

Looping through, we reach the first node 1, which contains the edge list of 3, 2. Using the algorithm, we see 3 hasn't been added so we keep it. Then check 2, which we keep and see it's smaller than 3 so we put that to the front of the list, giving us $1 \rightarrow 2 \rightarrow 3$

Next, we have node 2 with $2 \rightarrow 1, 3, 3, 3$. Repeating this process, we check 1 and keep it, check 3 and keep it which is greater than 1 so it stays in the same position.

The next 2 are already contained in the list, so we just delete the representation giving us $2 \rightarrow 1, 3$

We repeat this for the rest of the adjacency list and we come to our (ii) case at node $4 \rightarrow 4, 5, 2, 5, 1$.

Since we want to remove self-loops, node 4 cannot have an edge with itself, so it's deleted and the process continues from above giving us $4 \rightarrow 1, 2, 5$.

Thus, the algorithm will convert G into G' removing self-loops and making a directed multiedge into a single directed edge.

Pseudocode input is the adjacency list.

transform(G)

loop through G // get each vertex linked-list

loop through $G[i]$ linked list

if ($G[i] = \text{edge}[i]$)

delete $\text{edge}[i]$ // removes self loop

else if ($\text{edge}[i] = \text{visited}$) // already in list

delete $\text{edge}[i]$

else

if ($\text{edge}[i] < \text{edge}[i-1]$)

swap $\text{edge}[i]$ and $\text{edge}[i-1]$

$\text{edge}[i] = \text{visited}$

add $\text{edge}[i]$ to linked list

$i++$