



Chapter 4

Listen

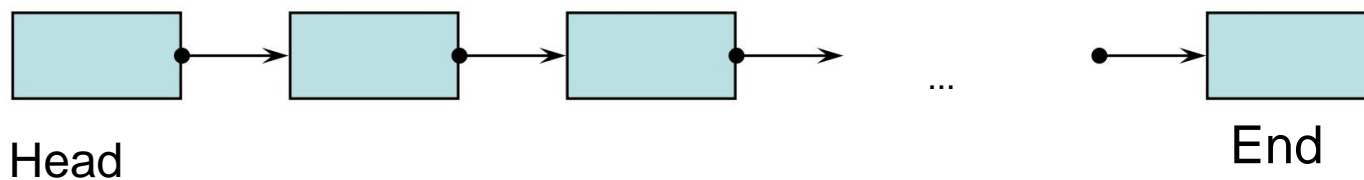
4.1 Definition Listen

A (linear) list is a data structure for managing an **arbitrarily large number** of elements of a **uniform type**.

Access to the individual elements of a (simple) list is only possible from **Head** off possible.

The **end** of the list is also called the **tail** .

The elements are arranged in a **sequence** that can (usually) be derived from the **order of entries** (disordered).





abstraction

Data structures represent an abstraction of a
conceptual model

Concept of **Abstract Data Type (ADT)**

Says nothing about the physical realization on the computer

Various realizations conceivable!

Realization often depends on the problem, programming environment,
objectives, ...

Possible conceptual model “list”

“String of pearls”, beads are threaded at one end

The definition:

- A list L is an ordered set of elements $L = (x_1, x_2, \dots, x_n)$
- The length of a list is given by $|L| = |(x_1, x_2, \dots, x_n)| = n$
- An empty list has length 0.
- The i th element of a list L is denoted by $L[i]$, therefore $1 \leq i \leq |L|$



Methods on ADT list

Insert

Add: Insert element at the head

access

FirstElement: Determine head element

Delete

RemoveFirst: Remove head element

Generate

Constructor: Create new list

Length determination

Length: Determine the number of elements

Inclusion test

Member: Test whether element is included

Others
Operations conceivable

Declaration C++, Class

```
typedef ... ItemType;  
...  
class List {  
public:  
    List(); // Constructor void  
    Add(itemType a);  
    ItemType FirstElement(); void  
    RemoveFirst();  
    int Length(); int  
    Member(itemType a);  
}
```

for use in classes
Def., better approach
with C++ templates

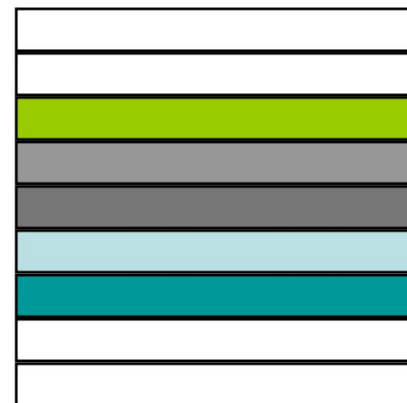
4.2 Implementation of lists

Storage types

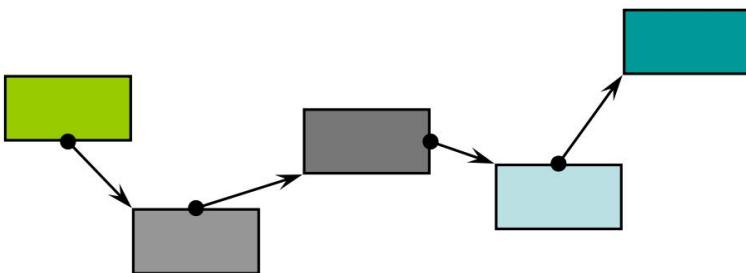
Contiguous memory



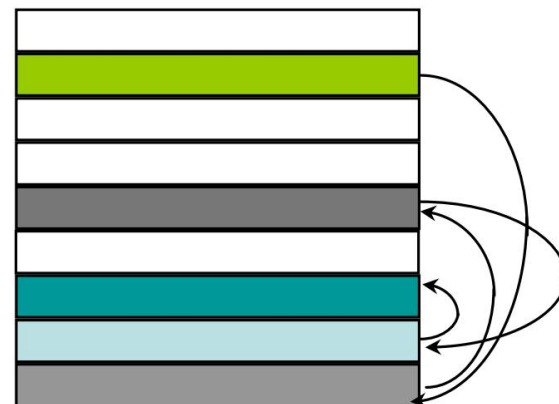
22200
22208
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Scattered (Linked) memory



22200
22208
22216
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22240
22248
22256
22264





Memory Typen

Contiguous memory

Physically **contiguous** storage area, extremely rigid as the final size is fixed when created.

Management via the **system**.

Data structures based on contiguous memory can only do one accommodate **a limited** number of items.

Scattered (Linked) memory

Physically distributed storage area, very **flexible** because of the extent can be **dynamically** adjusted.

Management (usually) via the **application program**.

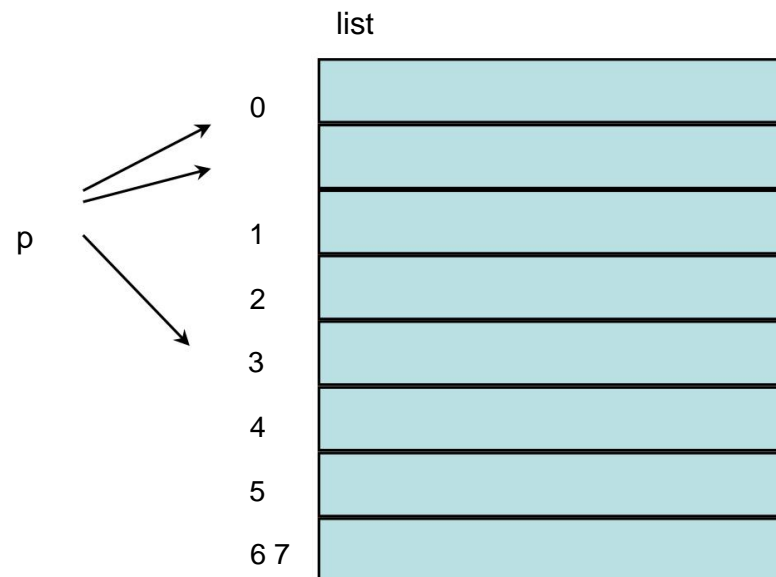
Data structures can be **of any size** .

4.2.1 List - static - structure

Statische Implementation - contiguous memory

Store the elements in a field of limited length

```
typedef int ItemType; class  
List {  
private:  
    ItemType list[8];  
        // data structure  
    int p; //  
        next free position  
    ...  
}
```



Length = 8

List - static - Create - Destroy - Insert



Generate,

```
List::List() {p = 0;}
```

Destroy

```
List::~~List() {p = 0;}
```

Insert

```
void List::Add(ItemType a) { if(p < 8) {
```

```
    list[p] = a;
```

```
    p++;
```

```
} else cout << "Error-add\n";
```

```
}
```





List - static - access - delete

access

```
ItemType List::FirstElement() { if(p > 0)
    return list[p-1]; else cout << "Error-
first\n";
}
```

Delete

```
void List::RemoveFirst() {
    if(p > 0) p--; else
    cout << "Error-remove\n";
}
```

List - static - Length - inclusion test



Long,

```
int List::Length() {  
    return p;  
}
```

Inclusion test

```
int List::Member(ItemType a) {  
    int i = 0;  
    while(i < p && list[i] != a) i++; if(i < p) return 1;  
    else return 0;  
}
```

4.2.2 List - dynamic - structure (1)

Dynamische Implementation - linked memory

Dynamically expandable list of unlimited length

```
typedef int ItemType;
```

```
class List
```

```
{ public:
```

```
    class Element {
```

// Element class

```
        ItemType value;
```

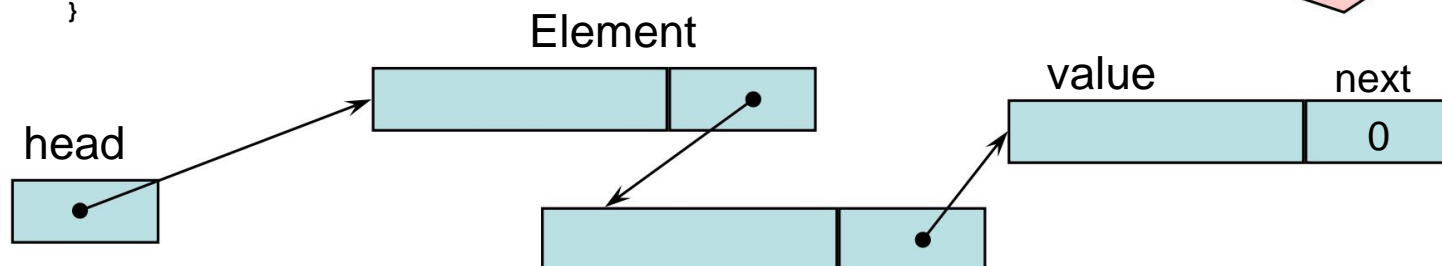
```
        Element* next;
```

```
    };
```

```
    Element* head; // DS Kopf
```

```
    ...
```

```
}
```



Recursive data structure

A data structure is called **recursive** or **circular** if it is in their definition itself references

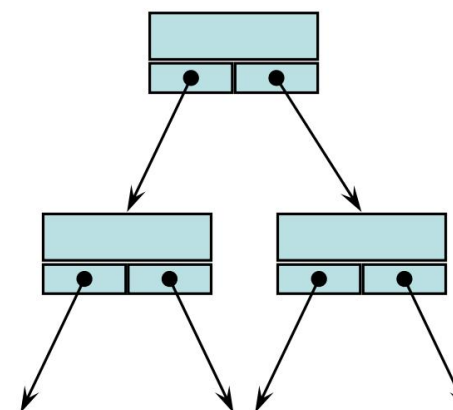
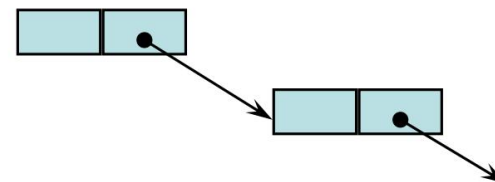
Basic model for dynamically extendable data structures

List

```
class Element{
    InfoType Info;
    Element* Next;
}
```

Baum

```
class Node {
    KeyType Key;
    Node* LeftChild;
    Node* RightChild;
}
```



List - dynamic - insert

Insert

```
void List::Add(ItemType a) {
```

```
    Element* help; help
```

```
    = new Element; help->next
```

```
    = head; help->value = a;
```

```
    head = help;
```

```
}
```

Typically at the
top of the list



Before inserting



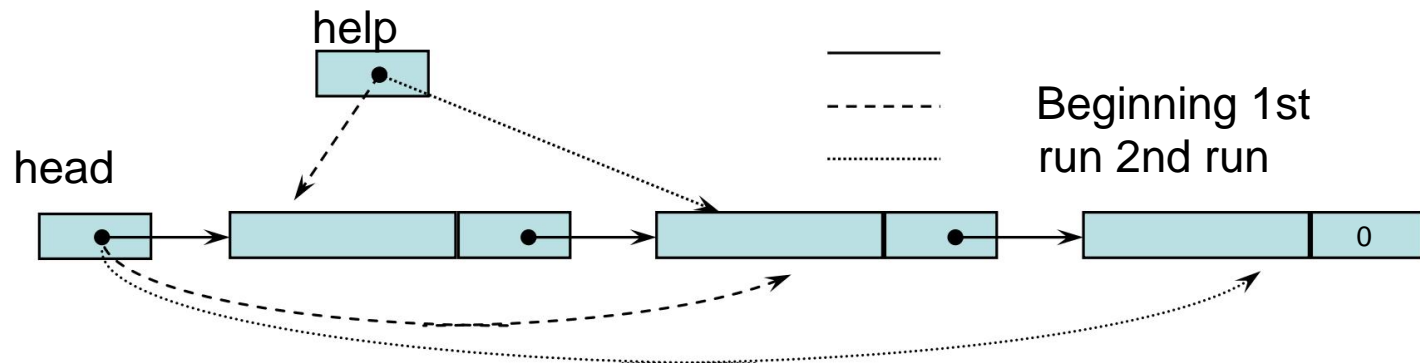
List - dynamic - Create - Destroy



Create, delete

```
List::List() { head = 0;}
```

```
List::~~List() {  
    Element* help;  
    while(head != 0) {  
        help = head;  
        head = head->next;  
        delete help;  
    }  
}
```





List - dynamic - access

access

```
ItemType List::FirstElement() {  
    if(head != 0)  
        return head->value;  
    else  
        cout << "Error-first\n";  
}
```

List - dynamic - delete

Delete

```
void List::RemoveFirst() {
    if(head != 0) {
        Element* help; help
        = head; head =
        head->next;
        delete help;
    } else cout << "Error-remove\n";
}
```



Before deleting



List - dynamic - length

Length

```
int List::Length() {
```

```
    Element* help = head; int
```

```
    length = 0; while(help !
```

```
    = 0) {
```

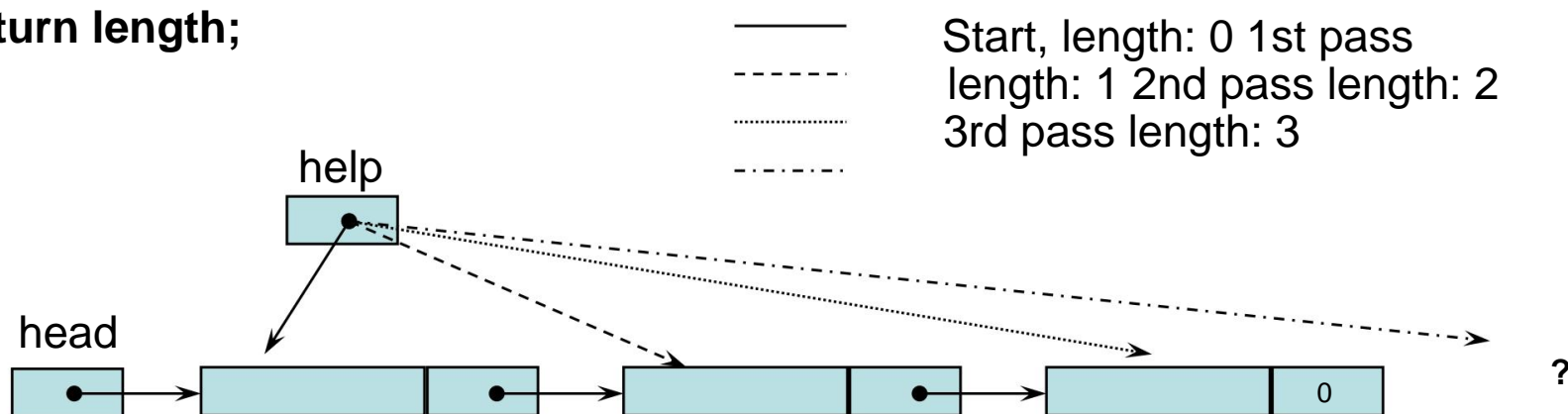
```
        length++;
```

```
        help = help->next;
```

```
    }
```

```
    return length;
```

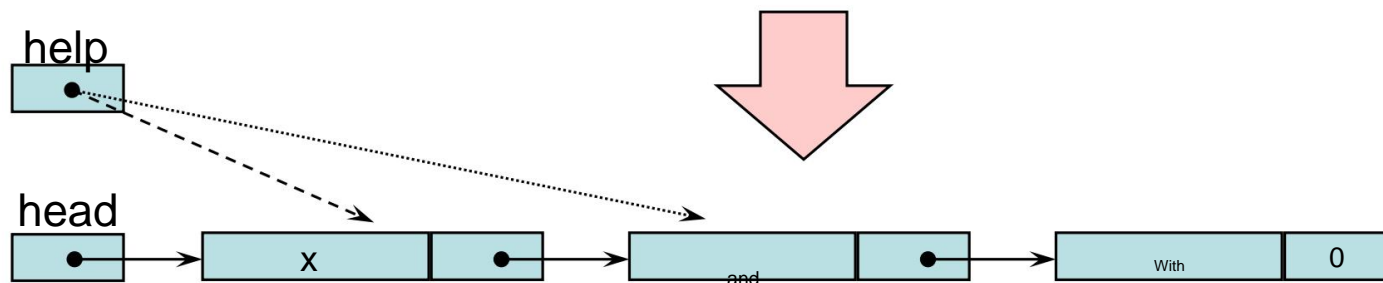
```
}
```



List - dynamic - inclusion test

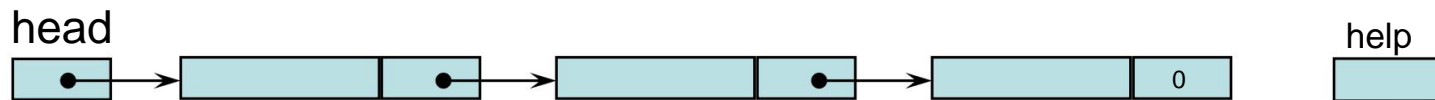
Inclusion test

```
int List::Member(ItemType a) {
    Element* help = head;
    while(help != 0 && help->value != a)
        help = help->next;
    if(help != 0) return 1;
    else return 0;
}
```



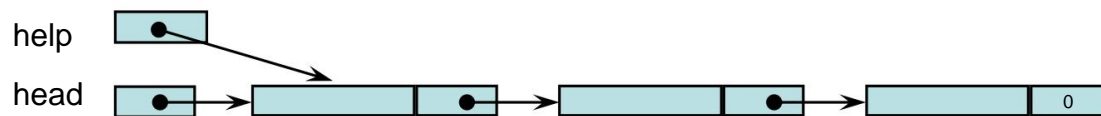
List - Ferries

Scheme for sequential processing of a list (iterative),
i.e. “visiting all elements”



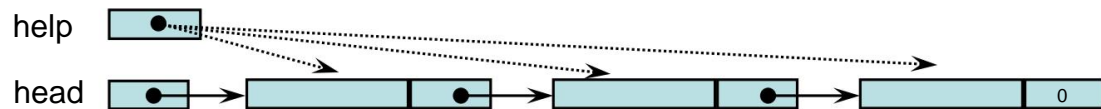
1. Initialize the auxiliary pointer

help = head;



2. Continue moving the auxiliary pointer (position)

help = help -> next;



3. Query for end of list (and search criterion)

while (help != 0 && ...) { ... }



4.3 Stack

The **stack (basement memory)** is a special case of the list that contains the Elements managed according to the **LIFO** (last-in, first-out) principle

Idea of the stack: You can only access the top, most recently placed element (compare book stacks, piles of wood, ...)

Applications: pushdown machines,
memory management, HP calculators (UPN), ...

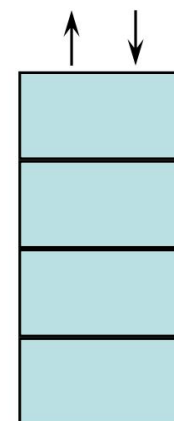
The behavior of the stack can be described by its (quite simple) operations

push: push element onto the stack

top: Access the top element of the stack

pop: Remove element from stack

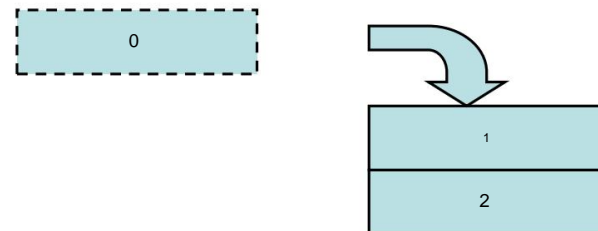
isEmpty: Test for empty stack



Methods on Stacks

Methode 'Push'

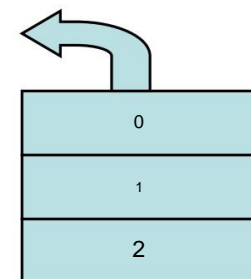
Element is placed on the stack (at the top position).



Method 'Top'

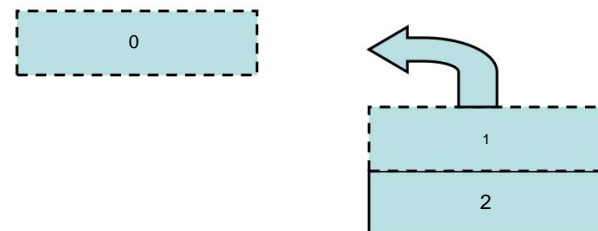
Returns the contents of the top element of the stack.

0



Method 'Pop'

Top element of the stack is removed.





Stack as a list

Stack is a special list, so the stack operations are expressed by list operations.

Push(S,a) \ddot{y} Add(S,a)

Top(S) \ddot{y} FirstElement(S)

Pop(S) \ddot{y} RemoveFirst(S)

IsStackEmpty(S)

\ddot{y} wenn $\text{Length}(S) = 0$ return true

otherwise false

4.4 Queue

The queue is a special case of the list that
Elements managed according to the **FIFO** (first-in, first-out) principle

Idea: The elements are arranged one after the other, whereby
elements can only be added to the end of the list and
removed from the beginning of the list

Applications: Queues, buffer management, process
management, metabolism,...

Simple operations

Enqueue

Place element at the end of the queue

Front

Access first element of the queue

Dequeue

Remove first item from queue

IsEmpty

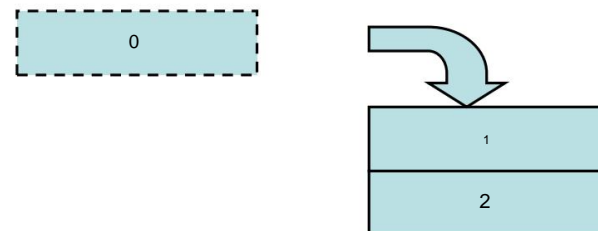
Test for empty queue



Methods on queue

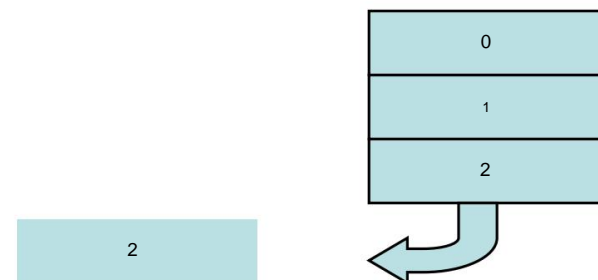
Method 'Enqueue'

Element will be at the end of the
Queue placed (at last
position)



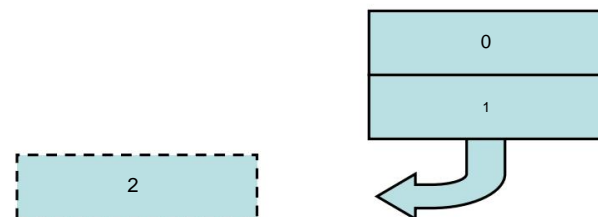
Method 'Front'

Delivers the content of the
first element of the
Queue



Method 'Dequeue'

First element of the queue
is removed



Queue as a list

Queue is also a special list, so everyone should
Queue operations can also be expressed by list operations .

Enqueue(Q,a) \rightarrow Add(S,a)

Front(Q) \rightarrow ?

Accordingly (Q) \rightarrow ?



Not entirely trivial!

Possibility (inconvenient!)

Accessing the first queue element (last in the list) by iteratively removing all elements and simultaneously building a 'collapsed' auxiliary list. Then reverse the process.



Comparison of “our” data structures

General distinction between static and dynamic realization static R.:
contiguous

memory, fields dynamic R.:

dynamic memory, dynamic objects

Data management

Insertion and deletion is supported

Data volume

static R.: limited, depending on the field size

dynamic R.: unlimited

depending on the size of the available storage space

rather simple models

Effort comparison of “our” lists

Implementations



	List static	List dynamic
Storage space $O(n)$		$O(n)$
Konstruktor $O(1)$		$O(1)$
destructor	$O(1)$	$O(n)$
Add	$O(1)$	$O(1)$
FirstElement $O(1)$		$O(1)$
RemoveFirst $O(1)$		$O(1)$
Length	$O(1)$	$O(n)$
Member	$O(n)$	$O(n)$

Attention: Actual effort $O(n)$ in
Add and RemoveFirst hidden



4.5 Special Lists

Doubly Linked List

double linked list

Circular List

Circular verkettete Liste

Ordered List

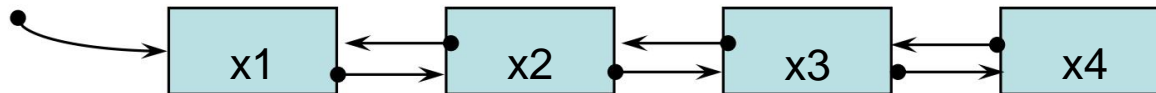
Ordered list

Double Ended List

Double headed list

Doubly Linked List

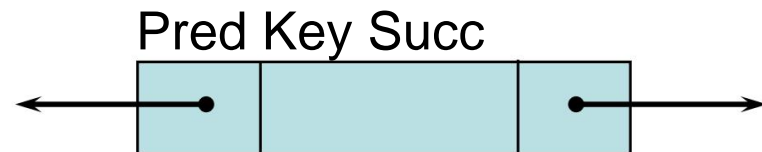
Double linked list



Each element has 2 pointers, one pointing to the previous one
and the other points to the subsequent element

Basic operations easy

```
class Node {
    KeyType Key;
    Node* Before;
    Node* Succ;
}
```



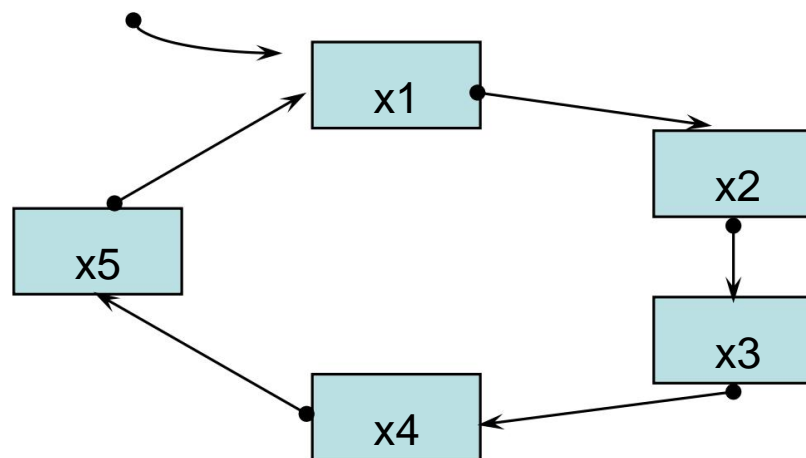
Circular List

Circular verkettete Liste

Pointer of the last element refers again to the first element Ring

Buffer Be

careful when entering and deleting the first element!



Ordered List

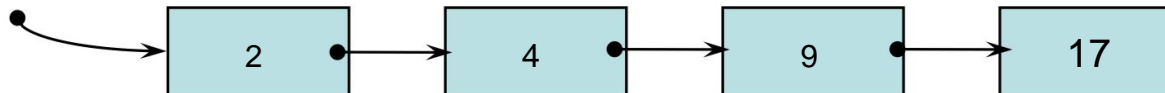
Ordered list

Items are added to the list more specifically according to their value

Registered position

Mostly ordered by size

Enter in a specific place that has to be found first
traverse

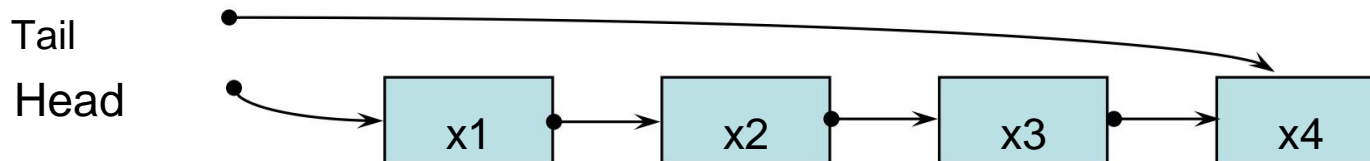


Double Ended List

List of 2 “heads”

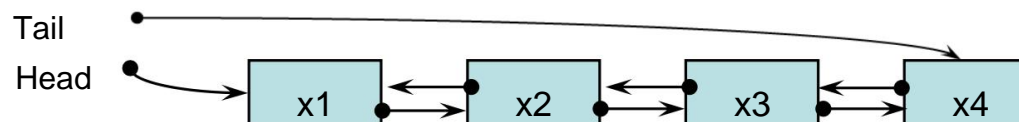
Each list has 2 pointers that point to the head and the end of the list

Makes it easier to insert at the top and bottom of the list



Can be combined with other list structures, e.g

Doubly Linked Double Ended List





What do we take with us?

Listen

- The operation
storage

- Contiguous - Scattered memory

Stack – Queue

Comparison

Special lists

- Doubly Linked List

- Circular List

- Ordered List

- Double Ended List