

# Lecture\_12

February 28, 2023

## 1 Solar System Formation

The general picture of formation of the solar system suggests that it was formed from the collapse of a giant dust cloud (called a protosolar nebula, more on this in 3rd year) which was mostly composed of hydrogen. A key feature of this model is that the total angular momentum of the system must be conserved.

There is some direct observational evidence for this feature:

- The direction of the Sun's rotation, and of the rotation and orbital motion of (nearly) all the planets coincide ("prograde" direction).
- The rotation axes of nearly all planets are within  $25\text{-}30^\circ$  of being perpendicular to their orbital planes
- The planets orbital planes all coincide to within  $7^\circ$  (most are even within  $1\text{-}3^\circ$ )

So, since the angular momentum for the Sun's rotation, the planet's rotation, and the planet's orbital motion all have the same direction, then it was likely the angular momentum for the protosolar nebula.

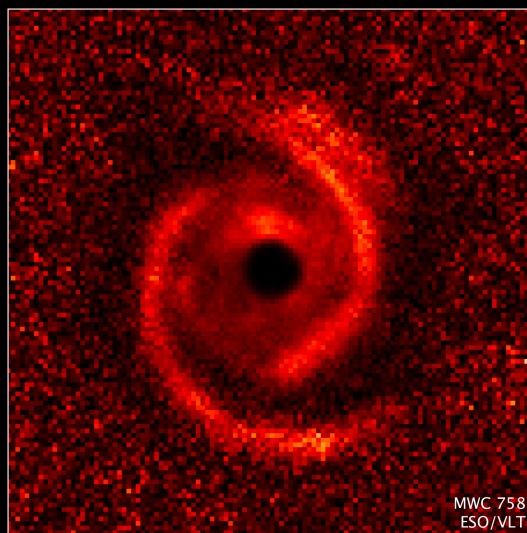
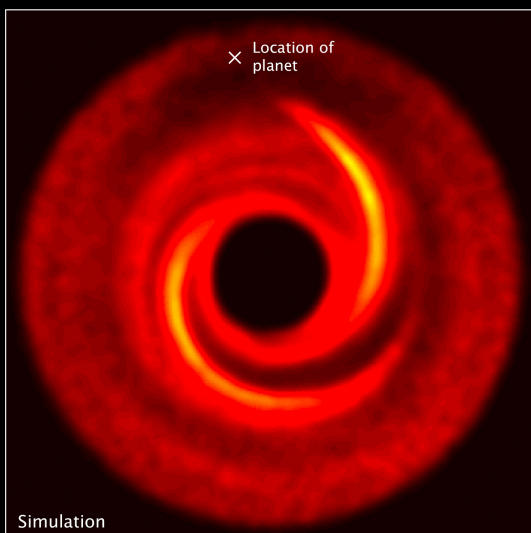
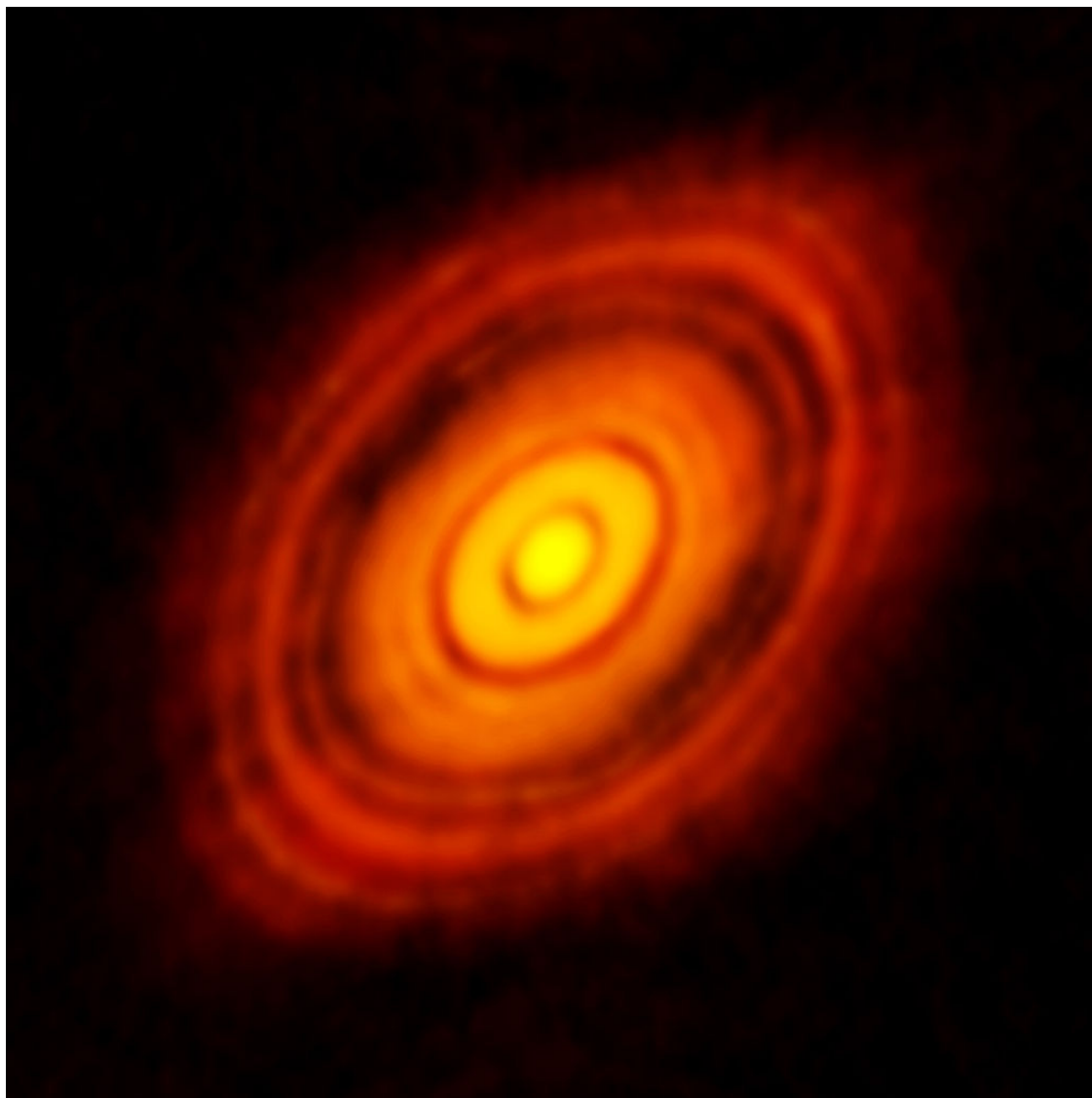
Now, not all observational evidence does support this model:

- Venus and Uranus' rotations are "retrograde" (that is, they rotate opposite to everything else)
- Uranus' rotational axis is inclined  $98^\circ$  to its orbital plane (that is, it's rotating on its side)
- Earth, Mars, Saturn, and Neptune have angles between their orbital and rotational planes of  $23\text{-}29^\circ$

A proposed solution to all of these issues is that these planets collided with planetesimals during formation.

### 1.1 Protoplanetary discs

Below, I've included some real/simulated observations of protoplanetary discs.

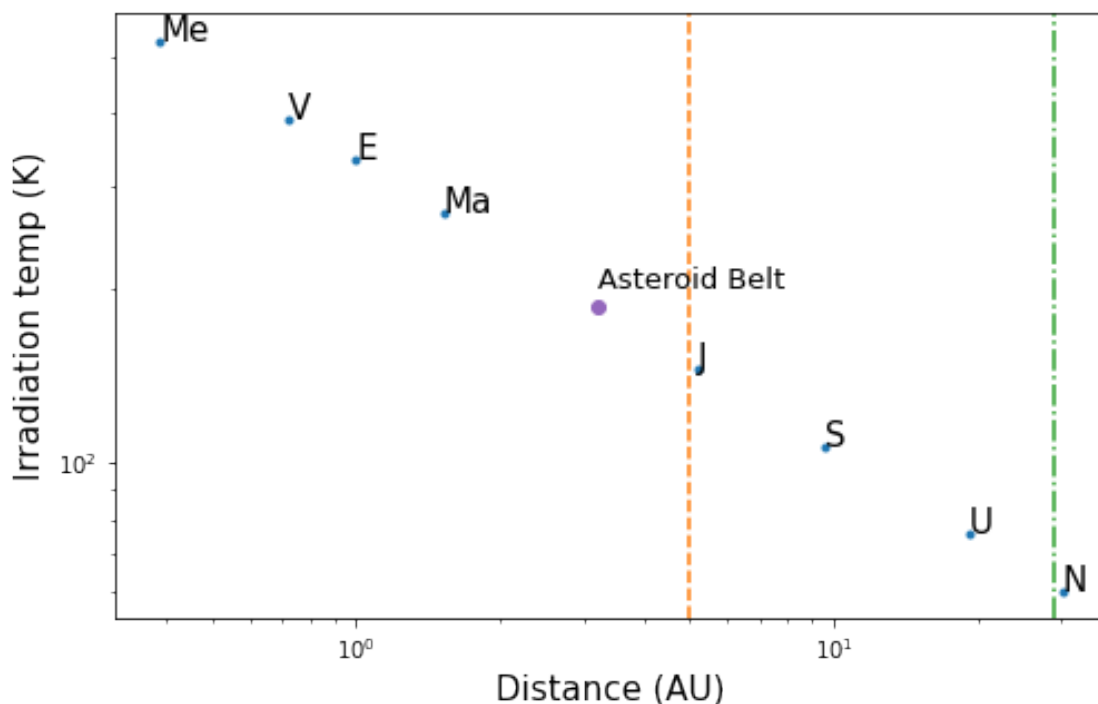


Protoplanetary Disk ■ Simulated Spiral Arm vs. Observational Data  
ESO/VLT

## 1.2 Terrestrial versus Gas Giant Planets

So why do we have these two types of planets? And how does this feed into a model of forming the solar system? First, let's propose a model.

- As the protosolar nebula contracted and formed a disc, heavier elements condensed out first.
- Water had not yet condensed when terrestrial planet formed. It's suspected most water on Earth comes from collisions with cometary nuclei.
- Water could condense beyond some distance from Sun, near orbit of Jupiter (as shown below, where we've calculated the irradiation temperature for different distances from the Sun, and found where the snow line (condensation temperature for water = 150 K) lies.



## 2 Quirks of planets

### 2.1 Mercury

- Its rotation is studied using radar signals transmitted by the Arecibo radio telescope (which has since collapsed) in 1965, using the Doppler effect. The rotational period is  $P_{\text{rot}} = 58.65$  d.
- This is exactly  $2/3$  of the orbital period of the planet ( $P_{\text{orb}} = 87.97$  d). Since Mercury feels the strongest tidal force at perihelion (point of closest approach to the Sun), this means that the tidal bulges always line up with the Sun at this time (as there is 1.5 rotations per orbit, see figure).
- Gravitational influence of other planets causes the perihelion to shift in a counter clockwise rotation by  $574''/\text{century}$ . Newtonian gravity can only explain  $531''/\text{century}$  - the remainig

43"/century explained using Einstein's theory of general relativity.

## 2.2 Mars and the asteroid belt (between Mars and Jupiter)

- Mars has a low mass of  $0.107 M_{\oplus}$ .
- To explain this, it may be that Jupiter became very massive before Mars finished forming, which perturbed orbits of planetesimals near Mars.
- This would mean the "missing mass" of Mars has ended up in the asteroid belt.
- Numerical simulations suggest Mars rotational axis may vary chaotically with tilts between  $11-49^\circ$  on timescales as short as a few million years (due to its low mass and gravitational influence of other planets).

## 2.3 Venus

- Also studied using radar signals sent from Earth, but also using Doppler shifts of reflected sunlight.
- Venus rotates in a retrograde direction, with  $P_{\text{rot}} = 243$  d and  $P_{\text{orb}} = 224.7$  d.
- Main gas in atmosphere is CO<sub>2</sub> (96.4%). At the base of its atmosphere, it has  $T = 740$  K and a pressure of 90 atm.
- This temperature is 2-3 times higher than the irradiation temperature we get when we use the formula from last week - due to the greenhouse effect.
- Surface accurately mapped by the Magellan spacecraft. The frequency of the radio signals sent to Earth were Doppler shifted depending on the speed of the spacecraft as it passed over regions of higher/lower mean density.
- It also potentially has traces of phosphine in its upper atmosphere (which **may** be due to life).

## 2.4 Gas Giants

All planets produce heat due to the decay of radioactive nuclei, including the terrestrial planets, but the Gas Giants show excess heat on top of this. To figure out why Gas Giants show this, and terrestrial planets do not, let's think about the energy that was released by the gravitational collapse of the disc into the planets, and how long it should take for bodies to dissipate this heat:

$$\tau_{\text{cool}} = \frac{\text{total energy}}{\text{energy loss rate}} \sim \frac{V}{A} \sim \frac{r^3}{r^2} \sim r$$

So, the bigger the planet's radius, the longer it takes for it to dissipate all of the heat due to contraction. This is the Kelvin-Helmholtz mechanism. Given this, we would expect Jupiter to still be contracting due to its formation.