## Proof Portfolio Problem 7

Chose one problem from each numbered group. So, choose only one of 7A, 7B, and 7C.

As always, remind yourself of the academic honesty guidelines for the proof portfolio.  $Please\ see\ me\ when\ you\ need\ support.$ 

The initial deadline for problems 5-8 is Monday, March 23 by 11:59PM, with the final deadline Friday, March 27 by 11:59PM.

Conjecture 7A. For all natural numbers  $n, 8 \mid 3^{2n} - 1$ .

Conjecture 7B. Conjecture and prove a formula for the  $n^{th}$  derivative of  $f(x) = e^{2x}$  for each  $n \in \mathbb{N}$ .

Conjecture 7C. Let  $f_n$  be the  $n^{th}$  Fibonacci number. For all natural numbers n,

$$f_2 + f_4 + \dots + f_{2n} = f_{2n+1} - 1.$$