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# Law of Large Graphs

### 1 Introduction

OCP/HCP/FCP connectome setting examples of  $\bar{A}$  being used work done with ASE/SBM [1] [3] [4] [5]

## 2 Background and Notation

RDPG SBM ASE ARE [7] [9]

## 3 Theory/Proof

Proof for asymptotic variance of  $\hat{P}$ Will lead into relative efficiency [2]

## 4 Simulations

Simulations for Asymptotic variance of  $\hat{P}$  varying N and M. Simulations for relative efficiency modifying  $\rho$ 

#### 5 Real Data

Estimates of Population Means of connectomes Show Difference between  $\bar{A}$  and  $\hat{P}$  cross-validation perhaps currently working on FCP data

#### 6 Discussion

[6] NMF

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### References

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