Law of Large Graphs 1

## Law of Large Graphs

June 17, 2015

- 1 Introduction
- 2 Background
- 3 Theory
- 4 Simulations

To demonstrate the previous results, we simulate random graphs from a SBM with parameters.

$$B = \begin{bmatrix} .42 & .2 \\ .2 & .7 \end{bmatrix}, \qquad \rho = \begin{bmatrix} .5 & .5 \end{bmatrix}$$

From this model we sample M Adjacency Matrices with N vertices to calculate both  $\bar{A}$  and  $\hat{P}$ . With these estimators for P, we calculate the mean squared error of each block region in the model, and compare these with our predictions.

Law of Large Graphs 2

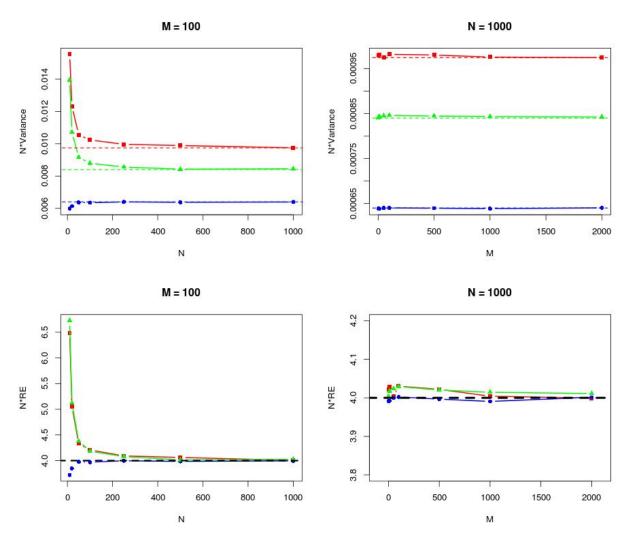


Figure 1: N\*Variance( $\hat{P}$ ) and RE, dotted lines represent the predictions and each color represents unique values within the true  $P \in \{.2, .42, .7\}$ 

We now examine simulations where we vary the  $\rho$  vector for the SBM with the following parameters:

$$B = \begin{bmatrix} .42 & .2 \\ .2 & .7 \end{bmatrix}, \qquad N = 500, \qquad M = 100$$

Law of Large Graphs 3

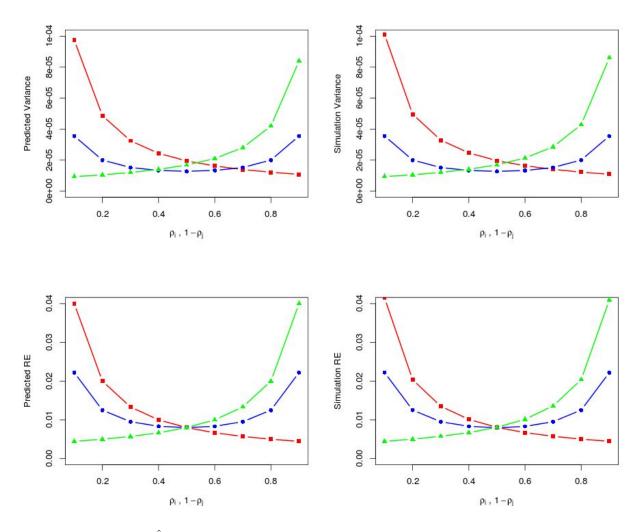


Figure 2: N\*Variance( $\hat{P}$ ) and RE, plots on the left are Predicted values corresponding to the right plot and each color represents unique values within the true  $P \in \{.2, .42, .7\}$ 

## 5 Real Data

## 6 Discussion