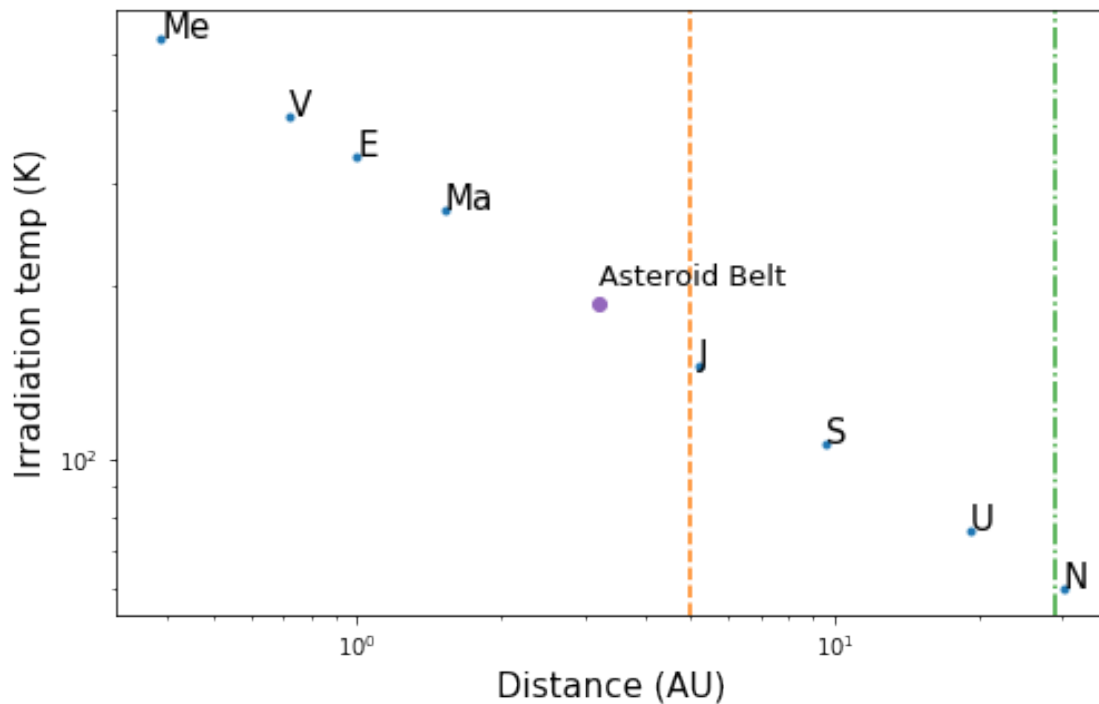


# Lecture\_19

March 24, 2022

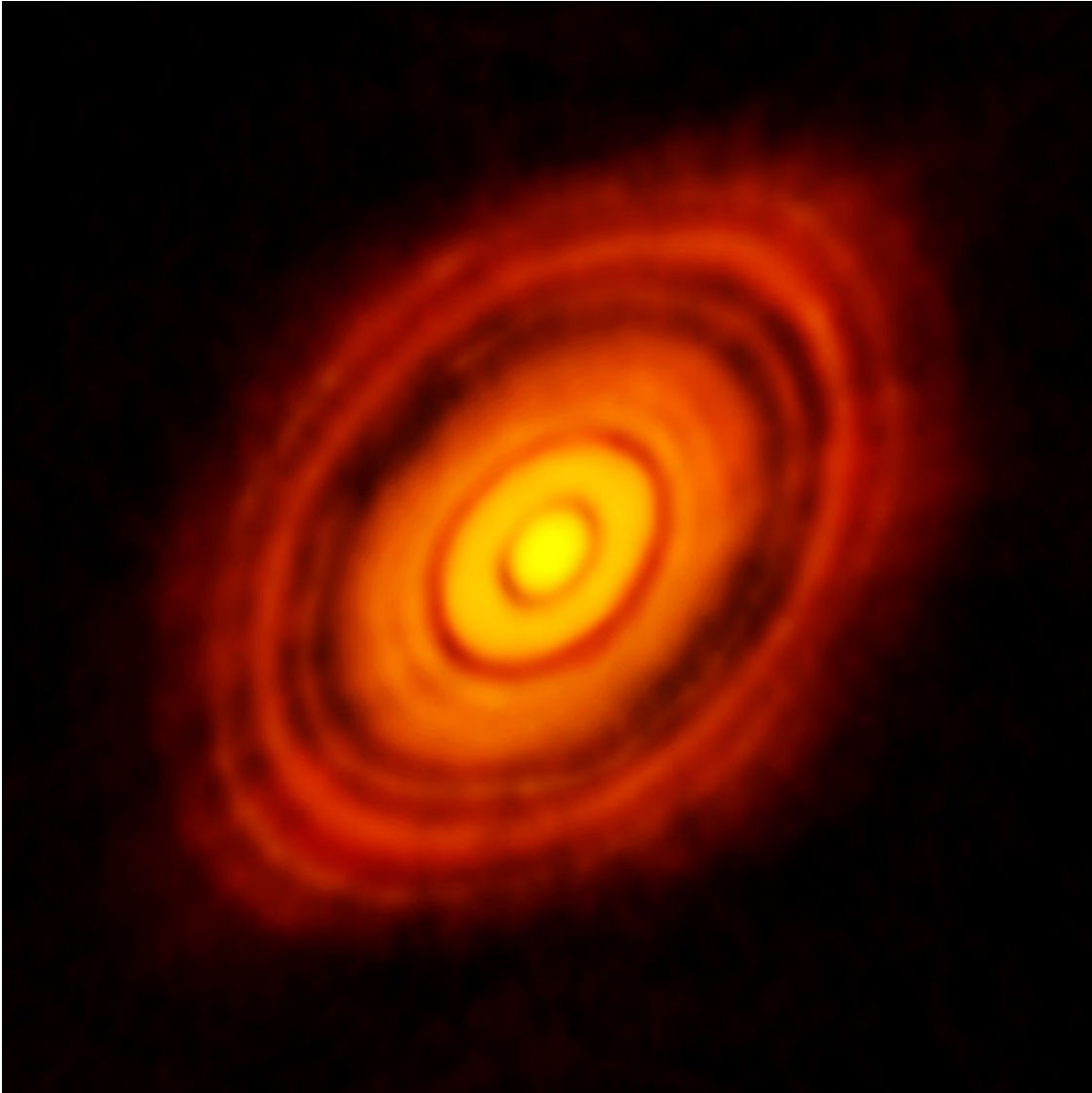
## 1 Terrestrial versus Gas Giant Planets

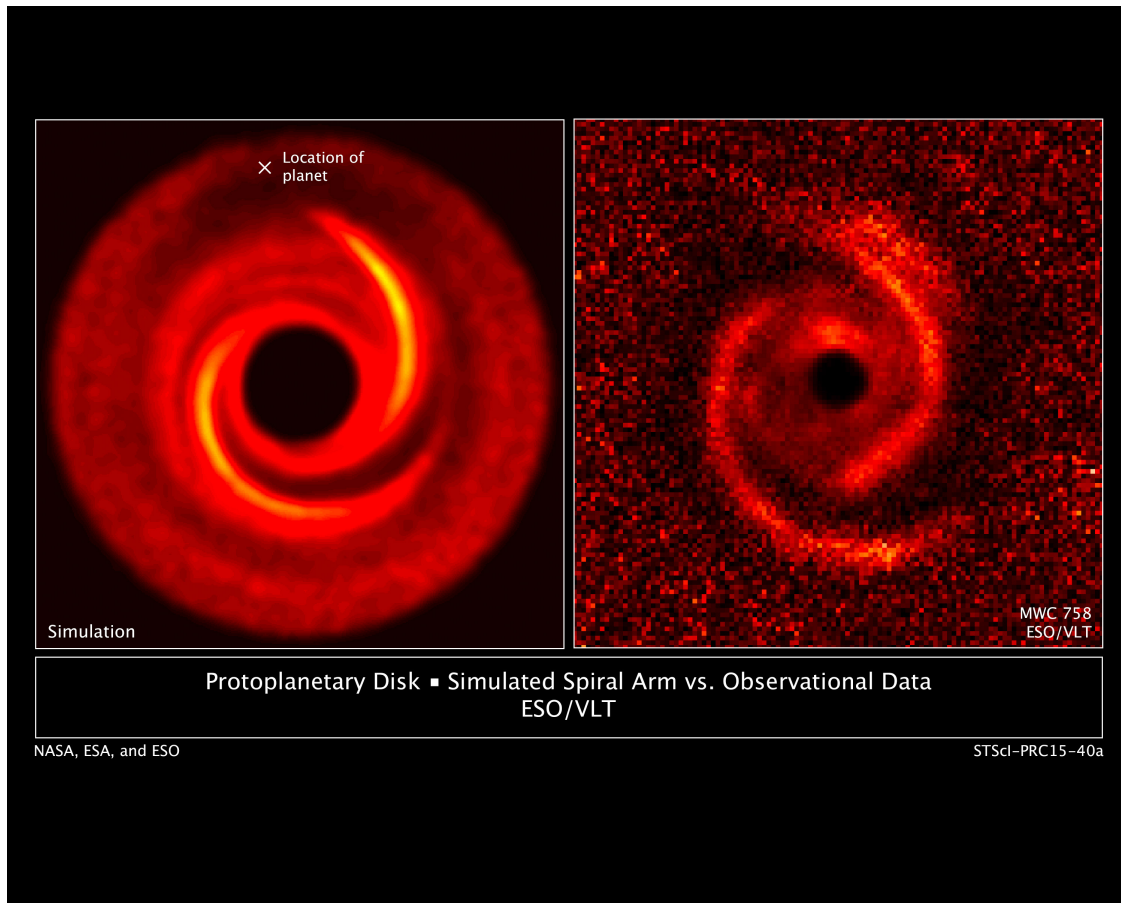
So why do we have these two types of planets? And how does this feed into a model of forming the solar system? First, let's propose a model. - As the protosolar nebula contracted and formed a disc, heavier elements condensed out first. - Water had not yet condensed when terrestrial planets formed. It's suspected most water on Earth comes from collisions with cometary nuclei. - Water could condense beyond some distance from Sun, near orbit of Jupiter (as shown below, where we've calculated the irradiation temperature for different distances from the Sun, and found where the snow line (condensation temperature for water = 150 K) lies.



- When fusion began in the centre of the Sun, it led to a very strong solar wind. This pushed matter not bound in the inner planets away from the Sun.
- Water pushed beyond the snow line. There, it condensed onto Jupiter, increasing its mass. This enabled Jupiter to capture H and He, further increasing its mass.

## 2 Protoplanetary discs





### 3 Quirks of planets

#### 3.1 Mercury

- Its rotation is studied using radar signals transmitted by the Arecibo radio telescope (which has since collapsed) in 1965, using the Doppler effect. The rotational period is  $P_{\text{rot}} = 58.65$  d.
- This is exactly  $2/3$  of the orbital period of the planet ( $P_{\text{orb}} = 87.97$  d). Since Mercury feels the strongest tidal force at perihelion (point of closest approach to the Sun), this means that the tidal bulges always line up with the Sun at this time (as there is 1.5 rotations per orbit, see figure).
- Gravitational influence of other planets causes the perihelion to shift in a counter clockwise rotation by  $574''/\text{century}$ . Newtonian gravity can only explain  $531''/\text{century}$  - the remaining  $43''/\text{century}$  explained using Einstein's theory of general relativity.

#### 3.2 Mars and the asteroid belt (between Mars and Jupiter)

- Mars has a low mass of  $0.107 M_{\oplus}$ .
- To explain this, it may be that Jupiter became very massive before Mars finished forming, which perturbed orbits of planetesimals near Mars.
- This would mean the “missing mass” of Mars has ended up in the asteroid belt.
- Numerical simulations suggest Mars' rotational axis may vary chaotically with tilts between

11-49° on timescales as short as a few million years (due to its low mass and gravitational influence of other planets).

### 3.3 Venus

- Also studied using radar signals sent from Earth, but also using Doppler shifts of reflected sunlight.
- Venus rotates in a retrograde direction, with  $P_{\text{rot}} = 243$  d and  $P_{\text{orb}} = 224.7$  d.
- Main gas in atmosphere is CO<sub>2</sub> (96.4%). At the base of its atmosphere, it has  $T = 740$  K and a pressure of 90 atm.
- This temperature is 2-3 times higher than the irradiation temperature we get when we use the formula from last week - due to the greenhouse effect.
- Surface accurately mapped by the Magellan spacecraft. The frequency of the radio signals sent to Earth were Doppler shifted depending on the speed of the spacecraft as it passed over regions of higher/lower mean density.
- It also potentially has traces of phosphine in its upper atmosphere (which **may** be due to life).

### 3.4 Gas Giants

All planets produce heat due to the decay of radioactive nuclei, including the terrestrial planets, but the Gas Giants show excess heat on top of this. To figure out why Gas Giants show this, and terrestrial planets do not, let's think about the energy that was released by the gravitational collapse of the disc in to the planets, and how long it should take for bodies to dissipate this heat:

$$\tau_{\text{cool}} = \frac{\text{total energy}}{\text{energy loss rate}} \sim \frac{V}{A} \sim \frac{r^3}{r^2} \sim r$$

So, the bigger the planets radius, the longer it takes for it to dissipate all of the heat due to contraction. This is the Kelvin-Helmholtz mechanism. Given this, we would expect Jupiter to still be contracting due to its formation. First, let's consider the virial theorem again, which states that:

$$\begin{aligned} \langle K \rangle &= -\frac{1}{2} \langle U \rangle \\ \langle E \rangle &= \frac{1}{2} \langle U \rangle = \frac{3}{5} \frac{GM^2}{r} \end{aligned}$$

Now, let's look at the time derivative of this:

$$\begin{aligned} \frac{dE}{dt} &= \frac{1}{2} \frac{dU}{dt} = \frac{1}{2} \frac{dU}{dr} \frac{dr}{dt} \\ \frac{dE}{dt} &= -\frac{3GM^2}{10r^2} \frac{dr}{dt} \end{aligned}$$

Given that  $\frac{dE}{dt} = P$ , we can solve for  $\frac{dr}{dt}$ :

$$\frac{dr}{dt} = -\frac{10r^2 P}{3GM^2}$$

So if Jupiter's measured power output per unit area is 7.5 W/m<sup>2</sup>, then we get a change in radius of -3mm/year, which we are not sensitive to!

Jupiter's heat production can be explained in this way - that is, the excess we see matches what we'd expect from this cooling time for an object of Jupiter's radius. However, Saturn's heat production is too high. - The most likely explanation is that the excess heat in Saturn is generated through the action of the virial theorem continuous as He sinks slowly through the H<sub>2</sub> atmosphere.

$$-3.231095 \frac{\text{mm}}{\text{yr}}$$