

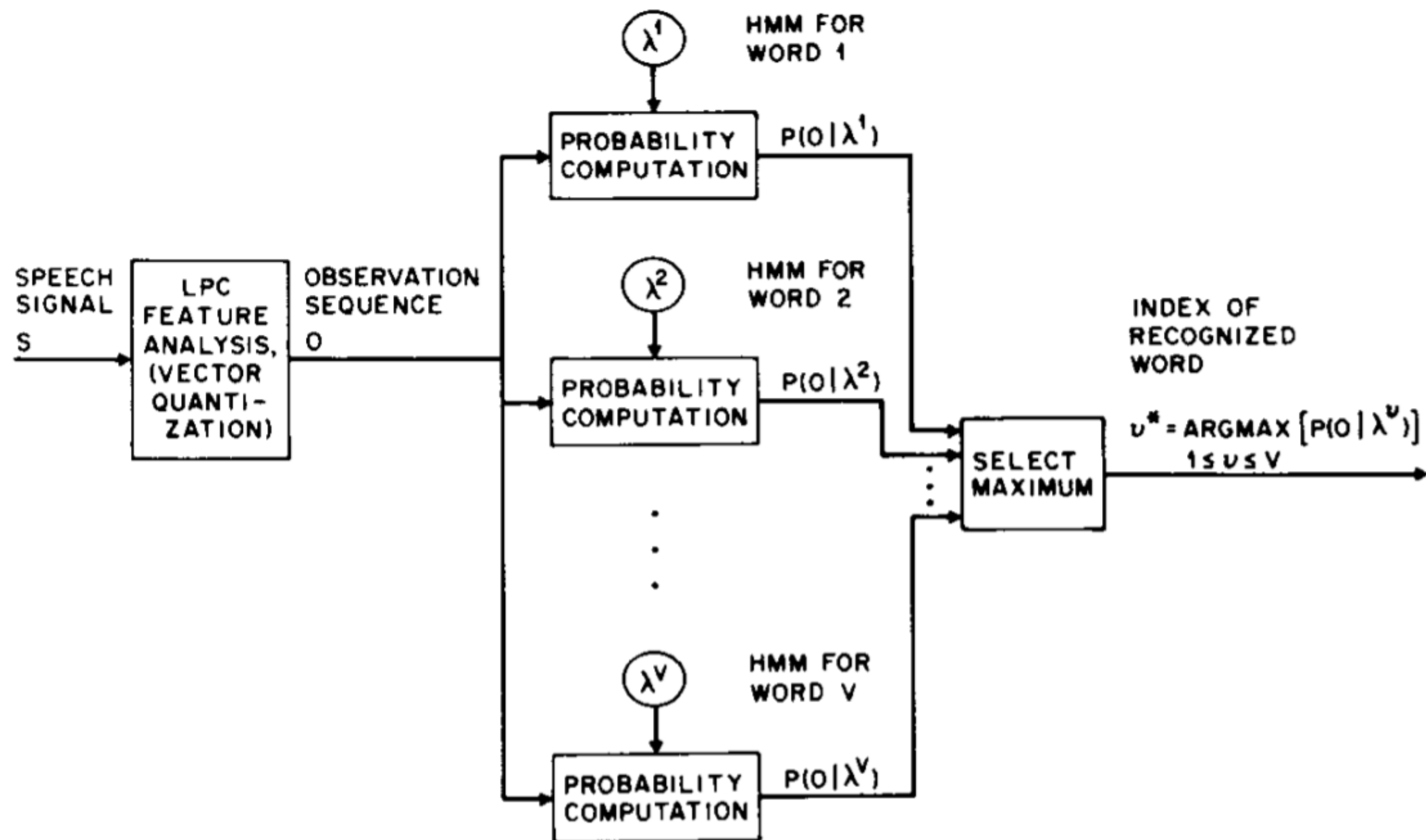
$$\bar{c}_{jk} = \frac{\sum_{t=1}^T \gamma_t(j, k)}{\sum_{t=1}^T \sum_{k=1}^M \gamma_t(j, k)}$$

$$\bar{U}_{jk} = \frac{\sum_{t=1}^T \gamma_t(j, k) \cdot (\mathbf{O}_t - \boldsymbol{\mu}_{jk})(\mathbf{O}_t - \boldsymbol{\mu}_{jk})'}{\sum_{t=1}^T \gamma_t(j, k)}$$

$$\bar{\boldsymbol{\mu}}_{jk} = \frac{\sum_{t=1}^T \gamma_t(j, k) \cdot \mathbf{O}_t}{\sum_{t=1}^T \gamma_t(j, k)}$$

$$\gamma_t(j, k) = \left[\frac{\alpha_t(j) \beta_t(j)}{\sum_{j=1}^N \alpha_t(j) \beta_t(j)} \right] \left[\frac{c_{jk} \mathfrak{N}(\mathbf{O}_t, \boldsymbol{\mu}_{jk}, \mathbf{U}_{jk})}{\sum_{m=1}^M c_{jm} \mathfrak{N}(\mathbf{O}_t, \boldsymbol{\mu}_{jm}, \mathbf{U}_{jm})} \right].$$

(The term $\gamma_t(j, k)$ generalizes to $\gamma_t(j)$ in the case of a simple mixture, or a discrete density.)



Probabilistic approach – statistical sequence recognition

Using Bayes' Theorem

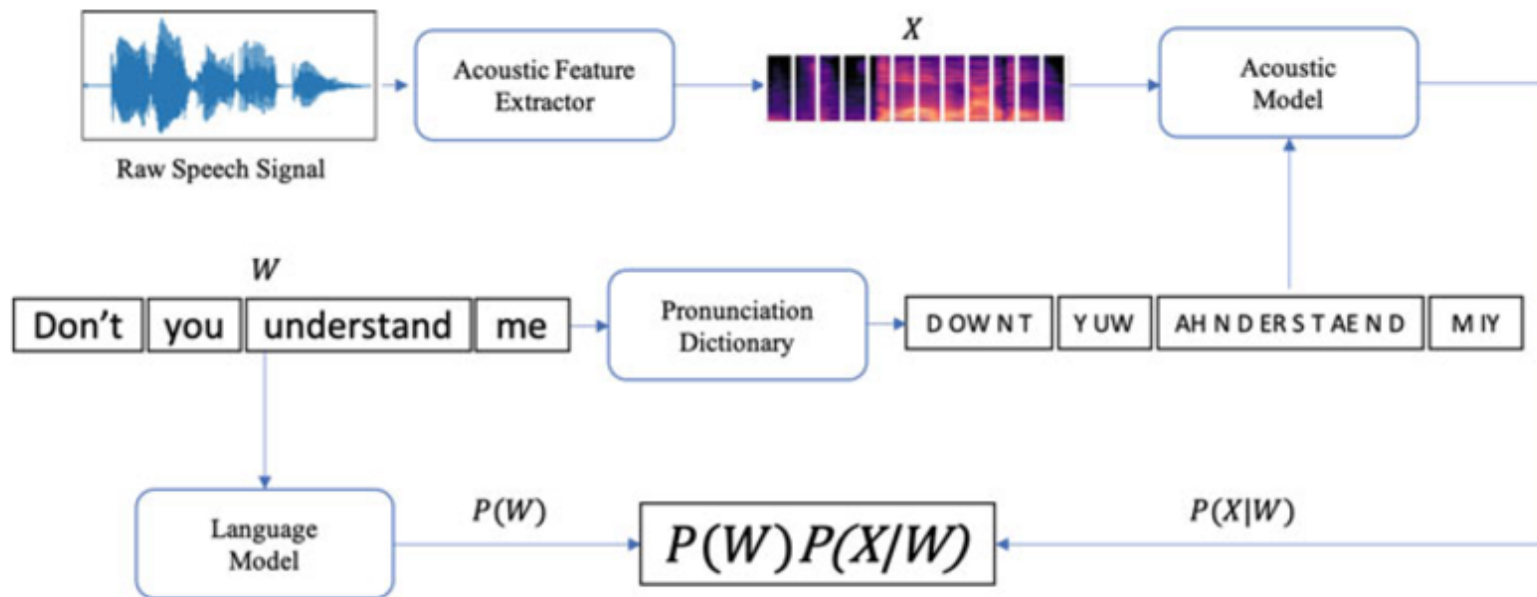
$$P(W|X) = \frac{P(X|W)P(W)}{P(X)}$$



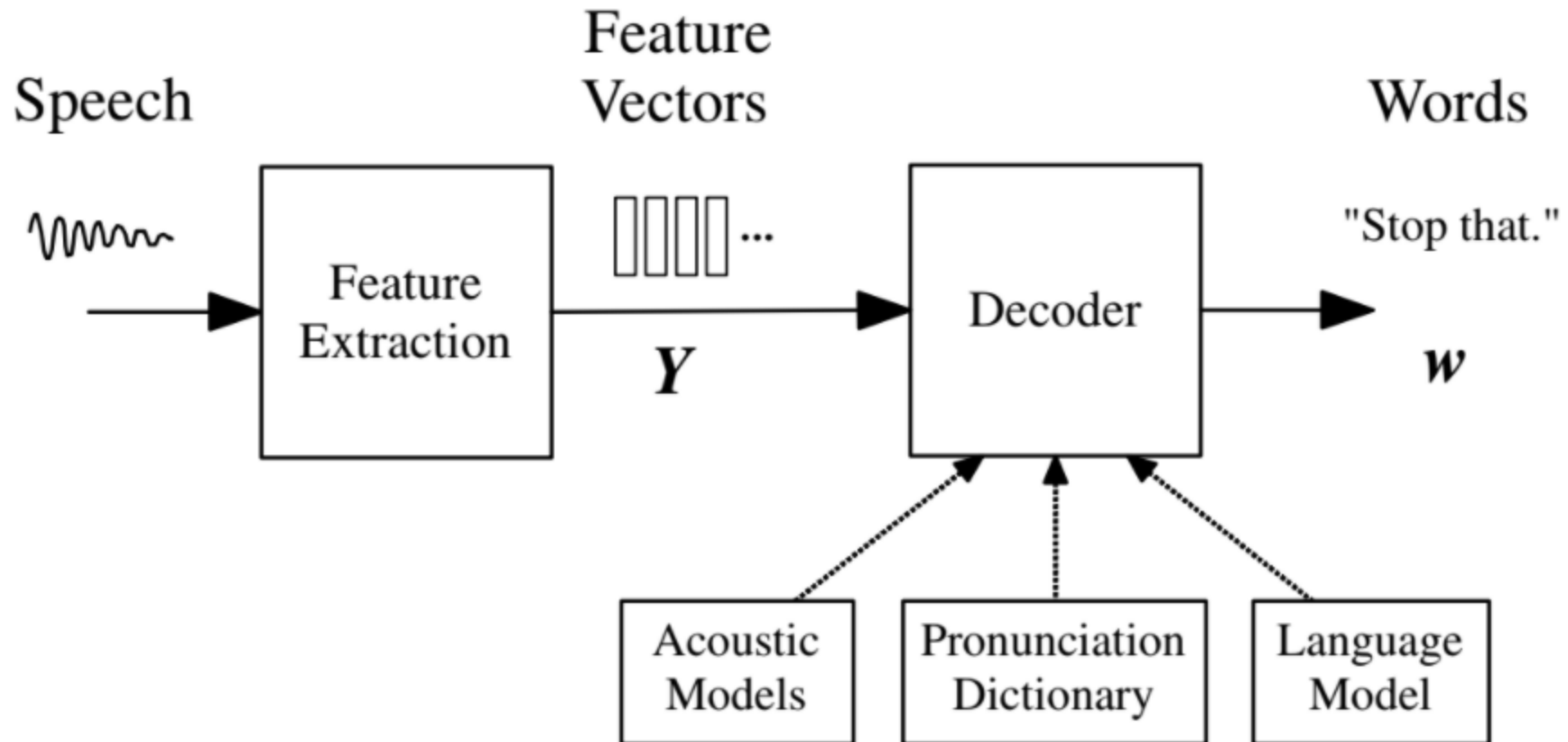
$$W^* = \operatorname{argmax}_{W \in V^*} P(X|W)P(W)$$

**Acoustic
Model**

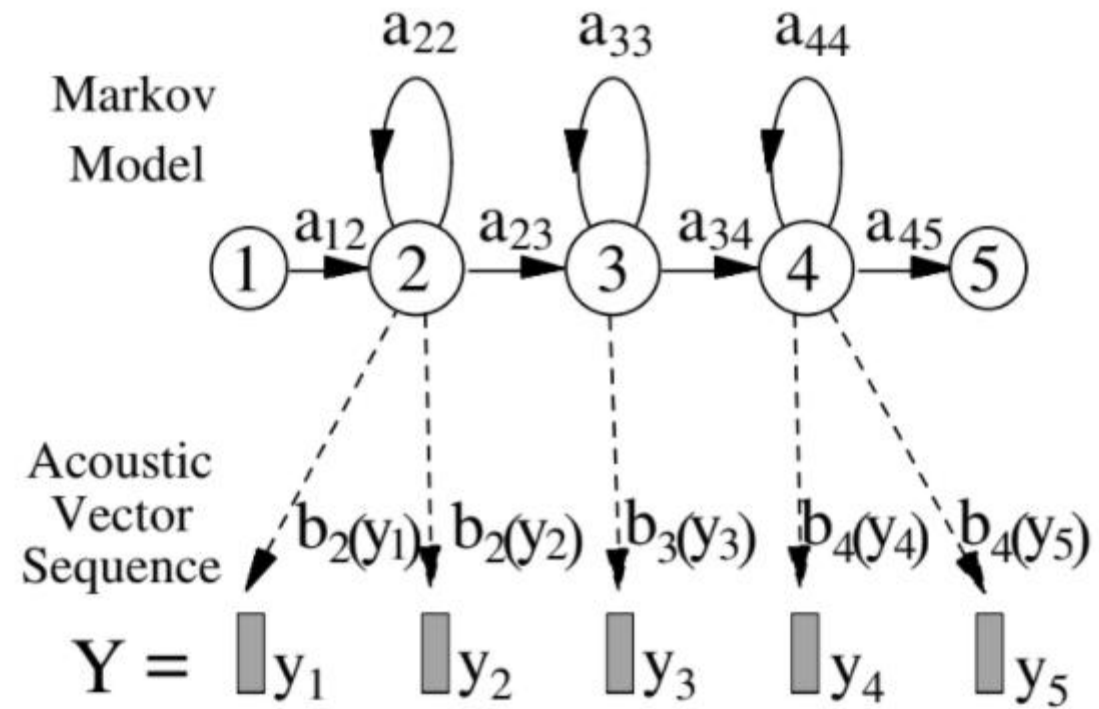
**Language
Model**



Architecture of HMM-based recognizer



HMM-based phone model



Viterbi through a Non-Emitting State

