaries (entrance and exit EFBs) from which the dipole field is drawn are defined from geometric boundaries, the shape and position of which are determined by the following parameters (in the same manner as in *DIPOLE*, *DIPOLE-M*) (see Fig. 11-A page 88, and Fig. 30)

 ACN_i : arbitrary inner angle, used for EFBs positioning

 ω : azimuth of an EFB with respect to ACN

 θ : angle of an EFB with respect to its azimuth (wedge angle)

 $R_1,\,R_2$: radius of curvature of an EFB $U_1,\,U_2$: extent of the linear part of an EFB

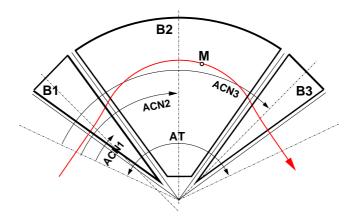


Figure 30: Definition of a dipole N-tuple (N=3, a triplet here) using the DIPOLES or FFAG procedures.

Calculation of the Field From a Single Dipole

The magnetic field is calculated in polar coordinates. At all (R, θ) in the median plane (z = 0), the magnetic field due a single one (index i) of the dipoles of a N-tuple FFAG magnet is written

$$B_{Zi}(R,\theta) = B_{Z0,i} \mathcal{F}_i(R,\theta) (R/R_M)^{K_i}$$

wherein $B_{Z0,i}$ is a reference field, at reference radius RM_i , whereas $\mathcal{F}(R,\theta)$ is calculated as described below.

Calculation of $\mathcal{F}_i(R,\theta)$

The fringe field coefficient $\mathcal{F}_i(R,\theta)$ associated with a dipole is computed as in the procedure *DIPOLES* (eq. 4.4.12), including (rigorously if the interpolation method is used, see page 112, or to order zero if the analytic method is used, see page 113) radial dependence of the gap size

$$g(R) = g_0 (RM/R)^{\kappa} \tag{4.4.15}$$

so to simulate the effect of gap shaping on $B_{Zi}(R,\theta)|_R$ field fall-off, over the all radial extent of a scaling FFAG dipole (with normally - but not necessarily in practice - $\kappa \approx K_i$).

Calculation of the Field Resulting From All N Dipoles

For the rest, namely, calculation of the full field at particle position from the N dipoles, analytical calculation or numerical interpolation of the mid-plane field derivatives, extrapolation off median plane, etc., things are performed exactly as in the case of the *DIPOLES* procedure (see page 112).

Sharp Edge

Sharp edge field fall-off at a field boundary can only be simulated if the following conditions are fulfilled:

- entrance (resp. exit) field boundary coincides with entrance (resp. exit) dipole limit (it means in particular, see Fig. 11, $\omega^+ = ACENT$ (resp. $\omega^- = -(AT ACENT)$), together with $\theta = 0$ at entrance (resp. exit) EFBs),
 - analytical method for calculation of the mid-plane field derivatives is used.

FFAG-SPI : Spiral FFAG magnet, N-tuple [39, 45]

FFAG-SPI works much like FFAG as to the field modelling, with essentially a different axial dependence.

The FFAG-SPI procedure allows overlapping of fringe fields of neighboring dipoles, thus simulating in some sort the field in a dipole N-tuple (similar to Fig. 30, page 125). This allows for instance accounting for fringe field effects, or clamps, as schemed in Fig. 31.

The dimensioning of the magnet is defined by

AT: total angular aperture

RM: mean radius used for the positioning of field boundaries

For each one of the N=1 to (maximum) 5 dipoles of the N-tuple, the two effective field boundaries (entrance and exit EFBs) from which the dipole field is drawn are defined from geometric boundaries, the shape and position of which are determined by the following parameters

 ACN_i : arbitrary inner angle, used for EFBs positioning

 ω : azimuth of an EFB with respect to ACN

 ξ : spiral angle

with ACN_i and ω as defined in Fig. 31 (similar to what can be found in Figs. 30 and 11-A).



Figure 31: A N-tuple spiral sector FFAG magnet (N=3 here, simulating active field clamps at entrance and exit side of a central dipole).

Calculation of the Field From a Single Dipole

The magnetic field is calculated in polar coordinates. At all (R, θ) in the median plane (Z = 0), the magnetic field due a single one (index i) of the dipoles of a N-tuple spiral FFAG magnet is written

$$B_{Zi}(R,\theta) = B_{Z0,i} \mathcal{F}_i(R,\theta) (R/R_M)^{K_i}$$

wherein $B_{Z_{0,i}}$ is a reference field, at reference radius RM_i , whereas $\mathcal{F}(R,\theta)$ is calculated as described below.

Calculation of $\mathcal{F}_i(R,\theta)$

The fringe field coefficient $\mathcal{F}_i(R,\theta)$ associated with a dipole is computed as in the procedure *DIPOLES* (eq. 4.4.12), including radial dependence of the gap size

$$g(R) = g_0 \left(RM/R \right)^{\kappa} \tag{4.4.16}$$

so to simulate the effect of gap shaping on $B_{Zi}(R,\theta)|_R$ field fall-off, over the all radial extent of the dipole (with normally - yet not necessarily in practice - $\kappa \approx K_i$).

Calculation of the Full Field From All N Dipoles

For the rest, namely calculation of the full field at particle position, as resulting from the N dipoles, calculation of the mid-plane field derivatives, extrapolation off median plane, etc., things are performed in the same manner as for the DIPOLES procedure (see page 112).

MAP2D: 2-D Cartesian uniform mesh field map - arbitrary magnetic field [49]

MAP2D reads a 2-D field map that provides the three components B_X , B_Y , B_Z of the magnetic field at all nodes of a 2-D Cartesian uniform mesh in an (X,Y) plane. No particular symmetry is assumed, which allows the treatment of any type of field (e.g., solenoidal, or dipole, helical dipole, at arbitrary Z elevation - the map needs not be a mid-plane map).

The field map data file has to be be filled with a format that satisfies the *FORTRAN* reading sequence below (in principle compatible with *TOSCA* code outputs), details and possible updates are to be found in the source file 'fmapw.f':

IX~(JY) is the number of longitudinal (transverse horizontal) nodes of the 2-D uniform mesh, Z is the considered Z-elevation of the map. For binary files, FNAME must begin with 'B_' or 'b_', a flag 'BINARY' will thus be set to '.TRUE.'. The field $\vec{B} = (B_X, B_Y, B_Z)$ is next normalized with BNORM, prior to ray-tracing. As well the coordinates X, Y are normalized with X-, Y-NORM coefficients (useful to convert to centimeters, the working units in **zgoubi**).

At each step of the trajectory of a particle, the field and its derivatives are calculated using a second or fourth degree polynomial interpolation followed by a Z extrapolation (see sections 1.3.4 page 25, 1.4.3 page 29). The interpolation grid is 3*3-node for 2nd order (option IORDRE = 2) or 5*5 for 4th order (option IORDRE = 4).

Entrance and/or exit integration boundaries may be defined, in the same way as for *CARTEMES*.

MAP2D-E: 2-D Cartesian uniform mesh field map - arbitrary electric field

MAP2D-E reads a 2-D field map that provides the three components E_X , E_Y , E_Z of the electric field at all nodes of a 2-D Cartesian uniform mesh in an (X,Y) plane. No particular symmetry is assumed, which allows the treatment of any type of field (e.g., field of a parallel-plate mirror with arbitrary <math>Z elevation - the map needs not be a mid-plane map).

The field map data file has to be be filled with a format that satisfies the *FORTRAN* reading sequence below (in principle compatible with *TOSCA* code outputs), details and possible updates are to be found in the source file 'fmapw.f':

IX~(JY) is the number of longitudinal (transverse horizontal) nodes of the 2-D uniform mesh, Z is the considered Z-elevation of the map. For binary files, FNAME must begin with 'E_ ' or 'b_', a flag 'BINARY' will thus be set to '.TRUE.'. The field $\vec{E}=(E_X,E_Y,E_Z)$ is next normalized with ENORM, prior to ray-tracing. As well the coordinates X, Y are normalized with X-, Y-NORM coefficients (useful to convert to centimeters, the working units in **zgoubi**.

At each step of the trajectory of a particle, the field and its derivatives are calculated using a second or fourth degree polynomial interpolation followed by a Z extrapolation (see sections 1.3.4 page 25, 1.4.3 page 29). The interpolation grid is 3*3-node for 2nd order (option IORDRE = 2) or 5*5 for 4th order (option IORDRE = 4).

Entrance and/or exit integration boundaries may be defined, in the same way as for *CARTEMES*.

MARKER: Marker

MARKER does nothing. Just a marker. No data.

As any other keyword, *MARKER* is allowed two *LABELs*. Using '.plt' as a second *LABEL* will cause storage of current coordinates into zgoubi.plt.

MULTIPOL: Magnetic multipole

The simulation of multipolar magnetic field \vec{M} by MULTIPOL proceeds by addition of the dipolar $(\vec{B}1)$, quadrupolar $(\vec{B}2)$, sextupolar $(\vec{B}3)$, etc., up to 20-polar $(\vec{B}10)$ components, and of their derivatives up to fourth order, following

$$\begin{split} \vec{M} &= \vec{B}1 + \vec{B}2 + \vec{B}3 + \ \dots \ + \vec{B}10 \\ \frac{\partial \vec{M}}{\partial X} &= \frac{\partial \vec{B}1}{\partial X} + \frac{\partial \vec{B}2}{\partial X} + \frac{\partial \vec{B}3}{\partial X} + \ \dots \ + \frac{\partial \vec{B}10}{\partial X} \\ \frac{\partial^2 \vec{M}}{\partial X \partial Z} &= \frac{\partial^2 \vec{B}1}{\partial X \partial Z} + \frac{\partial^2 \vec{B}2}{\partial X \partial Z} + \frac{\partial^2 \vec{B}3}{\partial X \partial Z} + \ \dots \ + \frac{\partial^2 \vec{B}10}{\partial X \partial Z} \end{split}$$

The independent components $\vec{B}1$, $\vec{B}2$, $\vec{B}3$, ..., $\vec{B}10$ and their derivatives up to the fourth order are calculated as described in section 1.3.7.

The entrance and exit fringe fields are treated separately. They are characterized by the integration zone X_E at entrance and X_S at exit, as for *QUADRUPO*, and by the extent λ_E at entrance, λ_S at exit. The fringe field extents for the dipole component are λ_E and λ_S . The fringe field for the quadrupolar (sextupolar, ..., 20-polar) component is given by a coefficient E_2 (E_3 , ..., E_{10}) at entrance, and S_2 (S_3 , ..., S_{10}) at exit, such that the extent is $\lambda_E * E_2$ ($\lambda_E * E_3$, ..., $\lambda_E * E_{10}$) at entrance and $\lambda_S * S_2$ ($\lambda_S * S_3$, ..., $\lambda_S * S_{10}$) at exit.

If $\lambda_E=0$ ($\lambda_S=0$) the multipole lens is considered to have a sharp edge field at entrance (exit), and then, $X_E\left(X_S\right)$ is forced to zero (for the mere purpose of saving computing time). If $E_i=0$ ($S_i=0$) (i=2,10), the entrance (exit) fringe field for the multipole component i is considered as a sharp edge field. In sharp edge field model, the wedge angle vertical first order focusing effect (if $\vec{B}1$ is non zero) is simulated at magnet entrance and exit by a kick $P_2=P_1-Z_1\tan(\epsilon/\rho)$ applied to each particle (P_1,P_2 are the vertical angles upstream and downstream of the EFB, Z_1 is the vertical particle position at the EFB, ρ the local horizontal bending radius and ϵ the wedge angle experienced by the particle; ϵ depends on the horizontal angle T).

Any multipole component $\vec{B}i$ can be rotated independently by an angle RXi around the longitudinal X-axis, for the simulation of positioning defects, as well as skew lenses.

Magnet (mis-)alignment is assured by *KPOS*. *KPOS* also allows some degrees of automatic alignment useful for periodic structures (section 4.6.7).

OCTUPOLE: Octupole magnet (Fig. 32)

The meaning of parameters for *OCTUPOLE* is the same as for *QUADRUPO*. In fringe field regions the magnetic field $\vec{B}(X,Y,Z)$ and its derivatives up to fourth order are derived from the scalar potential approximated to the 8-th order in Y and Z

$$V(X,Y,Z) = \left(G(X) - \frac{G''(X)}{20} (Y^2 + Z^2) + \frac{G''''(X)}{960} (Y^2 + Z^2)^2\right) (Y^3 Z - Y Z^3)$$
 with $G_0 = \frac{B_0}{R_0^3}$

The modelling of the fringe field form factor G(X) is described under QUADRUPO, p. 138.

Outside fringe field regions, or everywhere in sharp edge dodecapole ($\lambda_E=\lambda_S=0$), $\vec{B}(X,Y,Z)$ in the magnet is given by

$$B_X = 0$$

 $B_Y = G_0(3Y^2 - Z^2) Z$
 $B_Z = G_0(Y^2 - 3Z^2) Y$



Figure 32: Octupole magnet

POISSON : Read magnetic field data from POISSON output

This keyword allows reading a field profile B(X) from *POISSON* output. Let *FNAME* be the name of this output file (normally, *FNAME* = outpoi.lis); the data are read following the *FORTRAN* statements here under

where X(I) is the longitudinal coordinate, and B(I) is the Z component of the field at a node (I) of the mesh. Ks and Rs are dummy variables appearing in the *POISSON* output file outpoi.lis but not used here.

From this field profile, a 2-D median plane map is built, with a rectangular and uniform mesh; mid-plane symmetry is assumed. The field at each node (X_i, Y_j) of the map is $B(X_i)$, independent of Y_j (i.e., the distribution is uniform in the Y direction).

For the rest, *POISSON* works in a way similar to *CARTEMES*.

POLARMES: 2-D polar mesh magnetic field map

Similar to *CARTEMES*, apart from the polar mesh frame: IX is the number of angular nodes, JY the number of radial nodes; X(I) and Y(J) are respectively the angle and radius of a node (these parameters are similar to those entering in the definition of the field map in DIPOLE-M).

PS170: Simulation of a round shape dipole magnet

PS170 is dedicated to a 'rough' simulation of CERN PS170 spectrometer dipole.

The field B_0 is constant inside the magnet, and zero outside. The pole is a circle of radius R_0 , centered on the X axis. The output coordinates are generated at the distance XL from the entrance (Fig. 33).



Figure 33: Scheme of the PS170 magnet simulation.

QUADISEX, SEXQUAD: Sharp edge magnetic multipoles

SEXQUAD defines in a simple way a sharp edge field with quadrupolar, sextupolar and octupolar components. QUADISEX adds a dipole component. The length of the element is XL. The vertical component $B \equiv B_Z(X,Y,Z=0)$ of the field and its derivatives in median plane are calculated at each step using the following expressions

$$B = B_0 \left(U + \frac{N}{R_0} Y + \frac{B}{R_0^2} Y^2 + \frac{G}{R_0^3} Y^3 \right)$$

$$\frac{\partial B}{\partial Y} = B_0 \left(\frac{N}{R_0} + 2 \frac{B}{R_0^2} Y + 3 \frac{G}{R_0^3} Y^2 \right)$$

$$\frac{\partial^2 B}{\partial Y^2} = B_0 \left(2 \frac{B}{R_0^2} + 6 \frac{G}{R_0^3} Y \right)$$

$$\frac{\partial^3 B}{\partial Y^3} = 6 B_0 \frac{G}{R_0^3}$$

and then extrapolated out of the median plane by Taylor expansion in Z (see section 1.3.3). With option SEXQUAD, U=0, while with QUADISEX, U=1.

QUADRUPO: Quadrupole magnet (Fig. 34)

The length of the magnet XL is the distance between the effective field boundaries (EFB), Fig. 35. The field at the pole tip R_0 is B_0 .

The extent of the entrance (exit) fringe field is characterized by $\lambda_E(\lambda_S)$. The distance of ray-tracing on both sides of the EFBs, in the field fall off regions, will be $\pm X_E$ at the entrance, and $\pm X_S$ at the exit (Fig. 35), by prior and further automatic change of frame.

In the fringe field regions $[-X_E, X_E]$ and $[-X_S, X_S]$ on both sides of the EFBs, $\vec{B}(X, Y, Z)$ and its derivatives up to fourth order are calculated at each step of the trajectory from the analytical expressions of the three components B_X , B_Y , B_Z obtained by differentiation of the scalar potential (see section 1.3.7) expressed to the 8th order in Y and Z.

$$V(X,Y,Z) = \left(G(X) - \frac{G''(X)}{12} (Y^2 + Z^2) + \frac{G''''(X)}{384} (Y^2 + Z^2)^2 - \frac{G'''''(X)}{23040} (Y^2 + Z^2)^3\right) YZ$$

$$(G^{(n)}(X) = d^n G(X) / dX^n, etc.)$$

where G(X) is the gradient on axis [34]:

$$G(X) = \frac{G_0}{1 + \exp P(d(X))}$$
 with $G_0 = \frac{B_0}{R_0}$

and,

$$P(d) = C_0 + C_1 \left(\frac{d}{\lambda}\right) + C_2 \left(\frac{d}{\lambda}\right)^2 + C_3 \left(\frac{d}{\lambda}\right)^3 + C_4 \left(\frac{d}{\lambda}\right)^4 + C_5 \left(\frac{d}{\lambda}\right)^5$$

where d(X) is the distance to the field boundary and λ stands for λ_E or λ_S (normally, $\lambda \simeq 2 * R_0$). When fringe fields overlap inside the magnet $(XL \le X_E + X_S)$, the gradient G is expressed as

$$G = G_E + G_S - 1$$

where, G_E is the entrance gradient and G_S is the exit gradient.

If $\lambda_E = 0$ ($\lambda_S = 0$), the field at entrance (exit) is considered as sharp edged, and then $X_E(X_S)$ is forced to zero (for the mere purpose of saving computing time).

Outside of the fringe field regions (or everywhere when $\lambda_E = \lambda_S = 0$) $\vec{B}(X,Y,Z)$ in the magnet is given by

$$B_X = 0$$

$$B_Y = G_0 Z$$

$$B_Z = G_0 Y$$

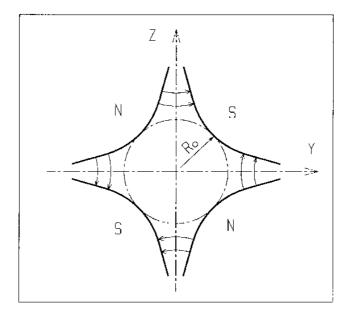


Figure 34: Quadrupole magnet



Figure 35: Scheme of the longitudinal field gradient G(X). (OX) is the longitudinal axis of the reference frame (0,X,Y,Z) of **zgoubi**. The length of the element is XL. Trajectories are ray-traced from $-X_E$ to $XL + X_S$, by means of respectively prior and final automatic change of frame.

SEPARA: Wien Filter - analytical simulation

Note: simulation by stepwise integration can be found in WIENFILTER.

SEPARA provides an analytic simulation of an electrostatic separator. Input data are the length L of the element, the electric field E and the magnetic field B. The mass m and charge q of the particles are entered by means of the keyword PARTICUL.

The subroutines involved in *SEPARA* solve the following system of three equations with three unknown variables S, Y, Z (while $X \equiv L$), that describe the cycloidal motion of a particle in \vec{E}, \vec{B} static fields (Fig. 36).

$$X = -R\cos\left(\frac{\omega S}{\beta c} + \epsilon\right) - \frac{\alpha S}{\omega \beta c} + \frac{C_1}{\omega}$$
$$Y = R\sin\left(\frac{\omega S}{\beta c} + \epsilon\right) - \frac{\alpha}{\omega^2} - \frac{C_2}{\omega} + Y_0$$
$$Z = S\sin(P_0) + Z_0$$

where, S is the path length in the separator, $\alpha=-\frac{Ec^2}{\gamma}$, $\omega=-\frac{Bc^2}{m\gamma}$, $C_1=\beta\sin(T_0)\cos(P_0)$ and $C_2=\frac{Ec^2}{m\gamma}$

 $\beta c \cos(T_0) \cos(P_0)$ are initial conditions. c = velocity of light, βc = velocity of the particle, $\gamma = (1 - \beta^2)^{-\frac{1}{2}}$ and $\tan \epsilon = (C_2 + \frac{\alpha}{\omega})/C_1$. Y_0 , T_0 , Z_0 , P_0 are the initial coordinates of the particle in the **zgoubi** reference frame. Here βc and γ are assumed constant, which is true as long as the change of momentum due to the electric field remains negligible all along the separator.

The option index IA in the input data allows switching to inactive element (thus equivalent to ESL), horizontal or vertical separator. Normally, E, B and the value of β_W for wanted particles are related by

$$B(T) = -\frac{E\left(\frac{V}{m}\right)}{\beta_W \cdot c\left(\frac{m}{s}\right)}$$



Figure 36: Horizontal separation between a wanted particle, (W), and an unwanted particle, (U). (W) undergoes a linear motion while (U) undergoes a cycloidal motion.

SEXTUPOL: Sextupole magnet (Fig. 37)

The meaning of parameters for SEXTUPOL is the same as for QUADRUPO.

In fringe field regions the magnetic field $\vec{B}(X,Y,Z)$ and its derivatives up to fourth order are derived from the scalar potential approximated to 7th order in Y and Z

$$\begin{split} V(X,Y,Z) &= \left(G(X) - \frac{G''(X)}{16} \left(Y^2 + Z^2\right) + \frac{G''''(X)}{640} \left(Y^2 + Z^2\right)^2\right) \left(Y^2 Z - \frac{Z^3}{3}\right) \\ \text{with } G_0 &= \frac{B_0}{R_0^2} \end{split}$$

The modelling of the fringe field form factor G(X) is described under QUADRUPO, p. 138.

Outside fringe field regions, or everywhere in sharp edge sextupole ($\lambda_E = \lambda_S = 0$), $\vec{B}(X,Y,Z)$ in the magnet is given by

$$B_X = 0$$

$$B_Y = 2G_0YZ$$

$$B_Z = G_0(Y^2 - Z^2)$$

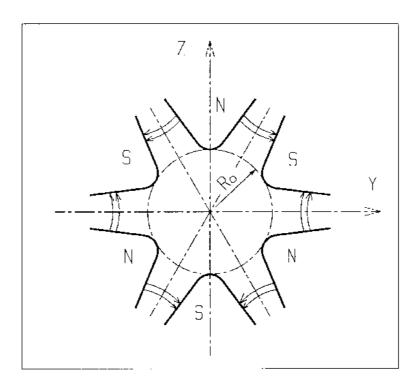


Figure 37: Sextupole magnet

SOLENOID: Solenoid (Fig. 38)

The solenoidal magnet has an effective length XL, a mean radius R_0 and an asymptotic field $B_0 = \mu_0 NI/XL$ (i.e., $\int_{-\infty}^{\infty} B_X(X,r) dX = \mu_0 NI$, $\forall r < R_0$), wherein B_X =longitudinal field component, NI = number of ampere-Turns, $\mu_0 = 4\pi 10^{-7}$.

The distance of ray-tracing beyond the effective length XL, is X_E at the entrance, and X_S at the exit (Fig. 38).

Two methods are available for the computation of the field $\vec{B}(X,r)$ and its derivatives.

Method $1: \vec{B}(X,r)$, $r=(Y^2+Z^2)^{1/2}$ and its derivatives up to second order at all (X,Y,Z) are calculated following Ref. [50], based on the three complete elliptic integrals K, E and Π . The latter are calculated with the algorithm proposed in the same reference, their derivatives are calculated by means of recursive relations [51].

This analytical model for the solenoidal field allows simulating an extended range of coil geometries (length, radius) provided that the coil thickness is small enough compared to the mean radius R_0 .

In particular the field on-axis writes (taking X = r = 0 at the center of the solenoid)

$$B_X(X, r = 0) = \frac{\mu_0 NI}{2XL} \left[\frac{XL/2 - X}{\sqrt{(XL/2 - X)^2 + R_0^2}} + \frac{XL/2 + X}{\sqrt{(XL/2 + X)^2 + R_0^2}} \right]$$

and yields the magnetic length

$$L_{mag} \equiv \frac{\int_{-\infty}^{\infty} B_X(X, r < R_0) dX}{B_X(X = r = 0)} = XL\sqrt{1 + \frac{4R_0^2}{XL^2}} > XL$$
 (4.4.17)

with in addition

$$B_X(\text{center}) \equiv B_X(X = r = 0) = \frac{\mu_0 NI}{XL\sqrt{1 + \frac{4R_0^2}{XL^2}}}.$$

Method 2: The second method available uses eq. 4.4.17 above as a 1-D model and uses off-axis extrapolation to derive the field and its derivatives at all (X, Y, Z), following the method described in section 1.3.1.



Figure 38: Solenoidal magnet.

SPINR: Spin rotation [52]

SPINR causes spin precession, a local transformation on the spin vector of the particles, as, e.g., in a local helical spin rotator. Two options are available, as follows.

IOPT = 0 inhibits the keyword.

If IOPT = 1: the precession is defined by its axis, at angle ϕ_Z with respect to **zgoubi**'s X-axis and assumed in the horizontal plane, and by its value, μ .

If IOPT = 2: given the spin precession axis ϕ_Z - defined as above - the spin precession angle follows a function of the *reference* Lorentz factor:

$$\mu(\gamma) = \left(\frac{B}{B_0}\right)^2 \times \left(C_0 + \frac{C_1}{\gamma} + \frac{C_2}{\gamma^2} + \frac{C_3}{\gamma^3}\right)$$

with B and B_0 normally a nominal and a reference magnetic field value, and C_i empirical coefficients. The reference Lorentz factor corresponds to the reference rigidity BORO, as defined for instance with [MC]OBJET, possibly updated in the presence of acceleration (see section 4.6.1, page 168).

TOSCA: 2-D and 3-D Cartesian or cylindrical mesh field map

TOSCA is dedicated to the reading and treatment of 2-D or 3-D Cartesian or cylindrical mesh field maps. It was first created in order to read *TOSCA* magnet computer code style of fieldmap output and formatting, hence its name. However the actual origin of the fieldmap, TOSCA or other computer code, does not matter.

A double-flag, MOD[.MOD2], determines whether Cartesian or Z-axis cylindrical mesh is used, and the nature and/or form of the field map data set.

The total number of field data files to be read is determined by the MOD[.MOD2] flag (see below) and by the parameter IZ that appears in the data list following the keyword. Each of these files contains the field components B_X , B_Y , B_Z on an (X,Y) mesh. IZ=1 for a 2-D map, and in this case B_X and B_Y are assumed zero all over the map⁸. For a 3-D map with mid-plane symmetry, described with a set of 2-D maps at various Z, then MOD=0 and $IZ\geq 2$, and thus, the first data file whose name follows in the data list is supposed to contain the median plane field (assuming Z=0 and $B_X=B_Y=0$), while the remaining IZ-1 file(s) contain the IZ-1 additional planes in increasing Z order. For arbitrary 3-D maps, no symmetry assumed, then MOD=1 and the total number of maps (whose names follow in the data list) is IZ, such that map number [IZ/2]+1 is the Z=0 elevation one.

The field map data file has to be be filled with a format that fits the *FORTRAN* reading sequence. The following is an instance, details and possible updates are to be found in the source file 'fmapw.f':

```
DO 1 K = 1, KZ

OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED'])

DO 1 J = 1, JY

DO 1 I = 1, IX

IF (BINARY) THEN

READ(NL) Y(J), Z(K), X(I), BY(J,K,I), BZ(J,K,I), BX(J,K,I)

ELSE

READ(NL,100) Y(J), Z(K), X(I), BY(J,K,I), BZ(J,K,I), BX(J,K,I)

100

FORMAT(1X,6E11.2)

ENDIF

1 CONTINUE
```

IX (JY, KZ) is the number of longitudinal (transverse horizontal, vertical) nodes of the 3-D uniform mesh. For letting **zgoubi** know that these are binary files, FNAME must begin with 'B_' or 'b_'.

Other *MOD[.MOD2]* cases in addition to the above, are listed in table 1. The *FORTRAN* subroutine fmapw.f and its entries FMAPR, FMAPR2 can be looked up for more details, in particular regarding the formatting of the field map data file(s).

Once the field map(s) reading is completed, the field $\vec{B} = (B_X, B_Y, B_Z)$ is normalized by means of *BNORM* in a similar way as in *CARTEMES*. As well the coordinates X and Y (and Z in the case of 3-D field maps) are normalized by the X-[, Y-, Z-]NORM coefficient (useful to convert to centimeters, the working units in **zgoubi**).

At each step of the trajectory of a particle inside the map, the field and its derivatives are calculated

- in the case of 2-D map, by means of a second or fourth order polynomial interpolation, depending on IORDRE (IORDRE = 2, 25 or 4), as for CARTEMES,
- in the case of 3-D map, by means of a second order polynomial interpolation with a $3 \times 3 \times 3$ -point parallelepipedic grid, as described in section 1.4.4.

Entrance and/or exit integration boundaries between which the trajectories are integrated in the field may be defined, in the same way as in *CARTEMES*.

⁸Use MAP2D in case non-zero B_X , B_Y are to be taken into account in a 2-D map.

Table 1: The various IZ, MOD and MOD2 possibilities, when using TOSCA.

IZ	MOD	.MOD2			
$MOD \le 19$: Cartesian mesh					
1	0	none	2-D map, a single data file for $B_Z(X,Y) _{Z=0}$, mid-plane symmetry.		
> 1	0	none	3-D map, 1+IZ/2 data files of upper half of magnet, one per $(X,Y) _{0\leq Z\leq Z_{max}}$ plane, mid-plane symmetry.		
	0	.1, .2, .3	As previous case, just different reading formats.		
1	1	none	2-D map, one mid-plane $B_Y(X,Y)$ data field map.		
> 1	1	none	3-D map, IZ files containing $B_{X,Y,Z}(X,Y,Z)$ data, one per (X,Y) plane, no symmetry assumed.		
	1	.1, .2, .3	As previous case, just different reading formats.		
	3	none or .1	AGS main magnet field map, 2-D, mid-plane symmetry assumed. MOD2=1 causes field to be perturbed by $(1+n_1dY+n_2dY^2+n_3dY^3)$ factor.		
	12	none	3-D map, single file, upper half of magnet, symmetry with respect to (X,Y) mid-plane.		
	12	.1	3-D map, single file, whole magnet volume (thus no symmetry assumed).		
	12	.2	3-D map, single file, $1/8$ th of the magnet, symmetry wrt. (X,Y) , (X,Z) , (Y,Z) planes.		
>1	15	.1–.6	3-D map data file(s) (up to 6), whole magnet volume each (thus no symmetry assumed). Fields summed up : at all node, $\vec{B} = \sum_{i=1}^{i=MOD2} a_i \vec{B}_i$. Each map file contains $B_{X,Y,Z}(X,Y,Z)$ data over $\it IZ$ equally $\it Z$ -spaced $\it (X,Y)$ planes		
$MOD \ge 20$: Cylindrical mesh					
	20, 21		3-D map, single file, half a magnet, cyl. symmetry with respect to (Y,Z) plane.		
	22, 24		3-D map, single file, half a magnet, symmetry with respect to (X,Y) mid-plane.		

TRANSMAT : Matrix transfer

TRANSMAT performs a second order transport of the particle coordinates in the following way

$$X_{i} = \sum_{j} R_{ij} X_{j}^{0} + \sum_{j,k} T_{ijk} X_{j}^{0} X_{k}^{0}$$

where, X_i stands for any of the current coordinates Y, T, Z, P, path length and momentum dispersion, and X_i^0 stands for any of the initial coordinates. $[R_{ij}]$ ($[T_{ijk}]$) is the first order (second order) transfer matrix as usually involved in second order beam optics [28]. Second order transfer is optional. The length of the element represented by the matrix may be introduced for the purpose of path length updating.

Note: MATRIX delivers $[R_{ij}]$ and $[T_{ijk}]$ matrices in a format suitable for straightforward use with TRANS-MAT.

TRAROT: Translation-Rotation of the reference frame

UNDER DEVELOPMENT. Check before use.

This procedure transports particles into a new frame by translation and rotation. Effect on spin tracking, particle decay and gas-scattering are taken into account (but not on synchrotron radiation).

UNDULATOR: Undulator magnet

UNDULATOR magnet. UNDER DEVELOPMENT.

UNIPOT: Unipotential cylindrical electrostatic lens

The lens is cylindrically symmetric about the X-axis.

The length of the first (resp. second, third) electrode is X1 (resp. X2, X3). The distance between the electrodes is D. The potentials are V1 and V2. The inner radius is R_0 (Fig. 39). The model for the electrostatic potential along the axis is [53]

$$V(x) = \frac{V2 - V1}{2\omega D} \left[\ln \frac{\cosh \frac{\omega \left(x + \frac{X2}{2} + D\right)}{R_0}}{\cosh \frac{\omega \left(x + \frac{X2}{2}\right)}{R_0}} + \ln \frac{\cosh \frac{\omega \left(x - \frac{X2}{2} - D\right)}{R_0}}{\cosh \frac{\omega \left(x - \frac{X2}{2}\right)}{R_0}} \right]$$

(x = distance from the center of the central electrode; $\omega = 1{,}318$; cosh = hyperbolic cosine), from which the field $\vec{E}(X,Y,Z)$ and its derivatives are deduced following the procedure described in section 1.3.1.

Use PARTICUL prior to UNIPOT, for the definition of particle mass and charge.

The total length of the lens is X1 + X2 + X3 + 2D; stepwise integration starts at entrance of the first electrode and terminates at exit of the third one.

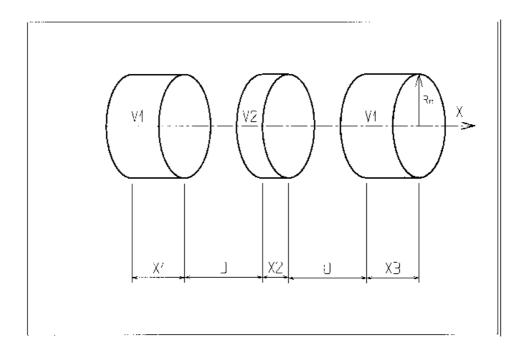


Figure 39: Three-electrode cylindrical unipotential lens.

VENUS: Simulation of a rectangular shape dipole magnet

VENUS is dedicated to a 'rough' simulation of SATURNE Laboratory's VENUS dipole. The field B_0 is constant inside the magnet, with longitudinal extent XL and transverse extent $\pm YL$; outside these limits, $B_0=0$ (Fig. 40).



Figure 40: Scheme of VENUS rectangular dipole.

WIENFILT: Wien filter

WIENFILT simulates a Wien filter, with transverse and orthogonal electric and magnetic fields \vec{E}_Y , \vec{B}_Z or \vec{E}_Z , \vec{B}_Y (Fig. 36). It must be preceded by PARTICUL for the definition of particle mass and charge.

The length XL of the element is the distance between its entrance and exit EFBs. The electric and magnetic field intensities E_0 and B_0 in the central, uniform field region, normally satisfy the relation

$$B_0 = -\frac{E_0}{\beta_W c}$$

for the selection of "wanted" particles of velocity $\beta_W c$. Ray-tracing in field fall-off regions extends over a distance $X_E(X_S)$ beyond the entrance (exit) EFB by means of prior and further automatic change of frame. Four sets of coefficients λ , $C_0 - C_5$ allow the description of the entrance and exit fringe fields outside the uniform field region, following the model [34]

$$F = \frac{1}{1 + \exp(P(s))}$$

where P(s) is of the term

$$P(s) = C_0 + C_1 \left(\frac{s}{\lambda}\right) + C_2 \left(\frac{s}{\lambda}\right)^2 + C_3 \left(\frac{s}{\lambda}\right)^3 + C_4 \left(\frac{s}{\lambda}\right)^4 + C_5 \left(\frac{s}{\lambda}\right)^5$$

and s is the distance to the EFB. When fringe fields overlap inside the element (i.e., $XL \le X_E + X_S$), the field fall-off is expressed as

$$F = F_E + F_S - 1$$

where $F_E(F_S)$ is the value of the coefficient respective to the entrance (exit) EFB.

If $\lambda_E=0$ ($\lambda_S=0$) for either the electric or magnetic component, then both are considered as sharp edge fields and $X_E(X_S)$ is forced to zero (for the purpose of saving computing time). In this case, the magnetic wedge angle vertical first order focusing effect is simulated at entrance and exit by a kick $P_2=P_1-Z_1\tan(\epsilon/\rho)$ applied to each particle (P_1 , P_2 are the vertical angles upstream and downstream the EFB, Z_1 the vertical particle position at the EFB, ρ the local horizontal bending radius and ϵ the wedge angle experienced by the particle; ϵ depends on the horizontal angle T). This is not done for the electric field, however it is advised not to use a sharp edge electric dipole model since this entails non symplectic mapping, and in particular precludes accounting for momentum effects of the non zero longitudinal electric field component.

YMY : Reverse signs of Y and Z reference axes

YMY performs a 180° rotation of particle coordinates with respect to the X-axis, as shown in Fig. 41. This is done by means of a change of sign of Y and Z axes, and therefore coordinates, as follows

$$Y2 = -Y1$$
, $T2 = -T1$, $Z2 = -Z1$ and $P2 = -P1$



Figure 41: The use of YMY in a sequence of two identical dipoles of opposite signs.

4.5 Output Procedures 153

4.5 Output Procedures

These procedures are dedicated to the storage or printing of particle coordinates, histograms, spin coordinates, etc. They may be called for at any spot in the data pile.

FAISCEAU, FAISCNL, FAISTORE: Print/Store particle coordinates

- FAISCEAU can be introduced anywhere in a structure data list (zgoubi.dat). It produces a print (into zgoubi.res) of initial and actual coordinates of the IMAX particles at the location where it stands, together tagging indices and letters, etc.
- FAISCNL produces a lot more information on particles at current location, including spin components, decay distance, mass, charge, etc. (see list below), and stores it in a dedicated file FNAME (advised name is FNAME = 'zgoubi.fai' (formatted write) or 'b_zgoubi.fai' (binary write) if post-processing with zpop should follow). This file may further on be read by means of OBJET, option KOBJ= 3, or used for other purposes such as graphics (see Part D of the Guide).

The data written to that file are formatted and ordered according to the *FORTRAN* sequence in the subroutine impfai.f, where details and possible updates are to found. The following is an instance:

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'NEW')
                IF(BINARY) THEN
                     DO 2 I=1,IMAX
                               P = BORO*CL9 *F(1,I) * AMQ(2,I)
                               ENERG = SQRT(P*P + AMQ(1,I)*AMQ(1,I))
                               ENEKI = ENERG - AMQ(1,I)
                               WRITE (NFAI)
                               IEX(I),-1.D0+FO(1,I),(FO(J,I),J=2,MXJ),
                                                                                                                                                                                  tag, initial D-1,Y,T,Z,P,S,Time
                                                                                                                                                                                current D_i,Y,T,Z,P,S,Time
             2
                               -1.D0+F(1,I),F(2,I),F(3,I),(F(J,I),J=4,MXJ),
                               (SI(J,I),J=1,4),(SF(J,I),J=1,4),
                                                                                                                                                                                  spin components, initial and current
                               ENEKI, ENERG,
                                                                                                                                                                                  energy
                                \texttt{I,IREP(I), SORT(I),(AMQ(J,I),J=1,5),RET(I),DPR(I),PS,} \quad \texttt{particle\#,loss S,mass,Q,G,life time } \\ \texttt{I,IREP(I), SORT(I),(AMQ(J,I),J=1,5),RET(I),DPR(I),PS,} \\ \texttt{particle\#,loss S,mass,Q,G,life time } \\ \texttt{I,IREP(I), SORT(I),(AMQ(J,I),J=1,5),RET(I),DPR(I),PS,} \\ \texttt{particle\#,loss S,mass,Q,G,life time } \\ \texttt{particle\#,loss S
             4
             5
                               BORO, IPASS, NOEL, KLEY, LBL1, LBL2, LET(I)
                                                                                                                                                                                   BORO, pass#,element#,keyword,labels
                   CONTINUE
              ELSE
                     DO 1 I=1, IMAX
                          P = BORO*CL9 *F(1,I) * AMQ(2,I)
                          ENERG = SQRT(P*P + AMQ(1,I)*AMQ(1,I))
                          ENEKI = ENERG - AMQ(1,I)
                          WRITE(NEAT.110)
             1
                        IEX(I), -1.D0+FO(1,I), (FO(J,I), J=2, MXJ),
                          -1.D0+F(1,I),F(2,I),F(3,I),
                         (F(J,I),J=4,MXJ),
                         (SI(J,I),J=1,4),(SF(J,I),J=1,4),
                         ENEKI, ENERG,
             6
                          I, IREP(I), SORT(I), (AMQ(J,I), J=1,5), RET(I), DPR(I), PS,
                         BORO, IPASS, NOEL,
                          TX1, KLEY, TX1, TX1, LBL1, TX1, TX1, LBL2, TX1, TX1, LET(I), TX1
                          INCLUDE "FRMFAI.H"
                    CONTINUE
                ENDIF
  110
                       FORMAT(1X,
                                            KEX,
                                                                      XXXO, (FO(J,IT),J=2,MXJ)
             > 1P,
                                                               7(1X,E16.8)
                                         1X,I2,
C2
                                         XXX,Y,T*1.D3,
                                        ,3(1X,E24.16)
                       Z,P*1.D3,SAR,TAR
C3
                       .4(1X.E24.16)
C4
                        SXo, SYo, SZo, So, SX, SY, SZ, S
                        ,8(1X,E15.7)
                         ENEKI, ENERG
C5
                        ,2(1X,E16.8)
                                                           SORT(IT), (AMQ(J,I),J=1,5), RET(IT), DPR(IT), PS
C6
                       IT, IREP(IT),
                                                      9(1X,E16.8)
                        ,2(1X,I6),
C7
                           BORO,
                                              IPASS, NOEL,
                        ,1X,E16.8, 2(1X,I6)
C8
                                    'KLEY'.
                                                                 ('LABEL(NOEL,I)',I=1,2),
                                                                                                                                                           'LET(TT)'
                          ,1X,A1,A10,A1,
                                                                   2(1X,A1,A ,A1),
```

The meaning of the main data is the following (see the keyword *OBJET*)

LET(I) : one-character string, for tagging particle number I

IEX, I, IREP(I): flag, particle number, index

FO(1-6,I) : coordinates D,Y,T,Z,P and path length at the origin of the structure

F(1-6,I) : idem at the current position

SORT(I) : path length at which the particle has possibly been stopped

(see CHAMBR or COLLIMA)

RET(I), DPR(I): synchrotron phase space coordinates; RET =phase (radian),

DPR = momentum dispersion (MeV/c) (see CAVITE)

IPASS : turn number (see *REBELOTE*)

etc. :

- FAISTORE has an effect similar to FAISCNL, with two more features.
- On the first data line, *FNAME* may be followed by a series of up to 10 *LABELs*. If there is no label, the print occurs by default at the location of *FAISTORE*; if there are labels the print occurs right downstream of all optical elements wearing those labels (and no longer at the *FAISTORE* location).
- The next data line gives a parameter, IP: printing will occur at pass 1 and then at every IP other pass, if using REBELOTE with $NPASS \ge IP 1$.

For instance the following data input in zgoubi.dat:

```
FAISTORE
zgoubi.fai HPCKUP VPCKUP
12
```

will result in output prints into zgoubi.fai, at pass 1 and then at every 12 other pass, each time elements of the zgoubi.dat data list labeled either *HPCKUP* or *VPCKUP* are encountered.

Note

Binary storage can be obtained from *FAISCNL* and *FAISTORE*. This is for the sake of compactness and access speed, for instance in case voluminous amounts of data would have to be manipulated using **zpop**.

This is achieved by giving the storage file a name of the form *b_FNAME* or *B_FNAME* (*e.g.*, 'b_zgoubi.fai'). The *FORTRAN WRITE* list is the same as in the *FORMATTED* case above.

This is compatible with the *READ* statements in **zpop** that will recognize binary storage from that very radical 'b_' or 'B_'.

FOCALE, IMAGE[S]: Particle coordinates and beam size; localization and size of horizontal waist

FOCALE calculates the dimensions of the beam and its mean transverse position, at a longitudinal distance XL from the position corresponding to the keyword FOCALE.

IMAGE computes the location and size of the closest horizontal waist.

IMAGES has the same effect as *IMAGE*, but, in addition, for a non-monochromatic beam it calculates as many waists as there are distinct momenta in the beam, provided that the object has been defined with a classification of momenta (see *OBJET*, *KOBJ*= 1, 2 for instance).

Optionally, for each of these three procedures, **zgoubi** can list a trace of the coordinates in the X, Y and in the Y, Z planes.

The following quantities are calculated for the N particles of the beam (IMAGE, FOCALE) or of each group of momenta (IMAGES)

• Longitudinal position :

$$\begin{aligned} \textit{FOCALE}: \quad X &= XL \\ \textit{IMAGE[S]}: \quad X &= -\frac{\sum_{i=1}^{N} Y_i * \mathsf{tg} T_i - \left(\sum_{i=1}^{N} Y_i * \sum_{i=1}^{N} \mathsf{tg} T_i\right) / N}{\sum_{i=1}^{N} \mathsf{tg}^2 T_i - \left(\sum_{i=1}^{N} \mathsf{tg} T_i\right)^2 / N} \\ Y &= Y_1 + X * \mathsf{tg} T_1 \end{aligned}$$

where Y_1 and T_1 are the coordinates of the first particle of the beam (IMAGE, FOCALE) or the first particle of each group of momenta (IMAGES).

• Transverse position of the center of mass of the waist (IMAGE[S]) or of the beam (FOCALE), with respect to the reference trajectory

$$YM = \frac{1}{N} \sum_{i=1}^{N} (Y_i + X t g T_i) - Y = \frac{1}{N} \sum_{i=1}^{N} Y M_i$$

• FWHM of the image (IMAGE[S]) or of the beam (FOCALE), and total width, respectively, W and WT

$$W = 2.35 \left(\frac{1}{N} \sum_{i=1}^{N} Y M_i^2 - Y M^2\right)^{\frac{1}{2}}$$

$$WT = \max(YM_i) - \min(YM_i)$$

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FOCALEZ, IMAGE[S]Z: Particle coordinates and beam size; localization and size of vertical waist

Similar to FOCALE and IMAGE[S], but the calculations are performed with respect to the vertical coordinates Z_i and P_i , in place of Y_i and T_i .

HISTO: 1-D histogram

Any of the coordinates used in **zgoubi** may be histogrammed, namely initial Y_0 , T_0 , Z_0 , P_0 , S_0 , D_0 or current Y, T, Z, P, S, D particle coordinates (S = path length; D may change in decay process simulation with MCDESINT, or when ray-tracing in \vec{E} fields), and also spin coordinates and modulus S_X , S_Y , S_Z and $\|\vec{S}\|$.

HISTO can be used in conjunction with MCDESINT, for statistics on the decay process, by means of TYP. TYP is a one-character string. If it is set equal to 'S', only secondary particles (they are tagged with an 'S') will be histogrammed. If it is set equal to 'P', then only parent particles (non-'S') will be histogrammed. For no discrimination between S-econdary and P-arent particles, TYP = 'Q' must be used.

The dimensions of the histogram (number of lines and columns) may be modified. It can be normalized with NORM = 1, to avoid saturation.

Histograms are indexed with the parameter *NH*. This allows making independent histograms of the same coordinate at several locations in a structure. This is also useful when piling up problems in a single input data file (see also *RESET*). *NH* is in the range 1-5.

If REBELOTE is used, the statistics on the 1+NPASS runs in the structure will add up.

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 $IMAGE[S][Z]: Localization \ and \ size \ of \ vertical \ waists$

See FOCALE[Z].

MATRIX: Calculation of transfer coefficients, periodic parameters

MATRIX causes the calculation of the transfer coefficients through the optical structure, from the OBJET down to the location where MATRIX is introduced in the structure, or, upon option, down to the horizontal focus closest to that location. In this last case the position of the focus is calculated automatically in the same way as the position of the waist in IMAGE. Depending on option IFOC, MATRIX also delivers the beam matrix and betatron phase advances or (case of a periodic structure) periodic beam matrix and tunes, chromaticities and other global parameters.

Depending on the value of option IORD, different procedures follow

- If IORD = 0, MATRIX is inhibited (equivalent to FAISCEAU, whatever IFOC).
- If IORD = 1, the first order transfer matrix $[R_{ij}]$ is calculated, from a third order approximation of the coordinates. For instance

$$Y^{+} = \left(\frac{Y}{T_0}\right) T_0 + \left(\frac{Y}{T_0^2}\right) T_0^2 + \left(\frac{Y}{T_0^3}\right) T_0^3, \quad Y^{-} = -\left(\frac{Y}{T_0}\right) T_0 + \left(\frac{Y}{T_0^2}\right) T_0^2 - \left(\frac{Y}{T_0^3}\right) T_0^3$$

will yield, neglecting third order terms,

$$R_{11} = \left(\frac{Y}{T_0}\right) = \frac{Y^+ - Y^-}{2T_0}$$

In addition, if OBJET, KOBJ = 5.1 is used (hence introducing initial optical function values, $\alpha_{Y,Z}$, $\alpha_{Y,Z}$, $D_{Y,Z}$, $D'_{Y,Z}$), then, using the R_{ij} above, MATRIX will transport the optical functions and phase advances ϕ_Y , ϕ_Z , following

$$\begin{pmatrix} \beta \\ \alpha \\ \gamma \end{pmatrix}_{at \; MATRIX} = \begin{pmatrix} R_{11}^2 & -2R_{11}R_{12} & R_{12}^2 \\ -R_{11}R_{21} & R_{12}R_{21} & R_{11}R_{12} \\ R_{21}^2 & -2R_{21}R_{22} & R_{22}^2 \end{pmatrix} \begin{pmatrix} \beta \\ \alpha \\ \gamma \end{pmatrix}_{at \; OBJET}$$

$$\Delta\phi_Y = A \tan \frac{R_{12}}{(R_{11}\beta_{Y,objet} - R_{12}\alpha_{Y,objet})}, \quad \Delta\phi_Z = A \tan \frac{R_{34}}{(R_{33}\beta_{Z,objet} - R_{34}\alpha_{Z,objet})}, \quad (4.5.1)$$

$$\phi_{Y,Z} \to \phi_{Y,Z} + 2\pi$$
 if $\phi_{Y,Z} < 0$, given $[0,\pi]$ Atan determination

and print these out.

• If IORD = 2, fifth order Taylor expansions are used for the calculation of the first order transfer matrix $[R_{ij}]$ and of the second order matrix $[T_{ijk}]$. Other higher order coefficients are also calculated.

An automatic generation of an appropriate object for the use of *MATRIX* can be obtained using the procedure *OBJET* (pages 49, 239), as follows

- if IORD = 2, use OBJET(KOBJ = 6) that generates 61 sets of initial coordinates.

The next option, IFOC, acts as follows

• If IFOC = 0, the transfer coefficients are calculated at the location of MATRIX, and with respect to the reference trajectory. For instance, Y^+ and T^+ above are defined for particle number i as $Y^+ = Y^+(i) - Y(Ref)$, and $T^+ = T^+(i) - T(ref.)$.

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- If IFOC = 1, the transfer coefficients are calculated at the horizontal focus closest to MATRIX (determined automatically), while the reference direction is that of the reference particle. For instance, Y^+ is defined for particle number i as $Y^+ = Y^+(i) Y_{\text{focus}}$, while T^+ is defined as $T^+ = T^+(i) T(\text{ref.})$).
- If IFOC = 2, no change of reference frame is performed: the coordinates refer to the current frame. Namely, $Y^+ = Y^+(i)$, $T^+ = T^+(i)$, etc.

Periodic Structures

• If *IFOC* = 10 + *NPeriod*, then, from the 1-turn transport matrix as obtained in the way described above, *MATRIX* calculates periodic parameters characteristic of the structure such as optical functions and tune numbers, assuming that it is *NPeriod*-periodic, and in the coupled hypothesis, based on the Edwards-Teng method [30]. This only makes senss when met at the end of the zgoubi.dat sequence.

If IORD = 2 additional periodic parameters are computed such as chromaticities, beta-function momentum dependence, etc.

Addition of "PRINT" following IORD, IFOC [, coupled] will cause stacking of MATRIX output data into zgoubi.MATRIX.out file (convenient for use with e.g. gnuplot type of data treatment software).

Addition of "coupled" next to IORD, IFOC [, PRINT], in the case of periodic beam matrix request (i.e., IFOC = 10 + NPeriod) will cause use of coupled formalism.

About the source code:

The program matric computes the transport matrix coefficients, it is called by zgoubi when the keyword *MATRIX* is met along the zgoubi.dat sequence. matimp, called by matric, ensures the print out of the matrix (and possibly the beam matrix) in zgoubi.res, and upon 'PRINT' option in zgoubi.MATRIX.out as well.

PICKUPS: Bunch centroid path; orbit

PICKUPS computes the average values of the coordinates of the particles in a bunch (coordinates of the bunch centroid) at one or more keywords specified by their *LABELs*. The list of *LABEL(s)* concerned is specified by the user, as part of the arguments under the keyword *PICKUPS*.

In conjunction with *REBELOTE* in the case of a periodic structure, with *REBELOTE* thus being used to cause multi-turn tracking, *PICKUPS* are zeroed at start of each turn.

Pickup data computed during **zgoubi** execution are stored in the file zgoubi.PICKUP.out, usable for further analysis, or for plotting (for instance, using gnuplot).

A summary of the list of pickups and their individual bunch data is listed in the result file zgoubi.res (below the *END* keyword) at the end of **zgoubi** execution. It is concluded with statistics as the *rms*, minimum and maximum values of the bunch centroid data over the ensemble of pickups.

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PLOTDATA: Intermediate output for the PLOTDATA graphic software [54]

PLOTDATA was at the origin implemented for the purpose of plotting particle coordinates using the TRI-UMF PLOTDATA package. However nothing precludes using it with a different aim.

The *PLOTDATA* keyword can be introduced at up to 20 locations in zgoubi.dat. There, particle coordinates will be stored in a local array, FF. They are overwritten at each pass. Usage of FF is left to the user, see *FORTRAN* subroutine pltdat.f.

SPNPRNL, SPNSTORE: Print/Store spin coordinates

• SPNPRNL has similar effect to SPNPRT (page 165), except that the information is stored in a dedicated file FNAME (should post-processing with **zpop** follow, advised name is FNAME = 'zgoubi.spn' (formatted write) or 'b_zgoubi.spn' (binary write)). The data are formatted and ordered according to the FORTRAN sequence found in the subroutine spnprn.f, with meaning of printed quantities as follows:

LET(I), IEX(I): tagging character and flag (see OBJET)

SI(1-4,I) : spin components SX, SY, SZ and modulus, at the origin

SF(1-4,I) : idem at the current position GAMMA : Lorentz relativistic factor

I : particle number

IMAX : total number of particles ray-traced (see *OBJET*)

IPASS : turn number (see *REBELOTE*)

- SPNSTORE has an effect similar to SPNPRNL, with two more features.
- On the first data line, *FNAME* may be followed by a series of up to 10 *LABELs* proper to the elements of the zgoubi.dat data file at the exit of which the print should occur; if no label is given, the print occurs by default at the very location of *SPNSTORE*; if labels are given, then print occurs right downstream of all optical elements wearing those labels (and no longer at the *SPNSTORE* location).
- The next data line gives a parameter, IP : printing will occur every IP other pass, when using REBELOTE with NPASS > IP 1.

For instance the following data input in zgoubi.dat:

```
SPNSTORE zgoubi.spn HPCKUP VPCKUP 12
```

will result in output prints into zgoubi.spn, every 12 other pass, each time elements of the zgoubi.dat data list labeled either *HPCKUP* or *VPCKUP* are encountered.

Note

Binary storage can be obtained from *SPNPRNL* and *SPNSTORE*. This is for the sake of compactness and I/O access speed by zgoubi or zpop, for instance in case voluminous amounts of data should be manipulated. This is achieved by giving the storage file a name of the form *b_FNAME* or *B_FNAME* (*e.g.*, 'b_zgoubi.spn'). The *FORTRAN WRITE* output list is the same as in the *FORMATTED* case above.

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SPNPRT: Print spin coordinates

SPNPRT can be introduced anywhere in a structure. It produces a print out (to zgoubi.res) of various informations such as the initial and actual coordinates and modulus of the spin of the IMAX particles, their Lorentz factor γ , the mean values of the spin components, etc., at the location where it is placed in the zgoubi.dat data list.

If the keyword *SPNPRT* is followed by "*PRINT*" as its first label, then spin data will also be stored in zgoubi.SPNPRT.Out, an output storage file opened at the first such occurence of "*PRINT*". In particular, if *REBELOTE* is used then data will be stacked in zgoubi.SPNPRT.Out.

SRPRNT: Print SR loss statistics

SRPRNT may be introduced anywhere in a structure. It allows switching on synchrotron radiation loss computation. It produces in addition a print out (to zgoubi.res) of current state of statistics on several parameters related to SR loss presumably activated beforehand with keyword *SRLOSS*.

TWISS: Calculation of periodic optical parameters

TWISS causes the calculation of transport coefficients and various other global parameters, in particular periodical quantities as tunes and optical functions, in the coupled hypothesis. TWISS is normally placed at the end of the structure; it causes a series of up to 5 successive passes in the structure (at the manner of REBELOTE).

The object necessary for these calculations will be generated automatically if one uses OBJET with option KOBJ=5.

TWISS works in a way similar to MATRIX, iterating the MATRIX process wherever necessary, changing for instance the reference trajectory in OBJET for dp/p related computations. In particular:

- It assumes that the reference particle (particle #1 of 11, when using *OBJET[KOBJ=5]*) is located on the closed orbit. *This condition has to be satisfied for TWISS to work consistently*, because *TWISS* does not look for the closed orbit by itself (this is under installation).
- A first pass (the only one if *KTW*=1) through the structure allows computing the periodic optical functions from the rays.
- The periodic dispersions are used to define chromatic closed orbits at $\pm \delta p/p$. A second and a third pass (which terminate the process if KTW=2) with chromatic objects centered respectively on $\pm \delta p/p$ chromatic orbits will then compute the chromatic first order transport matrices. From these the chromaticities are deduced.
- Anharmonicities need two additional passes (which terminate the process if *KTW=3*). They are deduced from the difference in tunes for particles tracked on different transverse invariants, horizontal or vertical.

The execution of *TWISS* will cause printout to the file zgoubi.TWISS.out, a MADX type "twiss" file, with similar formatting, including periodic optical data as a header (tunes, chromaticities, etc.) and, in sequence, optical functions and strengths at all elements.

About the source code:

The program beamat ensures the transport of the beam matrix along the zgoubi.dat sequence. beamat is called by optice, itself called after each optical element, in the program zgoubi.

The starting beam matrix value is in the array FI, initialized by the program twiss when met at the end of the zgoubi.dat sequence. The array F0 contains the running beam matrix.

The program optimp, called from opticc, prints to zgoubi. TWISS.out after each optical element of the zgoubi.dat sequence.

4.6 Complements Regarding Various Functionalities

4.6.1 Reference rigidity

zgoubi computes the strengths of optical elements (they are usually defined by their field) from the reference rigidity *BORO* as defined in *[MC]OBJET*. However using *CAVITE*, and indirectly *SCALING*, may affect the reference rigidity, following

$$B\rho_{ref} = BORO \longrightarrow B\rho_{ref} = BORO + \delta B\rho_s$$

with normally $\delta B \rho_s$ the synchronous rigidity increase (or decrease). A typical configuration where this would occur is that of multi-turn tracking in a pulsed synchrotron, where in general strengths have to follow the acceleration (see section 4.6.6).

4.6.2 Time Varying Fields

Fields can be varied as a function of time (in some cases this may mean as a function of turn number, see section 4.6.6), by means of the *SCALING* keyword.

Eventually some families of magnets may be given a different timing law for the simulation of special processes (*e.g.*, time varying orbit bump, fast crossing of spin resonances with families of jump quadrupoles).

4.6.3 Backward Ray-Tracing

For the purpose of parameterization for instance, it may be interesting to ray-trace backward from the image toward the object. This can be performed by first reversing the position of optical elements in the structure, and then reversing the integration step sign in all the optical elements.

An illustration of this feature is given in the following Figure 42.

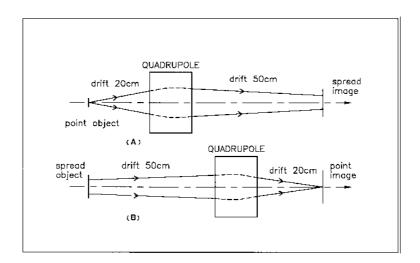


Figure 42: A. Regular forward ray-tracing, from object to image.

B. Same structure, with backward ray-tracing from image to object: negative integration step XPAS is used in the quadrupole.

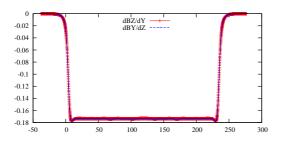
4.6.4 Checking Fields and Trajectories Inside Optical Elements

• In all optical elements, an option IL is available. It is normally set to IL = 0 and in this case has no effect.

IL=1 causes a print in zgoubi.res of particle coordinates and field along trajectories in the optical element. In the meantime, a calculation and summation of the values of $\vec{\nabla} \cdot \vec{B}$, $\vec{\nabla} \times \vec{B}$ and $\nabla^2 \vec{B}$ (same for \vec{E}) at all integration steps is performed, which allows a check of the behavior of \vec{B} (or \vec{E}) in field maps (all these derivatives should normally be zero).

IL=2 causes a print of particle coordinates and other informations into the file zgoubi.plt at each integration step; this information can further be processed with \mathbf{zpop}^9 . In order to minimize the volume of that storage file (when dealing with small step size, large number of particles, etc.) it is possible to print out every other 10^n integration step by taking $IL=2\times 10^n$ (for instance, IL=200 would cause output into zgoubi.plt every 100 other step).

IL = 7 causes a print of particle coordinates, fields, field derivatives and other informations into the file zgoubi.impdev.out, one line of data at each integration step. This information can be further plotted (e.g., using **zpop**, or gnuplot). An example is given in fig. 43, a plot of the quadrupole and sextupole field indices along the reference orbit in a combined function main dipole pertaining to the AGS lattice [55].



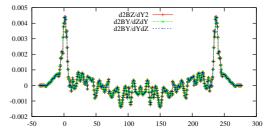


Figure 43: Typical field and derivatives, here, along the 10 GeV proton orbit across an AGS A-type main magnet. They are obtained from second degree polynomial interpolation from the magnet measured field map. Left: $dB_Z(s)/dY$ and $dB_Y(s)/dZ$, bottom: $d^2B_Z(s)/dY^2,\ d^2B_Y(s)/dZdY,\ d^2B_Y(s)/dYdZ$. These data were stored in zgoubi.impdev.out during execution, by stating $I\!L=7$ under TOSCA keyword.

• When dealing with field maps (e.g., CARTEMES, ELREVOL, TOSCA), an option index IC is available. It is normally set to IC = 0 and in this case has no effect.

IC = 1 causes a print of the field map in zgoubi.res.

IC=2 will cause a print of field maps into the file zgoubi.map which can further be processed with **zpop** for plotting and other data treatment purposes.

4.6.5 Labeling Keywords

Keywords in **zgoubi** input data file zgoubi.dat can be LABEL'ed, for the purpose of the execution of such procedures as REBELOTE, PICKUPS, FAISCNL, FAISTORE, SCALING, and also for the purpose of particle coordinate storage into zgoubi.plt (see section 4.6.4, IL=2 option).

A keyword in zgoubi.dat accepts two *LABELs*. The first one is used for the above mentioned purposes, the second one (set to ".plt" in that case) is used essentially with *MARKER* for storage of current particle data into zgoubi.plt. The keyword and its *LABEL[s]* should fit within a 110-character long string on a single line (a quantity set in the *FORTRAN* file prdata.f).

4.6.6 Multi-turn Tracking in Circular Machines

Multi-turn tracking in circular machines can be performed by means of the keyword *REBELOTE*. *REBELOTE* is introduced in the zgoubi.dat data list with its argument *NPASS*+1 being the number of turns to be performed. It will cause a jump of the "multi-turn pointer" back to (details on page 73), either the beginning of the data list (default case), or to a particular *LABEL* in that list. From then on, tracking resumes down to *REBELOTE* again, and so forth until the requested number of passes has been reached.

⁹See Part D of the Guide.

Possible magnet timing laws B(T) during the multi-turn process (with T=1 to NPASS+1 counted in number of turns) can be introduced by means of SCALING.

In order that the IMAX particles of the beam start a new pass with the coordinates they had reached at the end of the previous one, the option K = 99 has to be specified in REBELOTE.

Synchrotron acceleration can be simulated, using following the procedure:

- CAVITE appears in the zgoubi.dat data list (normally before REBELOTE), with option $IOPT \neq 0$,
- the RF frequency of the cavity may be given a timing law $f_{RF}(T)$ by means of *SCALING*, family *CAVITE*,
- the magnets are given a field timing law B(T), (with T=1 to NPASS+1 counted in number of turns) by means of SCALING.

Eventually some families of magnets may be given a different timing law for the simulation of special processes (*e.g.*, time varying orbit bump, fast crossing of spin resonances with families of jump quadrupoles).

4.6.7 Positioning, (Mis-)Alignment, of Optical Elements and Field Maps

The last record in most optical elements and field maps is the positioning option *KPOS*. *KPOS* is followed by the positioning parameters, *e.g.*, *XCE*, *YCE* for translation and *ALE* for rotation. The positioning works in two different ways, depending whether the element is defined in Cartesian (X, Y, Z) coordinates (e.g., QUADRUPO, TOSCA), or polar (R, θ, Z) coordinates (DIPOLE).

Cartesian Coordinates:

If KPOS = 1, the optical element is moved (shifted by XCE, YCE and Z-rotated by ALE) with respect to the incoming reference frame. Trajectory coordinates after traversal of the element refer the element frame.

If KPOS=2, the shifts XCE and YCE, and the tilt angle ALE are taken into account, for mis-aligning the element with respect to the incoming reference, as shown in Fig. 44. The effect is equivalent to a CHANGREF(XCE, YCE, ALE) upstream of the optical element, followed by CHANGREF(XCS, YCS, ALS = -ALE) downstream of it, with computed XCS, YCS values as schemed in Fig. 44.

KPOS = 3 option is available for a limited number of magnets (e.g., BEND, MULTIPOL, AGSMM); it is effective only if a non zero dipole component B1 is present, or if ALE is non-zero. It positions automatically the magnet in a symmetric manner with respect to the incoming and outgoing reference axis, convenient for periodic structures, as follows (Fig 45).

Both incoming and outgoing reference frames are tilted w.r.t. the magnet,

- either, by an angle ALE if ALE $\neq 0$,
- or, if ALE=0 by half the Z-rotation $\theta_Z/2$ such that $L=2\frac{BORO}{B1}\sin(\theta_Z/2)$, wherein L= geometrical length, BORO= reference rigidity as defined in OBJET.

Next, the optical element is Y-shifted by YCE (XCE is not used) in a direction orthogonal to the new magnet axis (i.e., at an angle $ALE + \pi/2$ wrt. the X axis of the incoming reference frame).

KPOS=4 applies to a limited number of optical elements, as AGSMM (AGS main magnet). By default, it aligns the magnet in a way similar to KPOS=3, with reference frame Z-rotated by $\theta_Z/2$ as drawn from $L=2\frac{BORO}{B1}\sin(\theta_Z/2)$. However magnet mis-alignment (alignment errors) are handled in a specific way,

as follows.

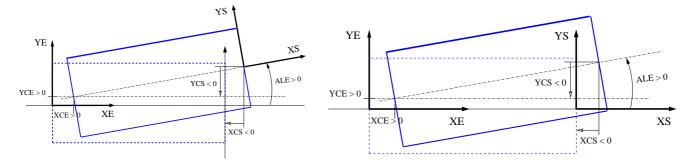


Figure 44: Case of Cartesian frame optical element. Left: moving an optical element using KPOS = 1. Right: Mis-aligning an optical element using KPOS = 2. (X_E, Y_E) and (X_S, Y_S) are respectively the incoming and outgoing reference frames.

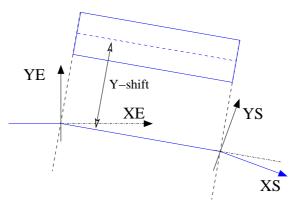
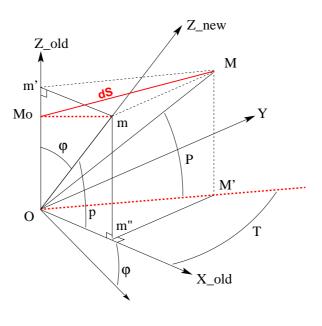


Figure 45: Case of Cartesian frame optical element. Alignment of a bend by half the deviation, using KPOS = 3. (X_E, Y_E) and (X_S, Y_S) are respectively the incoming and outgoing reference frames.

All 6 types of misalignments, namely, X-, Y-, Z-shift, X-, Y-, Z-rotation, can be accounted for, in an arbitrary order. They are specified using the "new style" *CHANGREF* method as described in page 103. Longitudinal rotation "XR" is taken *wrt.* the longitudinal axis, whereas radial and axial rotations, "YR" and "ZR", are with respect to an axis going through the center of the magnet.



X new

Figure 46: Pitch angle, φ , in the "YR" type of rotation, using KPOS = 4. M is the new position, in the rotated plane (Y, Z_{new}) , of a particle with velocity $\vec{v}//\vec{M_o}M$ located at former position M_o in the old, (Y, Z_{old}) , plane. M', m, m' are projections of M, m'' is projection of M'. T and P are the horizontal and vertical angles as defined in Fig. 1. p is the projection of P.

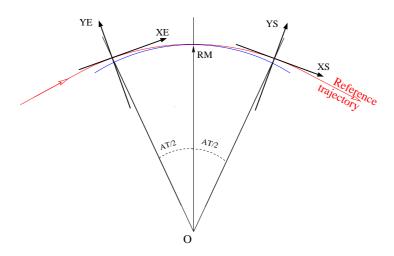


Figure 47: Positioning of a polar field map, using KPOS = 1.

Polar Coordinates

If KPOS=1, the element is positioned automatically in such a way that a particle entering with zero initial coordinates and $1+DP=B\rho/BORO$ relative rigidity will reach position $(RM,\frac{AT}{2})$ in the element with T=0 angle with respect to the moving frame in the polar coordinates system of the element (Fig. 47; see DIPOLE-M and POLARMES).

If KPOS = 2, the map is positioned in such a way that the incoming reference frame is presented at radius RE with angle TE. The exit reference frame is positioned in a similar way with respect to the map, by means of the two parameters RS (radius) and TS (angle) (see Fig. 11A page 88A).

4.6.8 Coded Integration Step

In several optical elements (e.g., all multipoles, BEND) the integration step (in general noted XPAS) can be coded under the form $XPAS = \#E \mid C \mid S$, with E, C, S integers, E is the number of steps in the entrance fringe field region, C is the number of steps in the magnet body, and S is the number of steps in the exit fringe field region.

4.6.9 Ray-tracing of an Arbitrarily Large Number of Particles

Monte Carlo multi-particle simulations involving an arbitrarily large number of particles can be performed using MCOBJET together with REBELOTE, put at the end of the optical structure, with its argument NPASS being the number of passes through REBELOTE, and (NPASS+1)*IMAX the number of particles to be ray-traced. In order that new initial conditions (D, Y, T, Z, P, X) be generated at each pass, K=0 has to be specified in REBELOTE.

Statistics on coordinates, spins, and other histograms can be performed by means of such procedures as *HISTO*, *SPNTRK*, etc. that stack the information from pass to pass.

4.6.10 Stopped Particles: The IEX Flag

As described in OBJET, each particle I=1, IMAX is attached a value IEX(I) of the IEX flag. Normally, IEX(I)=1. Under certain circumstances, IEX may be changed to a negative value by **zgoubi**, as follows.

- -1: the trajectory happened to wander outside the limits of a field map
- -2: too many integration steps in an optical element (a quantity controlled in MXSTEP. H include file)
- -3: deviation happened to exceed $\pi/2$ in an optical element not designed to allow that
- -4: stopped by walls (procedures CHAMBR, COLLIMA)
- -5: too many iterations in subroutine depla.f
- -6: energy loss exceeds particle energy
- -7: field discontinuities larger than 50% within a field map
- -8: reached field limit in an optical element

Only in the case IEX = -1 will the integration not be stopped since in this case the field outside the map is extrapolated from the map data, and the particle may possibly get back into the map (see section 1.4.2 on page 27). In all other cases the particle will be stopped.

4.6.11 Negative Rigidity

zgoubi can handle negative rigidities $B\rho = p/q$. This is equivalent to considering either particles with negative charge (q < 0) or momentum (p < 0), or reversed fields (wrt. the field sign that shows in the zgoubi.dat optical element data list).

Negative rigidities may be specified in terms of BORO < 0 or $D = B\rho/BORO < 0$ when defining the initial coordinates with OBJET or MCOBJET.

PART B

Keywords and input data formatting

Glossary of Keywords, Part B

Zgoubi.dat data formatting, where to find a keyword

AGSMM	AGS main magnet	183
AGSQUAD	AGS quadrupole	184
AIMANT	Generation of dipole mid-plane 2-D map, polar frame	185
AUTOREF	Transport beam into a new reference frame	189
BEAMBEAM	Beam-beam lens	190
BEND	Bending magnet, Cartesian frame	191
BINARY	BINARY/FORMATTED data converter	192
BREVOL	1-D uniform mesh magnetic field map	193
CARTEMES	2-D Cartesian uniform mesh magnetic field map	194
CAVITE	Accelerating cavity	196
CHAMBR	Long transverse aperture limitation	197
CHANGREF	Transformation to a new reference frame	198
CIBLE	Generate a secondary beam following target interaction	199
COLLIMA	Collimator	200
DECAPOLE	Decapole magnet	201
DIPOLE	Dipole magnet, polar frame	202
DIPOLE-M	Generation of dipole mid-plane 2-D map, polar frame	203
DIPOLES	Dipole magnet N-tuple, polar frame	205
DODECAPO	Dodecapole magnet	206
DRIFT	Field free drift space	207
EBMULT	Electro-magnetic multipole	208
EL2TUB	Two-tube electrostatic lens	210
ELMIR	Electrostatic N-electrode mirror/lens, straight slits	211
ELMIRC	Electrostatic N-electrode mirror/lens, circular slits	212
ELMULT	Electric multipole	213
ELREVOL	1-D uniform mesh electric field map	214
EMMA	2-D Cartesian or cylindrical mesh field map for EMMA FFAG	
END	End of input data list	220
ESL	Field free drift space	
ERRORS	Injecting errors	
FAISCEAU	Print particle coordinates	
FAISCNL	Store particle coordinates in file FNAME	
FAISTORE	Store coordinates every <i>IP</i> other pass at labeled elements	
FFAG	FFAG magnet, N-tuple	
FFAG-SPI	Spiral FFAG magnet, N-tuple	
FIN	End of input data list	
FIT,FIT2	Fitting procedure	
FOCALE	Particle coordinates and horizontal beam size at distance XL	
FOCALEZ	Particle coordinates and vertical beam size at distance XL	
GASCAT	Gas scattering	
GETFITVAL	Get values of variables as saved from former FIT[2] run	
HISTO	1-D histogram	
IMAGE	Localization and size of horizontal waist	
IMAGES	Localization and size of horizontal waists	
IMAGESZ	Localization and size of vertical waists	
IMAGEZ	Localization and size of vertical waist	
MAP2D	2-D Cartesian uniform mesh field map - arbitrary magnetic field	
MAP2D-E	2-D Cartesian uniform mesh field map - arbitrary electric field	231

MARKER	Marker	
MATRIX	Calculation of transfer coefficients, periodic parameters	233
MCDESINT	Monte-Carlo simulation of in-flight decay	
MCOBJET	Monte-Carlo generation of a 6-D object	
MULTIPOL	Magnetic multipole	
OBJET	Generation of an object	239
OBJETA	Object from Monte-Carlo simulation of decay reaction	242
OCTUPOLE	Octupole magnet	243
OPTICS	Write out optical functions	244
OPTIONS	Global options	245
ORDRE	Taylor expansions order	246
PARTICUL	Particle characteristics	247
PICKUPS	Bunch centroid path; orbit	248
PLOTDATA	Intermediate output for the PLOTDATA graphic software	249
POISSON	Read magnetic field data from POISSON output	
POLARMES	2-D polar mesh magnetic field map	251
PS170	Simulation of a round shape dipole magnet	252
QUADISEX	Sharp edge magnetic multipoles	253
QUADRUPO	Quadrupole magnet	254
REBELOTE	'Do it again'	256
RESET	Reset counters and flags	258
SCALING	Power supplies and R.F. function generator	259
SEPARA	Wien Filter - analytical simulation	260
SEXQUAD	Sharp edge magnetic multipole	261
SEXTUPOL	Sextupole magnet	262
SOLENOID	Solenoid	263
SPINR	Spin rotation	264
SPNPRNL	Store spin coordinates into file FNAME	265
SPNSTORE	Store spin coordinates every <i>IP</i> other pass at labeled elements	265
SPNPRT	Print spin coordinates	265
SPNTRK	Spin tracking	266
SRLOSS	Synchrotron radiation energy loss	267
SRPRNT	Print SR loss statistics	
SYNRAD	Synchrotron radiation spectral-angular densities	269
SYSTEM	System call	270
TARGET	Generate a secondary beam following target interaction	199
TOSCA	2-D and 3-D Cartesian or cylindrical mesh field map	
TRANSMAT	Matrix transfer	273
TRAROT	Translation-Rotation of the reference frame	274
TWISS	Calculation of periodic optical parameters	275
UNDULATOR	Undulator magnet	276
UNIPOT	Unipotential cylindrical electrostatic lens	
VENUS	Simulation of a rectangular shape dipole magnet	278
WIENFILT	Wien filter	
VMV	Reverse signs of V and Z reference axes	280

Optical elements versus keywords

What can be simulated What keyword(s) can be used for that

This glossary gives a list of keywords suitable for the simulation of common optical elements. These are classified in three categories: magnetic, electric and combined electro-magnetic elements.

Field map procedures are also listed; they provide a means for ray-tracing through measured or simulated electric and/or magnetic fields.

MAGNETIC ELEMENTS

AGS main magnet AGSMM

Cyclotron magnet or sector DIPOLE[S], DIPOLE-M, FFAG, FFAG-SPI

Decapole DECAPOLE, MULTIPOL

Dipole[s], spectrometer dipole AIMANT, BEND, DIPOLE[S][-M], MULTIPOL, QUADISEX

Dodecapole DODECAPO, MULTIPOL

FFAG magnets DIPOLES, FFAG, FFAG-SPI, MULTIPOL

Helical dipole HELIX

Multipole MULTIPOL, QUADISEX, SEXQUAD

Octupole OCTUPOLE, MULTIPOL, QUADISEX, SEXQUAD Quadrupole QUADRUPO, MULTIPOL, SEXQUAD, AGSQUAD Sextupole SEXTUPOL, MULTIPOL, QUADISEX, SEXQUAD

Skew multipoles MULTIPOL
Solenoid SOLENOID
Undulator UNDULATOR

Using field maps

1-D, cylindrical symmetry BREVOL

2-D, mid-plane symmetry CARTEMES, POISSON, TOSCA

2-D, no symmetry

2-D, polar mesh, mid-plane symmetry

3-D, no symmetry

TOSCA

EMMA FFAG quadrupole doublet

linear composition of field maps

TOSCA

ELECTRIC ELEMENTS

2-tube (bipotential) lens **EL2TUB** 3-tube (unipotential) lens **UNIPOT** Decapole **ELMULT** Dipole **ELMULT** Dodecapole **ELMULT** Multipole **ELMULT** N-electrode mirror/lens, straight slits **ELMIR** N-electrode mirror/lens, circular slits **ELMIRC** Octupole **ELMULT** Quadrupole **ELMULT** R.F. (kick) cavity **CAVITE** Sextupole **ELMULT** Skew multipoles **ELMULT**

Using field maps

1D, cylindrical symmetry ELREVOL

2-D, no symmetry MAP2D-E

ELECTRO-MAGNETIC ELEMENTS

Decapole **EBMULT** Dipole **EBMULT** Dodecapole **EBMULT** Multipole **EBMULT** Octupole **EBMULT** Quadrupole **EBMULT** Sextupole **EBMULT** Skew multipoles EBMULT

Wien filter SEPARA, WIENFILT

INTRODUCTION

Here after is given a detailed description of input data formatting and units. All available keywords appear in alphabetical order.

Keywords are read from the input data file by an unformatted *FORTRAN READ* statement. They be enclosed between quotes (e.g., 'DIPOLE').

Text string data such as comments or file names, are read by formatted READ statements, no quotes should be used in that case.

Numerical variables and indices are read by unformatted READ. It may therefore be necessary that integer variables be assigned an integer value.

In the following tables

- the first column shows the expected input parameters (actually, their values are expected), indices and text strings,
- the second column gives brief comments regarding their meaning and use,
- the third column gives the units or ranges,
- the fourth column indicates whether the expected parameter types are integer (I), real (E) or text string (A). For example, "I, 3*E" means that one integer followed by 3 reals is expected. "A80" means that a text string of maximum 80 characters is expected.

AGSMM

R1, R2, R3

X_E, λ_E, E_2, E_3	Entrance face Integration zone ; fringe field extent :	2*cm, 2*no dim.	4*E
NBLW, NBLW times : NW, I	Number of back-leg windings; for each back-leg winding: number of windings, current.	≤2, <i>NBLW</i> × (any, Amp.)	I, NBLW× (I, E)
$MOD[.MOD2], dL, R_0, dB1, dB2, dB3$	Type of magnet model 1 [type of back-leg winding model 2]; unused; pole tip radius, $10~\rm cm$ if set to zero; relative error on dipole, quadrupole, sextupole component.	2*no dim., cm, 3*no dim.	I[.I], 5*E
IL	$IL=1,2[\times 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I

quadrupole fringe field extent = $\lambda_E * E_2$; sextuppole fringe field extent = $\lambda_E * E_3$ (sharp edge if field extent is zero)

dipole fringe field extent = λ_E ;

Skew angles of field components

NCE, $C_0 - C_5$ same as QUADRUPO 0-6, 6*no dim. I, 6*E

Exit face

AGS main magnet

 X_S, λ_S, S_2, S_3 Integration zone; as for entrance 2*cm, 2*no dim. 4*E

NCS, $C_0 - C_5$ 0-6, 6*no dim. I, 6*E

3*rad

10*E

XPAS Integration step cm E

KPOS, XCE, KPOS=1: element aligned, 2: misaligned; 1-4, 2*cm, rad I, 3*E YCE, ALE shifts, tilt (unused if KPOS=1).

KPOS = 3: effective only if $B1 \neq 0$: entrance and exit frames are shifted by YCE and tilted wrt. the magnet by an angle of

• either ALE if ALE $\neq 0$

• or $2 \operatorname{Arcsin}(B1 \, XL \, / \, 2BORO)$ if ALE=0 KPOS = 4 : same as KPOS = 3 however

with possible X- or Y- or Z-misalignment or -rotation

(under development)

¹MOD=1 : centered multipole model ; MOD=2 : long-shifted dipole model ; MOD=3 : short-shifted dipole model.

 $^{^2}MOD2 = 0 \text{ (default)} : \text{user defined back-leg windings (defined in routine } \text{agsblw.f}); \\ MOD2 = 1 : \text{actual AGS data are taken, namely} : \text{MM_A16AD} : \text{NBLW} = 1, \text{SIGN} = 1.D0, \text{NW} = 10 ; \text{MM_A18CF} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 10 ; \text{MM_A19BD} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 10 ; \text{MM_A19BD} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 12 ; \text{MM_B02BF} : \text{NBLW} = 2, \text{SIGN} = 1.D0, \text{NW} = 12, \text{SIGN} = 1.D0, \text{NW} = 12, \text{SIGN} = 1.D0, \text{NW} = 12, \text{SIGN} = 1.D0, \text{NW} = 10 ; \text{MM_B03CD} : \text{NBLW} = 1, \text{SIGN} = 1.D0, \text{NW} = 10 ; \text{MM_B05A} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 10 ; \text{MM_B05D} : \text{NBLW} = 1, \text{SIGN} = 1.D0, \text{NW} = 10 ; \text{MM_B05A} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 10 ; \text{MM_B01BD} : \text{NBLW} = 1, \text{SIGN} = 1.D0, \text{NW} = 6 ; \text{MM_K19BD} : \text{NBLW} = 1, \text{SIGN} = 1.D0, \text{NW} = 6 ; \text{MM_K20B} : \text{NBLW} = 1, \text{SIGN} = 1.D0, \text{NW} = 6 ; \text{MM_L13CF} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_A07CD} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_A08C} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_B01B} : \text{NBLW} = 1, \text{SIGN} = 1.D0, \text{NW} = 6 ; \text{MM_L06A} : \text{NBLW} = 1, \text{SIGN} = 1.D0, \text{NW} = 5 ; \text{MM_L07C} : \text{NBLW} = 1, \text{SIGN} = 1.D0, \text{NW} = 5 ; \text{MM_L07C} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_L07C} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E06A} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E06A} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E07CD} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E07CD} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E07CD} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E06A} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E06A} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E06A} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E06A} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E06A} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E06A} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E06A} : \text{NBLW} = 1, \text{SIGN} = -1.D0, \text{NW} = 5 ; \text{MM_E06A} : \text{NBLW} = 1, \text{SIGN} = -1.$

MOD2 = 1: User defined - implementation to be completed.

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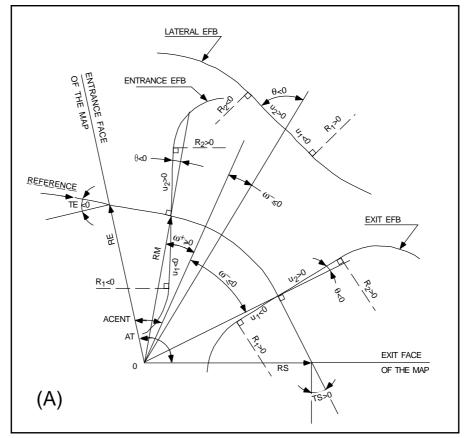
AGSQUAD	AGS quadrupole		
IL	$IL=1,2[imes 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
XL , R_0 , $IW1$, $IW2$, $IW3$ $dIW1$, $dIW2$, $dIW3$	3, Length of element; radius at pole tip; current in windings; relative error on currents.	2*cm,3*A 3*no dim	5*E 3*E
X_E, λ_E	Entrance face Integration zone; fringe field extent. (sharp edge if field extent is zero)	2*cm,9*no dim.	11*E
NCE , $C_0 - C_5$	Same as QUADRUPO	0-6, 6*no dim.	I, 6*E
X_S, λ_S	Exit face Integration zone; as for entrance	2*cm, 9*no dim.	11*E
NCS , $C_0 - C_5$		0-6, 6*no dim.	I, 6*E
R1	Roll angle	10*rad	10*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<i>KPOS</i> =1 : element aligned, 2 : misaligned; shifts, tilt (unused if <i>KPOS</i> =1).	1-2, 2*cm, rad	I, 3*E

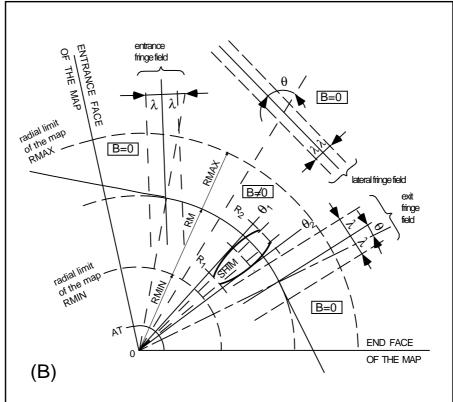
AIMANT	Generation of dipole mid-plane 2-D map, polar frame $B_Z = \mathcal{F}B_0 \left(1 - N\left(\frac{R - RM}{RM}\right) + B\left(\frac{R - RM}{RM}\right)^2 + G\left(\frac{R - RM}{RM}\right)^$	$\frac{M}{2}$	
NFACE, IC, IL	Number of field boundaries $IC=1,2$: print field map $IL=1,2[\times 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$2-3; 0-2; 0-2[\times 10^n],$	73*I
IAMAX, IRMAX	Azimuthal and radial number of nodes of the mesh	$\leq 400, \leq 10^4$	2*I
B_0 , N , B , G	Field and field indices	kG, 3*no dim.	4*E
AT, ACENT, RM, RMIN, RMAX	Mesh parameters : total angle of the map ; azimuth for EFBs positioning ; reference radius ; minimum and maximum radii	2*deg, 3*cm	5*E
	ENTRANCE FIELD BOUNDARY		
λ, ξ	Fringe field extent (normally \simeq gap size); flag: - if $\xi \geq 0$: second order type fringe field with linear variation over distance ξ - if $\xi = -1$: exponential type fringe field: $F = (1 + \exp(P(s)))^{-1}$ $P(s) = C_0 + C_1(\frac{s}{\lambda}) + C_2(\frac{s}{\lambda})^2 + + C_5(\frac{s}{\lambda})^5$	cm, (cm)	2*E
NC , $C_0 - C_5$, shift	NC = 1 + degree of $P(s)$; C_0 to C_5 : see above ; EFB shift (ineffective if $\xi \geq 0$)	0-6, 6*no dim., cm	I, 7*E
$\omega^+, \theta, R_1, U_1, U_2, R_2$	Azimuth of entrance EFB with respect to <i>ACENT</i> ; wedge angle of EFB; radii and linear extents of EFB (use $\mid U_{1,2} \mid = \infty$ when $R_{1,2} = \infty$)	2*deg, 4*cm	6*E
	(Note : $\lambda = 0$, $\omega^+ = \text{ACENT}$ and $\theta = 0$ for sharp edge)		
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDARY)		
λ, ξ $NC, C_0 - C_5$, shift $\omega^-, \theta, R_1, U_1, U_2, R_2$	Fringe field parameters See above Positioning and shape of the exit EFB	cm, (cm) 0-6, 6*no dim., cm 2*deg, 4*cm	2*E 1, 7*E 6*E

(Note : $\lambda=0,\,\omega^-=\text{-AT+ACENT}$ and $\theta=0$ for

sharp edge)

If NFACE = 3	LATERAL FIELD BOUNDARY (See ENTRANCE FIELD BOUNDA Next 3 records <i>only</i> if <i>NFACE</i> = 3	RY)	
λ, ξ $NC, C_0 - C_5$, shift $\omega^-, \theta, R_1, U_1, U_2, R_2$, RM3	Fringe field parameters See above Positioning and shape of the lateral EFB; RM3 is the radial position on azimuth ACENT	cm, (cm) 0-6, 6*no dim., cm 2*deg, 5*cm	2*E I, 7*E 7*E
NBS	Option index for perturbations to the field map	$-2 - 0 \text{ or } \ge 1$	I
If $NBS = 0$	Normal value. No other record required		
If $NBS = -2$	The map is modified as follows:		
$R_0, \Delta B/B_0$	B transforms to $B*\left(1+rac{\Delta B}{B_0}rac{R-R_0}{RMAX-RMIN} ight)$	cm, no dim.	2*E
If $NBS = -1$	the map is modified as follows:		
$\theta_0, \Delta B/B_0$	B transforms to $B*\left(1+rac{\Delta B}{B_0}rac{ heta- heta_0}{AT} ight)$	deg, no dim.	2*E
If NBS ≥ 1	Introduction of NBS shims		
For $I = 1$, NBS	The following 2 records must be repeated NBS times		
$R_1, R_2, \theta_1, \theta_2, \lambda$	Radial and angular limits of the shim ; λ is unused	2*cm, 2*deg, cm	5*E
$\gamma, \alpha, \mu, \beta$	geometrical parameters of the shim	2*deg, 2*no dim.	4*E
IORDRE	Degree of interpolation polynomial: 2 = second degree, 9-point grid 25 = second degree, 25-point grid 4 = fourth degree, 25-point grid	2, 25 or 4	I
XPAS	Integration step	cm	E
KPOS	Positioning of the map, normally 2. Two options :	1-2	I
If KPOS = 2 RE, TE, RS, TS	Positioning as follows: Radius and angle of reference, respectively, at entrance and exit of the map.	cm, rad, cm, rad	4*E
If KPOS = 1 <i>DP</i>	Automatic positioning of the map, by means of reference relative momentum	no dim.	E

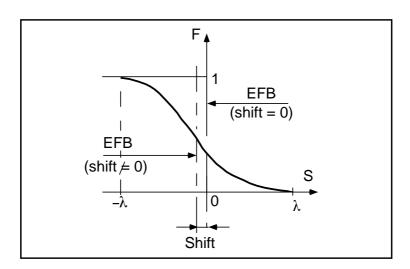




 $A: Parameters \ used \ to \ define \ the \ field \ map \ and \ geometrical \ boundaries.$ $B: Parameters \ used \ to \ define \ the \ field \ map \ and \ fringe \ fields.$



Second order type fringe field.



Exponential type fringe field.

AUTOREF Transport beam into a new reference frame

I	$1: \mbox{Equivalent to global $\it CHANGREF(XCE=0,YCE=Y(1),ALE=T(1))$.}$	1-2	I
	2: Equivalent to global $CHANGREF(XW, YW, T(1))$, with (XW, YW) the location of the intersection (waist) of particles 1, 4 and 5 (useful with $MATRIX$, for automatic positioning of the first order focus).		
	3: Equivalent to global $CHANGREF(XW,YW,T(I1))$, with (XW,YW) the location of the intersection (waist) of particles $I1$, $I2$ and $I3$ (for instance: $I1$ = central trajectory, $I2$ and $I3$ = paraxial trajectories that intersect at the first order focus).		
	4 : Equivalent to global <i>CHANGREF</i> (<i>XCE</i> , <i>YCE</i> , <i>ALE</i>). 4.1 : Equivalent to global <i>CHANGREF</i> (<i>XCE</i> , <i>YCE</i> , <i>ALE</i>) with in addition centering of the beam on a new relative momentum <i>DCE</i> .		
	5: The beam is centered vertically on ZCE, PLE.		
If $I = 3$ I1, I2, I3	Provide next record if $I=3$ Three particle numbers	3*(1- <i>IMAX</i>)	3*I
If $I = 4$ XCE, YCE, ALE	Provide next record if $I=4$ XCE and beam centroid new coordinates YCE, ALE	2*cm, mrad	3*E
If $I = 4.1$ XCE, YCE, ALE, DCE	Provide next record if $I=4$ XCE and beam centroid new coordinates YCE, ALE, DCE	2*cm, mrad, -	4*E
If $I = 5$ ZCE, PLE	Provide next record if $I=5$ New vertical beam centroid coordinates $\it ZCE$, $\it PLE$	cm, mrad	2*E

BEAMBEAM	Beam-beam lens		
SW, I	0/1 : off/on; beam intensity. Use SPNTRK to activate spin kicks.	0-2, Amp	I, E
$\alpha_Y, \ \beta_Y, \ \epsilon_{Y,norm}/\pi$	Beam parameters, horizontal.	- , m, m.rad	3*E
$\alpha_Z, \ \beta_Z, \ \epsilon_{Z,norm}/\pi$	Beam parameters, vertical.	- , m, m.rad	3*E
$\sigma_X,~\sigma_{dp/p}$	rms bunch length; rms momentum spread.	m, -	2*E
C , α	Ring circumference; momentum compaction.	m, -	2*E
$Q_Y,\ Q_Z,\ Q_s$	Tunes, horizontal, vertical, synchrotron.	-, -, -	3*E
A_Y, A_Z, A_X	Amplitudes, horizontal, vertical, longitudinal.	-, -, -	3*E

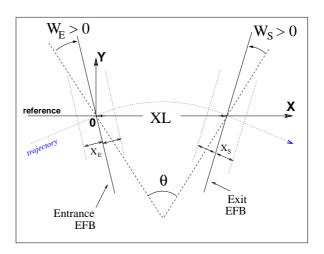
BEND Bending magnet, Cartesian frame

IL	$IL = 1, 2[\times 10^n], 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
XL, Sk, B1	Length; skew angle; field	cm, rad, kG	3*E
$X_{\mathrm{E}}, \lambda_{\mathrm{E}}, W_{\mathrm{E}}$	Entrance face: Integration zone extent; fringe field extent (normally \simeq gap height; zero for sharp edge); wedge angle	cm, cm, rad	3*E
$N, C_0 - C_5$	Unused ; fringe field coefficients : $B(s)=B1$ $F(s)$ with $F(s)=1/(1+\exp(P(s))$ and $P(s)=\sum_{i=0}^5 C_i(s/\lambda)^i$	unused, 6*no dim.	I, 6*E
	Exit face :		
X_S, λ_S, W_S	See entrance face	cm, cm, rad	3*E
$N, C_0 - C_5$		unused, 6*no dim.	I, 6*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	 KPOS=1: element aligned, 2: misaligned; shifts, tilt (unused if KPOS=1) KPOS = 3: entrance and exit frames are shifted by YCE 	1-2, 2*cm, rad	I, 3*E

and tilted wrt. the magnet by an angle of

 \bullet or $2 \operatorname{Arcsin}(B1XL / 2BORO)$ if ALE=0

ullet either ALE if ALE $\neq 0$



Geometry and parameters of BEND: XL = length, θ = deviation, W_E , W_S are the entrance and exit wedge angles. The motion is computed in the Cartesian frame (O,X,Y,Z)

BINARY BINARY/FORMATTED data converter

NF[.J], NCol, NHDR Number of files to convert [READ format type, see below],

 $\leq 20, \leq 7, 0-9$ 3*I1

of data columns, of header lines.

The next NF lines :

FNAME Name of the file to be converted. File content is assumed binary

A80

iff name begins with "B_" or "b_", assumed formatted otherwise.

READ format, case of formatted input file:

If FRM not given Format is '*'

If FRM=1 Format is '1X, 7E11.*'

READ format, case of binary input file:

Expected format is 7 column rows.

BREVOL

	X-axis cylindrical symmetry is assumed		
$I\!C,I\!L$	$I\!C=1,2$: print the map $I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[\times 10^n], 7$	2*I
BNORM, XN	Field and X-coordinate normalization coeff.	2*no dim.	2*E
TITL	Title. Start with "FLIP" to get field map X-flipped.		A80
IX	Number of longitudinal nodes of the map	≤ 400	I
FNAME [, SUM] $^{1,\;2}$	File name		A80
ID, A, B, C [, A', B', C' , B'' , etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID=0$. $ID=$ -1, 1 or ≥ 2 : as for <i>CARTEMES</i>	≥ -1 , 2*no dim., cm [,2*no dim., cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	Unused	2, 25 or 4	I
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E

1-D uniform mesh magnetic field map

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED']) DO 1 I = 1, IX IF (BINARY) THEN READ(NL) X(I), BX(I) ELSE READ(NL,*) X(I), BX(I) ENDIF 1 CONTINUE
```

where X(I) and BX(I) are the longitudinal coordinate and field component at node (I) of the mesh. Binary file names must begin with FNAME 'B_' or 'b_'. 'Binary' will then automatically be set to '.TRUE.'.

```
myMapFile1 SUM
myMapFile2 SUM
myMapFile3
```

(all maps must all have their mesh defined in identical coordinate frame).

 $^{^1}$ FNAME (e.g., solenoid.map) contains the field data. These must be formatted according to the following FORTRAN sequence :

² Sumperimposing (summing) field maps is possible. To do so, pile up file names with 'SUM' following each name but the last one. *e.g.*, in the following example, 3 field maps are read and summed:

CARTEMES

	mid-plane symmetry is assumed		
IC, IL	$IC=1,2$: print the map $IL=1,2[imes 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[\times 10^n], 7$	2*I
BNORM, XN, YN	Field and X-,Y-coordinate normalization coeffs.	3*no dim.	3*E
TITL	Title. Start with "FLIP" to get field map X-flipped.		A80
IX, JY	Number of longitudinal (IX) and transverse (JY) nodes of the map	$\leq 400, \leq 200$	2*I
FNAME ¹	File name		A80
ID, A, B, C [, A', B', C', A'', B'' , etc., if $ID \ge 2$]	Integration boundary. Normally $ID=0$. $ID=-1$: integration in the map begins at entrance boundary defined by $AX+BY+C=0$. $ID=1$: integration in the map is terminated at exit boundary defined by $AX+BY+C=0$. $ID\geq 2$: entrance (A,B,C) and up to $ID-1$ exit $(A',B',C',A'',B'',etc.)$ boundaries	$\geq -1.2*$ no dim., cm [,2*no dim., cm, etc.]	I, 3*E [3*E,etc.]
IORDRE	Degree of interpolation polynomial (see DIPOLE-M)	2, 25 or 4	I
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E

2-D Cartesian uniform mesh magnetic field map

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED'])
IF (BINARY) THEN
READ(NL) (Y(J), J=1, JY)
ELSE
READ(NL,100) (Y(J), J=1, JY)
ENDIF
100 FORMAT(10 F8.2)
DO 1 I=1,IX
IF (BINARY) THEN
READ(NL) X(I), (BMES(I,J), J=1, JY)
ELSE
READ(NL,101) X(I), (BMES(I,J), J=1, JY)
101 FORMAT(10 F8.2)
ENDIF
1 CONTINUE
```

where X(I) and Y(J) are the longitudinal and transverse coordinates and BMES is the Z field component at a node (I,J) of the mesh. For binary files, FNAME must begin with 'B_' or 'b_'.

 $^{^2}$ FNAME (e.g., spes2.map) contains the field data. These must be formatted according to the following FORTRAN sequence :

^{&#}x27;Binary' will then automatically be set to '.TRUE.'



OXY is the coordinate system of the mesh. Integration zone limits may be defined, using $ID \neq 0$: particle coordinates are extrapolated linearly from the entrance face of the map, into the plane A'X + B'Y + C' = 0; after ray-tracing inside the map and terminating on the integration boundary AX + BY + C = 0, coordinates are extrapolated linearly to the exit face of the map.

CAVITE ¹	Accelerating cavity $\Delta W = qV sin(2\pi hf\Delta t + \varphi_s) \text{ and other voltage and frequency laws}.$		
IOPT[.i]	Option. $i=1$ causes info output into <code>zgoubi.CAVITE.Out</code>	0-7	I
If IOPT=0	Element inactive		
X, X X, X	Unused Unused		
If IOPT=1 ²	f_{RF} follows the timing law given by SCALING		
$egin{aligned} \mathcal{L},h\ \hat{V},X \end{aligned}$	Reference closed orbit length; harmonic number R.F. peak voltage; unused	m, no dim. V, unused	2*E 2*E
If IOPT=2	f_{RF} follows $\Delta W_s = q \hat{V} sin \phi_s$		
$\mathcal{L}, h \ \hat{V}, \phi_s$	Reference closed orbit length; harmonic number R.F. peak voltage; synchronous phase	m, no dim. V, rad	2*E 2*E
If IOPT=3	No synchrotron motion : $\Delta W = q \hat{V} sin \phi_s$		
X, X \hat{V}, ϕ_s	Unused ; unused R.F. peak voltage ; synchronous phase	2*unused V, rad	2*E 2*E
If IOPT=6	Read RF frequency and/or phase law from external file, "zgoubi.freqLaw.	ſn".	
\mathcal{L}, E_k \hat{V}, Φ_s	Orbit length and kinetic energy at start of acceleration. R.F. peak voltage; synchronous phase.	m, MeV V, rad	2*E 2*E
If IOPT=7	Quasi- or isochronous acceleration.		
X, E_k \hat{V}, Φ_s	Unused; RF frequency; R.F. peak voltage; synchronous phase.	- , Hz V, rad	2*E 2*E

 $^{^1}$ Use PARTICUL to declare mass and charge. 2 For ramping the R.F. frequency following $B\rho(t)$, use SCALING, with family CAVITE.

CHAMBR Long transverse aperture limitation ¹

IA

0: element inactive

1: (re)definition of the aperture

2: stop testing and reset counters, print

information on stopped particles.

IFORM[.J], C1, C2,

IFORM = 1: rectangular aperture;

1-2[.0-1]

0-2

I[.I], 4*E

I

C3, C4

IFORM = 2: elliptical aperture.

J=0, default : opening is $^2\pm YL=\pm C1,\,\pm ZL=\pm C2,$ centered at $YC=C3,\,ZC=C4.$

J = 1: opening is ², in Y: [C1, C2], in Z: [C3, C4]

¹ Any particle out of limits is stopped.

When used with an optical element defined in polar coordinates (e.g., DIPOLE) YL is the radius and YC stands for the reference radius (normally, $YC \simeq RM$).

CHANGREF Transformation to a new reference frame

"Old Style" (Figure below):

XCE, YCE, ALE Longitudinal and transverse shifts, 2*cm, deg 3*E followed by Z-axis rotation

"New Style" (example below). In an arbitrary order, up to 9 occurrences of :

XS 'val', YS 'val', ZS 'val', XR 'val', YR 'val', ZR 'val'

cm or deg up to 9*(A2,E)



Parameters in the CHANGREF procedure.

Example:

```
Using CHANGREF "New Style
'OBJET'
51.71103865921708
                                       Electron, Ekin=15MeV.
                                          One particle, with
1 1
2. 0. 0.0 0.0 0.0 1. 'R'
                        Y_0=2 cm, other coordinates zero.
1 1 1 1 1 1 1
'MARKER'
          BEG
                                    -> list into zgoubi.plt.
                 .plt
'DRIFT'
                                                10 cm drift.
10.
'CHANGREF'
ZR -6.34165 YS 1.
                           First half Z-rotate, Next Y-shift.
'CHANGREF'
0.1.0.
             Combined function multipole, dipole + quadrupole.
'MULTIPOL'
                                    -> list into zgoubi.plt.
5 10. 2.064995867082342 2. 0. 0. 0. 0. 0. 0. 0. 0.
0 0 5. 1.1 1.00 1.00 1.00 1.00 1.00 1. 1. 1. 1.
 4 .1455 2.2670 -.6395 1.1558 0. 0. 0.
0 0 0 0 0 0 0 0 0 0
.1 step size
1 0.0.0.
'CHANGREF'
YS -1. ZR -6.341
                      First Y-shift back, next half Z-rotate.
'DRIFT'
                                                10 cm drift.
'FAISCEAU'
'END'
```

CIBLE, TARGET Generate a secondary beam following target interaction

M_1, M_2, M_3, Q T_2, θ, β	Target, incident and scattered particle masses; Q of the reaction; incident particle kinetic energy; scattering angle; angle of the target	$5*\frac{MeV}{c^2}$, 2*deg	7*E
NT, NP	Number of samples in T and P coordinates after \emph{CIBLE}		2*I
TS, PS, DT	Sample step sizes; tilt angle	3*mrad	3*E
BORO	New reference rigidity after CIBLE	kG.cm	E



Scheme of the principles of CIBLE (TARGET)

A,T= position, angle of incoming particle 2 in the entrance reference frame P= position of the interaction

B, T = position, angle of the secondary particle in the exit reference frame

 θ = angle between entrance and exit frames

 β = tilt angle of the target

1-2[.0-1]

2*cm or 2*s,

11-16, no.dim,

2*m, no.dim

2*no.dim or 2*MeV

I[.I], 4*E

I, 4*E

I, 4*E

COLLIMA Collimator ¹

IA0: element inactive

0-2 I 1: element active

2: element active and print information on stopped

particles

Physical-space collimation

IFORM[.J], C1, C2, IFORM = 1: rectangular aperture; C3, C4

IFORM = 2: elliptical aperture.

J = 0, default : opening is $\pm YL = \pm C1$, $\pm ZL = \pm C2$,

centered at YC = C3, ZC = C4.

J = 1: opening is, in Y: [C1, C2], in Z: [C3, C4]

Longitudinal collimation

IFORM.J, H_{min} , H_{max} , IFORM = 6 or 7 for horizontal variable resp^{ly} S or Time,

J=1 or 2 for vertical variable resply 1+dp/p, kinetic-E (MeV); V_{min}, V_{max}

horizontal and vertical limits

Phase-space collimation

IFORM, α , β , ϵ/π , N_{σ} IFORM = 11, 14: horizontal collimation; horizontal

ellipse parameters (unused if 14)², emittance, cut-off IFORM = 12, 15: vertical collimation; vertical ellipse parameters (unused if 15)², emittance, cut-off IFORM = 13, 16: longitudinal collimation; to be

implemented

¹ Any particle out of limits is stopped.

² The rejection boundary is the *rms* ellipse matched to the particle distribution.

Integration step

KPOS=1 : element aligned, 2 : misaligned; shifts, tilt (unused if *KPOS*=1)

XPAS

KPOS, XCE, YCE, ALE

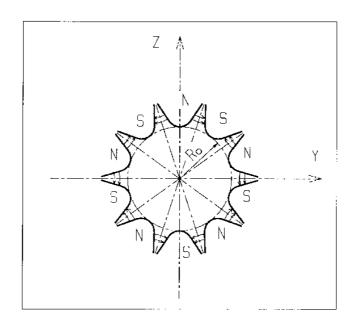
E

I, 3*E

cm

1-2, 2*cm, rad

DECAPOLE	Decapole magnet		
IL	$IL=1,2[imes 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
XL , R_0 , B_0	Length; radius and field at pole tip	2*cm, kG	3*E
X_E, λ_E	Entrance face : Integration zone extent ; fringe field extent ($\lesssim 2R_0$, $\lambda_E=0$ for sharp edge)	2*cm	2*E
NCE , $C_0 - C_5$	NCE = unused C_0-C_5 = Fringe field coefficients such that $G(s)=G_0/(1+\exp P(s))$, with $G_0=B_0/R_0^4$ and $P(s)=\sum_{i=0}^5 C_i(s/\lambda)^i$	unused, 6*no dim.	I, 6*E
X_S, λ_S NCS, $C_0 - C_5$	Exit face : see entrance face	2*cm 0-6, 6*no dim.	2*E I, 6*E



DIPOLE			
	$B_Z = \mathcal{F}B_0 \left(1 + N \left(\frac{R - RM}{RM} \right) + B \left(\frac{R - RM}{RM} \right)^2 + G \left(\frac{R - RM}{RM} \right)^2 \right)$	$\left(\frac{M}{2}\right)^3$	
IL	$IL=1,2[imes 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
AT,RM	Total angular extent of the dipole; reference radius	deg, cm	2*E
$ACENT, B_0, N, B, G$	Azimuth for positioning of EFBs; field and field indices	deg., kG, 3*no dim.	5*E
	ENTRANCE FIELD BOUNDARY		
λ, ξ	Fringe field extent (normally \simeq gap size); unused. Exponential type fringe field $F=1/(1+\exp(P(s)))$ with $P(s)=C_0+C_1(\frac{s}{\lambda})+C_2(\frac{s}{\lambda})^2++C_5(\frac{s}{\lambda})^5$	cm, unused	2*E
NC , $C_0 - C_5$, shift	Unused; C_0 to C_5 : see above; EFB shift	0-6, 6*no dim., cm	I, 7*E
$\omega^+, \theta, R_1, U_1, U_2, R_2$	Azimuth of entrance EFB with respect to ACENT; wedge angle of EFB; radii and linear extents of EFB (use $\mid U_{1,2} \mid = \infty$ when $R_{1,2} = \infty$)	2*deg, 4*cm	6*E
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDARY)		
λ, ξ $NC, C_0 - C_5$, shift	Fringe field parameters	cm, unused 0-6, 6*no dim., cm	2*E 1, 7*E
$\omega^-, \theta, R_1, U_1, U_2, R_2$	Positioning and shape of the exit EFB	2*deg, 4*cm	6*E
	LATERAL FIELD BOUNDARY (See ENTRANCE FIELD BOUNDA	RY)	
λ, ξ $NC, C_0 - C_5$, shift	LATERAL EFB is inhibited if $\xi = 0$	cm, unused 0-6, 6*no dim., cm	2*E 1, 7*E
$\omega^{-}, \theta, R_1, U_1, U_2, R_2,$ $RM3$	Positioning and shape of the EFB	2*deg, 5*cm	7*E
IORDRE, Resol	Degree of interpolation polynomial: 2 = second degree, 9-point grid 25 = second degree, 25-point grid 4 = fourth degree, 25-point grid; resolution of flying mesh is XPAS/Resol	2, 25 or 4; no dim.	I, E
XPAS	Integration step	cm	Е
KPOS	Positioning of the map, normally 2. Two options :	1-2	I
If KPOS = 2 RE, TE, RS, TS	Positioning as follows: Radius and angle of reference, respectively, at entrance and exit of the map.	cm, rad, cm, rad	4*E
If KPOS = 1 <i>DP</i>	Automatic positioning of the map, by means of reference relative momentum	no dim.	E

DIPOLE-M			
	$B_Z = \mathcal{F}B_0 \left(1 + N \left(\frac{R - RM}{RM} \right) + B \left(\frac{R - RM}{RM} \right)^2 + G \left(\frac{R - RM}{RM} \right)^2 \right)$	$\left(\frac{d}{d}\right)^3$	
NFACE, IC, IL	Number of field boundaries $IC = 1, 2$: print field map $IL = 1, 2[\times 10^n]$, 7: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$2-3; 0-2; 0-2[\times 10^n],$	7 3*I
IAMAX, IRMAX	Azimuthal and radial number of nodes of the mesh	$\leq 400, \leq 200$	2*I
B_0, N, B, G	Field and field indices	kG, 3*no dim.	4*E
AT, ACENT, RM, RMIN, RMAX	Mesh parameters: total angle of the map; azimuth for positioning of EFBs; reference radius; minimum and maximum radii	2*deg, 3*cm	5*E
	ENTRANCE FIELD BOUNDARY		
λ, ξ	Fringe field extent (normally \simeq gap size); unused. Exponential type fringe field $F=1/(1+\exp(P(s)))$ with $P(s)=C_0+C_1(\frac{s}{\lambda})+C_2(\frac{s}{\lambda})^2++C_5(\frac{s}{\lambda})^5$	cm, unused	2*E
NC , $C_0 - C_5$, shift	Unused; C_0 to C_5 : see above; EFB shift	0-6, 6*no dim., cm	I, 7*E
$\omega^+, \theta, R_1, U_1, U_2, R_2$	Azimuth of entrance EFB with respect to ACENT; wedge angle of EFB; radii and linear extents of EFB (use $\mid U_{1,2} \mid = \infty$ when $R_{1,2} = \infty$)	2*deg, 4*cm	6*E
	(Note : $\lambda = 0$, $\omega^+ = ACENT$ and $\theta = 0$ for sharp edge)		
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDARY)		
λ, ξ $NC, C_0 - C_5$, shift	Fringe field parameters	cm, unused 0-6, 6*nodim., cm	2*E 1, 7*E
$\omega^-, \theta, R_1, U_1, U_2, R_2$	Positioning and shape of the exit EFB	2*deg, 4*cm	6*E
	(Note : $\lambda = 0$, $\omega^- = -AT + ACENT$ and $\theta = 0$ for sharp edge)		
If NFACE = 3 λ, ξ NC, $C_0 - C_5$, shift $\omega^-, \theta, R_1, U_1, U_2, R_2,$ $RM3$	LATERAL FIELD BOUNDARY (See ENTRANCE FIELD BOUNDA Next 3 records <i>only</i> if <i>NFACE</i> = 3 Fringe field parameters Positioning and shape of the lateral EFB; RM3 is the radial position on azimuth <i>ACENT</i>	cm, (cm) 0-6, 6*no dim., cm 2*deg, 5*cm	2*E I, 7*E 7*E
NBS	Option index for perturbations to the field map	normally 0	I
If $NBS = 0$	Normal value. No other record required		
If $NBS = -2$	The map is modified as follows:		
$R_0, \Delta B/B_0$	B transforms to $B*\left(1+rac{\Delta B}{B_0}rac{R-R_0}{RMAX-RMIN} ight)$	cm, no dim.	2*E
If NBS = -1	the map is modified as follows:		

$\theta_0, \Delta B/B_0$	B transforms to $B*\left(1+rac{\Delta B}{B_0}rac{ heta- heta_0}{AT} ight)$	deg, no dim.	2*E
If NBS ≥ 1	Introduction of NBS shims		
For $I = 1$, NBS	The following 2 records must be repeated NBS times		
$R_1, R_2, \theta_1, \theta_2, \lambda$	Radial and angular limits of the shim ; λ is unused	2*cm, 2*deg, cm	5*E
$\gamma, \alpha, \mu, \beta$	geometrical parameters of the shim	2*deg, 2*no dim.	4*E
IORDRE	Degree of interpolation polynomial: 2 = second degree, 9-point grid 25 = second degree, 25-point grid 4 = fourth degree, 25-point grid	2, 25 or 4	I
XPAS	Integration step	cm	E
KPOS	Positioning of the map, normally 2. Two options :	1-2	I
If KPOS = 2 RE, TE, RS, TS	Positioning as follows: Radius and angle of reference, respectively, at entrance and exit of the map.	cm, rad, cm, rad	4*E
If KPOS = 1 DP	Automatic positioning of the map, by means of reference relative momentum	no dim.	E

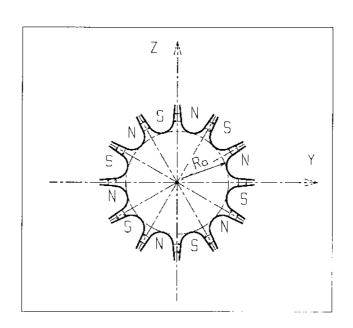
DIPOLES	Dipole magnet N -tuple, polar frame (i) $B_Z = \sum_{i=1}^N B_{Z0,i} \mathcal{F}_i(R,\theta) \left(1 + b_{1_i}(R - RM_i) / RM_i + b_{2_i}(R - RM_i) \right)$ (ii) $B_Z = B_{Z0,i} + \sum_{i=1}^N \mathcal{F}_i(R,\theta) \left(b_{1_i}(R - RM_i) + b_{2_i}(R - RM_i) + b_{2_i}(R - RM_i) + b_{2_i}(R - RM_i) \right)$	$-RM_i)^2/RM_i^2 + \dots)$ $(1)^2 + \dots)$	
IL	$IL=1,2[\times 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
N, AT, RM	Number of magnets in the N -tuple; total angular extent of the dipole; reference radius	no dim., deg, cm	I, 2*E
Repeat N times the follo	wing sequence		
ACN, δRM^{-1} , B_0 , ind, b_i , $(i = 1, ind)$	Positioning of EFBs : azimuth, $R\!M_i=R\!M+\delta R\!M$; field ; number of, and field coefficients	$\begin{array}{l} \deg., \mathrm{cm}, \mathrm{kG},\\ (ind+1)*\mathrm{no} \dim. \end{array}$	3*E, I, ind*E
	ENTRANCE FIELD BOUNDARY		
g_0, κ	Fringe field extent $(g = g_0 (RM/R)^{\kappa})$ Exponential type fringe field $F = 1 / (1 + \exp(P(s)))$ with $P(s) = C_0 + C_1(\frac{s}{g}) + C_2(\frac{s}{g})^2 + + C_5(\frac{s}{g})^5$	cm, no dim.	2*E
NC , C_0-C_5 , shift	Unused ; C_0 to C_5 : see above ; EFB shift	0-6, 6*no dim., cm	I, 7*E
$\omega^+, \theta, R_1, U_1, U_2, R_2$	Azimuth of entrance EFB with respect to ACN ; wedge angle of EFB; radii and linear extents of EFB (use $\mid U_{1,2} \mid = \infty$ when $R_{1,2} = \infty$)	2*deg, 4*cm	6*E
	(Note : $g_0 = 0$, $\omega^+ = ACENT$, $\theta = 0$ and KIRD=0 for sharp edge)		
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDARY)	
g_0, κ $NC, C_0 - C_5$, shift $\omega^-, \theta, R_1, U_1, U_2, R_2$	(Note : $g_0=0,\omega^-=-AT+ACENT,\theta=0$ and KIRD=0 for sharp	cm, no dim. $0 - 6$, $6*$ no dim., cm $2*$ deg, $4*$ cm	2*E 1, 7*E 6*E
	(1vote: $g_0 = 0, \omega = 111 + 122211, v = 0$ and Kirch-o for small	<u>cuge</u>)	
	LATERAL FIELD BOUNDARY to be implemented - following date		
g_0, κ $NC, C_0 - C_5$, shift $\omega^-, \theta, R_1, U_1, U_2, R_2, R$ End of repeat		cm, no dim. 0-6, 6*no dim., cm 2*deg, 5*cm	2*E 1, 7*E 7*E
KIRD[.n], Resol	If KIRD=0: analytical computation of field derivatives; n=0: default, B_Z formula (i) above, n=1: B_Z formula (ii). Resol = 2/4 for 2nd/4th order field derivatives computation If KIRD=2, 25 or 4: numerical interpolation of field derivatives; size of flying interpolation mesh is $XPAS/Resol$ KIRD=2 or 25: second degree, 9- or 25-point grid KIRD=4: fourth degree, 25-point grid	0, 2, 25 or 4; no dim	. I,E
XPAS	Integration step	cm	E
KPOS	Positioning of the magnet, normally 2. Two options :	1-2	I
If KPOS = 2 RE, TE, RS, TS	Positioning as follows: Radius and angle of reference, respectively, at entrance and exit of the magnet	cm, rad, cm, rad	4*E
If KPOS = 1 DP	Automatic positioning of the magnet, by means of		

 $^{^1\,}$ Non-zero $\delta R\!M$ requires KIRD= 2,4 or 25.

DODECAPO

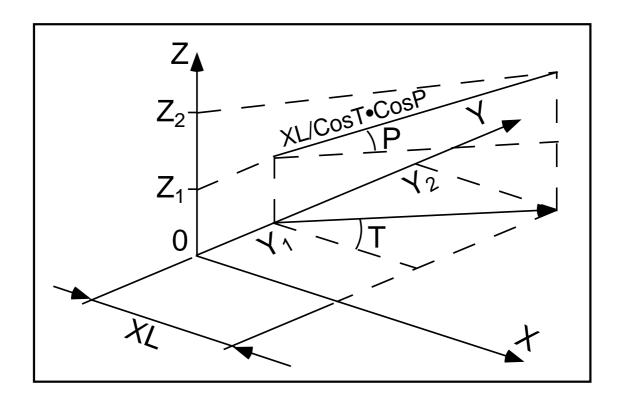
IL	$I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
XL, R_0, B_0	Length; radius and field at pole tip	2*cm, kG	3*E
X_E, λ_E	Entrance face : Integration zone extent ; fringe field extent ($\lesssim 2R_0, \lambda_E = 0$ for sharp edge)	2*cm	2*E
$NCE, C_0 - C_5$	NCE = unused C_0-C_5 = Fringe field coefficients such that $G(s)=G_0/(1+\exp P(s))$, with $G_0=B_0/R_0^5$ and $P(s)=\sum_{i=0}^5 C_i(s/\lambda)^i$	unused, 6*no dim.	I, 6*E
X_S, λ_S $NCS, C_0 - C_5$	Exit face : see entrance face	2*cm 0-6, 6*no dim.	2*E I, 6*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	KPOS=1 : element aligned, 2 : misaligned; shifts, tilt (unused if KPOS=1)	1-2, 2*cm, rad	I, 3*E

Dodecapole magnet



DRIFT, ESL Field free drift space

XL length cm E



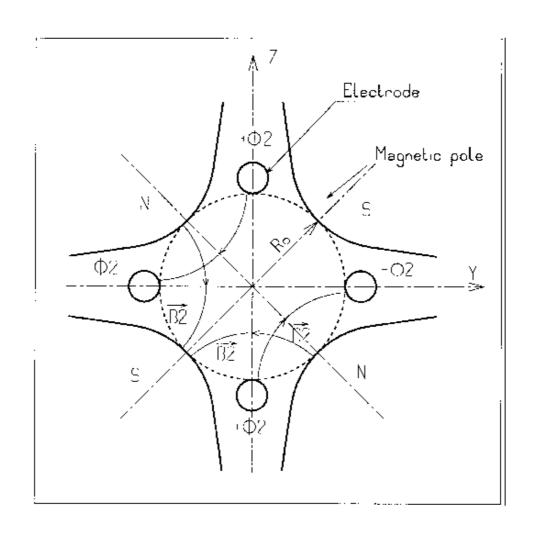
EBMULT ¹

EDIVICEI	Electro-magnetic munipole		
IL	$I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0\text{-}2[\times 10^n], 7$	I
$XL, R_0, E1, E2,, E10$	Electric poles Length of element; radius at pole tip; field at pole tip for dipole, quadrupole,, 20-pole electric components	2*cm, 10*V/m	12*E
$X_E, \lambda_E, E_2,, E_{10}$	Entrance face Integration zone ; fringe field extent : dipole fringe field extent = λ_E ; quadrupole fringe field extent = $\lambda_E * E_2$; 20-pole fringe field extent = $\lambda_E * E_{10}$ (for any component : sharp edge if field extent is zero)	2*cm, 9*no dim.	11*E
$NCE, C_0 - C_5$	same as QUADRUPO	0-6, 6*no dim.	I,6*E
$X_S, \lambda_S, S_2,, S_{10}$ $NCS, C_0 - C_5$	Exit face Integration zone; as for entrance	2*cm, 9*no dim. 0-6, 6*no dim.	11*E I, 6*E
R1, R2, R3,, R10	Skew angles of electric field components	10*rad	10*E
$XL, R_0, B1, B2,, B10$	Magnetic poles Length of element; radius at pole tip; field at pole tip for dipole, quadrupole,, 20-pole magnetic components	2*cm, 10*kG	12*E
$X_E, \lambda_E, E_2,, E_{10}$	Entrance face Integration zone ; fringe field extent : dipole fringe field extent = λ_E ; quadrupole fringe field extent = $\lambda_E * E_2$;	2*cm, 9*no dim.	11*E
	20-pole fringe field extent = $\lambda_E * E_{10}$ (for any component : sharp edge if field extent is zero)		
NCE , $C_0 - C_5$	same as QUADRUPO	0-6, 6*no dim.	I,6*E

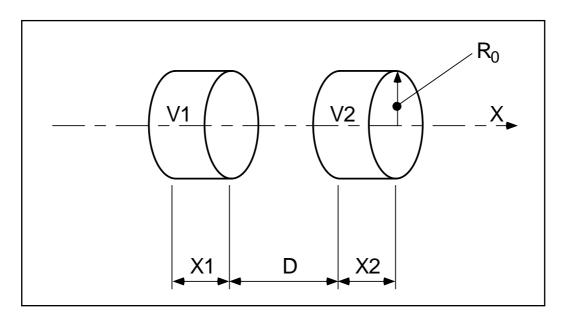
Electro-magnetic multipole

¹ Use *PARTICUL* to declare mass and charge.

$X_S, \lambda_S, S_2,, S_{10}$	Exit face Integration zone ; as for entrance	2*cm, 9*no dim.	11*E
NCS , $C_0 - C_5$		0-6, 6*no dim.	I, 6*E
R1, R2, R3,, R10	Skew angles of magnetic field components	10*rad	10*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E



EL2TUB ¹	Two-tube electrostatic lens		
IL	$I\!L=1,2[\times 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
X_1, D, X_2, R_0	Length of first tube; distance between tubes; length of second tube; inner radius	3*m	4*E
V_1, V_2	Potentials	2*V	2*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E



Two-electrode cylindrical electric lens.

 $^{^{1}\,}$ Use PARTICUL to declare mass and charge.

ELMIR	Electrostatic N-electrode mirror/lens, straight slits

IL	$IL=1,2[imes 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0\text{-}2[\times10^n], 7$	I
N,L1,, LN, D, MT	Number of electrodes; electrode lengths; gap; mode (11/H-mir, 12/V-mir, 21/V-lens, 22/H-lens)	2-7, N*m, m	I, N*E, E, I
V1,, VN	Electrode potentials (normally $V1 = 0$)	N*V	N*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	KPOS=1: element aligned; 2: misaligned; shifts, tilt (unused if $KPOS=1$); 3: automatic positioning, $YCE = pitch$, $ALE = half-deviation$	1-2, 2*cm, rad	I, 3*E



Electrostatic N-electrode mirror/lens, straight slits, in the case N=3, in horizontal mirror mode (MT=11). Possible non-zero entrance quantities YCE, ALE should be specified using CHANGREF, or using KPOS=3 with YCE and ALE=half-deviation matched to the reference trajectory.

ELMIRC	Electrostatic N-electrode mirror/le	ns, circular slits

IL	$I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
R1, R2, AT, D	Radius of first and second slits; total deviation angle; gap	4*m 2*m, rad, m	4*E 4*E
V - VA, VB - V	Potential difference	2*V	2*E
XPAS	Integration step	cm	E
KPOS RE, TE, RS, TS	Normally $KPOS=2$ for positioning; Radius and angle at respectively entrance and exit.	1-2 cm, rad, cm, rad	I 4*E

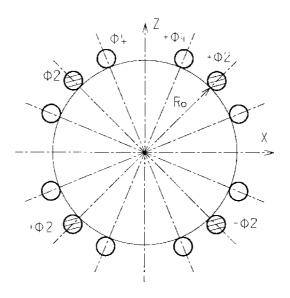


Electrostatic N-electrode mirror/lens, circular slits, in the case N=3, in horizontal mirror mode.

Electric multipole

ELMULT 1

IL	$I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0\text{-}2[\times10^n], 7$	I
$XL, R_0, E1, E2,, E10$	Length of element; radius at pole tip; field at pole tip for dipole, quadrupole,, dodecapole components	2*cm, 10*V/m	12*E
$X_E, \lambda_E, E_2,, E_{10}$	Entrance face Integration zone ; fringe field extent : dipole fringe field extent = λ_E ; quadrupole fringe field extent = $\lambda_E * E_2$; 20-pole fringe field extent = $\lambda_E * E_{10}$ (sharp edge if field extent is zero)	2*cm, 9*no dim.	11*E
$NCE, C_0 - C_5$	same as QUADRUPO	0-6, 6*no dim.	I, 6*E
$X_S, \lambda_S, S_2,, S_{10}$ $NCS, C_0 - C_5$	Exit face Integration zone ; as for entrance	2*cm, 9*no dim. 0-6, 6*no dim.	11*E I, 6*E
R1, R2, R3,, R10	Skew angles of field components	10*rad	10*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E



 $^{^{1}\,}$ Use PARTICUL to declare mass and charge.

ELREVOL 1

	X-axis cylindrical symmetry is assumed		
IC, IL	$I\!C=1,2$: print the map $I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[\times 10^n], 7$	2*I
ENORM, X-NORM	Field and X-coordinate normalization coeff.	2*no dim.	2*E
TITL	Title. Start with "FLIP" to get field map X-flipped.		A80
IX	Number of longitudinal nodes of the map	≤ 400	I
FNAME ²	File name		A80
ID, A, B, C [, A', B', C' , B'' , etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID=0$. $ID=$ -1, 1 or ≥ 2 : as for <i>CARTEMES</i>	≥ -1 , 2*no dim., cm [,2*no dim., cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	Unused	2, 25 or 4	I
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E

1-D uniform mesh electric field map

where X(I) and EX(I) are the longitudinal coordinate and field component at node (I) of the mesh. Binary file names FNAME must begin with 'B_' or 'b_'. 'Binary' will then automatically be set to '.TRUE.'

 $^{^{1}\,}$ Use PARTICUL to declare mass and charge.

 $^{^2}$ FNAME (e.g., e-lens.map) contains the field data. These must be formatted according to the following FORTRAN sequence:

EMMA 2-D Cartesian or cylindrical mesh field map for EMMA FFAG

IL	$IL=1,2[\times 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
BNORM, XN, YN, ZN	Field and X-,Y-,Z-coordinate normalization coefficients	4*no dim.	4*E
TITL	Title. Start with "FLIP" to get field map X-flipped		A80
IX, IY, IZ, MOD[.i]	Number of nodes of the mesh in the X , Y and Z directions, $IZ = 1$ for single 2-D map; MOD : operational and map $FORMAT$ reading mode 1 $MOD \le 19$: Cartesian mesh; $MOD \ge 20$: cylindrical mesh; $.i$, optional, tells the reading $FORMAT$, default is '*'.	$\leq 400, \leq 200,$ $1, \geq 0[.1-9]$	3*I
FNAME 1 $(K = 1, NF)$	Names of the NF files that contain the 2-D maps, ordered from $Z(1)$ to $Z(NF)$. If $MOD=0$: a single map, superimposition of QF and QD ones, is built for tracking. If $MOD=1$: a single map, interpolated from QF[x_F] and QD[x_D] ones, is built for tracking. If $MOD=22$: a single map, superimposition of QF and QD ones, is built for tracking. If $MOD=24$: field at particle is interpolated from a (QF,QD) pair of maps, closest to current (x_F, x_D) value, taken from of set of (QF,QD) pairs registered in FNAME		
$ID, A, B, C \ [, A', B', C', B'', etc., if ID \ge 2]$	Integration boundary. Ineffective when $ID=0$. $ID=-1, 1 \text{ or } \geq 2$: as for <i>CARTEMES</i>	≥ -1 , 2*no dim., cm [,2*no dim., cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	If $IZ = 1$: as in <i>CARTEMES</i> If $IZ \neq 1$: unused	2, 25 or 4	I
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E

 $^{^1}$ FNAME normally contains the field map data. If MOD=24 FNAME(K) contains the names of the QF maps and QD maps, as well as the QF-QD distance attached to each one of these pairs.

ERRORS Injecting errors

(UNDER DEVELOPMENT)

ONF, NBR, SEED [, PRINT] On/off switch (0/1); number of error sets to be injected (i.e., 3*I [,A] ,,,[,]

as well, number of lines following this one); random seed.

Occurence of PRINT will save error series in

zgoubi.ERRORS.out.

The next line depends on the optical element of concern, and is to be one of the following: (only one possibility at the moment, namely MULTIPOL keyword)

N. TYP. AR. UG.

VC, HW, CUTOFF

MULTIPOL[{LBL1 [,LBL2]}], Keyword concerned [optionally, first and/or second label];

TYP= BP: field at pole; AR=A or R: field value is absolute

N=1-10: pole concerned (dipole to 20-pole);

,[,],,,,2*kG, A[,A[,A]],I, A2, A1, A1, 3*E

or relative (to current one); UG=U or G: uniform or Gaussian random law; VC= central value; HW= half-width (case UG=U) or sigma (case UG=G); cut-off value in units of sigma (unused

in uniform case)

Example

'ERRORS' 1 1 123456

MULTIPOL {VKICK} BP A U 0.d0 1.

In this example the various attributes of the error keyword take the following value and meaning: First line:

- ONF = 1, error setting is on, NBR=1, only one line follows (only on set of errors in a single keyword, seed = 123456 second line:
 - MULTIPOL keywords in zgoubi.dat sequence are concerned, only those MULTIPOL featuring "VKICK" as first label,
 - multipole component N=6, i.e., dodecapole component, will be modified, as follows
- BP, A, U, 0.d0, 1., 3: absolute (AR=A) field value (TYP=BP) for that component, will be sorted in a uniform (UG=U) random distribution centered on 0 (VC=0.d0) with half-width 1 kG (HW=1.), CUTOFF=3 here is unused (only used for Gaussian distributions, case UG=G).

FAISCEAU Print particle coordinates

Print particle coordinates at the location where the keyword is introduced in the structure.

FAISCNL Store particle coordinates in file FNAME

FNAME¹ Name of storage file

(e.g., zgoubi.fai, or b_zgoubi.fai for binary storage).

FAISTORE Store coordinates every IP other pass [, at elements with appropriate label]

FNAME 1 Name of storage file (e.g. zgoubi.fai) [; label(s) of the element(s) at the exit [,LABEL(s)] of which the store occurs (10 labels maximum)]. If either FNAME or first LABEL

is 'none' then no storage occurs. Store occurs at all elements if first

LABEL is 'all' or 'ALL'.

IP Store every IP other pass (when using REBELOTE

with $NPASS \ge IP - 1$).

A80

A80, [, 10*A10]

I

¹ Stored data can be read back from FNAME using OBJET, KOBJ = 3.

FFAG	FFAG magnet, N -tuple UNDER DEVELOPMENT $B_Z = \sum_{i=1}^N B_{Z0,i} \mathcal{F}_i(R,\theta) \left(R/R_{M,i} \right)^{K_i}$		
IL	$I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
N, AT, RM	Number of dipoles in the FFAG N -tuple ; total angular extent of the dipole ; reference radius	no dim., deg, cm	I, 2*E
Repeat N times the follow	wing sequence		
ACN , δRM , B_{Z0} , K	Azimuth for dipole positioning ; $R_{M,i} = R\!M + \delta R\!M$; field at $R_{M,i}$; index	deg, cm, kG, no dim.	4*E
	ENTRANCE FIELD BOUNDARY		
g_0 , κ NC , $C_0 - C_5$, shift ω^+ , θ , R_1 , U_1 , U_2 , R_2	Fringe field extent $(g=g_0(RM/R)^\kappa)$ Unused; C_0 to C_5 : fringe field coefficients; EFB shift Azimuth of entrance EFB with respect to ACN ; wedge angle of EFB; radii and linear extents of EFB (use $\mid U_{1,2}\mid =\infty$ when $R_{1,2}=\infty$)	cm, no dim. 0-6, 6*no dim, cm 2*deg, 4*cm	2*E I, 7*E 6*E
	(Note : $g_0 = 0$, $\omega^+ = ACENT$, $\theta = 0$ and KIRD=0 for sharp edge)		
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDARY)	
g_0, κ $NC, C_0 - C_5$, shift $\omega^-, \theta, R_1, U_1, U_2, R_2$	Fringe field parameters, see above	cm, no dim 0-6, 6*no dim, cm 2*deg, 4*cm	2*E 1, 7*E 6*E
	(Note : $g_0 = 0$, $\omega^- = -AT + ACENT$, $\theta = 0$ and KIRD=0 for sharp	edge)	
	LATERAL FIELD BOUNDARY to be implemented - following date	ta not used	
g_0, κ $NC, C_0 - C_5$, shift $\omega^-, \theta, R_1, U_1, U_2, R_2$		cm, no dim 0-6, 6*no dim, cm 2*deg, 4*cm	2*E 1, 7*E 6*E
End of repeat			
KIRD, Resol	If KIRD=0: analytical computation of field derivatives; Resol = 2/4 for 2nd/4th order field derivatives computation If KIRD = 2, 4 or 25: numerical interpolation of field derivatives; size of flying interpolation mesh is XPAS/Resol KIRD=2 or 25: second degree, 9- or 25-point grid KIRD=4: fourth degree, 25-point grid	0, 2, 25 or 4; no dim.	I, E
XPAS	Integration step	cm	Е
KPOS	Positioning of the magnet, normally 2. Two options :	1-2	I
If KPOS = 2 RE, TE, RS, TS	Positioning as follows: Radius and angle of reference, respectively, at entrance and exit of the magnet	cm, rad, cm, rad	4*E
If KPOS = 1 <i>DP</i>	Automatic positioning of the magnet, by means of reference relative momentum	no dim.	Е

FFAG-SPI	Spiral FFAG magnet, N -tuple UNDER DEVELOPMENT $B_Z = \sum_{i=1}^N B_{Z0,i} \mathcal{F}_i(R,\theta) \left(R/R_{M,i}\right)^{K_i}$		
IL	$I\!L=1,2[\times 10^n],~7$: print coordinates along trajectories, fields, etc., into zgoubi.res (1) or zgoubi.plt (2[$\times 10^n$]) or zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
N, AT, RM	Number of dipoles in the FFAG N -tuple ; total angular extent of the dipole ; reference radius.	no dim., deg, cm	I, 2*E
Repeat N times the follo	wing sequence		
ACN , δRM , B_{Z0} , K	Azimuth for dipole positioning ; $R_{M,i}=R\!M+\delta R\!M$; field at $R_{M,i}$; index.	deg, cm, kG, no dim.	4*E
	ENTRANCE FIELD BOUNDARY		
g_0, κ $NC, C_0 - C_5$, shift $\omega^+, \xi, 4$ dummies	Fringe field extent $(g = g_0 (RM/R)^{\kappa})$ Unused; C_0 to C_5 : fringe field coefficients; EFB shift Azimuth of entrance EFB with respect to ACN ; spiral angle; $4 \times$ unused.	cm, no dim. 0-6, 6*no dim, cm 2*deg, 4*unused	2*E I, 7*E 6*E
	EXIT FIELD BOUNDARY (See ENTRANCE FIELD BOUNDARY)	
g_0, κ $NC, C_0 - C_5$, shift $\omega^-, \xi, 4$ dummies	Fringe field parameters, see above	cm, no dim 0-6, 6*no dim, cm 2*deg, 4*unused	2*E 1, 7*E 6*E
	LATERAL FIELD BOUNDARY to be implemented - following date	ta not used	
g_0, κ $NC, C_0 - C_5$, shift $\omega^-, \theta, R_1, U_1, U_2, R_2$	LATERAL FIELD BOUNDARY to be implemented - following date	cm, no dim 0-6, 6*no dim, cm 2*deg, 4*cm	2*E 1, 7*E 6*E
NC , $C_0 - C_5$, shift	LATERAL FIELD BOUNDARY to be implemented - following date	cm, no dim 0-6, 6*no dim, cm	1, 7*E
NC , $C_0 - C_5$, shift ω^- , θ , R_1 , U_1 , U_2 , R_2 End of repeat	LATERAL FIELD BOUNDARY to be implemented - following date and the state of the stat	cm, no dim 0-6, 6*no dim, cm	1, 7*E
NC , $C_0 - C_5$, shift ω^- , θ , R_1 , U_1 , U_2 , R_2 End of repeat		cm, no dim 0-6, 6*no dim, cm	1, 7*E
NC , $C_0 - C_5$, shift ω^- , θ , R_1 , U_1 , U_2 , R_2 End of repeat Integration boundaries - IntLim, ID , A , B , C	next line is optional, starting with string IntLim: Integration boundary. Line has to start with 'IntLim'. $ID = -1$: integration in the magnet begins at entrance boundary defined by A, B, C. $ID = 1$: integration is terminated at exit boundary defined by A', B', C'.	cm, no dim 0-6, 6*no dim, cm 2*deg, 4*cm	1, 7*E 6*E I, 3*E
NC , $C_0 - C_5$, shift ω^- , θ , R_1 , U_1 , U_2 , R_2 End of repeat Integration boundaries = IntLim, ID , A , B , C [, A' , B' , C']	next line is optional, starting with string IntLim: Integration boundary. Line has to start with 'IntLim'. $ID = -1$: integration in the magnet begins at entrance boundary defined by A, B, C. $ID = 1$: integration is terminated at exit boundary defined by A', B', C'. $ID = 2$: both entrance and exit boundaries. If KIRD=0: analytical computation of field derivatives; Resol = $2/4$ for 2 nd/4th order field derivatives computation. If KIRD = 2 , 4 or 2 5: numerical interpolation of field derivatives; size of flying interpolation mesh is $XPAS/Resol$. KIRD=2 or 2 5: second degree, 9- or 2 5-point grid	cm, no dim 0-6, 6*no dim, cm 2*deg, 4*cm -1, 1, 2; deg; cm; deg [; id.]	1, 7*E 6*E I, 3*E [,3*E]

FIN, END End of input data list

Any information in zgoubi.dat following these keywords will be ignored

FIT, FIT2	Fitting procedure	< 20 [nofinal]	I [A 7]
NV [, 'nofinal'] [, 'save' [, FileName]]	NV: Number of physical parameters to be varied; 'nofinal': will avoid final run (default is: final run performed using fitted values, once fit is done); 'save': will save fit variables when fit is completed, either in 'FileName' if specified, or by default in zgoubi.FITVALS.out.	<pre>< 20 [, nofinal] save [string]</pre>	I [, A7] [, A4 [, A80]]
For I = 1, NV	repeat NV times the following sequence		
either:	Number of the element in the atmost are	ZMWI 1 ZMWD	2*I 2*E
IR, IP, XC, DV	Number of the element in the structure; number of the physical parameter in the element; coupling switch (off = 0); variation range (\pm)	\leq MXL ¹ , \leq MXD, \pm MXD.MXD ² , relative	2*I, 2*E
or:			
$IR, IP, XC, [V_{min}, V_{max}]$		\leq MXL, \leq MXD,	2*I, 3*E
NC [, Penalty [,ITER]] ³	Number of constraints [, penalty [, max. numb. of iterations]].	$\leq 20 [, 10^{-n} [, > 0]]$	I [, E [, I]]
For $I = 1$, NC	repeat NC times the following sequence :		
$IC, I, J, IR, V^4, WV,$	IC, I and J define the type of constraint (see table below);	0-5, 3*(>0),	4*I, 2*E,
$NP \ [, \ p_i (i=1, NP)]$	IR: number of the element after which the constraint applies;	current unit,	I, <i>№</i>
	V : value; W : weight (the stronger the lower WV) NP : number of parameters; if $NP \ge 1$, $p_i(i=1,NP)$:	2*no dim., curr. units	
	NP : number of parameters; if $NP \ge 1$, $p_i(i=1,NP)$: parameter values.	cuii. uiits	

 $^{^1\,}$ MXL value is set in include file MXLD . H. $^2\,$ MXD value is set in include file MXLD . H. Data is of the form "integer.iii" with i a 1-digit integer.

³ FIT[2] will stop when the sum of the squared residuals gets < penalty, or when the maximum allowed number of iterations is reached.

⁴ V is in current **zgoubi** units in the case of particle coordinates (cm, mrad). It is in MKSA units (m, rad) in the case of matrix coefficients.

Type of				Parameters defining the constraints					Recommended
constraint	IC	I	J	Constraint	A NP	dditional paravalue(s),			[MC]OBJET, and other comments
σ -matrix	0	1 - 6	1 - 6	$\sigma_{IJ} \ (\sigma_{11} = \beta_Y, \sigma_{21, 12} = \alpha_Y, \text{etc.})$					OBJET/KOBJ=5,6
Periodic parameters (N=1-9 for MATRIX block 1-9))	0.N	1 - 6 7 8 9 10	1 - 6 any any any any	$\sigma_{IJ} (\sigma_{11} = \cos \mu_Y + \alpha_Y \sin \mu_Y, \text{ etc.})$ $Y\text{-tune} = \mu_Y/2\pi$ $Z\text{-tune} = \mu_Z/2\pi$ $\cos(\mu_Y)$ $\cos(\mu_Z)$					OBJET/KOBJ=5.N
First order transport coeffs.	1	$ \begin{array}{c c} 1-6 \\ 7 \\ 8 \end{array} $	$egin{array}{c} 1-6 \ & \mathrm{i} \ & \mathrm{j} \end{array}$	Transport coeff. R_{IJ} $i \neq 8$: YY-determinant; i=8: YZ-det. $j \neq 7$: ZZ-determinant; j=7: ZY-det.					OBJET/KOBJ=5
Second order transport coeffs.	2	1 - 6	11 – 66	Transport coeff. $T_{I,j,k}$ $(j = [J/10], k = J - 10[J/10])$					OBJET/KOBJ=6
Trajectory coordinates (I = particle number; J=1-7 for D,Y,T,Z,P,S,time)	3.1 3.2 3.4	1 - IMAX -1 -2 -3 1 - IMAX 1 - IMAX 1 - IMAX	1-7 $1-7$ $1-7$ $1-7$ $1-7$ $1-7$	$F(J,I) \\ < F(J,i) >_{i=1,IMAX} \\ Sup(F(J,i))_{i=1,IMAX} \\ Dist F(J,I) _{i=I1,I2,d_{1,2}} \\ F(J,I) - FO(J,I) \\ F(J,I) + FO(J,I) \\ F(J,I) - F(J,K) $	3	I_1 $K < IMAX$	I_2	$d_{1,2}$	[MC]OBJET
Ellipse parameters	3.5	1 - IMAX $1 - 6$	1 - 7 $1 - 6$	$(F(J,I) - F(J,K))/F(J,K)$ $\sigma_{IJ} (\sigma_{11} = \beta_Y,$ $\sigma_{12} = \sigma_{21} = \alpha_Y, \text{ etc.})$	1	$K \leq IMAX$			OBJET/KOBJ=8; MCOBJET/KOBJ
Number of particles	5	$ \begin{array}{c c} -1 \\ 1-3 \\ 4-6 \end{array} $	any any any	$N_{survived}/ ext{IMAX} \ N_{in \; \epsilon_{Y,Z,X}}/N_{survived} \ N_{in \; best \; \epsilon_{Y,Z,X,rms}}/N_{survived}$	1	ϵ/π			OBJET MCOBJET MCOBJET
Coordinates and fields, across optical elements	7.1 7.2 7.3	$\begin{vmatrix} 1 - IMAX \\ 1 - IMAX \\ 1 - IMAX \end{vmatrix}$	$egin{array}{c} 1-7 \ 1-7 \ 1-7 \end{array}$	min. (1) or max. (2) of $F(J, I)$ $\max(F(J, I)) - \min(F(J, I))$ $\min(F(J, I)) + \max(F(J, I))$	1	1-2			[MC]OBJET
$(J=1, 2, 3 \text{ for } B_{X, Y, Z})$	7.6 7.7 7.8 7.9	1 - IMAX 1 - IMAX 1 - IMAX 1 - IMAX	1 - 3 $1 - 3$ $1 - 3$ $1 - 3$	min. (1) or max. (2) value of B_J $\max(B_J) - \min(B_J)$ $\min(B_J) + \max(B_J)$ $\int B_J ds$	1	1-2			
Spin	10 10.1	$\begin{vmatrix} 1 - IMAX \\ 1 - IMAX \end{vmatrix}$	1 - 4 $1 - 3$	$ S_{X,Y,Z}(I), \vec{S}(I) S_{X,Y,Z}(I) - SO_{X,Y,Z}(I) $					[MC]OBJET +SPNTRK

• Combining FIT and REBELOTE : An example

In the example below, FIT requests that (i) the particle trajectory with initial coordinates defined by OBJET have identical horizontal coordinates at both ends of the snake (this is achieved by varying Y_0 , T_0 in OBJET), and that (ii) the trajectory across the snake - an helix - be Y-centered along the snake axis.

The way this works:

FIT is executed a first time for $B\rho_{ref}=BORO=7205.1782956$ kG.cm, namely the execution loops between OBJET and FIT until the constraints are best fulfilled. Once this is completed, the execution pointer then goes to the next instruction in the data list, namely 'SPNPRT', this is discussed below, and then points to REBELOTE, which will have the effect of sending it back to the begining of zgoubi.dat data list. However, prior to that, the "1" flag, fourth data in first row in REBELOTE, requests a change of, next line, parameter number 35 in element "OBJET" (that is, the relative regidity of the particle, D). The list of values follows, namely, $\{1.3872739973\ 2.1368296674\ 4.8261190694\ 11.015241321\}$. The change occurs 4 times, according to NRBLT=4, the first data in REBELOTE data list.

Note that, (i) spin data so computed (spin vector components, precession, etc) are stored/stacked in zgoubi.SPNPRT.Out by placing the keyword 'SPNPRT' with label "PRINT", between FIT and REBELOTE; (ii) current updated FIT variables are saved in zgoubi.FITVALS.out_cat for each REBELOTE case, using SYSTEM.

```
Centering 5 helical orbits in the AGS warm helical snake 3-D OPERA map.
                    ! This data list may be copy-pasted and run, as is.
7.2051782956D3
                    ! Reference rigidity of the problem
2
1 1
                    ! A single particle. Initial coordinates :
-2.2 0.0.0.0.1.'0'
                                    ! Yo, To, Zo, Po, So, p/po
 'PARTICUL'
                    ! proton data are necessary for spin tracking
938.27203 1.602176487E-19 1.7928474 0 0
                                            ! M, Q, G factor
4.1
                    ! Initial spin is positionned vertical
0. 0. 1.
 'FAISCEAU'
 'SPNPRT'
'TOSCA'
0 20
      100. 100. 100.
1.e1
HEADER_0 wsnake
801 29 29 12.1
                    ! The map is a 801x29x29 node 3-D mesh
                    ! AGS warm snake 3-D OPERA map
warmSnake.map
0 0 0 0
                                                                This figure shows how, using REBELOTE, the
2
                                                                 helical trajectories at five different momenta
.1
  0. .0 0. 0.
                                                                are moved by the FIT procedure, one after the
                                                                other, from initial off-centered position to final
 'FAISCEAU'
                                                                   centering on the snake axis (at Y=Z=0).
 'FIT'
  save
                    ! Two variables. Save FIT variables (in zgoubi.FITVALS.out).
                       ! Vary initial coordinate Y_0 (horiz. position)
1 30 0 [-3,3]
1 31 0 [-3,3]
                        ! Vary initial coordinate T_0 (horiz. angle)
    1E-2
                    ! Three constraints (penalty 2E-3 requested) :
3.1 1 2 6 0. 1. 0
                       ! Y 0=Y after at exit of the magnet
3.1 1 3 6 0. 1. 0
                        ! T_0=T after at exit of the magnet
7.3 1 2 6 0. 1. 0
                        ! Y_min+Y_max=0 inside the OPERA field map
 'SPNPRT' PRINT
                    ! Stack spin data (in zgoubi.SPNPRT.Out).
                    ! Save zgoubi.FITVALS.out data following from successive REBELOTE.
 'SYSTEM'
1
cat zgoubi.FITVALS.out >> zgoubi.FITVALS.out_cat
 'REBELOTE'
                    ! Will loop on re-doing the FIT for 4 additional particle rigidities
4 0.1 0 1
1
                    ! List of 4 successive values of D in OBJET follows
OBJET 35 1.3872739973 2.1368296674 4.8261190694 11.015241321
 'SYSTEM'
                    ! Save a copy of zgoubi.FITVALS.out_cat and of zgoubi.SPNPRT.Out_cat
2
\cp zgoubi.FITVALS.out_cat zgoubi.FITVALS.out_cat_copy
\cp zgoubi.SPNPRT.Out
                          zgoubi.SPNPRT.Out_copy
 'END'
```

• FIT[2] options : An example

FIT[2] options, "nofinal", "save FileName", "penalty" and "ITER", are all specified in the example below.

```
An example with FIT options
'GETETTVAL'
zgoubi.FITVALS.In
 'MCOBJET'1
57.36635309d3
                   ! reference rigidity
3.1
2 2 2 2 1 1
0. 0. 0. 0. 0. 4.61943880E-01
2.703371 1.859656 1.48563786487e-99
-2.592712 2.421706 1.48563786487e-99 9
0.1.0.
12345 23456 34567
 'PARTICUL'
                                                                                              2
0.51099892 1.60217653e-19 1.15965218076e-3 0.0 0.0
'PICKUPS'
 #StartRing MULT BD2S #EndRing
'DRIFT'
           DRIF
                                                                                           7497
14.38218115
 'MARKER' #SSMid
                                                                                           7498
 'MARKER' #EndRing
                                                                                           7500
'FIT2'
4 save zgoubiFIT.result nofinal ! Variables saved in zgoubiFIT.result when FIT2 done. No final run.
!!! 4 save nofinal ! Would cause variables to be saved in default file zgoubi.FITVALS.out instead.
2 40 0 [-1.e-2,1.e-2]
                                 ! The four variables are Yo, To, Zo, Po in MCOBJET
2 41 0 [-1.e-2,1.e-2]
2 42 0 [-1.e-2,1.e-2]
2 43 0 [-1.e-2,1.e-2]
                              ! penalty=1e-10. Maximum allowed calls to zgoubi is 90.
   1e-10 90
3.1 1 2 7500 0. 1. 0
                              ! The four constraints are : initial Y, T, Z, P of
3.1 1 3 7500 0. 1. 0
                              ! particle #1 equal to its final Y, T, Z, P.
3.1 1 4 7500 0. 1. 0
3.1 1 5 7500 0. 1. 0
```

FOCALE	Particle coordinates and horizontal beam size at distance XL		
XL	Distance from the location of the keyword	cm	E
FOCALEZ	Particle coordinates and vertical beam size at distance XL		
XL	Distance from the location of the leaveyand	am	Е
Λ L	Distance from the location of the keyword	cm	E

GASCAT	Gas scattering		
KGA	Off/On switch	0, 1	I
AI, DEN	Atomic number; density		2*E

GETFITVAL Get values of variables as saved from former FIT[2] run

FNAME Name of storage file. Zgoubi will proceed silently if not found.

A

< 120, 1-5

HISTO

1-D histogram

 $J, X_{\min}, X_{\max}, NBK, NH$

J = type of coordinate to be histogrammed; the following are available:

• current coordinates:

1(D), 2(Y), 3(T), 4(Z), 5(P), 6(S),

• initial coordinates :

 $11(D_0)$, $12(Y_0)$, $13(T_0)$, $14(Z_0)$, $15(P_0)$, $16(S_0)$,

spin :

 $21(S_X)$, $22(S_Y)$, $23(S_Z)$, 24(< S >);

 X_{\min} , X_{\max} = limits of the histogram, in units of the coordinate of concern; NBK = number of channels; NH = number of the histogram (for independence of histograms of the same coordinate)

NBL, KAR, NORM, TYP Number of lines (= vertical amplitude); alphanumeric character; normalization if NORM = 1, otherwise NORM = 0; TYP = 'P': primary particles are histogrammed, or 'S': secondary, or Q: all particles - for use with MCDESINT

1-24, 2* I, 2*E, 2*I current units,

normally 10-40, I, A1, I, A1 char., 1-2, P-S-Q

IMAGE Localization and size of horizontal waist

IMAGES Localization and size of horizontal waists

For each momentum group, as classified by means of OBJET, KOBJ = 1, 2 or 4

IMAGESZ Localization and size of vertical waists

For each momentum group, as classified by means of OBJET, KOBJ = 1, 2 or 4

IMAGEZ Localization and size of vertical waist

MAP2D 2-D Cartesian uniform mesh field map - arbitrary magnetic field

IC, IL	$IC=1,2$: print the field map $IL=1,2[imes 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[\times 10^n], 7$	2*I
BNORM, XN,YN	Field and X-,Y-coordinate normalization coeffs.	3*no dim.	3*E
TITL	Title. Start with "FLIP" to get field map X-flipped.		A80
IX,JY	Number of longitudinal and horizontal-transverse nodes of the mesh (the Z elevation is arbitrary)	$\leq 400, \leq 200$	2*I
FNAME ¹	File name		A80
ID, A, B, C [, A', B', C', B'' , etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID=0$. $ID=$ -1, 1 or ≥ 2 : as for <i>CARTEMES</i>	≥ -1 , 2*no dim., cm [,2*no dim., cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	Degree of polynomial interpolation, 2nd or 4th order.	2, 4	I
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E

These must be formatted according to the following FORTRAN read sequence (normally compatible with TOSCA code OUTPUTS - details and possible updates are to be found in the source file 'fmapw.f'):

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD')
DO 1 J = 1, JY
DO 1 I = 1, IX
IF (BINARY) THEN
READ(NL) Y(J), Z(1), X(I), BY(I,J), BZ(I,J), BX(I,J)
ELSE
READ(NL,100) Y(J), Z(1), X(I), BY(I,J), BZ(I,J), BX(I,J)
100 FORMAT (1X, 6E11.4)
ENDIF
1 CONTINUE
```

where X(I), Y(J) are the longitudinal, horizontal coordinates in the at nodes (I,J) of the mesh, Z(1) is the vertical elevation of the map, and BX, BY, BZ are the components of the field.

For binary files, FNAME must begin with 'B_' or 'b_'~; a logical flag 'Binary' will then automatically be set to '.TRUE.'

 $^{^{1}\} FNAME\ (e.g.,\ magnet.map)$ contains the field map data.

MAP2D-E 2-D Cartesian uniform mesh field map - arbitrary electric field

IC, IL	$I\!C=1,2$: print the field map $I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[\times 10^n], 7$	2*I
ENORM, X-,Y-NORM	Field and X-,Y-coordinate normalization coeffs.	2*no dim.	2*E
TITL	Title. Start with "FLIP" to get field map X-flipped.		A80
IX,JY	Number of longitudinal and horizontal-transverse nodes of the mesh (the Z elevation is arbitrary)	$\leq 400, \leq 200$	2*I
FNAME ¹	File name		A80
ID, A, B, C [, A', B', C', B'' , etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID=0$. $ID=$ -1, 1 or ≥ 2 : as for <i>CARTEMES</i>	≥ -1 , 2*no dim., cm [,2*no dim., cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	Degree of polynomial interpolation, 2nd or 4th order.	2, 4	I
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E

```
\begin{aligned} & \text{OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD')} \\ & \text{DO 1 J = 1, JY} \\ & \text{DO 1 I = 1, IX} \\ & \text{IF (BINARY) THEN} \\ & \text{READ(NL) Y(J), Z(1), X(I), EY(I,J), EZ(I,J), EX(I,J)} \\ & \text{ELSE} \\ & \text{READ(NL,100) Y(J), Z(1), X(I), EY(I,J), EZ(I,J), EX(I,J)} \\ & \text{100} & \text{FORMAT (1X, 6E11.4)} \\ & \text{ENDIF} \\ & \text{1} & \text{CONTINUE} \end{aligned}
```

where X(I), Y(J) are the longitudinal, horizontal coordinates in the at nodes (I,J) of the mesh, Z(1) is the vertical elevation of the map, and EX, EY, EZ are the components of the field.

For binary files, FNAME must begin with 'B_' or 'b_'"; a logical flag 'Binary' will then automatically be set to '.TRUE.'

 $^{^1}$ FNAME (e.g., ''mirror.map'') contains the field map data. These must be formatted according to the following FORTRAN read sequence - details and possible updates are to be found in the source file 'fmapw.f':

MARKER Marker

Just a marker. No data

'.plt' as a second LABEL will cause storage of current coordinates into zgoubi.plt

MATRIX

Calculation of transfer coefficients, periodic parameters

IORD, IFOC [, PRINT] [, coupled] Options:

0-2, 0-1 or > 10 2*I [,A]

IORD = 0: Same effect as FAISCEAU

IORD = 1 (normally using OBJET, KOBJ = 5): First order transfer matrix; beam matrix, phase advance if using OBJET, KOBJ = 5.1; if IFOC > 10: periodic beam matrix, tune numbers IORD = 2 (normally using OBJET, KOBJ = 6): First order transfer

matrix $[R_{ij}]$, second order array $[T_{ijk}]$ and higher order transfer coefficients ; if $\mathit{IFOC} > 10$: periodic parameters,

IFOC = 0: matrix at actual location,

reference \equiv particle # 1

IFOC = 1: matrix at the closest first order horizontal focus,

 $reference \equiv particle \ \# \ 1$

IFOC = 10 + NPER: same as IFOC = 0, and also calculates

the Twiss parameters, tune numbers, etc.

(assuming that the DATA file describes one period of a

NPER-period structure).

"PRINT" will cause printout to zgoubi.MATRIX.out file.

"coupled", in the periodic case, will cause use of coupled formalism.

[INFO,] 2 $M2$, $M3$, $ au 2$ 3	[Switch,]; masses of the two decay products;	[-,] $2*MeV/c^2$, s	[A4,] 3*E
	COM lifetime of particle 2		
I1, I2, I3	Seeds for random number generators	$3* \simeq 10^6$	3*I



Particle 1 decays into 2 and 3; **zgoubi** then calculates trajectory of 2, while 3 is discarded. θ and ϕ are the scattering angles of particle 2 relative to the direction of the incoming particle 1. They transform to T_2 and P_2 in Zgoubi frame.

 $^{^{1}\,}$ MCDESINT must be preceded by PARTICUL, for the definition of the mass and lifetime of the incoming particle M1.

Presence of 'INFO' will cause more info on decay kinematics parameters to be printed zgoubi.res at each decay.

 $^{^3}$ τ 2 can be left blank, in which case the lifetime of particle 2 is set to zero (it decays immediately, which from a practical point of view means that it is not tracked).

5*E

3*I

no dim.

 $3*{\simeq}~10^6$

MCOBJET

 N_0, C_0, C_1, C_2, C_3

IR1, IR2, IR3

BORO	Reference rigidity	kG.cm	E
KOBJ	Type of support of the random distribution $KOBJ=1$: window $KOBJ=2$: grid $KOBJ=3$: phase-space ellipses	1-3	I
IMAX	Number of particles to be generated	$\leq 10^4$	
$KY, KT, KZ, KP, KX, KD^{-1}$	Type of probability density	6*(1-3)	6*I
$Y_0, T_0, Z_0, P_0, X_0, D_0$	Mean value of coordinates ($D_0 = B\rho/BORO$)	m, rad, m, rad, m, no dim.	6*E
If KOBJ = 1	In a window		
$\delta Y, \delta T, \delta Z, \delta P, \\ \delta X, \delta D$	Distribution widths, depending on KY , KT etc. ¹	m, rad, m, rad, m, no dim.	6*E
$N_{\delta Y},N_{\delta T},N_{\delta Z},N_{\delta P},\ N_{\delta X},N_{\delta D}$	Sorting cut-offs (used only for Gaussian density)	units of σ_Y , σ_T , etc.	6*E

Monte-Carlo generation of a 6-D object

Parameters involved in calculation of P(D)

Random sequence seeds

KD can take the values

¹ Let x = Y, T, Z, P or X. KY, KT, KZ, KP and KX can take the values

^{1:} uniform, $p(x) = 1/2\delta x$ if $-\delta x \le x \le \delta x$

^{2 :} Gaussian, $p(x) = \exp(-x^2/2\delta x^2)/\delta x \sqrt{2\pi}$

^{3 :} parabolic, $p(x) = 3(1-x^2/\delta x^2)/4\delta x$ if $-\delta x \le x \le \delta x$

^{1:} uniform, $p(D) = 1/2\delta D$ if $-\delta D \le x \le \delta D$

^{2:} exponential, $p(D) = \text{No } \exp(C_0 + C_1 l + C_2 l^2 + C_3 l^3)$ if $-\delta D \le x \le \delta D$

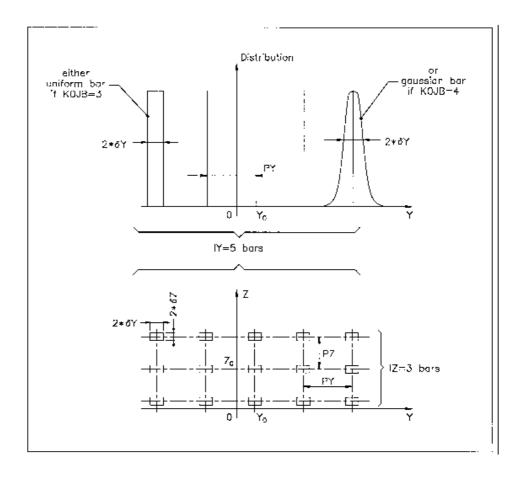
^{3:} kinematic, $D = \delta D * T$

If $KOBJ = 2$	On a grid		
IY, IT, IZ, IP, IX, ID	Number of bars of the grid		6*I
PY, PT, PZ, PP, PX, PD	Distances between bars	m, rad, m rad, m, no dim.	6*E
$\begin{array}{l} \delta Y, \delta T, \delta Z, \delta P, \\ \delta X, \delta D \end{array}$	Width of the bars (\pm) if uniform, Sigma value if Gaussian distribution	ibidem	6*E
$N_{\delta Y}, N_{\delta T}, N_{\delta Z}, N_{\delta P}, \\ N_{\delta X}, N_{\delta D}$	Sorting cut-offs (used only for Gaussian density)	units of σ_Y , σ_T , etc.	6*E
N_0, C_0, C_1, C_2, C_3	Parameters involved in calculation of $P(D)$	no dim.	5*E
IR1, IR2, IR3	Random sequence seeds	$3*\simeq 10^6$	3*I
If $KOBJ = 3$	On a phase-space ellipse ¹		
$(\alpha_Y, \beta_Y, \varepsilon_Y/\pi, N_{\sigma_{\epsilon_Y}})$ [, $N'_{\sigma_{\epsilon_Y}}$ if $N_{\sigma_{\epsilon_Y}} < 0$] ²	Ellipse parameters and emittance, Y-T phase-space; cut-off	no dim., m/rad, m, units of $\sigma(\varepsilon_Y)$	4*E [,E]
$(\alpha_Z, \beta_Z, \varepsilon_Z/\pi, N_{\sigma_{\epsilon_Z}})$ [, $N'_{\sigma_{\epsilon_Z}}$ if $N_{\sigma_{\epsilon_Z}} < 0$] ²	Ellipse parameters and emittance, Z-P phase-space; cut-off	no dim., m/rad, m, units of $\sigma(\varepsilon_Z)$	4*E [,E]
$\begin{array}{l} \alpha_X,\beta_X,\varepsilon_X/\pi,N_{\sigma_{\epsilon_X}}\\ [,N_{\sigma_{\epsilon_X}}' \text{ if }N_{\sigma_{\epsilon_X}}<0]^{2} \end{array}$	Ellipse parameters and emittance, X-D phase-space; cut-off	no dim., m/rad, m, units of $\sigma(\varepsilon_X)$	4*E [,E]
IR1, IR2, IR3	Random sequence seeds	$3*\simeq 10^6$	3*I

tier
$$\frac{1+\sigma_Y^2}{\beta_Y^2}Y^2+2\alpha_YYT+\beta_YT^2=\frac{\varepsilon_Y}{\pi}$$
 if $N_{\sigma_{\epsilon_Y}}>0$, or, if $N_{\sigma_{\epsilon_Y}}<0$ sorting within the ring

$$[\,|N_{\sigma_{\epsilon_Y}}|,N'_{\sigma_{\epsilon_Y}}\,]$$

 $^{^1\,}$ Similar possibilities, non-random, are offered with OBJET, KOBJ=8 (p. 240) $^2\,$ Works with Gaussian density type only : sorting within the ellipse fron-



A scheme of input parameters to MCOBJET when KOBJ= 2.

Top : Possible distributions of the ${\cal Y}$ coordinate

Bottom : A 2-D grid in (Y, Z) space.

IL	$IL=1,2[\times 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
$XL, R_0, B1, B2,, B10,$	Length of element; radius at pole tip; field at pole tip for dipole, quadrupole,, dodecapole components	2*cm,10*kG	12*E
$X_E, \lambda_E, E_2,, E_{10}$	Entrance face Integration zone ; fringe field extent : dipole fringe field extent = λ_E ; quadrupole fringe field extent = $\lambda_E * E_2$; 20-pole fringe field extent = $\lambda_E * E_{10}$ (sharp edge if field extent is zero)	2*cm,9*no dim.	11*E
NCE , $C_0 - C_5$	same as QUADRUPO	0-6, 6*no dim.	I, 6*E
$X_S, \lambda_S, S_2,, S_{10}$ $NCS, C_0 - C_5$	Exit face Integration zone; as for entrance	2*cm, 9*no dim. 0-6, 6*no dim.	11*E I, 6*E
R1, R2, R3,, R10	Skew angles of field components	10*rad	10*E
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	$KPOS=1$: element aligned, 2: misaligned; shifts, tilt (unused if $KPOS=1$) for $QUADRUPO$. $KPOS=3$: effective only if $B1 \neq 0$: entrance and exit frames are shifted by YCE and tilted wrt . the magnet by an angle of \bullet either ALE if $ALE\neq 0$ \bullet or $2 Arcsin(B1 XL / 2BORO)$ if $ALE=0$	1-3, 2*cm, rad	I, 3*E

OBJET

Generation of an object

	•		
BORO	Reference rigidity	kG.cm	E
KOBJ[.K2]	Option index [.More options]	1-6	I
If $KOBJ = 1[.1]$	[Non-] Symmetric object		
IY, IT, IZ, IP, IS, ID	Ray-Tracing assumes mid-plane symmetry Total number of points in $\pm Y$, $\pm T$, $\pm Z$, $\pm P$ [$+Z$, $+P$ with KOBJ = 1.1], $\pm S$. and $\pm D$ coordinates ($IY \leq 20,,ID \leq 20$)	$\text{IY*IT*IZ*IP*IS*ID} \leq 10^4$	6*1
PY, PT, PZ, PP, PS, PD	Step size in Y , T , Z , P , S and momentum ($PD = \delta B \rho / BORO$)	2(cm,mrad), cm, no dim.	6*E
YR, TR, ZR, PR, SR, DR	Reference ($DR = B\rho/BORO$)	2(cm,mrad), cm, no dim.	6*E
If $KOBJ = 2[.1]$	All the initial coordinates must be entered explicitly		
IMAX, IDMAX	total number of particles; number of distinct momenta (if $IDMAX > 1$, group particles of same momentum)	$IMAX \le 10^4$	2*I
For $I = 1$, $IMAX$	Repeat <i>IMAX</i> times the following line		
Y, T, Z, P, S, D, LET	Coordinates and tagging of the $IMAX$ particles; $If KOBJ = 2.1$ input units are different:	2(cm,mrad), cm, no dim., 2(m,rad), m, no dim.,	6*E, A1
IEX(I=1,IMAX)	IMAX times 1 or -9. If $IEX(I) = 1$ trajectory I is ray-traced, it is not if $IEX(I) = -9$.	1 or -9	IMAXI
If KOBJ=3[.N, N=00 - 3]	Reads coordinates from a storage file N=00 (default): [b_]zgoubi.fai like data file FORMAT N=01: read FORMAT is ``READ(NL,*) Y,T,Z,P,S,DP'' N=02: read FORMAT is ``READ(NL,*) X,Y,Z,PX,PY,PZ'' N=03: read FORMAT is ``READ(NL,*) DP,Y,T,Z,P,S,TIM	E,MASS,CHARGE''	
IT1, IT2, ITStep	Read particles numbered IT1 to IT2, step ITStep (For more than 10 ⁴ particles stored in <i>FNAME</i> , use ' <i>REBELOTE</i> ')	$\geq 1, \geq IT1, \geq 1$	3*I
IP1, IP2, IPStep	Read particles that belong in pass numbered IP1 to IP2, step IPStep	$\geq 1, \geq IP1, \geq 1$	3*I
YF, TF, ZF, PF, SF, DF, TF, TAG	Scaling factor. TAG-ing letter: no effect if $TAG=$ '*', otherwise only particles with TAG=LET are retained.	7*no.dim, char.	7*E, A1
YR, TR, ZR, PR, SR, DR, TR	Reference. Given the previous line of data, all coordinate C is transformed to C*CF+CR	2(cm, mrad), cm, no dim.,μs	7*E
InitC	0: set $new \ \vec{R}_0 = \vec{R}_0 \ as \ read$, $new \ \vec{R} = \vec{R} \ as \ read$; 1: set $new \ \vec{R}_0 = \vec{R} \ as \ read$, $new \ \vec{R} = \vec{R} \ as \ read$; 2: save $\vec{R} \ as \ read$ in $new \ \vec{R}_0$, set $new \ \vec{R} = \vec{R}_0 \ as \ read$.	0-1	I
FNAME	File name (<i>e.g.</i> , zgoubi.fai) (N in KOBJ=3.N determines storage FORMAT)		A80

240

If KOBJ = 5[.N, $N \ge 1$]	Generation of 11 particles, or 11*N if $I \geq 2$ (for use with <i>MAT</i>	RIX, IORD = 1)	
PY, PT, PZ, PP, PS, PD	Step sizes in Y, T, Z, P, S and D	2(cm,mrad), cm, no dim.	6*E
YR, TR, ZR, PR, SR, DR	Reference trajectory ($DR = B\rho/BORO$)	2(cm,mrad), cm, no dim.	6*E
If $KOBJ = 5.1$ $\alpha_Y, \beta_Y, \alpha_Z, \beta_Z, \alpha_S, \beta_S,$ D_Y, D_Y', D_Z, D_Z'	additional data line : Initial beam ellipse parameters ¹	2(no dim.,m), ?, ?, 2(m,rad)	6*E, 4*E
$ \iiint .mine If KOBJ = 5.1 $	N, $N \ge 2$ i = 1 to 98 (if, resp ^{ly} , $N \ge 2$) additional data lines :		
====== If KOBJ = 5.N, NN=2-99 ¿¿¿¿¿¿; .r499 YR, TR, ZR	i=1 to 98 (if, resp ^{ly} , NN=02 to 99) additional data lines : 2, PR (=6R) cDR ajectory # i ($DR = B\rho/BORO$)	2(cm,mrad), cm, no dim.	6*E
If $KOBJ = 6$	Generation of 61 particles (for use with $MATRIX$, $IORD = 2$)		
PY, PT, PZ, PP, PS, PD	Step sizes in Y, T, Z, P, S and D	2(cm,mrad), cm, no dim.	6*E
YR, TR, ZR, PR, SR, DR	Reference trajectory ; $DR = B\rho/BORO$	2(cm,mrad), cm, no dim.	6*E
If $KOBJ = 7$	Object with kinematics		
IY, IT, IZ, IP, IS, ID	Number of points in $\pm Y$, $\pm T$, $\pm Z$, $\pm P$, $\pm S$; ID is not used	$\mathit{IY*IT*IZ*IP*IS*ID} \leq 10^4$	6*I
PY, PT, PZ, PP, PS, PD	Step sizes in Y , T , Z , P and S ; PD = kinematic coefficient, such that $D(T) = DR + PD * T$	2 (cm,mrad), cm, mrad $^{-1}$	6*E
YR, TR, ZR, PR, SR, DR	Reference ($DR = B\rho/BORO$)	2(cm,mrad), cm, no dim.	6*E
If $KOBJ = 8$	Generation of phase-space coordinates on ellipses 2		
IY, IZ, IS	Number of samples in each 2-D phase-space; if zero the central value (below) is assigned	$\begin{split} 0 &\leq IY, IZ, IS \leq IMAX, \\ 1 &\leq IY * IZ * IS \leq IMAX \end{split}$	3*I
$Y_0, T_0, Z_0, P_0, S_0, D_0$	Central values ($D_0 = B\rho/BORO$)	m, rad, m, rad, m, no dim.	6*E
$ \alpha_Y, \beta_Y, \varepsilon_Y/\pi $ $ \alpha_Z, \beta_Z, \varepsilon_Z/\pi $ $ \alpha_S, \beta_S, \varepsilon_S/\pi $	ellipse parameters and emittances	no dim., m, m no dim., m, m no dim., m, m	3*E 3*E 3*E

 $^{^1~}$ They can be transported by using MATRIX $^2~$ Similar possibilities, random, are offered with MCOBJET, KOBJ=3 (p. 236)

• OBJET, KOBJ=3 recovering from a crash: An example

The job below, a 9 million turn tracking in RHIC, crashed at turn # 2,217,299. It can be read from the storage file b_zgoubi.fai (or infered as well from the *OBJET* and *CAVITE* data), that the reference (synchronous, theoretical) rigidity at the previously saved turn (turn# 2,217,298, the closest integer multiple of 67) was $B\rho_{\rm ref}=272.519214209$ T.m (magnet scaling coefficient under *SCALING*, right column below), which is $B\rho_{\rm ref}/BORO=3.111758007$ (as used in *SCALING*, CAVITE data, right column), with BORO=87.5772517 T.m the initial rigidity (25.33 GeV), top of left column.

The right column shows how these informations are transposed to the new tracking run based on *OBJET*, *KOBJ=3*, which allows resuming tracking from that last saved turn #2,217,298.

This run recovers from the crash, starting with particle, magnet and cavity data as found at turn number 2,217,299.

```
OBJET
This 9,000,000-turn job crashed at turn number 2,217,299.
                                                                       87.5772517e3
87.5772517e3
                                                                       1 8 1
                                                                                                  ! Will look for stored turn in
                ! Declare 8 particles, all
                                                                       2217290 2217299 1
                                                                       2217290 2217299 1 ! range (2217298 is concerned).
1. 1. 1. 0. 1. 0. '*' ! Zero factor to 'S' for correct
8 1
                ! on a 21mu_m, norm. vertical invariant.
             2.58575455E-01 -1.73487148E-01 0.1. 'o' 1.82840458E-01 1.21643409E-01 0.1. 'o'
0.
       0.
                                                                       0. 0. 0. 0. 0. 0. 0.
                                                                                                 ! path length/RF phase at CAVITE.
0.
       Ω
             1.58331802E-17
                                3.45516907E-01
                                                 0.1.'0'
       0.
0.
                                                                                        ! The storage file is used to recover
                                                                       b zgoubi.fai
             -1.82840458E-01
                               3.66991287E-01
                                                                                        ! particle coordinates at pass # 2217299.
            -2.58575455E-01
                               1.73487148E-01
0.
       0.
                                                 0.1. 'o'
                                                                       'PARTICIIL'
0.
       0.
            -1.82840458E-01 -1.21643409E-01
                                                 0.1.'0'
                                                                       9.382720300E+02 1.602176487E-19 1.792847400E+00 0.0.
       0.
0.
            -4.74995405E-17 -3.45516907E-01
                                                 0.1.'0'
                                                                        'SPNTRK
             1.82840458E-01 -3.66991287E-01
0.
       0.
                                                 0.1.'0'
-1 1 1 1 1 1 1 1 1 ! on/off switches. Particle 1 selected.
                                                                       'FAISCEAU'
'PARTICUL'
                    Particle data needed for spin tracking.
9.382720300E+02 1.602176487E-19 1.792847400 0. 0.
                                                                       'FAISTORE'
'SPNTRK'
                                                                       b_zgoubi_rest.fai
                                                                                            SNK1
                   ! All initial spins vertical.
                                                                       67
'FAISCEAU'
                                                                        'SCALING
'FAISTORE'
                   ! Storage location in sequence is at SNK1,
b_zgoubi.fai SNK1 ! the first of the two helicoidal snakes.
                                                                       BEND
                   ! Storage (at pass 1 and) every 67 passes.
'SCALING'
                                                                       272.519214209
1 5
                   ! 5 families of magnets ramped.
                   ! Magnet fields strictly follow cavity kick : ! (i) NT=-1 can be used, and (ii) CAVITE does
BEND
                                                                       MULTIPOL HKIC VKIC
-1
87.5772517
                   ! not need be declared under SCALING.
                                                                       0.
MULTIPOL HKIC VKIC
                                                                       MULTIPOL OUAD
-1
0.
                   ! Zero field in HKIC and VKIC magnet families.
                                                                       272.519214209
MULTIPOL QUAD
                                                                       MULTIPOL SEXT
87.5772517
                                                                       272.519214209
MULTIPOL SEXT
                                                                       MULTIPOL MULT
-1
87.5772517
                                                                       272.519214209
MULTIPOL MULT
                                                                       CAVITE
87.5772517
                                                                                      3.07555022085
                                                                                      6782702
 'OPTIONS'
                                                                       'OPTIONS'
WRITE OFF
'MARKER'
           MARK
                      RHICSSTART
                                                                       WRITE OFF
'MARKER'
           MARK
                      CLOCK6down
----- RHIC ring, from CLOCK6 to CLOCK6 ------
                                                                       'MARKER'
                                                                                 SNK1down
                                                                                            ! RHIC start changed to SNK1
'MARKER'
           MARK
                      CLOCK6up
                                                                         ---- RHIC ring, from snake 1 to snake 1 -
'MARKER'
           MARK
                      RHIC$END
                                                                       'MARKER'
                                                                                              ERHLX
'CAVITE'
          accelerating cavity
                                                                                    SNK1up
                                                                       'MARKER'
                                                                       'SPINR'
                                                                                   SNK1
                                                                                              OSNKE
3833.8456
             120.00 circumf., H
        2.61799387799
50e3
                                                                       +45. 180.
                                                                                                  ! snkAxis, spin angle
'REBELOTE'
                                                                       'CAVITE'
                                                                                                  ! accelerating cavity
8999999
          0.4 99
                      ! Repeat optical sequence 8999999 times.
                                                                       3833.8456
                                                                                     120.00
                                                                       50e3
                                                                               2.61799387799
                                                                       'REBELOTE'
                                                                       6782700
                                                                                 0.4 99
```

'END'

OBJETA	Object from Monte-Carlo simulation of decay reaction		
	$M1+M2\longrightarrow M3+M4$ and $M4\longrightarrow M5+M6$		
BORO	Reference rigidity	kG.cm	E
IBODY, KOBJ	Body to be tracked : $M3$ ($IBODY=1$), $M5$ ($IBODY=2$) $M6$ ($IBODY=3$) ; type of distribution for Y_0 and Z_0 : uniform ($KOBJ=1$) or Gaussian ($KOBJ=2$)	1-3,1-2	2*I
IMAX	Number of particles to be generated (use 'REBELOTE' for more)	$\leq 10^4$	I
M_1-M_6	Rest masses of the bodies	$6*GeV/c^2$	6*E
T_1	Kinetic energy of incident body	GeV	E
Y_0, T_0, Z_0, P_0, D_0	Only those particles in the range $Y_0 - \delta Y \le Y \le Y_0 + \delta Y$	2(cm,mrad), no dim.	5*E
	$D_0 - \delta D \le D \le D_0 + \delta D$ will be retained		
$\delta Y, \delta T, \delta Z, \delta P, \delta D$		2(cm,mrad), no dim.	5*E
XL	Half length of object : $-XL \le X_0 \le XL$ (uniform random distribution)	cm	Е
IR1, IR2	Random sequence seeds	$2*\simeq 0^6$	2*I

OCTUPOLE	Octupole magnet		
IL	$I\!L=1,2[\times 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
XL, R_0, B_0	Length; radius and field at pole tip of the element	2*cm, kG	3*E
X_E, λ_E	Entrance face : Integration zone ; Fringe field extent ($\lambda_E=0$ for sharp edge)	2*cm	2*E
NCE , $C_0 - C_5$	NCE = unused C_0-C_5 = fringe field coefficients such that : $G(s)=G_0/(1+\exp\ P(s))$, with $G_0=B_0/R_0^3$ and $P(s)=\sum_{i=0}^5 C_i(s/\lambda)^i$	any, 6*no dim.	I, 6*E
V	Exit face:	2*	2*E
X_S, λ_S	Parameters for the exit fringe field; see entrance	2*cm	2*E
NCS , $C_0 - C_5$		0-6, 6*no dim.	I, 6*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E



Octupole magnet

OPTICS Write out optical functions

IOPT, label [, IMP or 'PRINT'] [coupled]]

IOPT = 0/1: Off/On. Transport the beam matrix;

0-1, string, 0-1

I, A, I

'PRINT'] [, coupled]] 'label' : Can be 'all', 'ALL', or existing 'LABEL_1(NOEL)';

IMP = 1, or presence of 'PRINT', will cause storage of optical

functions in zgoubi.OPTICS.out;

optical function computation is in coupled hypothesis if specified, uncoupled otherwise.

Example

The following will cause a print of optical functions in zgoubi.res at all elements of the zgoubi.dat sequence, as well as their print out in zgoubi.OPTICS.out:

'OPTICS'

1 all PRINT

OPTIONS Global options

IOPT, NBOP IOPT = 0/1: Off/On. NBOP: total number of options. $0-1, \ge 0$ 2*I

NBOP lines should follow. Possible choices:

WRITE, ± 1 -1 inhibites (most of) write statements to zgoubi.res 'WRITE', ± 1 A,I

ORDRE Taylor expansions order

IO $\mbox{Taylor expansions of } \vec{R} \mbox{ and } \vec{u} \mbox{ up to } \vec{u}^{(IO)}$ $\mbox{(default is } IO=4 \mbox{)}$

2-5

I

PARTICUL Particle characteristics

 M, Q, G, τ, X Mass; charge; gyromagnetic factor; COM life-time; unused MeV/ c^2 , C, no dim., s 5*E

If M is of the form $\{M1\ M2\}$, then when masses are assigned to particles from a previously defined object, the first half of the particles are given the mass M1, and the second half are given the mass M2.

If Q is zero, the reference charge is left unchanged.

NOTE : Only the parameters of concern need their value be specified (for instance M, Q when electric lenses are used); others can be set to zero.

PICKUPS Bunch centroid path; orbit

Summation of particles coordinates at pickups may be printed out in zgoubi.PICKUP.out.

Pickup contents are zeroed at start of each pass, in multi-turn mode.

N 0: inactive

 ≥ 1 : number of LABELs at which beam centroid is computed ≥ 0 I

A list of N keywords' labels follows

LABEL1 [,LABEL2, [...]] The N labels at which beam data are to be computed/recorded.

N string(s)

N*A10

In case some "LABELi" in this list actually misses in zgoubi.dat optical sequence, then it is peacefully ignored.

Example

A trick:

```
'PICKUPS'

1
none labelA labelB ...
```

This is a possible way to inhibit an earlier use of *PICKUPS* with "labelA, labelB, …" keyword list. It is sufficient (and necessary) for that, that no keyword in zgoubi.dat data list have "none" as its first *LABEL*.

PLOTDATA Intermediate output for the PLOTDATA graphic software

To be documented.

POISSON

IC, IL	$IC=1,2$: print the field map $IL=1,2[\times 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	0-2; 0-2[$\times 10^n$], 7	2*I
BNORM, XN,YN	Field and X-,Y-coordinate normalization coeffs.	3*no dim.	3*E
TITL	Title. Start with "FLIP" to get field map X-flipped		A80
IX, IY	Number of longitudinal and transverse nodes of the uniform mesh	$\leq 400, \leq 200$	2*I
FNAME ¹	File name		A80
ID, A, B, C [, A', B', C', B'' , etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID=0$. $ID=$ -1, 1 or ≥ 2 : as for <i>CARTEMES</i>	≥ -1 , 2*no dim., cm [,2*no dim., cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	Degree of interpolation polynomial as for <i>DIPOLE-M</i>	2, 25 or 4	I
XPAS	Integration step	cm	Е
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E

Read magnetic field data from POISSON output

```
I = 0

11 CONTINUE

I = I+1

READ(LUN,101,ERR=99,END=10) K, K, K, R, X(I), R, R, B(I)

101 FORMAT(I1, I3, I4, E15.6, 2F11.5, 2F12.3)

GOTO II

10 CONTINUE
```

where X(I) is the longitudinal coordinate, and B(I) is the Z component of the field at a node (I) of the mesh. K's and R's are variables appearing in the *POISSON* output file outpoi.lis, not used here.

 $^{^1}$ FNAME (e.g., ''outpoi.lis'') contains the field map data. These must be formatted according to the following FORTRAN read sequence - details and possible updates are to be found in the source file 'fmapw.f':

POLARMES	2-D polar mesh magnetic field map mid-plane symmetry is assumed		
IC, IL	$IC=1,2$: print the map $IL=1,2[imes 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[\times 10^n], 7$	2*I
BNORM, AN,RN	Field and A-,R-coordinate normalization coeffs.	3*no dim.	3*E
TITL	Title. Start with "FLIP" to get field map X-flipped		A80
IA, JR	Number of angular and radial nodes of the mesh	$\leq 400, \leq 200$	2*I
FNAME ¹	File name		A80
ID, A, B, C [, A', B', C', B'' , etc., if $ID \ge 2$]	Integration boundary. Ineffective when $ID=0$. $ID=$ -1, 1 or ≥ 2 : as for <i>CARTEMES</i>	≥ -1 , 2*no dim., cm [,2*no dim., cm, etc.]	I,3*E [,3*E,etc.]
IORDRE	Degree of interpolation polynomial (see <i>DIPOLE-M</i>)	2, 25 or 4	I
XPAS	Integration step	cm	Е
KPOS If $KPOS = 2$ RE, TE, RS, TS If $KPOS = 1$	as for DIPOLE-M. Normally 2.	1-2	I
		cm, rad, cm, rad	4*E
DP		no dim.	E

```
OPEN (UNIT = NL, FILE = FNAME, STATUS = 'OLD' [,FORM='UNFORMATTED']) IF (BINARY) THEN READ(NL) (Y(J), J=1, JY) ELSE READ(NL,100) (Y(J), J=1, JY) ENDIF 100 FORMAT(10 F8.2) DO 1 I = 1,IX IF (BINARY) THEN READ (NL) X(I), (BMES(I,J), J=1, JY) ELSE READ(NL,101) X(I), (BMES(I,J), J=1, JY) 101 FORMAT(10 F8.1) ENDIF 1 CONTINUE
```

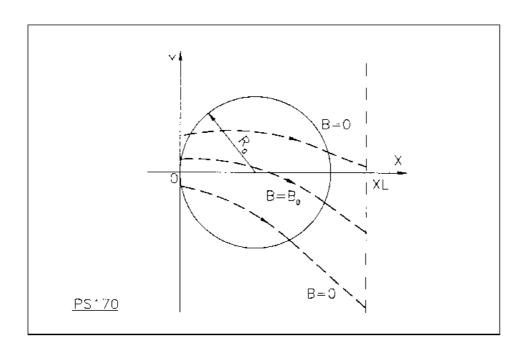
where X(I) and Y(J) are the longitudinal and transverse coordinates and BMES is the Z field component at a node (I,J) of the mesh. For binary files, FNAME must begin with 'B_' or 'b_'. 'Binary' will then automatically be set to '.TRUE.'

 $^{^1}$ FNAME (e.g., spes2.map) contains the field data. These must be formatted according to the following FORTRAN read sequence - details and possible updates are to be found in the source file 'fmapw.f':

PS170

IL	$I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
XL, R_0, B_0	Length of the element, radius of the circular dipole, field	2*cm, kG	3*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E

Simulation of a round shape dipole magnet



Scheme of the PS170 magnet simulation.

YCE, ALE

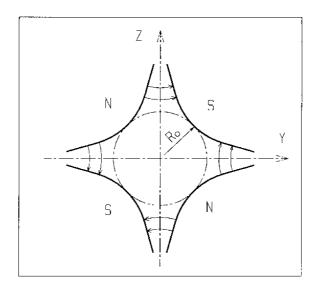
QUADISEX	Sharp edge magnetic multipoles $B_Z\mid_{Z=0}=B_0\left(1+\frac{N}{R_0}Y+\frac{B}{R_0^2}Y^2+\frac{G}{R_0^3}Y^3\right)$		
IL	$I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0\text{-}2[\times10^n], 7$	I
XL, R_0, B_0	Length of the element; normalization distance; field	2*cm, kG	3*E
N,EB1,EB2,EG1,EG2	Coefficients for the calculation of B. if $Y>0$: $B=EB1$ and $G=EG1$; if $Y<0$: $B=EB2$ and $G=EG2$.	5*no dim.	5*E
XPAS	Integration step	cm	E
KPOS, XCE,	KPOS=1: element aligned, 2: misaligned;	1-2, 2*cm, rad	I, 3*E

shifts, tilt (unused if *KPOS*=1)

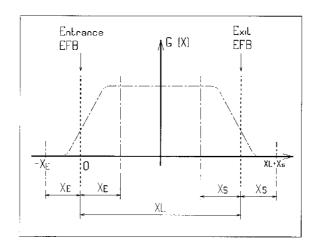
QUADRUPO

Q 01-1-1-1-1	Canal appear amigus		
IL	$I\!L=1,2[\times 10^n],~7: \mbox{print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).}$	$0\text{-}2[\times 10^n], 7$	I
XL , R_0 , B_0	Length; radius and field at pole tip	2*cm, kG	3*E
X_E, λ_E	Entrance face : Integration zone extent ; fringe field extent ($\simeq 2R_0$, $\lambda_E=0$ for sharp edge)	2*cm	2*E
$NCE, C_0 - C_5$	NCE = unused C_0-C_5 = Fringe field coefficients such that $G(s)=G_0/(1+\exp P(s))$, with $G_0=B_0/R_0$ and $P(s)=\sum_{i=0}^5 C_i(s/\lambda)^i$	any, 6*no dim.	I, 6*E
X_S, λ_S $NCS, C_0 - C_5$	Exit face See entrance face	2*cm 0-6, 6*no dim.	2*E I, 6*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E

Quadrupole magnet



Quadrupole magnet



Scheme of the elements QUADRUPO, SEXTUPOL, OCTUPOLE, DECAPOLE, DODECAPO and MULTIPOL

(OX) is the longitudinal axis of the reference frame (0, X, Y, Z) of **zgoubi**. The length of the element is XL, but trajectories are calculated from $-X_E$ to $XL + X_S$, by means of automatic prior and further X_E and X_S translations.

REBELOTE 'Do it again'

NPASS, KWRIT, K[.n], [IOPT],

[, Label1 [, Label2]]

NPASS: Number of runs; KWRIT = 1.1 (resp. 0.0) switches (inhibits) FORTRAN WRITEs to .res and to screen;

arbitrary; 0-1; 3*I 0, 99; [1[.any]] 2A10 0-1; 0, 22, 99 2A10

(inhibits) FORTRAN WRITEs to .res and to screen;

K option:

K = 0: initial conditions (coordinates and spins) are generated following the regular functioning of object definitions. If random generators are used (e.g. in MCOBJET) their seeds will not be reset.

K=99: coordinates at end of previous pass are used as initial coordinates for the next pass; idem for spin components.

K = 99.1: Label 1 is expected, subsequent passes will start from

element with Label1 down to REBELOTE and so forth;

K = 99.2: Label 1 and Label 2 are expected; last pass (# NPASS+1)

will end at element with Label2 whereupon execution will jump to the keyword

next to REBELOTE and will be carried out down to 'END'.

IOPT is optional:

IOPT = 1: will change the value of *NPRM* different parameters in one or a series of optical elements, using the data list in the next line.

If $IOPT = 1^{1}$

NPRM,

Number of parameters to be changed at each of the NPASS passes.

Ι

NPRM lines with the following sequence (tells parameters concerned, and for each, its successive values):

LMNT, PRM, NV*Val

LMNT: keyword number in zgoubi.dat sequence;

-, -, NV*dim ²

2*I, NV*E

PRM: parameter number under that keyword (similar nomenclature to FIT[2], see page 221); then follow the NPASS parameter values.

¹ IOPT=1 is compatible with use of the FIT[2] procedure: e.g., allows successive FITs in a single zgoubi run, with successive sets of optical parameter values.

V is in current zgoubi units in the case of particle coordinates (cm, mrad). It is in MKSA units (m, rad) in the case of matrix coefficients.

• Using **REBELOTE**: An example.

In this example of an energy-recovery electron recirculator based on FFAG arcs, the arguments in the keyword *AUTOREF* and *CAVITE* are changed 20 times by *REBELOTE*, over the 21-pass recirculation process [63]. The role of *AUTOREF* is to mimic a spreader-recombiner, *i.e.*, re-centering the beam on the design FFAG orbit at the start of each one of the 11 accelerated and 10 decelerated ring turns. The RF voltage in *CAVITE* is set positive (accelerating, from 7.944 GeV to 21.16 GeV) during the first 11 passes through the optical structure, and negative (decerating, from 21.16 to 7.944 GeV) over the remaining 10 passes. The voltage value at each pass is adjusted (for an energy of 1.322 GeV per turn on average) so to compensate the energy lost by synchrotron radiation in the arcs.

```
eRHIC ENERGY RECOVERY LINAC RECIRCULATOR WITH FFAG ARCS.
'MCOBJET'
57.36635309d3
                  reference rigidity (kG.cm)
2000
             5.059706E-3 0. 0. 0. 4.619439E-01 'o'
123456 234567 345678
0.51099892 1.60217653e-19 1.15965218076e-3 0.0 0.0
   srLoss
MULTIPOL
  123456
 'SCALING'
MULTIPOL
-1
57.36635309 57.36635309
  'MARKER' ARC#S_1
 'OPTIONS'
WRITE OFF
'MARKER'
'DRIFT'
           DRIF
14.547181
 'MULTIPOL' RBEN
11
                  BD2
```

```
'MULTIPOL' RBEN
                                                                                                          13
14.547181
                      MARK
   'MARKER'
                                          CELLEND
                                                                                                          15
 6*138-1 additional such FD cells, simulating a 6 arc
  6*138-1 additional such to cells, commence energy recovery ring, 138 cells per arc.
    OPTIONS'
                                                                                                      5821
 WRITE ON
                                                                                                      5822
 zgoubi.fai
 1
'FAISCEAU'
1.322e9 1.57079632679
   'AUTOREF'
                                                                                                      5825
       -5.168354E-01 4.169759E+00 5.38813280E-01
 20 0.1 99 1
4
AUTOREF 11 -4.7493E-01 -4.1290E-01 -3.3292E-01 -2.3684E-01
-1.26268E-01 -2.59705E-03 ... (a list of 20 values)
AUTOREF 12 3.34619E-00 2.58215E+00 1.87157E+00 1.20916
5.90197E-01 1.05897E-02 ... (a list of 20 values)
AUTOREF 13 .615682680 .692552080 .769421480 .84629088
.923160280 1.00002970 ... (a list of 20 values)
CAVITE 20 1.337399e9 1.33934e9 1.34012e9 1.34018e9
... (15 more voltage values) ... -1.30660e9 -1.309577e9
'SRPRNT' 5828
```

• Combining REBELOTE and FIT : An example is given page 223.

RESET Reset counters and flags

Resets counters involved in CHAMBR, COLLIMA, HISTO and INTEG procedures.

Switches off CHAMBR, MCDESINT, SCALING and SPNTRK options.

IOPT, NFAM IOPT = 0 (inactive) or 1 (active); 0-1; 1-9 2*I

NFAM = number of families to be scaled

For NF=1, NFAM: repeat *NFAM* times the following sequence:

NAMEF [, Lbl [, Lbl]] Name of family (i.e., keyword of concern) [, up to 2 labels] A10 [,A10[,A10]]

NT > 0: number of timings ; -2, -1 or 1-10 I

NT = -1: field scaling factor updated by *CAVITE*;

NT = -2: RF law in \overrightarrow{CAVITE} is read from external data file.

SCL(I), I = 1, NT Scaling values (a single one, normally 1, if NT = -1). relative NT*E

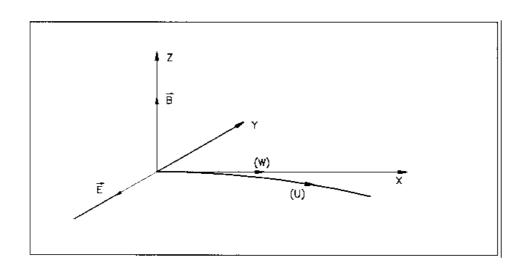
TIM(I), I = 1, NT Corresponding timings, in units of turns (1 if NT = -1). turn number NT*I

SEPARA ¹ Wien Filter - analytical simulation

IA, XL, E, B, IA = 0: element inactive 0-2, m, I, 3*E IA = 1: horizontal separation V/m, T

IA = 2: vertical separation;

Length of the separator; electric field; magnetic field.

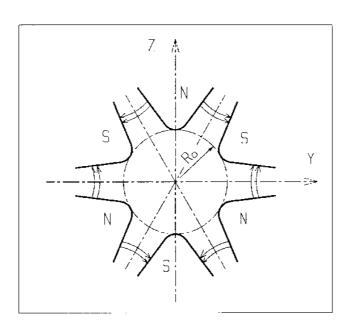


Horizontal separation between a wanted particle, (W), and an unwanted particle, (U). (W) undergoes a linear motion while (U) undergoes a cycloidal motion.

 $^{^{1}}$ SEPARA must be preceded by PARTICUL for the definition of mass and charge of the particles.

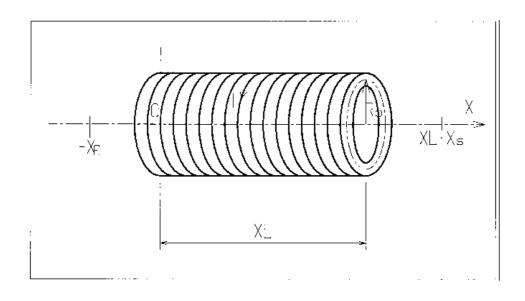
SEXQUAD	Sharp edge magnetic multipole $B_Z\mid_{Z=0}=B_0\left(rac{N}{R_0}Y+rac{B}{R_0^2}Y^2+rac{G}{R_0^3}Y^3 ight)$		
IL	$IL=1,2[\times 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
XL, R_0, B_0	Length of the element; normalization distance; field	2*cm, kG	3*E
N, EB1, EB2, EG1, EG2	Coefficients for the calculation of B. if $Y>0$: $B=EB1$ and $G=EG1$; if $Y<0$: $B=EB2$ and $G=EG2$.	5*no dim.	5*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E

SEXTUPOL	Sextupole Magnet		
IL	$IL=1,2[imes 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
XL , R_0 , B_0	Length; radius and field at pole tip of the element	2*cm, kG	3*E
X_E, λ_E	Entrance face : Integration zone ; fringe field extent ($\lambda_E=0$ for sharp edge)	2*cm	2*E
$NCE, C_0 - C_5$	NCE = unused C_0-C_5 = Fringe field coefficients such that $G(s)=G_0/(1+\exp P(s)),$ with $G_0=B_0/R_0^2$ and $P(s)=\sum_{i=0}^5 C_i(s/\lambda)^i$	any, 6* no dim.	I, 6*E
	Exit face :		
X_S, λ_S	Parameters for the exit fringe field; see entrance	2*cm	2*E
NCS , $C_0 - C_5$		0-6, 6*no dim.	I, 6*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E



Sextupole magnet

SOLENOID	Solenoid		
IL	$IL=1,2[\times 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
XL, R_0, B_0	Length ; radius ; asymptotic field (= $\mu_0 NI/XL$)	2*cm, kG	3*E
X_E, X_S	Entrance and exit integration zones	2*cm	2*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E



SPINR	Spin rotation		
IOPT	Option	0-2	I
If IOPT=0	Element inactive		
X, X	Unused	2*unused	2*E
If IOPT=1	Axis and spin precession angle values.		
ϕ_Z, μ	Angle (in (X,Y) plane) between the X-axis and the spin precession axis; spin precession angle around that axis.	deg, deg	2*E
If IOPT=2	Given the spin precession direction in the horizontal plane, the spin	_	
	angle follows a function of the Lorentz factor : $\mu(\gamma) = \left(\frac{B}{B_0}\right)^2*\left(\frac{B}{B_0}\right)^2$	$\left(C_0 + \frac{C_1}{\gamma} + \frac{C_2}{\gamma^2} + \frac{C_2}{\gamma$	$\frac{C_3}{\gamma^3}$
$\phi_Z, B, B_0, C_0, C_1, C_2, C_3$	Angle (in (X,Y) plane) between the X-axis and the spin precession axis; six coefficients that define the spin precession around that axis.	deg.; 6*no dim	7*E

SPNPRNL Store spin coordinates in file FNAME

FNAME ¹ Name of storage file (e.g., zgoubi.spn)

A80

I

SPNSTORE Store spin coordinates every IP other pass

FNAME 1 Name of storage file (e.g., zgoubi.spn) [; label(s) of the element(s) A80 [,LABEL(s)] 2 at the exit of which the store occurs (10 labels maximum)]. [, 10*A10]

IP Store every IP other pass (when using REBELOTE

with $NPASS \ge IP - 1$).

SPNPRT [PRINT] Print spin coordinates

Print spin coordinates in zgoubi.res, at the location where this keyword is introduced in the structure.

The first label, 'PRINT', is optional, if it appears, then local data are stored in the file zgoubi.SPNPRT.Out. That file is open at the first occurence of SPNPRT and left open until **zgoubi** execution is completed.

¹ FNAME = 'none' will inhibit printing.

² If first *LABEL* = 'none' then printing will be inhibited.

SPNTRK ¹	Spin tracking		
KSO	$KSO=0$: spin tracking [switched] off 2 ; $KSO=-1$: spin tracking resumes. Otherwise: as stated below.	-1 or 0 or 1-3 0r 4[.1] or 5	I
If KSO = 1 – 3	KSO = 1 (respectively 2, 3): all particles have their spin automatically set to $(1,0,0)$, longitudinal [respectively $(0,1,0)$, horizontal and $(0,0,1)$, vertical]		
If KSO = 4	Repeat <i>IMAX</i> times (corresponding to the <i>IMAX</i> particles in 'OBJET') the following sequence :		
S_X,S_Y,S_Z	X, Y and Z initial components of the initial spin.	3*no dim.	3*E
If KSO = 4.1			
S_X, S_Y, S_Z	X,Y and Z components of the initial spins. These will be assigned to all particles.	3*no dim.	3*E
If KSO = 5	Random distribution in a cone (see figure) Enter the following two sequences:		
$TO, PO, A, \delta A$	Angles of average polarization : $A = \text{angle of the cone}$; $\delta A = \text{standard deviation}$ of distribution around A	4*rad	4*E
IR	Random sequence seed	$\lesssim 10^6$	I

 $^{^{1}}$ SPNTRK must be preceded by PARTICUL for the definition of G and mass. 2 Spin tracking can be switched off at any location in zgoubi.dat data list using KSO=0, and further away resumed using KSO=-1.

SRLOSS	Synchrotron radiation energy loss		
KSR[.i]	On/off switch ; $i=1$ for info output into <code>zgoubi.SRLOSS.Out</code>	$0 \ or \ 1[.1]$	2*I
STR1, STR2	Options : $STR1 = 'ALL'$ or 'all' or a particular KEYWORD; $STR2 = 'scale'$ will scale fields with energy loss.		2*A
Option, seed	Option: 0 / no effect, 1 / SR causes dp only, 2 / SR causes dp and angle kick (not installed).	$1-3, > 10^5$	2*I

SRPRNT Print SR loss statistics into zgoubi.res

SYNRAD	Synchrotron radiation spectral-angular densities		
KSR	Switch 0: inhibit SR calculations 1: start 2: stop	0-2	I
If $KSR = 0$			
D1, D2, D3	Dummies		3*E
If $KSR = 1$			
X0, Y0, Z0	Observer position in frame of magnet next to SYNRAD	3*m	3*E
If KSR = 2			
ν_1, ν_2, N	Frequency range and sampling	2*eV, no dim.	2*E, I

SYSTEM System call

NCMD The number of calls to follow.

 ≥ 0

I

NCMD lines follow, one command per line.

• SYSTEM: An example (an additional example can be found page 223)

The first occurence of the command (top region in the data list below) allows establishing links from remote folders to the current one (the one in which **zgoubi** is presently run). These folders happen to contain files appearing in the *SCALING* command, as well as OPERA field maps of the siberian snakes used in subsequent *TOSCA* commands.

The second occurence of the command (bottom region in the data list below) allows saving zgoubi.res output file as resulting from the **zgoubi** run, under a different name.

```
AGS, polarized protons. 2 snakes. t = 145 ms. 
'GETFITVAL' fitVals.data 
'OBJET' LBL_OBJfit 
7069.3668040036146
5
.01 .01 .01 .01 0. .0001
0. 0. 0. 0. 0. 1.
'FAISCEAU'
'SYSTEM'
Ln -sf /rap/lattice_tools/zgoubi/AgsZgoubiModel/snakeFieldMaps/TOSC3D/Csnk3D ln -sf /rap/lattice_tools/zgoubi/AgsZgoubiModel/snakeFieldMaps/TOSC3D/Wsnk3D 'SCALING' LBL_SCLfit
AGSMM *AF *BF *CF !# of params 2Bchanged. dB0 (FIT#3) dB1 (FIT#4) dB2 -1 3 13 3E-20 14 -1.473595E-03 15 8.01942
-1 3
1.000000000 ! (FIT #6)
AGSMM *AD *BD *CD !# of params 2Bchanged. dB0 (FIT#9) dB1 (FIT#10) -1 3 13 9E-20 14 -1.011857
                                                              dB1 (FIT#10) dB2
14 -1.011857E-03 15 -1.70597
1.000000 ! (FIT#12)
AGSQUAD QH_* !# of params 2Bchanged. (FIT#15)
-1 1 15 0.0
1.000000
                           !# of params 2Bchanged.
AGSQUAD QV_* QP_*
1.000000
MULTIPOL QJUMP_*
7.06936680E+00
MULTIPOL SXH_*
7.06936680E+00
MULTIPOL SXV_*
1 AGSMM MM_F08CD MM_F09BF MM_G02BF MM_G03CD MM_G16AD MM_G17CF ! blw1 / G9 bump -1 1 22 -.0762e-99 ! Amp. (FIT #31)
1.0
AGSMM MM_H04CD MM_H05AF MM_H18CF MM_H19BD MM_I12BD MM_I13CF ! blw1 / H11 bump
MULTIPOL COH1
 /Csnk3D/Hlx68.2 Sol42.3/CHREF + dipolCORR.scal
MULTIPOL COV1
MULTIPOL COH2
 /Csnk3D/Hlx68.2_Sol42.3/CHREF_+_dipolCORR.scal
MULTIPOL COV2
1.10
./Csnk3D/Hlx68.2_Sol42.3/CHREF_+_dipolCORR.scal
1 7
MULTIPOL WOH1
1.10
 /Csnk3D/Hlx68.2_Sol42.3/CHREF_+_dipolCORR.scal_51.8_0.0
MULTIPOL WOV1
 /Csnk3D/Hlx68.2_Sol42.3/CHREF_+_dipolCORR.scal_51.8_0.0
MULTIPOL WOH2
./Csnk3D/Hlx68.2_Sol42.3/CHREF_+_dipolCORR.scal_51.8_0.0
MULTIPOL WOV2
1.10 ./Csnk3D/Hlx68.2_Sol42.3/CHREF_+_dipolCORR.scal_51.8_0.0
CHANGREF WSNKE
 /Csnk3D/Hlx68.2_Sol42.3/CHREF_+_dipolCORR.scal_51.8_0.0
CHANGREF WSNKO
 ./Csnk3D/Hlx68.2_Sol42.3/CHREF_+_dipolCORR.scal_51.8_0.0
CHANGREF CSNKE
1.12
CHANGREF CSNKO
./Csnk3D/Hlx68.2_Sol42.3/CHREF_+_dipolCORR.scal 1 1 1 2
```

```
'MARKER' #Start
 'OPTIONS'
1 1 ! options
WRITE OFF
'AGSMM' MM_A01BF
 3 0 0 0.00000E+00 1.00000E+00 1.00000E+00 1.0
3 0 0 0.00000E+00 1.00000E+00 1.00000E+00 1.0
2.1 1 0. 1 0.
0. 0.10.00 4.0 0.800 0.00 0.00 0.00 0.00 0.0 0. 0. 0. 0.
4 1455 2.2670 -.6395 1.1558 0. 0. 0.
0. 10.00 4.0 0.800 0.00 0.00 0.00 0.00 0.0 0. 0. 0.
4 1455 2.2670 -.6395 1.1558 0. 0. 0.
0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.
3.0 Dip MM_AOIBF
4 0. 0. 0. 0. 0. 0. 0.
 [.....]
'TOSCA'
0 0
1.e-3 100. 100. 100.
HEADER_4 csnake
281 29 29 15.2 .682 .423
./Csnk3D/Hlx68.2_sol42.3/b_table_for_Helix_3T.tab
  ./Csnk3D/Hlx68.2 Sol42.3/b table for Solen.tab
.1
2 0. .00 0. 0.
[.....]
'TOSCA'
0 0
1.e-3 100. 100. 100.
1.e-3 100. 100. HEADER, 4 csnake
281 29 29 15.2 .518 1.e-30
./Csnk3D/Hlx68.2_Sol42.3/b_table_for_Helix_3T.tab_2
./Csnk3D/Hlx68.2_Sol42.3/b_table_for_Solen.tab_2
0 0 0 0
     0. .00 0. 0.
.....]
'MARKER' #End
'FAISCEAU'
'OPTIONS'
1 1 ! ~
1 1 ! options
WRITE ON
  'FAISCEAU'
 'MATRIX'
  'SYSTEM'
 cp zgoubi.res zgoubi.res_save
```

TOSCA

TOSCA	2-D and 3-D Cartesian of Cymluricar mesh neid map		
IC, IL	$I\!C=1,2$: print the map $I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2; 0-2[\times 10^n], 7$	2*I
BNORM, XN, YN, ZN	Field and X-,Y-,Z-coordinate normalization coefficients	4*no dim.	4*E
TITL	Title. Include "FLIP" to get field map X-flipped. Include "HEADER n" in case $FNAME$ starts with $n\geq 1$ header lines.		A80
IX, IY, IZ, $MOD[.MOD2]$	Number of nodes of the mesh in the X,Y and Z directions, $IZ=1$ for single 2-D map; MOD : operational and map $FORMAT$ reading mode 2 ; $MOD \le 19$: Cartesian mesh; $MOD \ge 20$: cylindrical mesh. $MOD2$, optional, tells the reading $FORMAT$, default is '*'.	$\leq MXX^{1}, \leq MXY,$ $\leq IZ, \geq 0[.1-9]$	3*I
FNAME 1 ($K = 1, NF$)	Names of the NF files that contain the 2-D maps, from $Z(1)$ to $Z(N)$ If $MOD=0$: $NF=1+[IZ/2]$, the NF 2-D maps are for $0 \le Z \le Z$ they are symmetrized with respect to the $Z(1)=0$ plane. If $MOD=1$: $NF=IZ$, no symmetry assumed; $Z(1)=Z_{max}$, $Z(1+[IZ/2])=0$ and $Z(NF)=-Z_{max}$. If $MOD=12$: a single $FNAME$ file contains the all 3-D volume. If $MOD=20-22$: other symmetry options, see toscap.f routine		A80
$ID, A, B, C [, A', B', C', A'', etc., if ID \ge 2]$	Integration boundary. Ineffective when $ID=0$. $ID=-1, 1 \text{ or } \geq 2$: as for <i>CARTEMES</i>	≥ -1 , cm, $2*$ no dim. [, $idem$]	I,3*E [,3*E,etc.]
IORDRE	If $IZ=1$: 3, 4, 25, as in <i>CARTEMES</i> ; unused if $IZ\neq 1$.	2, 25 or 4	I
XPAS	Integration step	cm	E
If Cartesian mesh (see M KPOS, XCE, YCE, ALE If polar mesh: KPOS If KPOS = 2	OD): KPOS=1: element aligned, 2: misaligned; shifts, tilt as for POLARMES. Normally 2.	1-2, 2*cm, rad 1-2	I, 3*E I
RE, TE, RS, TS		cm, rad, cm, rad	4*E

2-D and 3-D Cartesian or cylindrical mesh field map

```
\begin{array}{lll} DO\;K=1,\,NF \\ OPEN\;(UNIT=NL,\,FILE=FNAME(K),\,STATUS=\,'OLD'\;[,FORM='UNFORMATTED']) \\ DO\;J=1,\;JY\;; &DO\;I=1,\,IX \\ IF\;(BINARY)\;THEN \\ READ(NL)\;Y(J),\,Z(K),\,X(I),\,BY(J,K,I),\,BZ(J,K,I),\,BX(J,K,I) \\ ELSE \\ READ(NL,*)\;Y(J),\,Z(K),\,X(I),\,BY(J,K,I),\,BZ(J,K,I),\,BX(J,K,I) \\ ENDIF \\ ENDDO\;; &ENDDO \\ NL=NL+1 \\ ENDDO \end{array}
```

For 2-D maps BX and BY are assumed zero at all nodes of the 2-D mesh, regardless of BX(J,1,I), BY(J,1,I) values. For binary files, FNAME must begin with 'B_' or 'b_'.

 $^{^1 \}textit{MXX}, \textit{MXY}, \textit{IZ}$ may be changed, they are stated in the include file <code>PARIZ.H.</code>

 $^{^2}$ Each file FNAME(K) contains the field specific to elevation Z(K) and must be formatted according to the following FORTRAN read sequence (that usually fits TOSCA code OUTPUTS - details and possible updates are to be found in the source file 'fmapw.f'):

TRANSMAT	Matrix transfer		
IORDRE	Transfer matrix order	1-2	I
XL	Length (ineffective, for updating)	m	Е
For $IA = 1, 6$:			
R(IA, IB), IB = 1, 6	First order matrix	m, rad	6 lines
If IORDRE = 2	Following records <i>only</i> if <i>IORDRE</i> = 2		6*E each
T(IA,IB,IC),	Second order matrix, six 6*6 blocks	m, rad	36 lines 6*E each

TRAROT **Translation-Rotation**

TX, TY, TZ, RX, RY, RZ

Translations, rotations

3*m, 3*rad

6*E

TWISS Calculation of periodic optical parameters and printout to zgoubi.TWISS.out

KTW[.KTW2], FacD, FacA

KTW=0/1/2/3 : Off / as MATRIX / add computation of chromaticities / add computation of anharmonicities.

0-3[.1], 2*any

I1[.I1], 2*E

KTW2 = 1: long write-up to zgoubi.res.

 $FacD \times D = \delta p/p$ value applied, with D the momentum sampling

in OBJET; FacA: unused.

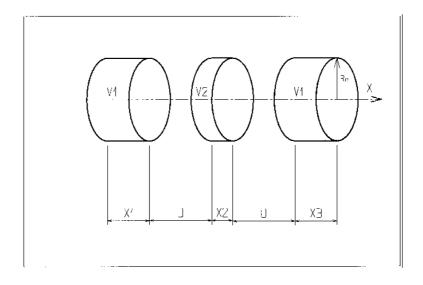
Example

- "KTW=3" under TWISS will cause 3 successive executions of zgoubi.dat and will result in delivery (print out to zgoubi.res) of
 - the on-momentum matrix of the optical structure,
 - off-momentum matrices at $\frac{dp}{p} = \pm FacD * \delta D$,
 - the Twiss parameters in the hypothesis of a stable periodic structure,
 - the momentum compaction, chromaticities, etc.

UNDULATOR Undulator magnet

Under development, to be documented

UNIPOT	Unipotential electrostatic lens		
ΙL	$I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0\text{-}2[\times 10^n], 7$	I
X_1, D, X_2, X_3, R_0	Length of first tube; distance between tubes; length of second and third tubes; radius	5*m	5*E
V_1, V_2	Potentials	2*V	2*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E



VENUS

XPAS

cm

E

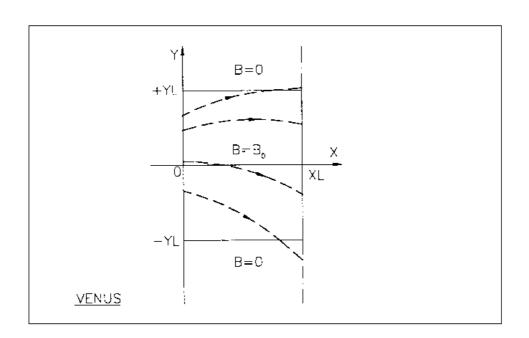
IL	$IL=1,2[\times 10^n],\ 7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
XL, YL, B_0	Length; width = $\pm YL$; field	2*cm, kG	3*E

Simulation of a rectangular dipole magnet

KPOS=1 : element aligned, 2 : misaligned; KPOS, XCE, 1-2, 2*cm, rad I, 3*E

YCE, ALE shifts, tilt (unused if *KPOS*=1)

Integration step



Scheme of VENUS rectangular dipole.

WIENFILT ¹	Wien filter		
IL	$I\!L=1,2[imes 10^n],~7$: print coordinates, fields, etc., along trajectories in zgoubi.res (1), zgoubi.plt (2), zgoubi.impdev.out (7).	$0-2[\times 10^n], 7$	I
XL, E, B, HV	Length; electric field; magnetic field; option: element inactive ($HV=0$) horizontal ($HV=1$) or vertical ($HV=2$) separation	m, V/m, T, 0-2	3*E, I
$X_{\mathrm{E}}, \lambda_{E_E}, \lambda_{B_E}$	Entrance face : Integration zone extent ; fringe field extents, E and B respectively (\simeq gap height)	3*cm	3*E
C_{E0} – C_{E5}	Fringe field coefficients for E	6*no dim.	6*E
C_{B0} – C_{B5}	Fringe field coefficients for B	6*no dim.	6*E
	Exit face:		
$X_S, \lambda_{E_S}, \lambda_{B_S}$	See entrance face	3*cm	3*E
C_{E0} – C_{E5}		6*no dim.	6*E
C_{B0} – C_{B5}		6*no dim.	6*E
XPAS	Integration step	cm	E
KPOS, XCE, YCE, ALE	<pre>KPOS=1 : element aligned, 2 : misaligned ; shifts, tilt (unused if KPOS=1)</pre>	1-2, 2*cm, rad	I, 3*E

 $^{^{1}\,}$ Use PARTICUL to declare mass and charge.

YMY Reverse signs of Y and Z axes

Equivalent to a 180° rotation with respect to X-axis



The use of YMY in a sequence of two dipoles of opposite signs.

PART C

Examples of input data files and output result files

Examples 283

INTRODUCTION

Several examples of the use of **zgoubi** are given here. They show the contents of the input and output data files, and are also intended to help understanding some subtleties of the data definition.

Example 1: checks the resolution of the QDD spectrometer SPES 2 of SATURNE Laboratory [56], by means of a *Monte Carlo initial object* and an *analysis of images* at the focal plane with histograms. The *measured field maps* of the spectrometer are used for that purpose. The layout of SPES 2 is given in Fig. 48.

Example 2: calculates the *first and second order transfer matrices* of an 800 MeV/c kaon beam line [57] at each of its four foci: at the end of the first separation stage (vertical focus), at the intermediate momentum slit (horizontal focus), at the end of the second separation stage (vertical focus), and at the end of the line (double focusing). The first bending is represented by its *3-D map* previously calculated with the TOSCA magnet code. The second bending is simulated with *DIPOLE*. The layout of the line is given in Fig. 49.

Example 3: illustrates the use of MCDESINT and REBELOTE with a simulation of the in-flight decay

$$K \longrightarrow \mu + \nu$$

in the SATURNE Laboratory spectrometer SPES 3 [31]. The angular acceptance of SPES 3 is ± 50 mrd horizontally and ± 50 mrd vertically; its momentum acceptance is $\pm 40\%$. The bending magnet is simulated with *DIPOLE*. The layout of SPES 3 is given in Fig. 50.

Example 4: illustrates the operation of *the fitting procedure*: a quadrupole triplet is tuned from -0.7/0.3 T to field values leading to transfer coefficients R12=16.6 and R34=-.88 at the end of the beam line. Other example can be found in [58].

Example 5: shows the use of the *spin and multi-turn tracking procedures*, applied to the case of the SATURNE 3 GeV synchrotron [7, 10, 59]. Protons with initial vertical spin $(\vec{S} \equiv \vec{S}_Z)$ are accelerated through the $\gamma G = 7 - \nu_Z$ depolarizing resonance. For easier understanding, some results are summarized in Figs. 52, 53 (obtained with the graphic post-processor **zpop**, see Part D).

Example 6: shows *ray-tracing through a micro-beam line* that involves *magneto-electrostatic quadrupoles* for the suppression of second order (chromatic) aberrations [6]. The extremely small beam spot sizes involved (less than 1 micrometer) reveal the high accuracy of the ray-tracing (Figs. 54).

Many more examples can be found on the **zgoubi** development web site [5].

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1 MONTE CARLO IMAGES IN SPES 2

Former Saclay/SATURNE and CERN QDD mass spectrometer [56].

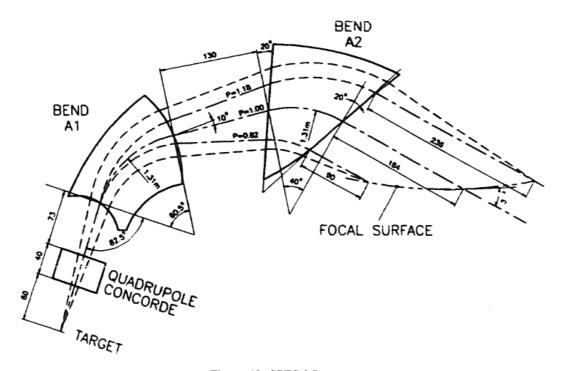


Figure 48: SPES 2 Layout.

zgoubi data file.

SPES2 QDD SPECTROMETER, USING FIELD MAPS; MONTE-CARLO OBJECT WITH MOMENTUM GRID. 'MCOBJET' 2335. REFERENCE RIGIDITY. REFERENCE RIGIDITY. DISTRIBUTION IN GRID. NUMBER OF PARTICLES. UNIFORM DISTRIBUTIONS 2 10000 10000 1 1 1 1 1 1 1 0 0 0 0 0 0 1. 1 1 1 1 1 5 0 0 0 0 0 0 0 001 0 50.e-3 0 50.e-3 0 0. 1 1 1 1 1 1 1 1 9 9 9 9 9 9 9 186387 548728 472874 UNIFORM DISTRIBUTIONS CENTRAL VALUES OF BARS. NUMBER OF BARS IN MOMENTUM. SPACE BETWEEN MOMENTUM BARS. WIDTH OF BARS. SORTING CUT-OFFS (UNUSED) FOR P(D) (UNUSED) SEEDS. 186387 548728 472874 'HISTO' 1 .997 1.003 80 1 20 'D' 1 'Q' 'HISTO' 3 -60. 60. 80 1 20 'T' 1 'Q' 'HISTO' 5 -60. 60. 80 1 20 'P' 1 'Q' 'DRIFT' 41.5 'CARTEMES' 0 0 .96136E-3 1. 1. ++++ CONCORDE ++++ 39 23 concord.map HISTO OF D. HISTO OF THETAO. HISTO OF PHIO. QUADRUPOLE MAP. IC IL. BNORM, XNORM, YNORM IX IY. field map file name, quadrupole NO LIMIT PLANE. IORDRE. XPAS. KPOS. concord.map 2 2.5 2 0 0 0 'DRIFT' 21.8 'CHANGREF' POSITIONING OF THE 8 0. 32.5 -35.6 'CARTEMES' 1-ST BENDING. 0 0 1.04279E-3 1. 1. ++++ A1 ++++ 117 52 field map file name, first dipole al.map 0 0 0 0 2.5 'CHANGREF' 0. -28.65 -27.6137 'DRIFT' POSITIONING OF THE EXIT FRAME. 11 33.15 'CHANGREF' 0. 27.5 -19.88 'CARTEMES' POSITIONING OF THE 12 2-ND BENDING. 13 0 0 1.05778E-3 1. 1. ++++ A2 ++++ 132 80 field map file name, second dipole a2.map 0 0 0 0 2 2.5 2 0 0 0 'CHANGREF' POSITIONING OF THE EXIT FRAME. 14 'DRIFT' 15 HISTO OF Y: SHOWS THE RESOLUTION OF THE SPECTROMETER. 2 -.5 2. 80 1 20 'Y' 1 'Q' 'END' 'HISTO' 16

Excerpt from zgoubi.res: histograms of initial beam coordinates.

		*** omo	n-m	**************************************			
		HISTOGRAMME PARTICULES					
		DANS LA FE					
		NORMALISE					
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19							
18					_		
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15		D	D	D	D	D	
14		D	D	D	D	D	
13 12		D D	D D	D D	D D	D D	
11		D	D	D	D	D	
10		0	0	0	0	0	
9		D D	D D	D D	D D	D D	
7		D	D	D	D	D	
6		D	D	D	D	D	
5		D	D	D	D	D	
4		D D	D D	D D	D D	D D	
2		D	D	D	D	D	
1		D		D		D	
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		_ 3	*	5	J	, 0	-
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CO	MPTAGE AU	CANAL MOIEN		2038			
VA	L. PHYS. A	U	: 1	1.000			
RE	SOLUTION	PAR CANAL	: 7				
PA	RAMETRES	PHYSIQUES DE					
		COMPTAGE =			, MAX-MIN =	4 00000-03	
		MIN - 0.550) , MA2			4.0000.4	
		MOYENNE =	1.000				
	******	********	0.9980 (0.000 -30.2	4 0.000 44.	63 0.0000 0.	
*****	******	SIGMA = 1.4 P,S,time: 1 ************* HISTOGRAMME PARTICULES DANS LA FE	0.9980 (DE LA (PRIMAIRES	0.000 -30.2 ******** COORDONNEE ET SECON	4 0.000 44. ***********************************	*****	
*****	******	SIGMA = 1.4 P,S,time: 1 ************* HISTOGRAMME PARTICULES DANS LA FE	0.9980 (******** DE LA (PRIMAIRES	0.000 -30.2 ******** COORDONNEE ET SECON	4 0.000 44. ***********************************	*****	
***** 3 H	******	SIGMA = 1.4 P,S,time: 1 ************* HISTOGRAMME PARTICULES DANS LA FE	0.9980 (DE LA (PRIMAIRES	0.000 -30.2 ******** COORDONNEE ET SECON	4 0.000 44. ***********************************	*****	
****** 3 H 20	******	SIGMA = 1.4 P,S,time: 1 ************* HISTOGRAMME PARTICULES DANS LA FE	0.9980 (DE LA (PRIMAIRES	0.000 -30.2 ******** COORDONNEE ET SECON	4 0.000 44. ***********************************	*****	
****** 3 H 20 19	******	SIGMA = 1.4 P,S,time: 1 ************* HISTOGRAMME PARTICULES DANS LA FE	0.9980 (DE LA (PRIMAIRES	0.000 -30.2 ******** COORDONNEE ET SECON	4 0.000 44. ***********************************	(MRD)	***
****** 3 H 20 19 18 17	******	SIGMA = 1.4 P.S.time : 1 HISTOGRAMME PARTICULES DANS LA FFE NORN	0.9980 (DE LA (PRIMAIRES	0.000 -30.2	4 0.000 44. ***********************************	(MRD)	
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******* 3 H 20 19 18 17 16 15 14 13 12	**************************************	SIGMA = 1.4 P.S.time : 1 HISTOGRAMME PARTICULES DANS LA FF NORN T T T T T T TTTT T TT T TTTTTTTTTT	DE LA (PRIMAIRES INSTRE: IALISE TT TTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTT	COORDONNEE ET SECON -60.00 T T T T T T T T T T T T T T T T T	THETA DAIRES / 60.00 T T T T TTTTTTTTTTTTTTTTTTTTTTTTTT	(MRD) T T T T T T TTTTTTTTTTTTTTTTTTTTTTT	********* T T
******* 3 H 20 19 18 17 16 15 14 13 12 11	ISTO	SIGMA = 1.4 P.S.time : 1 HISTOGRAMME PARTICULES DANS LA FF T T T T T T T T T T T T T T T T T T	DE LA (PRIMAIRES INSTERE: LALISE TT TTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTT	COORDONNEE ET SECON -60.00 T T T T T T T T T T T T T T T T T	THETA DAIRES / 60.00 T T T T TTTTTTTTTTTTTTTTTTTTTTTTTT	T T TT TT TT TTTTTTTTTTTTTTTTTTTTTTTTT	******* T T T T T O
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### HISTO

### HISTOGRAMME DE LA COORDONNEE PHI
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DANS LA FENETRE : -60.00 / 60.00 (MRD)

NORMALISE

***DANS LA FENETRE : -60.00 / 60.00 (MRD)

NORMALISE

***DANS LA FENETRE : -60.00 / 60.00 (MRD)

NORMALISE

***DANS LA FENETRE : -60.00 / 60.00 (MRD)

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Excerpt from zgoubi.res: the final momentum resolution histogram at the spectrometer focal surface.

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16 HISTO
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                           HISTOGRAMME DE LA COORDONNEE Y PARTICULES PRIMAIRES ET SECONDAIRES DANS LA FENETRE : -0.5000 / NORMALISE
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VAL. PHYS. AU " "
RESOLUTION PAR CANAL
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                                                       246
0.750
                                                   : 3.125E-02 (CM)
         PARAMETRES PHYSIQUES DE LA DISTRIBUTION:

COMPTAGE = 10000 PARTICULES

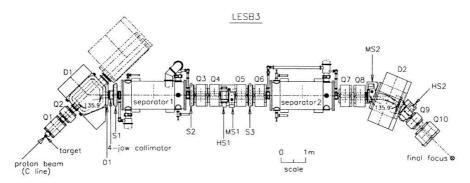
MIN = -0.1486 , MAX = 1.652

MOYENNE = 0.750

SIGMA = 0.4621 (CM)
                                                                           , MAX-MIN = 1.800
                                                                                                          (CM)
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2 TRANSFER MATRICES ALONG A TWO-STAGE SEPARATION KAON BEAM LINE

800 MeV/c kaon beam line at BNL Alternating Gradient Synchrotron [57]. The line includes two separation Wien filters.



Layout of LESB3 beamline.



Figure 49: 800 MeV/c kaon beam line layout.

zgoubi data file.

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10. 15.24 2.4 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 .4 1 0. 0. 0. 'DRIFT' 50.0 "MIENFILT' 0 2.16 55.E5 -0.215576 2 20. 10. 10. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 1. 1. 0. 0. 0. 'DRIFT' 30. 4 0.2490 5.3630 -2.4100 0 30. 30. 4 0.2490 5.3630 -2.4100 0 1.1 1 0. 0. 0. 'DRIFT' 10. 0. 0. 'DRIFT' 10. 0. 0. 0. 'DRIFT' 10. 0. 0. 0. 'DRIFT' 10. 0. 0. 0. 'MULTIPOL' 0 MULTIPOL' 0 10. 15.24 0. 08. 1.2 0. 0.	AT V 0.9870 0.9870 FIRST 0.0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0	0. 0. VERT	0. CICAL WIEN FILTER 0. 0.	15 16 17
10. 15.24 2.4 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 .4 1 0. 0. 0. 'WIENFILT' 50.0 'WIENFILT' 0 2.16 55.E50215576 2 20. 10. 10. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 1. 1. 0. 0. 0. 'DRIFT' 30. 'QUADRUPO' 0 45.72 15.24 -6.34 30. 30. 4 0.2490 5.3630 -2.4100 0 30. 30. 4 0.2490 5.3630 -2.4100 0 1.1 1 0. 0. 0. 'MULTIPOL' 0 10. 15.24 0. 08. 1.2 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.	AT V 0.9870 0.9870 FIRST 0.0.0.0.0.0.9870 SX2 + OF T 0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0	0. 0. VERT	0. 0. COMPENSATION Phi AND D2.Phi	15 16 17
10. 15.24 2.4 0. 0. 0. 0. 0. 4	AT V 0.9870 0.9870 0.9870 0.00 0.00 0.00 0.9870 0.9870 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0	0. 0. VERT 0. 0. OCTU, HE D. 0. 0. 0.	0. 0. CICAL WIEN FILTER 0. COMPENSATION Phi AND D2.Phi ABERRATIONS AT VF1 0.	15 16 17
10. 15.24 2.4 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 .4 1 0. 0. 0. 0. 'DRIFT' 50. 0. 'ZENTETLT' 0 2.16 55.E5 -0.215576 2 20. 10. 10. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 1. 1. 0. 0. 0. 'DRIFT' 30. 'QUADRUPO' 0 45.72 15.24 -6.34 30. 30. 4 0.2490 5.3630 -2.4100 0 1.1 1 0. 0. 0. 'DRIFT' 10. 0 11. 1 0. 0. 0. 'DRIFT' 10. 0 11. 1 0. 0. 0. 'DRIFT' 10. 0 4 0.2490 5.3630 -2.4100 0 1.1 1 0. 0. 0. 'DRIFT' 10. 0 4 0.2490 5.3630 -2.4100 0 0.0 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0	AT V 0.9870 0.9870 0.9870 0.00 0.00 0.00 0.9870 0.9870 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0	0. 0. VERT 0. 0. OCTU, HE D. 0. 0. 0.	0. 0. CICAL WIEN FILTER 0. COMPENSATION Phi AND D2.Phi ABERRATIONS AT VF1	15 16 17
10. 15.24 2.4 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 4 0.2490 5.3630 -2.4100 0 .4 1 0. 0. 0. 0. 'DRIFT' 50.0 "MIENFILT' 0 2.16 55.E5 -0.215576 2 20. 10. 10. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 1. 1. 0. 0. 0. 'DRIFT' 30. 'QUADRUPO' 0 45.72 15.24 -6.34 30. 30. 4 0.2490 5.3630 -2.4100 0 30. 30. 4 0.2490 5.3630 -2.4100 0 1.1 1 0. 0. 0. 'DRIFT' 10. 0 "MULTIPOL' 0 10. 15.24 0. 08. 1.2 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 5.3630 -2.4100 0 0. 0. 0. 0. 5.3630 -2.4100 0 0. 0. 0. 0. 5.3630 -2.4100 0 0. 0. 0. 0. 5.3630 -2.4100 0 0. 0. 0. 0. 5.3630 -2.4100 0 0. 0. 0. 0. 5.3630 -2.4100 0 0. 0. 0. 0. 5.3630 -2.4100 0 0. 0. 0. 0. 5.3630 -2.4100 0 0. 0. 0. 0. 5.3630 -2.4100 0 0. 0. 0. 0. 5.3630 -2.4100 0	AT V 0.9870 0.9870 0.9870 0.00 0.00 0.00 0.9870 0.9870 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0	0. 0. VERT 0. 0. OCTU, HE D. 0. 0. 0.	0. 0. CICAL WIEN FILTER 0. COMPENSATION Phi AND D2.Phi ABERRATIONS AT VF1 0.	15 16 17
10. 15.24 2.4 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 4 0.2490 5.3630 -2.4100 0 4 0.2490 5.3630 -2.4100 0 4 0.0. 0. 'MERTY' 50.0 'MIENFILT' 0 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.00. 0. 0. 4 0.2490 5.3630 -2.4100 0 0.00. 0.00. 0.00. 0.00. 0.00. 0. 4 0.2490 5.3630 -2.4100 0 0.00. 0.00. 0.00. 0.00. 0.00. 0. 4 0.2490 5.3630 -2.4100 0 0.00. 0.00. 0.00. 0.00. 0.00. 0. 4 0.2490 5.3630 -2.4100 0 0.00. 0.00. 0.00. 0.00. 0.00. 0. 4 0.2490 5.3630 -2.4100 0 0.00. 0.00. 0.00. 0.00. 0.00. 0.	AT V 0.9870 0.9870 0.9870 0.00 0.00 0.00 0.9870 0.9870 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0	0. 0. VERT 0. 0. OCTU, HE D. 0. 0. 0.	0. 0. CICAL WIEN FILTER 0. COMPENSATION Phi AND D2.Phi ABERRATIONS AT VF1 0.	15 16 17
10. 15.24 2.4 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 .4 1 0. 0. 0. 0. 'DRIFT' 50.0 'WIENFILT' 0 2.16 55.E50215576 2 20. 10. 10. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 0.2401 1.8639 -0.5572 0.3904 0. 1. 0. 0. 0. 0.2401 1.8639 -0.5572 0.3904 0. 1. 1. 0. 0. 0. 'DRIFT' 30. 'QUADRUPO' 0 45.72 15.24 -6.34 30. 30. 4 0.2490 5.3630 -2.4100 0 30. 30. 4 0.2490 5.3630 -2.4100 0 1. 1 0. 0. 0. 'WRITT' 10. 0 0 1. 1 0. 0. 0. 'WRITT' 10. 0. 0. 'WRITT' 10. 0. 0. 'WRITT' 10. 0. 0. 'BRIFT' 10. 0. 0. 'A 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 4 0.2490 5.3630 -2.4100 0 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.	AT V 0.9870 0.9870 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0	0. 0. VERT 0. 0. 0. 0. 0. 0. 0. 0.	0. 0. CICAL WIEN FILTER 0. COMPENSATION Phi AND D2.Phi ABERRATIONS AT VF1 0.	15 16 17

```
'COLLIMA'
                                                            FIRST VERTICAL FOCUS,
  2
2 14.6 .15E10 0.0.
                                                          MASS SLIT
  'DRIFT'
                                                                                                                      23
    20.0
  'OUADRUPO'
                                                             Q5
                                                                                                                      24
   45.72 15.24 10.93
   30. 30.
4 0.2490 5.3630 -2.4100 0.9870 0. 0.
   30. 30.
          0.2490 5.3630 -2.4100 0.9870 0. 0.
 4 0.2490
1.1
1 0.0.0.
'DRIFT'
10.0
'MULTIPOL'
                                                            COMPENSATION OF
ABERRATIONS AT VF2
                                                                                                                      26
 0 ABERRATIONS 1
10. 15.24 0. 0. 0. 1. 0. 0. 0. 0. 0. 0. 0.

10. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.

4 0.2490 5.3630 -2.4100 0.9870 0. 0.

4 0.2490 5.3630 -2.4100 0.9870 0. 0.

0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.

4 0.2490 5.3630 -2.4100 0.9870 0. 0.
 .4
1 0.0.0.
                                                                                                                      27
    10.0
  'QUADRUPO'
                                                               Q6
                                                                                                                      28
 'QUADRUPO' Q6
0
45.72 15.24 -11.18
30. 30.
4 0.2490 5.3630 -2.4100 0.9870 0. 0.
30. 30.
    3U. 3U.
4 0.2490 5.3630 -2.4100 0.9870 0. 0.
1.1
 1.1
1 0.0.0.
'DRIFT'
50.0
'WIENFILT'
                                                          SECOND VERTICAL WIEN FILTER
 0
2.16 -55.E5 .0215576 2
 2.16 -55.E5 .0215576 2
20.10.10.
0.2401 1.8639 -0.5572 0.3904 0. 0.
0.2401 1.8639 -0.5572 0.3904 0. 0.
20.10.10.
0.2401 1.8639 -0.5572 0.3904 0. 0.
0.2401 1.8639 -0.5572 0.3904 0. 0.
1.
1. 0. 0. 0.
'DRIFT'
                                                                                                                      31
 30.0
'QUADRUPO'
                                                               07
                                                                                                                      32
 45.72 15.24 -6.44
30. 30.
4 0.2490 5.3630 -2.4100 0.9870 0. 0.
          0.2490 5.3630 -2.4100 0.9870 0. 0.
 4 0.2490
1.1
1 0.0.0.
'DRIFT'
25.00000
                                                                                                                      33
  'QUADRUPO'
                                                                                                                      34
                                                              08
  45.72 15.24 8.085
30. 30.
  30. 30. 4 0.2490 5.3630 -2.4100 0.9870 0. 0. 30. 30. 4 0.2490 5.3630 -2.4100 0.9870 0. 0. 1.1 1 0. 0. 0. 0.
  'DRIFT'
                                                                                                                      35
    40.0
                                                         SECOND VERTICAL FOCUS,
MASS SLIT
  'COLLIMA'
                                                                                                                      36
 2 MASS SLIT
1 17. .2E10 0.0.
'MATRIX' TRANSFER COEFFICIENTS
 2 0
'DRIFT'
                                                                                                                      38
  -25.0
                                                          SIMULATION OF THE MAP
OF THE SECOND BENDING MAGNET
(UPGRADED VERSION OF 'AIMANT')
  'DIPOLE-M'
  79.3329 17.7000 1.0...
15. -1.
4 .1455 2.2670 -.6395 1.1558 0. 0. 0. 0.
0.00 21.91 1.E6 -1.E6 1.E6 1.E6
15. -1.
4 .1455 2.2670 -.6395 1.1558 0. 0. 0.
-43.80 -21.90 -1.E6 -1.E6 1.E6 1.E6 1.E6
0 0.
  0. 0. 4 .1455 2.2670 -.6395 1.1558 0. 0. 0. 4 .1455 2.2670 -1.E6 -1.E6 1.E6 -1.E6 1E6 NO SHIMMING
                                                            SCD ORDER INTERPOLATION
    2.5
   2
147.48099 -0.31007 147.48099 0.31007
  'DRIFT'
-15.00000
                                                                                                                      41
  'QUADRUPO'
                                                             09
  0

35.56 12.7 -13.69 -13.91

30. 25.4

4 0.2490 5.3630 -2.4100 0.9870 0. 0.

30. 25.4

4 0.2490 5.3630 -2.4100 0.9870 0. 0.

.5

1 0.0.0.0.
```

```
'DRIFT' 42
25.00000
'QUADRUPO' Q10 43
0
35.56 12.7 11.97
30. 25.4
4 0.2490 5.3630 -2.4100 0.9870 0. 0.
30. 25.4
4 0.2490 5.3630 -2.4100 0.9870 0. 0.
1.1
1 0.0.0.
'DRIFT' 44
200.0
'MATRIX' TRANSFER COEFFICIENTS 45
2 0 AT THE FINAL FOCUS
```

Excerpt of zgoubi.res: first and second order transfer matrices and higher order coefficients at the end of the line

```
FIRST ORDER COEFFICIENTS ( MKSA ):
                  3.60453
                                                  -4.453265E-02 -3.049728E-04
                                                                                                                           -1.165832E-04
                                                                                                                                                                      0.00000
                                                                                                                                                                                                      -5.229783E-02
                                               -4.453265E-02
0.270335
-8.687757E-07
-4.356398E-07
2.313953E-02
0.00000
                                                                                      -3.049728E-04
4.700517E-05
-3.60817
-2.05043
-2.264218E-05
0.00000
                                                                                                                                                                     0.00000
0.00000
0.00000
1.00000
0.00000
                                                                                                                           1.763910E-05
-1.731805E-02
-0.286991
                                                                                                                                                                                                      -9.561918E-02
-7.815367E-02
-3.983392E-02
                -2.05368
                2.240965E-05
                1.185290E-05
               DetY-1 = -0.1170246601, DetZ-1 =
                                                                                                                         0.0000034613
               R12=0 at 0.1647 m, R34=0 at -0.6034E-01 m
      First order sympletic conditions (expected values = 0) : -0.1170 \hspace{1.5cm} 3.4614 \text{E-} 06 \hspace{0.5cm} -1.8207 \text{E-} 04 \hspace{0.5cm} 3.0973 \text{E-} 05
                                                                                                                                            4.6007E-04 -8.0561E-05
                        SECOND ORDER COEFFICIENTS ( MKSA ):
           7.34 1 21 -1.78
-1.78 1 22 -530.
1.399E-02 1 23 -1.308E-03
1.456E-02 1 24 -1.743E-03
0.00 1 25 0.00
36.3 1 26 12.3
                                                                               1 31 1.399E-02
1 32 -1.308E-03
1 33 -0.611
1 34 -0.522
1 35 0.00
1 36 -2.771E-02
                                                                                                                           1 41 1.456E-02
1 42 -1.743E-03
1 43 -0.522
1 44 0.163
1 45 0.00
1 46 -2.211E-02
                                                                                                                                                                     1 51
1 52
1 53
1 54
1 55
1 56
                                                                                                                                                                                                               1 61 36.3
1 62 12.3
1 63 -2.771E-02
1 64 -2.211E-02
1 65 0.00
1 66 2.88
1 12
1 13
1 14
1 15
1 16
                                                                                                                                                                                      0.00
0.00
0.00
0.00
0.00
                                                                                 2 31 3.684E-02
2 32 -5.821E-04
2 33 1.05
2 34 1.94
2 35 0.00
2 36 -1.031E-02
                                                                                                                                                                                                               2 61 144.
2 62 -0.759
2 63 -1.031E-02
2 64 -4.285E-02
2 65 0.00
2 66 -65.3
                                                                                                                                                                                       0.00
0.00
0.00
0.00
0.00
             -303.
2 11
2 12
                                         2 21 3.81
2 22 -62.9
                                                                                                                            2 41 3.581E-02
2 42 -1.638E-04
                                                                                                                                                                      2 51
2 52
            -303.
3.81
3.684E-02
3.581E-02
0.00
144.
                                        2 23 -5.821E-04
2 24 -1.638E-04
2 25 0.00
2 26 -0.759
                                                                                                                            2 43 1.94
2 44 6.70
2 45 0.00
2 46 -4.285E-0
                                                                                                                                                                      2 53
2 54
2 55
2 56
                                                                                                                                        -4.285E-02
                                        3 21 2.158E-02
3 22 64.6
3 23 1.61
3 24 0.496
3 25 0.00
                                                                                 3 31 20.6
3 32 1.61
3 33 0.710
3 34 0.128
3 35 0.00
                                                                                                                                                                      3 51
3 52
3 53
3 54
3 55
3 11 -0.145
                                                                                                                            3 41
                                                                                                                                                                                       0.00
                                                                                                                                                                                                                3 61 -0.201
3 12 2.158E-02
3 13 20.6
3 14 86.0
3 15 0.00
                                                                                                                            3 42
3 43
3 44
3 45
                                                                                                                                         0.496
0.128
64.8
0.00
                                                                                                                                                                                       0.00
0.00
0.00
0.00
                                                                                                                                                                                                                3 62 8.793E-02
3 63 39.1
3 64 7.17
3 65 0.00
                                                      8.793E-02
                                                                                   3 36
                                                                                                                                                                                                                 3 66
3 16 -0.201
                                         3 26
                                                                                                   39.1
                                                                                                                            3 46
                                                                                                                                             7.17
                                                                                                                                                                       3 56
                                                                                                                                                                                       0.00
                                                                                                                                                                                                                                1.46
                                        4 21 1.146E-02
4 22 33.0
4 23 0.787
4 24 0.157
4 25 0.00
                                                                                   4 31
4 32
4 33
4 34
4 35
                                                                                                                            4 41
4 42
4 43
4 44
4 45
4 46
                                                                                                                                                                      4 51
4 52
4 53
4 54
4 55
4 56
4 11 -8.254E-02
                                                                                                   10.7
                                                                                               10.7
0.787
0.365
6.774E-02
0.00
17.5
                                                                                                                                                                                       0.00
0.00
0.00
0.00
0.00
                                                                                                                                                                                                                4 61
4 62
4 63
4 64
4 65
4 66
4 11 -8.254E-02
4 12 1.146E-02
4 13 10.7
4 14 47.3
4 15 0.00
                                                                                                                                         0.157
6.774E-02
33.1
0.00
                                                                                                                                                                                                                            3.566E-02
17.5
1.05
0.00
                                                                                   4 35
4 36
                                                      3.566E-02
4 16 -0.127
                                         4 26
                                                                                                                                             1.05
                                        5 21 -7.67
5 22 225.
5 23 1.283E-03
5 24 6.947E-04
5 25 0.00
5 26 2.77
                                                                                                                           5 41 -5.682E-02
5 42 6.947E-04
5 43 10.2
5 44 1.59
5 45 0.00
5 46 0.129
                                                                                                                                                                      5 51
5 52
5 53
5 54
5 55
5 56
                                                                                                                                                                                                               5 61
5 62
5 63
5 64
5 65
5 66
5 11 568.
5 12 -7.67
5 13 -5.970E-02
5 14 -5.682E-02
                                                                                5 31 -5.970E-02
5 32 1.283E-03
5 33 19.2
5 34 10.2
                                                                                                                                                                                                                            -251.
2.77
0.215
0.129
                                                                                                                                                                                       0.00
0.00
0.00
0.00
                                                                                                   0.00
               0.00
                                                                                   5 35 0.00
5 36 0.215
                                                                                                                                                                                                                                0.00
112.
5 16
            -251.
                           HIGHER ORDER COEFFICIENTS ( MKSA ):
                  V/V3
                                                       5784.8
                  Y/T3
Y/Z3
Y/P3
                                                   9.40037E+05
0.70673
0.42104
                  T/Y3
                                                     -18607
                                                   1.04607E+05
-0.10234
5.25793E-02
                   T/T3
                  T/Z3
T/P3
                  Z/T3
                  Z/Z3
                                                      -872.50
                  Z/P3
                                                    -785.20
                                                     15.460
7.5264
-409.98
-389.15
                  P/Y3
```

3 IN-FLIGHT DECAY IN SPES 3



Figure 50: Layout of SPES 3 spectrometer.

zgoubi data file

'MCOBJET' 3360. 1 200 1	CENTRAL VALUES OF BARS. WIDTH OF BARS.
'PARTICUL'	2
139.6000 0. 0. 26.03E-9 0. 'MCDESINT'	3
105.66 0. 136928 768370 548375 'ESL'	PION -> MUON + NEUTRINODECAY 4
77.3627	1
'CHAMBR'	STOPS ABERRANT MUONS. 5
1 100.10.245.0. 'DIPOLE'	6
2 80. 208.5	TOTAL ANGLE AT, CENTRAL RADIUS RM
33. 30. 0. 0. 0.	CENTRAL ANGLE, FIELD, INDICES
461. 414552 5.21405 -3.38307 14.0629	ENTRANCE EFB
15. 065. 0. 065	
461.	EXIT EFB
414552 5.21405 -3.38307 14.0629	
-15. 69. 85. 0. 1.E6 1 0. 0.	.E6 LATERAL EFB (INHIBITED)
414552 5.21405 -3.38307 14.0629	0. 0. 0.
414552 5.21405 -3.38307 14.0629 -15. 69. 85. 0. 1.E6 1	
-15. 69. 85. 0. 1.E6 1 2 10.0	
-15. 69. 85. 0. 1.E6 1 2 10.0 4.	.E6 1E6
-15. 69. 85. 0. 1.E6 1 2 10.0 4.	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM
-15. 69. 85. 0. 1.E6 1 2 10.0 4.	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0.	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF'	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF' 0. 049.	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8 FOCAL PLANE.
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF' 0. 049. 'HISTO'	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF' 0. 049.	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8 FOCAL PLANE.
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF' 0. 049. 'HISTO' 2 -170. 130. 60 1 20 'Y' 1 'Q' 'HISTO'	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8 FOCAL PLANE. TOTAL SPECTRUM (PION + MUON). 9 PION SPATIAL SPECTRUM 10
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF' 0. 049. 'HISTO' 2 -170. 130. 60 1 20 'Y' 1 'Q' 'HISTO' 2 -170. 130. 60 2	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8 FOCAL PLANE. TOTAL SPECTRUM (PION + MUON). 9
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF' 0. 049. 'HISTO' 2 -170. 130. 60 1 20 'Y' 1 'Q' 'HISTO' 2 -170. 130. 60 2 20 'P' 1 'P'	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8 FOCAL PLANE. TOTAL SPECTRUM (PION + MUON). 9 PION SPATIAL SPECTRUM 10 AT FOCAL PLANE.
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF' 0. 049. 'HISTO' 2 -170. 130. 60 1 20 'Y' 1 'Q' 'HISTO' 2 -170. 130. 60 2	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8 FOCAL PLANE. TOTAL SPECTRUM (PION + MUON). 9 PION SPATIAL SPECTRUM 10
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF' 0. 049. 'HISTO' 2 -170. 130. 60 1 20 'Y' 1 'Q' 'HISTO' 2 -170. 130. 60 2 20 'P' 1 'P' 'HISTO'	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8 FOCAL PLANE. TOTAL SPECTRUM (PION + MUON). 9 PION SPATIAL SPECTRUM 10 AT FOCAL PLANE. MUON SPATIAL SPECTRUM 11
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF' 0. 049. 'HISTO' 2 -170. 130. 60 1 20 'Y' 1 'Q' 'HISTO' 2 -170. 130. 60 2 20 'P' 1 'P' 'HISTO' 2 -170. 130. 60 3 20 'y' 1 'S' 'HISTO'	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8 FOCAL PLANE. TOTAL SPECTRUM (PION + MUON). 9 PION SPATIAL SPECTRUM 10 AT FOCAL PLANE. MUON SPATIAL SPECTRUM 11 AT FOCAL PLANE. MUON MOMENTUM SPECTRUM 12
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF' 0. 049. 'HISTO' 2 -170. 130. 60 1 20 'Y' 1 'Q' 'HISTO' 2 -170. 130. 60 2 20 'P' 1 'P' 'HISTO' 2 -170. 130. 60 3 20 'Y' 1 'S' 'HISTO' 1 .2 1.7 60 3	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8 FOCAL PLANE. TOTAL SPECTRUM (PION + MUON). 9 PION SPATIAL SPECTRUM 10 AT FOCAL PLANE. MUON SPATIAL SPECTRUM 11 AT FOCAL PLANE.
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF' 0. 049. 'HISTO' 2 -170. 130. 60 1 20 'Y' 1 'Q' 'HISTO' 2 -170. 130. 60 2 20 'P' 1 'P' 'HISTO' 2 -170. 130. 60 3 20 'y' 1 'S' 'HISTO'	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8 FOCAL PLANE. TOTAL SPECTRUM (PION + MUON). 9 PION SPATIAL SPECTRUM 10 AT FOCAL PLANE. MUON SPATIAL SPECTRUM 11 AT FOCAL PLANE. MUON MOMENTUM SPECTRUM 12
-15. 69. 85. 0. 1.E6 1 2 10.0 4. 2 164.755 .479966 233.554057963 'CHAMBR' 2 1 100. 10. 245. 0. 'CHANGREF' 0. 049. 'HISTO' 2 -170. 130. 60 1 20 'Y' 1 'Q' 'HISTO' 2 -170. 130. 60 2 20 'P' 1 'P' 'HISTO' 2 -170. 130. 60 3 20 'Y' 1 'S' 'HISTO' 1 .2 1.7 60 3 20 'd' 1 'S'	.E6 1E6 2ND DEGREE INTERP., MESH 0.4 CM STEP SIZE 7 TILT ANGLE OF 8 FOCAL PLANE. TOTAL SPECTRUM (PION + MUON). 9 PION SPATIAL SPECTRUM 10 AT FOCAL PLANE. MUON SPATIAL SPECTRUM 11 AT FOCAL PLANE. MUON MOMENTUM SPECTRUM 12 AT FOCAL PLANE.

Excerpt of zgoubi.res: histograms of primary and secondary particles at focal surface of SPES3.

```
9 HISTO
               TOTAL
                         SPECTRUM
                                                                                        HISTOGRAMME DE LA COORDONNEE Y
PARTICULES PRIMATRES ET SECONDAIRES
DANS LA FENETRE : -1.7000E+02 / 1.3000E+02 (CM)
NORMALISE
                                                                                                                     HISTOGRAMME DE LA COORDONNEE Y
PARTICULES SECONDAIRES
DANS LA FENETRE: -1.7000E+02 / 1.3000E+02 (CM)
                                                                                                                      NORMALISE
                                       YYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYY
                                        YYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYY
                                        YYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYY
                                        YYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYY
                                       1234567890123456789012345678901234567890123456789012345678901
                                                                                                                  123456789012345678901234567890123456789012345678901234567890
             TOTAL COMPTAGE
NUMERO DU CAI
                                                    9887 SUR 10000
             NUMERO DU CANAL MOYEN
COMPTAGE AU " "
VAL. PHYS. AU " "
RESOLUTION PAR CANAL
                                            : 55
: 281
: 0.000E+00 (CM)
: 5.000E+00 (CM)
                                                                                                         TOTAL COMPTAGE
                                                                                                                                                605 SUR 10000
                                                                                                         NUMERO DU CANAL MOYEN
COMPTAGE AU " "
                                                                                                                                                  50
                                                                                                         PARAMETRES PHYSIQUES DE LA DISTRIBUTION:

COMPTAGE = 9887 PARTICULES

MIN = -1.6687E+02, MAX = 9.4131E+01, MAX-MIN = 2.6100E+02(CM)

MOYENNE = -9.2496E-01 (CM)

SIGMA = 5.3583E+01 (CM)
                                                                                                        PARAMETRES PHYSIQUES DE LA DISTRIBUTION:

COMPTAGE = 605 PARTICULES

MIN=-1.6687E+02, MAX = 9.4131E+01, MAX-MIN = 2.6100E+02 (CM)

MOYENNE - -2.2782E+01 (CM)

SIGMA = 5.4452E+01 (CM)
 10 HISTO
               PION
                          SPATIAL
                      HISTOGRAMME DE LA COORDONNEE Y
PARTICULES PRIMATRES
DANS LA FENETRE: -1.7000E+02 / 1.3000E+02 (CM)
NORMALISE
                                                                                                                  HISTOGRAMME DE LA COORDONNEE DE DANTICULES SECONDAIRES
DANS LA FENETRE : 2.0000E-01 / 1.7000E+00
                                                                                                                  NORMALISE
19
18
17
16
15
14
13
                                       dd
                                                                                                                                       dd
                                                                                                                               ddddddddddddd ddddd
                                                                                                                              dddddddddddddddddddd
                                                                                                                             ddddddddddddddddddd ddd
                                       123456789012345678901234567890123456789012345678901
                                                                                                                  12345678901234567890123456789012345678901234567890123456789
             TOTAL COMPTAGE
NUMERO DU CAI
                                                   9282 SUR 10000
             NUMERO DU CANAL MOYEN
COMPTAGE AU " "
VAL. PHYS. AU " "
RESOLUTION PAR CANAL
                                                                                                        NUMERO DU CANAL MOYEN : 46
COMPTAGE AU " : 16
VAL PHYS. AU " : 8.250E-01
RESOLUTION PAR CANAL : 2.500E-02
                                             : 0.000E+00 (CM)
: 5.000E+00 (CM)
             PARAMETRES PHYSIQUES DE LA DISTRIBUTION:

COMPTAGE = 9282 PARTICULES

MIN=-9.5838E+01, MAX = 9.3504E+01, MAX-MIN = 1.8934E+02 (CM)

MOYENNE = 4.9971E-01 (CM)

SIGMA = 5.3215E+01 (CM)
                                                                                                        PARAMETRES PHYSIQUES DE LA DISTRIBUTION:

COMPTAGE = 605 PARTICULES

MIN = 3.7184E-01, MAX = 1.3837E+00, MAX-MIN = 1.0119E+00

MOYENNE = 8.16938-01

SIGMA = 2.2849E-01
```

4 USE OF THE FITTING PROCEDURE



Figure 51: Vary B in all quadrupoles, for fitting of the transfer coefficients R_{12} and R_{34} at the end of the line. The first and last quadrupoles are coupled so as to present the same value of B.

zgoubi data file.

```
MATCHING A SYMMETRIC QUADRUPOLE TRIPLET
 'OBJET'
                                                                                                                              1
2501.73
                     RIGIDITY (kG.cm)
                     11 PARTICLES GENERATED FOR USE OF MATRIX
2. 2. 2.
0. 0. 0.
              2. 0. .001
              0. 0.
 'ESL
                                                                                                                              2
200
 'QUADRUPO'
              3
                                                                                                                              3
0
40. 15. -7.
0. 0.
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
1 0. 0. 0.
 'ESL'
                                                                                                                              4
30.
 'QUADRUPO'
                                                                                                                              5
0
40. 15. 3.
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723 0. 0.
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
1 0. 0. 0.
 'ESL'
                                                                                                                              6
30.
 'QUADRUPO'
40. 15. -7.
0. 0.
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
0.
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
1 0. 0. 0.
 'ESL'
                                                                                                                              8
200
 'MATRIX'
                                                                                                                              9
 'FIT2'
                     VARY B IN QUADS FOR FIT OF R12 AND R34
                                                                                                                             10
                      # OF VARIABLES
3 12 7.12 2.
                     SYMMETRIC TRIPLET => QUADS #1 AND #3 ARE COUPLED
                     PRMTR #12 OF ELEMENTS #3, 5 AND 7 IS FIELD VALUE
# OF CONSTRAINTS, PENALTY
CNSTRNT #1 : R12=16.6 AFTER LAST DRIFT (LMNT #8)
CNSTRNT #2 : R34=-.88 AFTER LAST DRIFT
5
  12 0. 2.
  1.E-10
   1 2 8 16.6 1.
  3 4 8 -.88 1.
                                                                                                                             11
```

Excerpt of zgoubi.res: first order transfer matrices prior to and after fitting.

************************** TRANSFER MATRIX WITH STARTING CONDITIONS : MATRICE DE TRANSFERT ORDRE 1 (MKSA) 0.00000 0.00000 5.43427 17.0254 0.00000 0.00000 0.00000 5.43425 0.00000 0.00000 1.67580 0.00000 0.00000 -0.974288 0.00000 0.00000 -1.27003 0.00000 0.00000 0.00000 -0.629171 -1.27004 0.00000 0.00000 0.00000 0.00000 1.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 1.00000 ************************** STATE OF VARIABLES AFTER MATCHING: LMNT VAR PARAM MINIMUM INITIAL FINAL MAXIMUM STEP NAME LBL1 LBL2 1 -7.00 -6.972765137 -7.00 -6.972765137 3.00 3.229344585 3 7 12 -21.0 120 -6.97 7.00 7.00 1.707E-04 QUADRUPO 1.707E-04 1 120 5 2 12 -3.00 3.00 5.2255555 STATUS OF CONSTRAINTS (Target penalty = 1.0000E-10)

- TORROW WEIGHT REACHED 12 -3.00 3.00 3.229344585 9.00 1.266E-04 QUADRUPO TYPE I J LMNT# DESIRED WEIGHT REACHED

1 1 2 8 1.6600000E+01 1.0000E+00 1.6599981E+01

1 3 4 8 -8.8000000E-01 1.0000E+00 -8.8000964E-01 KI2 * Parameter(s) * 0: * 0: Fit reached penalty value 8.4374E-11 MATRIX, WITH NEW VARIABLES : 5.27056 0.00000 0.00000 0.00000 16.6000 0.00000 0.00000 0.00000 1.61443 5.27450 0.00000 0.00000 0.00000 0.00000 -1.24205 -0.880010 0.00000 0.00000 0.00000 0.00000 -0.622553 -1.24620 0.00000 0.00000 0.00000 0.00000 0.00000 1.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 1.00000 *******************

MULTITURN SPIN TRACKING IN SATURNE 3 GeV SYNCHROTRON

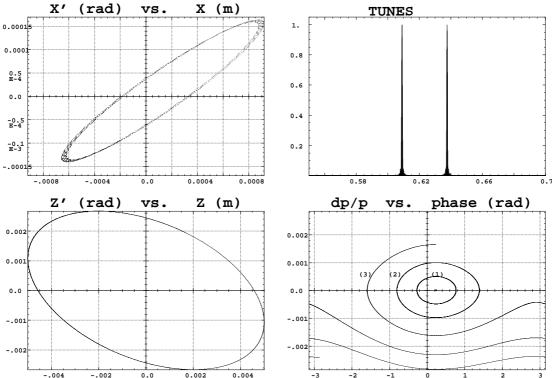


Figure 52: Tracking over 3000 turns. These simulations exhibit the first order parameters and motions as produced by the multi-turn raytracing.

- (A) Horizontal phase-space: the particle has been launched near to the closed orbit (the fine structure is due to Y-Z coupling induced by bends fringe fields, also responsible of the off-centering of the local closed orbit - at ellipse center).
- (B) Vertical phase-space: the particle has been launched with $Z_0 = 4.58 \ 10^{-3}$ m, $Z_0' = 0$. A least-square fit by $\gamma_Z Z^2 + 2\alpha_Z Z Z' + \beta_Z Z'^2 = \varepsilon_Z/\pi$ yields $\beta_Z = 2.055$ m, $\alpha_Z = 0.444$, $\gamma_Z = 0.582$ m⁻¹, $\varepsilon_Z/\pi = 12 \ 10^{-6}$ m.rad in agreement with matrix calculations.

 (C) Fractional tune numbers obtained by Fourier analysis for $\varepsilon_Y/\pi = \varepsilon_Z/\pi \simeq 12 \ 10^{-6}$ m.rad: $\nu_Y = 0.63795$, $\nu_Z = 0.60912$ (the integer
- (**D**) Longitudinal phase-space ("(DP, phase)" in Zgoubi notations): particles with initial momentum dispersion of 5 10^{-4} (1), 10^{-3} (2), $1.65 \cdot 10^{-3}$ (3) (out of acceptance), are accelerated at 1405 eV/turn ($\dot{B}=2.1 \text{ T/s}$); analytical calculations give accordingly momentum acceptance of $1.65 \ 10^{-3}$.



Figure 53: Crossing of $\gamma G = 7 - \nu_Z$, at $\dot{B} = 2.1$ T/s.

- (A) $\varepsilon_Z/\pi=12.2\ 10^{-6}$ m.rad. The strength of the resonance is $|\varepsilon|=3.3\ 10^{-4}$. As expected from the Froissart-Stora formula [60] the asymptotic polarization is about 0.44.
- (B) The emittance is now $\varepsilon_Z/\pi = 1.2 \ 10^{-6}$ m.rad; comparison with (A) shows that $|\varepsilon|$ is proportional to $\sqrt{\varepsilon_Z}$.
- (C) Crossing of this resonance for a particle having a momentum dispersion of 10^{-3} .

zgoubi data file (beginning and end).

```
SATURNE. CROSSING GammaG=7-NUz, NUz=3.60877(perturbed)
                                                                834.04 MeV, proton
 5015.388
                            .458 0. 0. 1.00 'o' EpsilonY/pi ~ 0. (Closed orbit) .458 0. 0. 1.0015 '1' .458 0. 0. 1.0011 '2' .458 0. 0. 1.0016 '3'
6.2E-02
               6.5E-02
1.024
               1.09
'SCALING'
  MULTIPOL
                                                   CROSSING GammaG=7-Nuz+/-14E, E=3.3E-4
AT 2.1 T/s, IN 3442 MACHINE TURNS,
FROM 834.041 TO 838.877 MeV
  5015.388E-3 5034.391E-3
1 3442
  QUADRUPO
  5015.388E-3 5034.391E-3
                    3442
  REND
   5015.388E-3 5034.391E-3
  CAVITE
  2
1.
                                                  RELATIVE CHANGE OF SYNCHRONOUS RIGIDITY
                  1.00378894
'DARTICIII.'
938.2723 1.6021892E-19 1.7928474 0. 0. 'SPNTRK'
'QUADRUPO'
 46.723 10. .763695
                                                 .763695 = FIELD FOR BORO=1 T.m
40.723 10. 0. 0. 6. .1122 6.2671 -1.4982 3.5882 -2.1209 1.723 0. 0. 6. .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
 #30|50|30 Quad
1 0. 0. 0.
                                    SD 2
                                                                                                 6
 71.6256
   'BEND'
                                  DIP 3 4 3
                                                                                                 7
 8
                                                                                                 9
10
 71.6256
                                   DIP 3 4 3
   'BEND'
                                                                                               11
 'BERD'
0
247.30039 0. 1.57776
20. 8. .04276056667
4 .2401 1.8639 -.5572 .3904 0. 0. 0.
20. 8. .04276056667
20. 8. .04276056667
4 .2401 1.8639 -.5572 .3904 0. 0. 0.
#30|120|30 bend 3 0. 0. 0. -.1963495408
'RSL' SD 2
                                                                                               12
 71.6256
  QUADRUPO'
                                                                                               13
 46.723 10. .763695
 6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
0. 0.
      .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
 #30|50|30 Quad
1 0. 0. 0.
'ESL'
71.6256
                                                                                               14
                                   DIP 3 4 3
                                                                                               15
   'BEND'
  U247.30039 0. 1.57776
20. 8. .04276056667
4 .2401 1.8639 -.5572 .3904 0. 0. 0.
20. 8. .04276056667
20. 8. .04276056667
20. 8. .0427605667
3 0. 0. 0. -.1963495408
                                                                                               16
 71.6256
  'MULTIPOL'
                                   OP 5
                                                                                               17
 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 430|50|30 Quad
```

```
18
 71.6256
                                      DIP 3 4 3
                                                                                                    19
   'BEND'
  247.30039 0.
  247.30039 0. 1.57776

20. 8. .04276056667

4 .2401 1.8639 -.5572 .3904 0. 0. 0.

20. 8. .04276056667 20. 8.

4 .2401 1.8639 -.5572 .3904 0. 0. 0.

#30|120|30 bend 3 0. 0. 0. -.19634
                            3 0. 0. 0. -.1963495408
SD 2
  'ESL
                                                                                                    20
 71.6256
  'QUADRUPO'
                                                                                                    21
 0
46.723 10. .763695
0. 0. 6. .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
0. 0. 6. .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
 #30|50|30 Quad
1 0. 0. 0.
                                                                                                    22
  'MULTIPOL'
                                    QP 5
 1 0. 0. 0.
'ESL'
                                                                                                    24
392.148
 'OUADRUPO'
                                     OP 1
                                                                                                    25
 46.723 10. .763695
 0. 0.
6 .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
     .1122 6.2671 -1.4982 3.5882 -2.1209 1.723
 #30|50|30 Quad
 1 0. 0. 0.
'ESL'
71.6256
'BEND'
                                                                                                    26
 247.30039 0. 1.57776
20. 8. .04276056667
4 .2401 1.8639 -.5572 .3904 0. 0. 0.
20. 8. .04276056667
20. 8. .04276056667
4 .2401 1.8639 -.5572 .3904 0. 0. 0.
#30|120|30 bend 3 0. 0. 0. -.1963495408
  247.30039 0.
  'MULTIPOL'
                                                                                                    29
 0. 0. 0. 0. 0. 0.
#30|50|30 Quad
                              0. 0. 0. 0.
 1 0. 0. 0.
'ESL'
                                    SD 2
                                                                                                    3.0
 71.6256
'BEND'
  'ESL'
 392.148
 'CAVITE'
1
105.5556848673 3.
6000. 0.
'FAISCNL'
                                             SIN(phis) = .234162, dE=1.40497 keV/Turn
 b_zgoubi.fai
'SPNPRNL'
                                                                                                    87
 zqoubi.spn
  SPNPRT
 'REBELOTE'
2999 0.1 99
END'
                                             TOTAL NUMBER OF TURNS = 3000
                                                                                                    91
```

6 MICRO-BEAM FOCUSING WITH $\vec{E} \times \vec{B}$ QUADRUPOLES



Figure 54: Upper plot: 50-particle beam tube ray-traced through a double focusing quadrupole doublet typical of the front end design of micro-beam lines. Initial conditions are : $Y_0 = Z_0 = 0$, angles T_0 and P_0 random uniform within ± 0.2 mrad, and momentum dispersion $\delta p/p$ uniform in $\pm 3\,10^{-4}$.

Lower plot: (**D**) sub-micronic cross-section at the image plane of a 4000-particle beam with initial conditions as above, obtained thanks to the second-order achromatic magneto-electrostatic quadrupole doublet (the image size would be $\Delta Y \approx \Delta Z \approx \pm 50 \mu m$ with regular magnetic quadrupoles, due to the momentum dispersion). Note the high resolution of the ray-tracing which still reveals image structure of nanometric size.

zgoubi data file.

```
MICROBEAM LINE, WITH A MAGNETO-ELECTROSTATIC QUADRUPOLE DOUBLET.
'MCOBJET' RANDOM OBJECT DEFINITION 20.435 RIGIDITY (20keV PROTONS).
1 DISTRIBUTION IN WINDOW.
200
                                                    NUMBER OF PARTICLES. UNIFORM DISTRIBUTION.
CENTRAL VALUE, AND HALF WIDTH OF DISTRIBUTION.
                                                    HALF WIDTH OF DISTRIBUTE
CUT-OFFS (UNUSED).
FOR P(D) - UNUSED.
SEEDS.
PARTICLE MASS AND CHARGE
  'PARTICUL'
938.2723 1.60217733E-19 0. 0. 0.
                                                      FOR INTEGRATION IN E-FIELD.
 'DRIFT'
                                                    DRIFT.
 'DRIFT'
                                                    DRIFT.
 59.
'EBMULT'
                                                    FIRST MAGNETO-ELECTROSTATIC
                                                        QUADRUPOLE.
ELECTRIC Q-POLE COMPONENT.
10.2 10. 0. -9272.986 0. 0. 0. 0. 0. 0. 0. 0.
ENTRANCE EFB, SHARP EDGE.
                                                          EXIT EFB. SHARP EDGE.
                                                           MAGNETIC Q-POLE COMPONENT.
ENTRANCE EFB, SHARP EDGE.
EXIT EFB, SHARP EDGE.
.8
1 0. 0. 0.
'DRIFT'
                                                                                         6
4.9
'EBMULT'
                                                    SECOND MAGNETO-ELECTROSTATIC
QUADRUPOLE.
.8
1 0. 0. 0.
 'DRIFT'
                                                    DRIFT.
 'HISTO'
 'HISTO'
2 -5E-6 5E-6
20 'Y' 1 'Q'
'HISTO'
                   60 2
                                                    OF THE Y COORDINATE.
4 -5E-6 5E-6
20 'Z' 1 'Q'
'FAISCNL'
                    60 2
                                                    OF THE Z COORDINATE.
                                         RAYS ARE STORED IN rays.out
                                                                                       11
                                         FOR FURTHER PLOTTING.
RUN AGAIN, FOR RAY-TRACING
A TOTAL OF 200*(19+1) PARTICLES.
rays.out
 'REBELOTE'
                                                                                       12
                                                                                       13
```

zgoubi.res file.

```
12 REBELOTE
                 RUN
                           AGAIN
    Multiple pass.
        From element # 1 : MCOBJET /label1=RANDOM /label2=OBJECT to REBELOTE /label1=RANDOM /label2=OBJECT ending at pass # 20 at element # 12 : REBELOTE /label1=RUN /label2=AGAIN
    End of pass # 19 through the optical structure
                Total of 3800 particles have been launched
Next pass is \# 20 and last pass through the optical structure
......
               RANDOM
    1 MCOBJET
                     OOM OBJECT
Reference magnetic rigidity = 20.435 KG*CM
         Object built up of 200 particles
Distribution in a Window
Central values (MKSA units):
YO, TO, ZO, PO, XO, BR/BORO:
Widdth (+/-, MKSA units):
DY, DT, DZ, DP, DX, DBR/BORO:
Cut-offs (*+/-Width):
NY, NT, NZ, NP, NX, NBR/BORO:
Type of sorting:
Y, T, Z, P, X, D:
Uniform Unit
                                           0.000 0.000 0.000 0.000 0.000
                                           0.00 2.000E-04 0.00 2.000E-04 0.00 3.000E-04
                                           1.00 1.00
                                                                1.00 1.00 1.00 1.00
                                           Uniform Uniform Uniform
                                                                          Uniform
                                                                                    Uniform
                                                                                              Uniform
.....
    2 PARTICUL PARTICLE MASS
    Particle properties :
                                              MeV/c2
                         = 938.272
= 1.602177E-19
                mag. rigidity (kG.cm)
mass (MeV/c2)
                                        20.435000
                                                     =p/q, such that dev.=B*L/rigidity
                mag, rigidity (kG.cm) | 20.435000 =p/q, such that dev.=B*L/rigidity
mass (MeV/c2) | 938.27230
momentum (MeV/c) | 6.1262621
energy, total (MeV) | 938.29230
energy, kinetic (MeV) | 1.99998909E-02
beta = v/c | 6.5291616518E-03
gamma | 1.00021316
beta *samma | 6.5293008252E-03
electric rigidity (MeV) | 3.9999376635E-02 =T[eV]*(gamma+1)/gamma, such that dev.=E*L/rigidity
```

```
3 DRIFT
                      DRIFT.
                                Drift, length = 500.00000 cm
TRAJ #1 IEX,D,Y,T,Z,P,S,time : 1 2.999865E-04 -2.027052E-02 -4.054104E-02 -9.359114E-02 -1.871823E-01 5.0000001E+02 2.55365E+00
 Cumulative length of optical axis = 5.00000000 m at ; Time (for ref. rigidity & particle) = 2.554417E-06 s
.....
      4 DRIFT
                     DRIFT.
                                Drift, length =
                                                     59.00000 cm
TRAJ #1 IEX,D,Y,T,Z,P,S,time : 1 2.999865E-04 -2.266244E-02 -4.054104E-02 -1.046349E-01 -1.871823E-01 5.5900001E+02 2.85498E+00
  \text{Cumulative length of optical axis = } \quad 5.59000000 \qquad \text{m at ; Time (for ref. rigidity \& particle) = } \quad 2.855839E-06 \text{ s} 
.....
                                 ELECTRO-MA
      5 EBMULT FIRST
      ---- MULTIPOLE : Length of element = 10.2000
Bore radius RO = 10.000
E-DIPOLE = 0.000000E+00 V/m
                E-QUADRUPOLE = -9.2729860E+03 V/m
                E-QUADRUPOLE = -9.2729860E+03 V/m
E-SEXTUPOLE = 0.0000000E+00 V/m
E-DECAPOLE = 0.0000000E+00 V/m
E-L4-POLE = 0.0000000E+00 V/m
E-14-POLE = 0.0000000E+00 V/m
E-16-POLE = 0.0000000E+00 V/m
E-18-POLE = 0.000000E+00 V/m
E-20-POLE = 0.000000E+00 V/m
                Entrance/exit field models are sharp edge FINTE. FINTS. gap: 0.0000E+00 0.0000E+00 5.0000E+00
                FINTE, FINTS, gap :
                 Length of
                             element = 10.200000
us RO = 10.000
                 Length or -
Bore radius RO = 10.000
POTPOLE = 0.0000000E+00 kG
                B-DIPOLE
                B-QUADRUPOLE = 1.8949300E+00 kG

        B-QUADRUPCILE
        1.89493008+00 kG

        B-SEXTUPOLE
        0.00000008+00 kG

        B-OCTUPOLE
        0.00000008+00 kG

        B-DECAPOLE
        0.00000008+00 kG

        B-DDDCAPOLE
        0.00000008+00 kG

        B-14-POLE
        0.00000008+00 kG

        B-16-POLE
        0.0000008+00 kG

        B-18-POLE
        0.0000008+00 kG

        B-20-POLE
        0.0000008+00 kG

        B-20-POLE
        0.0000008+00 kG

                Entrance/exit field models are sharp edge FINTE, FINTS, gap: 0.0000E+00 0.0000E+00 5.0000E+00
  *** Warning : sharp edge model, vertical wedge focusing approximated with first order kick. FINT at entrance = 0.000
  *** Warning: sharp edge model, vertical wedge focusing approximated with first order kick. FINT at exit = 0.000
                     Integration step : 0.8000
 Cumulative length of optical axis = 0.5.69200000 m; Time (for ref. rigidity & particle) = 0.2.907949E-06 s
6 DRIFT
                 DRIFT.
                                Drift, length =
                                                      4.90000 cm
TRAJ #1 IEX,D,Y,T,Z,P,S,time : 1 2.839285E-04 -1.310701E-02 9.564949E-01 -1.603604E-01 -5.590035E+00 5.7410014E+02 2.93210E+00
 Cumulative length of optical axis = 5.74100000 m at ; Time (for ref. rigidity & particle) = 2.932982E-06 s
EBMULT
                      SECOND
                                    ELECTRO-MA
      ---- MULTIPOLE
               Entrance/exit field models are sharp edge FINTE, FINTS, gap: 0.0000E+00 0.0000E+00 5.0000E+00
        ---- MULTIPOLE :
Length of
                ULTIPOLE : 10.200000
Bore radius R0 = 10.000
Bore radius R0 = 10.000
B-DIPOLE = 0.000000E+00 kG
B-QUADRUPOLE = -2.8159200E+00 kG
B-SEXTUPOLE = 0.0000000E+00 kG
B-DECAPOLE = 0.0000000E+00 kG
B-DECAPOLE = 0.0000000E+00 kG
B-DECAPOLE = 0.0000000E+00 kG
B-14-POLE = 0.0000000E+00 kG
                              = 0.0000000E+00 kG
= 0.0000000E+00 kG
= 0.0000000E+00 kG
                B-16-POLE
                B-18-POLE
                B-20-POLE
                Entrance/exit field models are sharp edge FINTE, FINTS, gap : 0.0000E+00 0.0000E+00 5.0000E+00
  *** Warning : sharp edge model, vertical wedge focusing approximated with first order kick. FINT at entrance =
  *** Warning : sharp edge model, vertical wedge focusing approximated with first order kick. FINT at exit =
                     Integration step : 0.8000
 Cumulative length of optical axis = 5.84300000
                                                          m ; Time (for ref. rigidity & particle) = 2.985092E-06 s
.....
```

```
9 HISTO
                         HISTOGRA
                                          HISTOGRAMME DE LA COORDONNEE Y
                                          PARTICULES PRIMAIRES ET SECONDAIRES DANS LA FENETRE: -5.0000E-06 / 5
                                                                                             5.0000E-06 (CM)
    20
19
18
17
16
15
14
13
12
11
10
9
8
7
6
5
                                                                 YYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYYY
                                          1234567890123456789012345678901234567890123456789012345678901\\
                                                                        4000 SUR 4000
                      TOTAL COMPTAGE
                      NUMERO DU CANAL MOYEN
COMPTAGE AU " "
VAL. PHYS. AU " "
RESOLUTION PAR CANAL
                                                                       51
109
                                                                : 0.000E+00 (CM)
: 1.667E-07 (CM)
                      PARAMETRES PHYSIQUES DE LA DISTRIBUTION:

COMPTAGE = 4000 PARTICULES

MIN = -3.4326E-06, MAX = 3.4347E-06, MAX-MIN = 6.8674E-06 (CM)

MOYENNE = -2.8531E-08 (CM)

SIGMA = 1.8619E-06 (CM)
TRAJ #1 D,Y,T,Z,P,S,IEX: 1.0002E+00 9.0257E-07 -2.3996E-01 -1.0770E-06 1.7947E+00 6.09300E+02 1

10 HISTO HISTOGRA
                                         HISTOGRAMME DE LA COORDONNEE Z
PARTICULES PRIMAIRES ET SECONDAIRES
DANS LA FENETRE: -5.0000E-06 / 5.
NORMALISE
                                                                                             5.0000E-06 (CM)
    20
19
18
17
16
15
14
13
12
11
10
9
8
7
6
5
4
3
2
                                                                                                Z
Z
Z
                                                                       ZZ
ZZ
ZZ
ZZ
00
                                                                                             000
                                                                       ZZZZ
                                                                                              ZZZ
                                                                      ZZZZZZZZZZZZZZZZZZZZZZZZ
                                         1234567890123456789012345678901234567890123456789012345678901
                      TOTAL COMPTAGE

NUMERO DU CANAL MOYEN
COMPTAGE AU " "

VAL. PHYS. AU " "

RESOLUTION PAR CANAL
                                                                 : 4000 SUR
: 51
: 169
: 0.000E+00 (CM)
: 1.667E-07 (CM)
                                                                      4000 SUR 4000
51
169
                      PARAMETRES PHYSIQUES DE LA DISTRIBUTION:

COMPTAGE = 4000 PARTICULES

MIN = -1.9150E-06, MAX = 1.9110E-06, MAX-MIN = 3.8260E-06 (CM)

MOYENNE = -3.8539E-09 (CM)

SIGMA = 1.1232E-06 (CM)
TRAJ #1 D,Y,T,Z,P,S,IEX: 1.0002E+00 9.0257E-07 -2.3996E-01 -1.0770E-06 1.7947E+00 6.09300E+02 1

11 FAISCNL RAYS ARE
Print[s] occur at
                                   AGAIN,
       12 REBELOTE RUN
                           **** FIN D'EFFET DE 'REBELOTE' ****
20 PASSAGES DANS LA STRUCTURE
# PARTICULES ENVOYEES : 4000
        IL Y A EU
```

PGM PRINCIPAL : ARRET SUR CLE REBELOTE

PART D

Running zgoubi and its post-processor/graphic interface zpop

INTRODUCTION

The **zgoubi** package, including this guide, examples, the **zpop** graphic/analysis post-processor, is available on web [5].

The **zgoubi** FORTRAN package is transportable; it has been compiled, linked and executed over the years on several types of systems (e.g. CDC, CRAY, IBM, DEC, HP, SUN, VAX, UNIX, LINUX).

An additional *FORTRAN* code, **zpop**, allows the post-processing and graphic treatment of **zgoubi** output files. **zpop** has been routinely used on DEC, HP, SUN stations, and is now on UNIX and LINUX systems.

1 GETTING TO RUN zgoubi AND zpop

1.1 Making the Executable Files zgoubi and zpop

1.1.1 The transportable package zgoubi

Compile and link the FORTRAN source files (normally, just run the Makefile), to create the executable zgoubi.

zgoubi is written in standard *FORTRAN*, mostly 77, therefore it does not require linking to any library.

1.1.2 The post-processor and graphic interface package zpop

Compile the FORTRAN source files (normally, just run the Makefile).

Link **zpop** with the graphic library, libminigraf.a [61]. This will create the executable **zpop**, that is to be run on an xterm type window.

1.2 Running zgoubi

The principles are the following:

- Fill up zgoubi.dat with the input data that describe the problem (see examples, Part C).
- Run zgoubi.
- Results of the execution will be printed into zgoubi.res and, upon options appearing in zgoubi.dat, into several other outputs files (see section 2 below).

1.3 Running zpop

- Run **zpop** on an xterm window. This will open a graphic window.
- To access the data plotting sub-menu, select option 7.
- To access the data treatment sub-menu, select option 8.
- An on-line Help provides some information regarding the available post-processing procedures (Fourier transform, elliptical fit, synchrotron radiation, field map contours, tune diagram, etc.).

2 STORAGE FILES

When explicitly requested by means of the adequate keywords, options, or dedicated *LABEL*'s, extra storage files are opened by **zgoubi** (*FORTRAN "OPEN*" statement) and filled.

Their content can be post-processed using the interactive program **zpop** and its dedicated graphic and analysis procedures.

306 2 STORAGE FILES

The **zgoubi** procedures that create and fill these extra output files are the following (refer to Part A and Part B of the guide):

- Keywords FAISCNL, FAISTORE: fill a '.fai' type file (normally named [b_]zgoubi.fai) with particle and spin coordinates and a lot of other informations.
- Keywords *SPNPRNL*, *SPNSTORE*: fill a '.spn' type file (normally named [b_]zgoubi.spn) with spin coordinates and other informations.
- Option IC = 2, with field map keywords (e.g. CARTEMES, TOSCA): fill zgoubi.map with 2-D field map.
- Option IL = 2, with magnetic and electric element keywords: fill zgoubi.plt with the particle coordinates and experienced fields, step after step, all along the optical element.
- Using the keyword MARKER with '.plt' as a second LABEL will cause storage of current coordinates into zgoubi.plt.

Typical examples of graphics that one can expect from the post-processing of these files by **zpop** are the following (see examples, Part C):

• '.fai' type files

Phase-space plots (transverse and longitudinal), aberration curves, at the position where FAISTORE or FAISCNL appears in the optical structure. Histograms of coordinates. Fourier analysis (e.g. , spin motion, tunes, in case of multi-turn tracking), calculation of Twiss parameters from phase-space ellipse matching.

• zgoubi.map

Isomagnetic field lines of 2-D map. Superimposing trajectories read from zgoubi.plt is possible.

• zgoubi.plt

Trajectories inside magnets and other lenses (these can be superimposed over field lines obtained from zgoubi.map). Fields experienced by the particles at the traversal of optical elements. Spectral and angular distributions of synchrotron radiation.

• zgoubi.spn

Spin coordinates and histograms, at the position where *SPNPRNL* appears in the structure. Resonance crossing when performing multi-turn tracking.

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