## **Batch Normalization**

One way to make deep networks easier to train is to use more sophisticated optimization procedures such as SGD+momentum, RMSProp, or Adam. Another strategy is to change the architecture of the network to make it easier to train. One idea along these lines is batch normalization which was proposed by [3] in 2015.

The idea is relatively straightforward. Machine learning methods tend to work better when their input data consists of uncorrelated features with zero mean and unit variance. When training a neural network, we can preprocess the data before feeding it to the network to explicitly decorrelate its features; this will ensure that the first layer of the network sees data that follows a nice distribution. However, even if we preprocess the input data, the activations at deeper layers of the network will likely no longer be decorrelated and will no longer have zero mean or unit variance since they are output from earlier layers in the network. Even worse, during the training process the distribution of features at each layer of the network will shift as the weights of each layer are updated.

The authors of [3] hypothesize that the shifting distribution of features inside deep neural networks may make training deep networks more difficult. To overcome this problem, [3] proposes to insert batch normalization layers into the network. At training time, a batch normalization layer uses a minibatch of data to estimate the mean and standard deviation of each feature. These estimated means and standard deviations are then used to center and normalize the features of the minibatch. A running average of these means and standard deviations is kept during training, and at test time these running averages are used to center and normalize features.

It is possible that this normalization strategy could reduce the representational power of the network, since it may sometimes be optimal for certain layers to have features that are not zero-mean or unit variance. To this end, the batch normalization layer includes learnable shift and scale parameters for each feature dimension.

[3] Sergey Ioffe and Christian Szegedy, "Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift", ICML 2015.

### In [2]:

```
# As usual, a bit of setup
import time
import numpy as np
import matplotlib.pyplot as plt
from cs231n.classifiers.fc_net import
from cs231n.data_utils import get CIFAR10 data
from cs231n.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
from cs231n.solver import Solver
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'
# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load ext autoreload
%autoreload 2
def rel error(x, y):
    """ returns relative error """
   return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
def print mean std(x,axis=0):
   print(' means: ', x.mean(axis=axis))
   print(' stds: ', x.std(axis=axis))
   print()
print ("done with setup")
```

done with setup

## In [3]:

```
# Load the (preprocessed) CIFAR10 data.
data = get_CIFAR10_data()
for k, v in data.items():
   print('%s: ' % k, v.shape)
print ("done loading")
```

```
X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
done loading
```

## **Batch normalization: forward**

In the file cs231n/layers.py, implement the batch normalization forward pass in the function batchnorm\_forward. Once you have done so, run the following to test your implementation.

Referencing the paper linked to above would be helpful!

```
In [4]:
# Check the training-time forward pass by checking means and variances
# of features both before and after batch normalization
# Simulate the forward pass for a two-layer network
np.random.seed(231)
N, D1, D2, D3 = 200, 50, 60, 3
X = np.random.randn(N, D1)
W1 = np.random.randn(D1, D2)
W2 = np.random.randn(D2, D3)
a = np.maximum(0, X.dot(W1)).dot(W2)
print('Before batch normalization:')
print mean std(a,axis=0)
gamma = np.ones((D3,))
beta = np.zeros((D3,))
# Means should be close to zero and stds close to one
print('After batch normalization (gamma=1, beta=0)')
a norm, = batchnorm forward(a, gamma, beta, {'mode': 'train'})
print mean std(a norm,axis=0)
gamma = np.asarray([1.0, 2.0, 3.0])
beta = np.asarray([11.0, 12.0, 13.0])
# Now means should be close to beta and stds close to gamma
print('After batch normalization (gamma=', gamma, ', beta=', beta, ')')
a norm, = batchnorm forward(a, gamma, beta, {'mode': 'train'})
print_mean_std(a_norm,axis=0)
# all checks out fine :) with two differenormalization of different parameters
Before batch normalization:
 means: [ -2.3814598 -13.18038246 1.91780462]
  stds: [27.18502186 34.21455511 37.68611762]
After batch normalization (gamma=1, beta=0)
  means: [ 1.33226763e-17 -3.94129174e-17 3.29597460e-17]
  stds: [0.99999999 1.
                                1.
After batch normalization (gamma= [1. 2. 3.], beta= [11. 12. 13.])
  means: [11. 12. 13.]
          [0.9999999 1.99999999 2.99999999]
In [5]:
```

```
# Check the test-time forward pass by running the training-time
# forward pass many times to warm up the running averages, and then
# checking the means and variances of activations after a test-time
# forward pass.

np.random.seed(231)
N, D1, D2, D3 = 200, 50, 60, 3
W1 = np.random.randn(D1, D2)
W2 = np.random.randn(D2, D3)
```

```
bn param = {'mode': 'train'}
gamma = np.ones(D3)
beta = np.zeros(D3)
# personal notes ->
# purpose here : keep an exponentially decaying running mean of the
# mean and variance of each feature, and these averages are used to normalize
# data at test-time
for t in range (50):
 X = np.random.randn(N, D1)
  a = np.maximum(0, X.dot(W1)).dot(W2)
  batchnorm_forward(a, gamma, beta, bn_param)
bn_param['mode'] = 'test'
X = np.random.randn(N, D1)
a = np.maximum(0, X.dot(W1)).dot(W2)
a_norm, _ = batchnorm_forward(a, gamma, beta, bn_param)
# Means should be close to zero and stds close to one, but will be
# noisier than training-time forward passes.
print('After batch normalization (test-time):')
print mean std(a norm,axis=0)
After batch normalization (test-time):
  means: [-0.03927354 -0.04349152 -0.10452688]
 stds:
          [1.01531428 1.01238373 0.97819988]
```

### **Batch normalization: backward**

Now implement the backward pass for batch normalization in the function  ${\tt batchnorm\_backward}$ .

To derive the backward pass you should write out the computation graph for batch normalization and backprop through each of the intermediate nodes. Some intermediates may have multiple outgoing branches; make sure to sum gradients across these branches in the backward pass.

Once you have finished, run the following to numerically check your backward pass.

```
In [11]:
```

```
# Gradient check batchnorm backward pass
np.random.seed (231)
N, D = 4, 5
x = 5 * np.random.randn(N, D) + 12
gamma = np.random.randn(D)
beta = np.random.randn(D)
dout = np.random.randn(N, D)
bn param = {'mode': 'train'}
fx = lambda x: batchnorm forward(x, gamma, beta, bn param)[0]
fg = lambda a: batchnorm_forward(x, a, beta, bn_param)[0]
fb = lambda b: batchnorm forward(x, gamma, b, bn param)[0]
dx_num = eval_numerical_gradient_array(fx, x, dout)
da_num = eval_numerical_gradient_array(fg, gamma.copy(), dout)
db num = eval numerical gradient array(fb, beta.copy(), dout)
 , cache = batchnorm forward(x, gamma, beta, bn param)
dx, dgamma, dbeta = batchnorm backward(dout, cache)
#You should expect to see relative errors between 1e-13 and 1e-8
print('dx error: ', rel error(dx num, dx))
print('dgamma error: ', rel_error(da_num, dgamma))
print('dbeta error: ', rel_error(db_num, dbeta))
dx error: 1.7029258328157158e-09
```

Batch normalization: alternative backward

dgamma error: 7.420414216247087e-13 dbeta error: 2.8795057655839487e-12 In class we talked about two different implementations for the sigmoid backward pass. One strategy is to write out a computation graph composed of simple operations and backprop through all intermediate values. Another strategy is to work out the derivatives on paper. For example, you can derive a very simple formula for the sigmoid function's backward pass by simplifying gradients on paper.

Surprisingly, it turns out that you can do a similar simplification for the batch normalization backward pass too.

Given a set of inputs  $X=\left(1_{N}\sum_{k=1}^N x_k$  and variance  $v=\frac{1}{N}\sum_{k=1}^N (x_k-y_k)^2.$ 

The meat of our problem is to get  $\frac{L}{\partial L}{\partial X}\$  from the upstream gradient  $\frac{L}{\partial L}\$  It might be challenging to directly reason about the gradients over \$X\$ and \$Y\$ - try reasoning about it in terms of \$x\_i\$ and \$y\_i\$ first.

You will need to come up with the derivations for  $\frac{\pi x_i}{\pi x_i}$ , by relying on the Chain Rule to first calculate the intermediate  $\frac{\pi x_i}{\pi x_i}$ ,  $\frac{x_i}{\pi x_i}$ . You should make sure each of the intermediary steps are all as simple as possible.

After doing so, implement the simplified batch normalization backward pass in the function <code>batchnorm\_backward\_alt</code> and compare the two implementations by running the following. Your two implementations should compute nearly identical results, but the alternative implementation should be a bit faster.

### In [12]:

```
np.random.seed (231)
N, D = 100, 500
x = 5 * np.random.randn(N, D) + 12
gamma = np.random.randn(D)
beta = np.random.randn(D)
dout = np.random.randn(N, D)
bn param = {'mode': 'train'}
out, cache = batchnorm forward(x, gamma, beta, bn param)
t1 = time.time()
dx1, dgamma1, dbeta1 = batchnorm backward(dout, cache)
t.2 = t.ime.t.ime()
dx2, dgamma2, dbeta2 = batchnorm backward alt(dout, cache)
t3 = time.time()
print('dx difference: ', rel_error(dx1, dx2))
print('dgamma difference: ', rel_error(dgamma1, dgamma2))
print('dbeta difference: ', rel error(dbeta1, dbeta2))
print('speedup: %.2fx' % ((t2 - t1) / (t3 - t2)))
dx difference: 9.20004371222927e-13
dgamma difference: 0.0
dbeta difference: 0.0
```

# **Fully Connected Nets with Batch Normalization**

Now that you have a working implementation for batch normalization, go back to your FullyConnectedNet in the file cs231n/classifiers/fc net.py . Modify your implementation to add batch normalization.

Concretely, when the normalization flag is set to "batchnorm" in the constructor, you should insert a batch normalization layer before each ReLU nonlinearity. The outputs from the last layer of the network should not be normalized. Once you are done, run the following to gradient-check your implementation.

HINT: You might find it useful to define an additional helper layer similar to those in the file  $cs231n/layer\_utils.py$ . If you decide to do so, do it in the file cs231n/classifiers/fc net.py.

### In [13]:

speedup: 1.25x

```
np.random.seed(231)
N, D, H1, H2, C = 2, 15, 20, 30, 10
X = np.random.randn(N, D)
y = np.random.randint(C, size=(N,))
# You should expect losses between 1e-4~1e-10 for W,
```

```
# losses between 1e-08~1e-10 for b,
# and losses between 1e-08~1e-09 for beta and gammas.
for reg in [0, 3.14]:
 print('Running check with reg = ', reg)
  model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                            reg=reg, weight scale=5e-2, dtype=np.float64,
                            use batchnorm=True)
  loss, grads = model.loss(X, y)
  print('Initial loss: ', loss)
  for name in sorted(grads):
   f = lambda : model.loss(X, y)[0]
    grad num = eval numerical gradient(f, model.params[name], verbose=False, h=1e-5)
    print('%s relative error: %.2e' % (name, rel error(grad num, grads[name])))
  if reg == 0: print()
print ("\n\n** done here ")
Running check with reg = 0
Initial loss: 2.2611955101340957
W1 relative error: 1.10e-04
W2 relative error: 2.85e-06
W3 relative error: 3.92e-10
b1 relative error: 4.44e-08
b2 relative error: 2.22e-08
b3 relative error: 4.78e-11
betal relative error: 7.33e-09
beta2 relative error: 1.89e-09
gamma1 relative error: 7.57e-09
gamma2 relative error: 1.96e-09
Running check with reg = 3.14
Initial loss: 6.996533220108303
W1 relative error: 1.98e-06
W2 relative error: 2.28e-06
W3 relative error: 1.11e-08
b1 relative error: 0.00e+00
b2 relative error: 2.22e-08
b3 relative error: 2.23e-10
betal relative error: 6.65e-09
beta2 relative error: 3.48e-09
gamma1 relative error: 5.94e-09
gamma2 relative error: 4.14e-09
   done here
```

# **Batchnorm for deep networks**

Run the following to train a six-layer network on a subset of 1000 training examples both with and without batch normalization.

### In [14]:

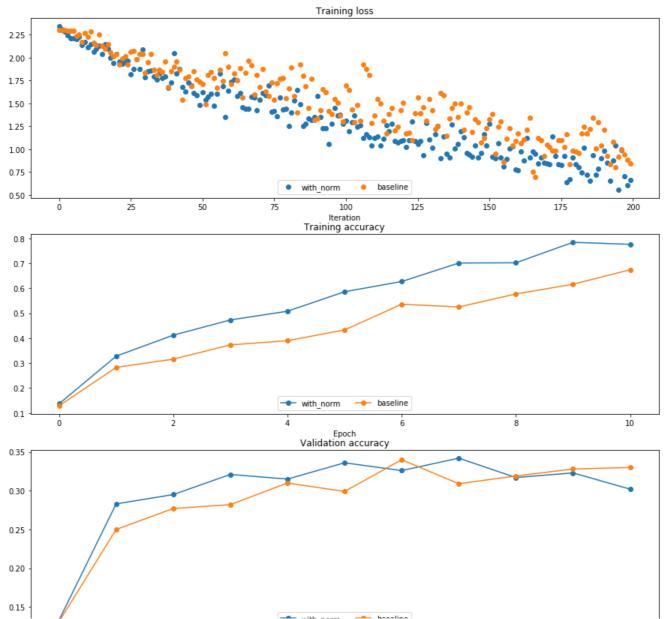
```
np.random.seed(231)
# Try training a very deep net with batchnorm
hidden dims = [100, 100, 100, 100, 100]
num train = 1000
small data = {
  'X_train': data['X_train'][:num_train],
  'y_train': data['y_train'][:num_train],
  'X val': data['X val'],
  'y_val': data['y_val'],
weight scale = 2e-2
bn model = FullyConnectedNet(hidden dims, weight scale=weight scale, use batchnorm=True)
model = FullyConnectedNet(hidden dims, weight scale=weight scale, use batchnorm=False)
bn solver = Solver(bn model, small data,
               num epochs=10, batch size=50,
                update rule='adam',
                optim config={
                  'learning rate' 10-3
```

```
TEATHTHY_TALE . TE J,
                verbose=True,print every=20)
bn solver.train()
print ("\n^{**} BN model done training\n^{"})
solver = Solver(model, small data,
                num epochs=10, batch size=50,
                update rule='adam',
                optim config={
                  'learning_rate': 1e-3,
                verbose=True, print every=20)
solver.train()
print ("\n^{**} normal model done training\n^{"})
print ("\n^*
               done training")
(Iteration 1 / 200) loss: 2.340974
(Epoch 0 / 10) train acc: 0.137000; val acc: 0.133000
(Epoch 1 / 10) train acc: 0.328000; val acc: 0.283000
(Iteration 21 / 200) loss: 2.039345
(Epoch 2 / 10) train acc: 0.412000; val acc: 0.295000
(Iteration 41 / 200) loss: 2.047471
(Epoch 3 / 10) train acc: 0.473000; val acc: 0.321000
(Iteration 61 / 200) loss: 1.739554
(Epoch 4 / 10) train acc: 0.508000; val_acc: 0.315000
(Iteration 81 / 200) loss: 1.251670
(Epoch 5 / 10) train acc: 0.586000; val_acc: 0.336000
(Iteration 101 / 200) loss: 1.312088
(Epoch 6 / 10) train acc: 0.627000; val acc: 0.326000
(Iteration 121 / 200) loss: 1.100514
(Epoch 7 / 10) train acc: 0.701000; val acc: 0.342000
(Iteration 141 / 200) loss: 1.198495
(Epoch 8 / 10) train acc: 0.702000; val acc: 0.317000
(Iteration 161 / 200) loss: 0.764990
(Epoch 9 / 10) train acc: 0.784000; val acc: 0.323000
(Iteration 181 / 200) loss: 0.833378
(Epoch 10 / 10) train acc: 0.776000; val acc: 0.302000
** BN model done training
(Iteration 1 / 200) loss: 2.302332
(Epoch 0 / 10) train acc: 0.129000; val acc: 0.131000
(Epoch 1 / 10) train acc: 0.283000; val acc: 0.250000
(Iteration 21 / 200) loss: 2.041970
(Epoch 2 / 10) train acc: 0.316000; val_acc: 0.277000
(Iteration 41 / 200) loss: 1.900473
(Epoch 3 / 10) train acc: 0.373000; val_acc: 0.282000
(Iteration 61 / 200) loss: 1.713157
(Epoch 4 / 10) train acc: 0.390000; val acc: 0.310000
(Iteration 81 / 200) loss: 1.660097
(Epoch 5 / 10) train acc: 0.433000; val acc: 0.299000
(Iteration 101 / 200) loss: 1.698795
(Epoch 6 / 10) train acc: 0.536000; val_acc: 0.340000
(Iteration 121 / 200) loss: 1.505215
(Epoch 7 / 10) train acc: 0.525000; val_acc: 0.309000
(Iteration 141 / 200) loss: 1.502351
(Epoch 8 / 10) train acc: 0.577000; val acc: 0.319000
(Iteration 161 / 200) loss: 1.174019
(Epoch 9 / 10) train acc: 0.616000; val acc: 0.328000
(Iteration 181 / 200) loss: 0.970633
(Epoch 10 / 10) train acc: 0.674000; val acc: 0.330000
** normal model done training
    done training
```

Run the following to visualize the results from two networks trained above. You should find that using batch normalization helps the network to converge much faster.

```
In [15]:
def plot_training_history(title, label, baseline, bn_solvers, plot_fn, bl_marker='.', bn_marker='.'
, labels=None):
```

```
"""utility function for plotting training history"""
    plt.title(title)
    plt.xlabel(label)
    bn plots = [plot fn(bn solver) for bn solver in bn solvers]
    bl_plot = plot_fn(baseline)
    num bn = len(bn plots)
    for i in range(num bn):
        label='with_norm'
        if labels is not None:
            label += str(labels[i])
        plt.plot(bn_plots[i], bn_marker, label=label)
    label='baseline'
    if labels is not None:
       label += str(labels[0])
    plt.plot(bl_plot, bl_marker, label=label)
    plt.legend(loc='lower center', ncol=num bn+1)
plt.subplot(3, 1, 1)
plot training history('Training loss','Iteration', solver, [bn solver], \
                      lambda x: x.loss history, bl marker='o', bn marker='o')
plt.subplot(3, 1, 2)
plot training history('Training accuracy', 'Epoch', solver, [bn solver], \
                      lambda x: x.train acc history, bl marker='-o', bn marker='-o')
plt.subplot(3, 1, 3)
plot training history('Validation accuracy', 'Epoch', solver, [bn solver], \
                      lambda x: x.val_acc_history, bl_marker='-o', bn_marker='-o')
plt.gcf().set size inches(15, 15)
plt.show()
```



## Batch normalization and initialization

We will now run a small experiment to study the interaction of batch normalization and weight initialization.

The first cell will train 8-layer networks both with and without batch normalization using different scales for weight initialization. The second layer will plot training accuracy, validation set accuracy, and training loss as a function of the weight initialization scale.

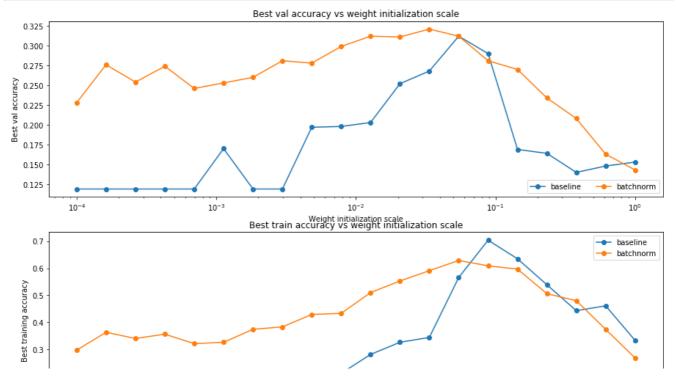
```
In [16]:
```

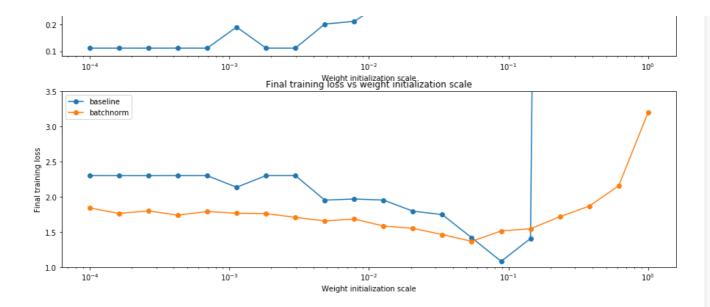
```
np.random.seed (231)
# Try training a very deep net with batchnorm
hidden dims = [50, 50, 50, 50, 50, 50, 50]
num train = 1000
small data = {
  'X_train': data['X_train'][:num_train],
  'y train': data['y train'][:num train],
  'X val': data['X_val'],
  'y_val': data['y_val'],
bn_solvers_ws = {}
solvers ws = {} {} {} {} {} {} {} {} {}
weight_scales = np.logspace(-4, 0, num=20)
for i, weight scale in enumerate (weight scales):
  print('Running weight scale %d / %d' % (i + 1, len(weight_scales)))
  bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=True)
  model = FullyConnectedNet(hidden dims, weight scale=weight scale, use batchnorm=False)
  bn solver = Solver(bn model, small data,
                   num epochs=10, batch size=50,
                   update_rule='adam',
                   optim config={
                     'learning_rate': 1e-3,
                   verbose=False, print every=200)
  bn solver.train()
  bn_solvers_ws[weight_scale] = bn_solver
  solver = Solver(model, small data,
                  num epochs=10, batch size=50,
                   update rule='adam',
                   optim config={
                     'learning rate': 1e-3,
                   verbose=False, print every=200)
  solver.train()
  solvers_ws[weight_scale] = solver
print ("\n\n** done training")
Running weight scale 1 / 20
```

```
Running weight scale 2 / 20
Running weight scale 3 / 20
Running weight scale 4 / 20
Running weight scale 5 / 20
Running weight scale 6 / 20
Running weight scale 7 / 20
Running weight scale 8 / 20
Running weight scale 9 / 20
Running weight scale 10 / 20
Running weight scale 11 / 20
Running weight scale 12 / 20
Running weight scale 13 / 20
Running weight scale 14 / 20
Running weight scale 15 / 20
Running weight scale 16 / 20
Running weight scale 17 / 20
Running weight scale 18\ /\ 20
Running weight scale 19 / 20
Running weight scale 20 / 20
```

#### In [17]:

```
# Plot results of weight scale experiment
best train accs, bn best train accs = [], []
best val accs, bn best val accs = [], []
final train loss, bn final train loss = [], []
for ws in weight scales:
  best train accs.append(max(solvers ws[ws].train acc history))
  bn best train accs.append(max(bn solvers ws[ws].train acc history))
 best val accs.append(max(solvers ws[ws].val acc history))
 bn_best_val_accs.append(max(bn_solvers_ws[ws].val_acc_history))
  final train loss.append(np.mean(solvers ws[ws].loss history[-100:]))
 bn_final_train_loss.append(np.mean(bn_solvers_ws[ws].loss_history[-100:]))
plt.subplot(3, 1, 1)
plt.title('Best val accuracy vs weight initialization scale')
plt.xlabel('Weight initialization scale')
plt.ylabel('Best val accuracy')
plt.semilogx(weight scales, best val accs, '-o', label='baseline')
plt.semilogx(weight_scales, bn_best_val_accs, '-o', label='batchnorm')
plt.legend(ncol=2, loc='lower right')
plt.subplot(3, 1, 2)
plt.title('Best train accuracy vs weight initialization scale')
plt.xlabel('Weight initialization scale')
plt.ylabel('Best training accuracy')
plt.semilogx(weight_scales, best_train_accs, '-o', label='baseline')
plt.semilogx(weight_scales, bn_best_train_accs, '-o', label='batchnorm')
plt.legend()
plt.subplot(3, 1, 3)
plt.title('Final training loss vs weight initialization scale')
plt.xlabel('Weight initialization scale')
plt.ylabel('Final training loss')
plt.semilogx(weight scales, final train loss, '-o', label='baseline')
plt.semilogx(weight scales, bn final train loss, '-o', label='batchnorm')
plt.legend()
plt.gca().set ylim(1.0, 3.5)
plt.gcf().set size inches(15, 15)
plt.show()
```





## **Inline Question 1:**

Describe the results of this experiment. How does the scale of weight initialization affect models with/without batch normalization differently, and why?

### **Answer:**

A very small weight intialization scale makes the batchnormalizatio lead to better results in train accurracy, minimal loss and validation accuracy. Batchnorm favour the small weight scales. Also important to note is that the batch norm trained network is more robust to the scale of weight initialisation for weight initializations betlow 1. Also important to note is that the baseline model training loss explodes when the weight initialisation is too large(very close to 1) while this does not happen to the batchnorm network. Through normalizing outputs of each layer, the batchnorm model becomes more robust and better.

## Batch normalization and batch size

We will now run a small experiment to study the interaction of batch normalization and batch size.

The first cell will train 6-layer networks both with and without batch normalization using different batch sizes. The second layer will plot training accuracy and validation set accuracy over time.

## In [18]:

```
def run_batchsize_experiments(normalization_mode):
    np.random.seed(231)
    # Try training a very deep net with batchnorm
    hidden dims = [100, 100, 100, 100, 100]
    num train = 1000
    small data = {
      'X train': data['X train'][:num train],
      'y_train': data['y_train'][:num_train],
      'X val': data['X val'],
      'y val': data['y val'],
    n epochs=10
    weight_scale = 2e-2
    batch sizes = [5,10,50]
    lr = 10**(-3.5)
    solver_bsize = batch_sizes[0]
    print('No normalization: batch size = ',solver_bsize)
    model = FullyConnectedNet(hidden dims, weight scale=weight scale, use batchnorm=False)
    solver = Solver(model, small data,
                    num_epochs=n_epochs, batch_size=solver_bsize,
                    update rule='adam',
                    optim config={
                      'learning_rate': lr,
                    verbose=False)
    solver.train()
```

```
bn solvers = []
    for i in range(len(batch sizes)):
        b size=batch sizes[i]
        print('Normalization: batch size = ',b size)
        bn model = FullyConnectedNet(hidden dims, weight scale=weight scale, use batchnorm=normaliz
ation mode)
        bn_solver = Solver(bn_model, small_data,
                         num_epochs=n_epochs, batch_size=b_size,
                         update rule='adam',
                         optim config={
                            'learning_rate': lr,
                         verbose=False)
        bn solver.train()
        bn solvers.append(bn solver)
    return bn solvers, solver, batch sizes
batch sizes = [5,10,50]
bn solvers bsize, solver bsize, batch sizes = run batchsize experiments(True)
print ("\n\n** done")
No normalization: batch size =
Normalization: batch size = 5
Normalization: batch size =
Normalization: batch size = 50
** done
In [19]:
plt.subplot(2, 1, 1)
plot_training_history('Training accuracy (Batch Normalization)','Epoch', solver_bsize,
bn solvers bsize, \
                       lambda x: x.train acc history, bl marker='-^', bn marker='-o', labels=batch s
zes)
plt.subplot(2, 1, 2)
plot training history('Validation accuracy (Batch Normalization)', 'Epoch', solver bsize,
bn solvers bsize, \
                       lambda x: x.val acc history, bl marker='-^', bn marker='-o', labels=batch siz
plt.gcf().set_size_inches(15, 10)
plt.show()
                                       Training accuracy (Batch Normalization)
 0.8
 0.7
 0.6
 0.5
 0.4
 0.3
 0.2
                                 with_norm5
                                          with_norm10
                                                       with_norm50
 0.1
                                                               6
                                                                                 8
                                                                                                   10
                                                    Epoch
                                       Validation accuracy (Batch Normalization)
0.35
0.30
0.25
 0.20
```



## **Inline Question 2:**

Describe the results of this experiment. What does this imply about the relationship between batch normalization and batch size? Why is this relationship observed?

### **Answer:**

This validates the representational power of a batch size in training, as it is representative of the whole training set. Increase in the batch size correlates the perfomance of the classification significantly in training, and the effects are less dominant in the validation batch sizes, as here the trained model is not changing, but more samples representative of the whole training set, increase its perfomance slightly.

## **Layer Normalization**

Batch normalization has proved to be effective in making networks easier to train, but the dependency on batch size makes it less useful in complex networks which have a cap on the input batch size due to hardware limitations.

Several alternatives to batch normalization have been proposed to mitigate this problem; one such technique is Layer Normalization [4]. Instead of normalizing over the batch, we normalize over the features. In other words, when using Layer Normalization, each feature vector corresponding to a single datapoint is normalized based on the sum of all terms within that feature vector.

[4] Ba, Jimmy Lei, Jamie Ryan Kiros, and Geoffrey E. Hinton. "Layer Normalization." stat 1050 (2016): 21.

### **Inline Question 3:**

Which of these data preprocessing steps is analogous to batch normalization, and which is analogous to layer normalization?

- 1. Scaling each image in the dataset, so that the RGB channels for each row of pixels within an image sums up to 1.
- 2. Scaling each image in the dataset, so that the RGB channels for all pixels within an image sums up to 1.
- 3. Subtracting the mean image of the dataset from each image in the dataset.
- 4. Setting all RGB values to either 0 or 1 depending on a given threshold.

### **Answer:**

batch normalization: 3 & 2.

layer normalization: 1

4 is more activation or dropping (I might be wrong)

# **Layer Normalization: Implementation**

Now you'll implement layer normalization. This step should be relatively straightforward, as conceptually the implementation is almost identical to that of batch normalization. One significant difference though is that for layer normalization, we do not keep track of the moving moments, and the testing phase is identical to the training phase, where the mean and variance are directly calculated per datapoint.

Here's what you need to do:

• In cs231n/layers.py, implement the forward pass for layer normalization in the function layernorm forward.

Run the cell below to check your results.

• In cs231n/layers.py, implement the backward pass for layer normalization in the function layernorm backward.

Run the second cell below to check your results.

• Modify cs231n/classifiers/fc\_net.py to add layer normalization to the FullyConnectedNet . When the normalization flag is set to "layernorm" in the constructor, you should insert a layer normalization layer before each ReLU nonlinearity.

Run the third cell below to run the batch size experiment on layer normalization.

```
In [21]:
```

```
# Check the training-time forward pass by checking means and variances
# of features both before and after layer normalization
# Simulate the forward pass for a two-layer network
np.random.seed(231)
N, D1, D2, D3 = 4, 50, 60, 3
X = np.random.randn(N, D1)
W1 = np.random.randn(D1, D2)
W2 = np.random.randn(D2, D3)
a = np.maximum(0, X.dot(W1)).dot(W2)
print('Before layer normalization:')
print mean std(a,axis=1)
gamma = np.ones(D3)
beta = np.zeros(D3)
# Means should be close to zero and stds close to one
print('After layer normalization (gamma=1, beta=0)')
a_norm, _ = layernorm_forward(a, gamma, beta, {'mode': 'train'})
print mean std(a norm,axis=1)
gamma = np.asarray([3.0,3.0,3.0])
beta = np.asarray([5.0, 5.0, 5.0])
# Now means should be close to beta and stds close to gamma
print('After layer normalization (gamma=', gamma, ', beta=', beta, ')')
a norm, = layernorm forward(a, gamma, beta, {'mode': 'train'})
print mean std(a norm,axis=1)
print ("\n\n** done")
Before layer normalization:
 means: [-59.06673243 -47.60782686 -43.31137368 -26.40991744]
          [10.07429373 28.39478981 35.28360729 4.01831507]
After layer normalization (gamma=1, beta=0)
 means: [ 4.81096644e-16  0.00000000e+00  0.00000000e+00  -2.96059473e-16]
  stds: [0.99999995 0.99999999 1.
                                            0.999999691
After layer normalization (gamma= [3. 3. 3.], beta= [5. 5. 5.])
 means: [5. 5. 5. 5.]
  stds: [2.99999985 2.99999998 2.99999999 2.99999907]
** done
```

### In [23]:

```
# Gradient check batchnorm backward pass
np.random.seed(231)
N, D = 4, 5
x = 5 * np.random.randn(N, D) + 12
gamma = np.random.randn(D)
beta = np.random.randn(D)
dout = np.random.randn(N, D)
ln param = {}
fx = lambda x: layernorm_forward(x, gamma, beta, ln_param)[0]
fg = lambda a: layernorm forward(x, a, beta, ln param)[0]
fb = lambda b: layernorm forward(x, gamma, b, ln param)[0]
dx num = eval numerical gradient array(fx, x, dout)
da_num = eval_numerical_gradient_array(fg, gamma.copy(), dout)
db_num = eval_numerical_gradient_array(fb, beta.copy(), dout)
, cache = layernorm forward(x, gamma, beta, ln param)
dx, dgamma, dbeta = layernorm backward(dout, cache)
```

```
#You should expect to see relative errors between 1e-12 and 1e-8
print('dx error: ', rel_error(dx_num, dx))
print('dgamma error: ', rel_error(da_num, dgamma))
print('dbeta error: ', rel_error(db_num, dbeta))
```

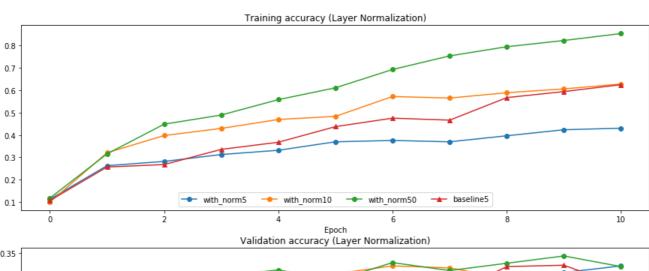
dx error: 1.433616168873336e-09 dgamma error: 4.519489546032799e-12 dbeta error: 2.276445013433725e-12

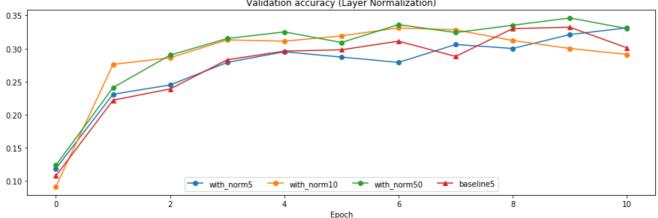
# Layer Normalization and batch size

We will now run the previous batch size experiment with layer normalization instead of batch normalization. Compared to the previous experiment, you should see a markedly smaller influence of batch size on the training history!

#### In [25]:

No normalization: batch size = 5 Normalization: batch size = 5 Normalization: batch size = 10 Normalization: batch size = 50





## **Inline Question 4:**

When is layer normalization likely to not work well, and why?

- 1. Using it in a very deep network
- 2. Having a very small dimension of features
- 3. Having a high regularization term

## **Answer:**

with ledd dimensions, the feature statistics of mean and variance will not be of good quality and thus not very good general classification.

In [ ]: