NATIONAL TECHNICAL UNIVERSITY OF UKRAINE "IGOR SIKORSKY KYIV POLYTECHNIC INSTITUTE"

Faculty of Informatics and Computer Engineering Department of Computer Engineering

Lab 2 Report

Investigating Neural Network Structure and Simulating a Two-Variable Function

Variant 12

Student, group $\underline{\text{IM-14}}_{\text{(group code)}}$

in the educational and professional program "Software Engineering For Computer System" Specialty 121 "Computer Engineering"

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Reviewer Associate Professor, Dr.Ph. Pavlov Valerii

(position, academic degree, academic status, surname and initials)

The purpose of the work: To investigate the structure and principle of operation of a neural network. With the help of a neural network, simulate the function of two variables

12	$y = \cos(x)/x - \sin(x)/x^2$	12	19.	7
12.	$z = \sin(x/2) + y \cdot \sin(x)$	12.	17.	/.

1 inner layer with 10 neurons;

```
In [7]: import numpy as np
import tensorflow as tf
import matplotlib.pyplot as plt

# Function of Two Variables
def func(X):
    y = np.cos(X[0]) / x[1] - np.sin(x[0]) / x[1]**2
    z = np.sin(x[0] / 2) + y * np.sin(x[0])
    return y, z

# Collecting Dataset
    x = np.linspace(12, 19, 7)
    x0, x1 = np.meshgrid(x, x)
    x0, x1 = x0.ravel(), x1.ravel()
    X = [[x0[i], x1[i]] for i in range(len(x0))]
    y, z = zip(*[func(x) for x in X])

split = int(len(X) * 0.8)
    x_train, y_train, z_train = X[:split], y[:split], z[:split]
    x_test, y_test, z_test = X[split:], y[split:], z[split:]

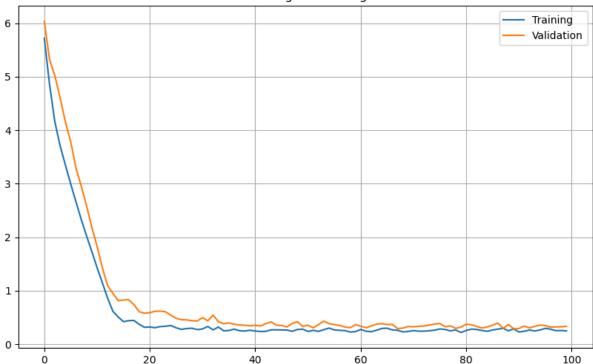
# Function to display
def visual(his):
    loss = his.history['ual_loss']
    val_loss = his.history['val_loss']
    epochs = range(len(loss))
```

```
plt.figure(figsize=(10, 6))
       plt.plot(epochs, loss, label='Training')
plt.plot(epochs, val_loss, label='Validation')
plt.title('Training and Testing')
        plt.legend()
       plt.grid()
        plt.show()
# Model with 1 inner layer and 10 neurons
model_fl = tf.keras.models.Sequential([
    tf.keras.layers.Dense(10, input_shape=(2,), activation='relu'),
    tf.keras.layers.Dense(2) # Two outputs for y and z
 ])
 model_fl.summary()
model_fl.compile(
    optimizer=tf.keras.optimizers.SGD(
             learning_rate=tf.keras.optimizers.schedules.ExponentialDecay(0.001, decay_steps=75, decay_rate=0.96)
       loss='mae',
metrics=['mae']
# Train the model
history_f = model_fl.fit(
       \label{eq:np.array} \mbox{np.array}(\mbox{x\_train}), \mbox{np.array}(\mbox{y\_train}, \mbox{z\_train}).\mbox{T, } \mbox{\# \textit{Two outputs}}
        epochs=100,
       validation_data=(np.array(x_test), np.array([y_test, z_test]).T),
# Display learning curves
visual(history f)
```

Performance results

```
Model: "sequential_6"
                                                                                 Layer (type)
                  Output Shape
                                   Param #
                                   30
dense_12 (Dense)
                  (None, 10)
dense_13 (Dense)
                  (None, 2)
                                   22
Total params: 52 (208.00 Byte)
Trainable params: 52 (208.00 Byte)
Non-trainable params: 0 (0.00 Byte)
Epoch 1/100
Epoch 1/100
2/2 [======
Epoch 2/100
2/2 [======
Epoch 3/100
2/2 [======
```

Training and Testing



1 inner layer with 20 neurons;

```
In [2]: import numpy as np
import tensorflow as tf
import matplotlib.pyplot as plt

# Function of Two Variables

def func(x):
    y = np.cos(x[0]) / x[1] - np.sin(x[0]) / x[1]**2
    z = np.sin(x[0] / 2) + y * np.sin(x[0])
    return y, z

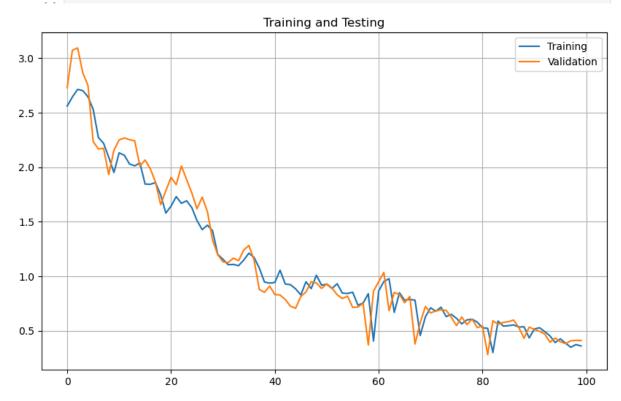
# Collecting Dataset
    x = np.linspace(12, 19, 7)
    x0, x1 = np.meshgrid(x, x)
    x0, x1 = x0.ravel(), x1.ravel()
    X = [[x0[i], x1[i]] for i in range(len(x0))]
    y, z = zip(*[func(x) for x in X])

split = int(len(X) * 0.8)
    x_train, y_train, z_train = X[:split], y[:split], z[:split]
    x_test, y_test, z_test = X[split:], y[split:], z[split:]

# Function to display
def visual(his):
    loss = his.history['loss']
    val_loss = his.history['val_loss']
    epochs = range(len(loss))
```

```
plt.figure(figsize=(10, 6))
    plt.plot(epochs, loss, label='Training')
plt.plot(epochs, val_loss, label='Validation')
    plt.title('Training and Testing')
    plt.legend()
    plt.grid()
    plt.show()
# Model with 1 inner layer and 20 neurons
model fl2 = tf.keras.models.Sequential([
    tf.keras.layers.Dense(20, input_shape=(2,), activation='relu'),
    tf.keras.layers.Dense(1)
])
model_fl2.summary()
model_fl2.compile(
    optimizer=tf.keras.optimizers.SGD(
        learning_rate=tf.keras.optimizers.schedules.ExponentialDecay(0.005, decay_steps=75, decay_rate=0.96)
    loss='mae',
metrics=['mae']
# Train the model
history_f2 = model_fl2.fit(
    np.array(x_train), np.array(y_train), # Assuming y_train is a single array
    validation_data=(np.array(x_test), np.array(y_test)), # Assuming y_test is a single array
# Display learning curves
visual(history f2)
```

Performance results



Network type: cascade-forward backprop:

1 inner layer with 20 neurons;

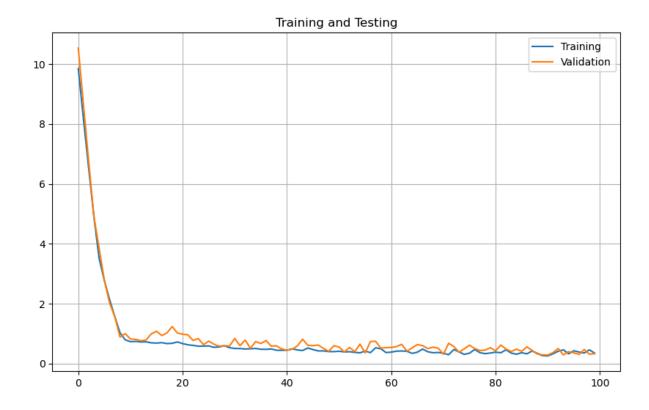
```
In [16]: import numpy as np
import tensorflow as tf
              import matplotlib.pyplot as plt
             # Function of Two Variables
def func(x):
                 y = \text{np.cos}(x[0]) / x[1] - \text{np.sin}(x[0]) / x[1]**2

z = \text{np.sin}(x[0] / 2) + y * \text{np.sin}(x[0])
                    return y, z
              # Collecting Dataset
             # cottecting bataset
x = np.linspace(12, 19, 7)
x0, x1 = np.meshgrid(x, x)
x0, x1 = x0.ravel(), x1.ravel()
X = [[x0[i], x1[i]] for i in range(len(x0))]
y, z = zip(*[func(x) for x in X])
              split = int(len(X) * 0.8)
x_train, y_train, z_train = X[:split], y[:split], z[:split]
x_test, y_test, z_test = X[split:], y[split:], z[split:]
              # Function to display
             def visual(his):
    loss = his.history['loss']
    val_loss = his.history['val_loss']
    epochs = range(len(loss))
                   plt.figure(figsize=(10, 6))
plt.plot(epochs, loss, label='Training')
plt.plot(epochs, val_loss, label='Validation')
               plt.figure(figsize=(10, 6))
plt.plot(epochs, loss, label='Training')
plt.plot(epochs, val_loss, label='Validation')
plt.title('Training and Testing')
                plt.legend()
                plt.grid()
                plt.show()
         # Model with 1 inner layer and 20 neurons
inputs = tf.keras.Input(shape=(2,))
x = tf.keras.layers.Dense(20, activation='relu')(inputs)
          \hbox{outputs = tf.keras.layers.Dense(2)(tf.keras.layers.concatenate([inputs, x]))} \ \ \textit{\# Two outputs for y and z } 
         model_cf1 = tf.keras.Model(inputs, outputs)
         model_cf1.summary()
         model_cf1.compile(
                optimizer=tf.keras.optimizers.SGD(
                      learning_rate=tf.keras.optimizers.schedules.ExponentialDecay(0.001, decay_steps=75, decay_rate=0.96)
               loss='mae',
metrics=['mae']
         # Train the model
         history_cf1 = model_cf1.fit(
               np.array(x_train), np.array([y_train, z_train]).T, # Two outputs
                epochs=100,
                validation_data=(np.array(x_test), np.array([y_test, z_test]).T),
         # Display learning curves
         visual(history cf1)
```

Creating a model

```
Model: "model_1"
Layer (type)
                              Output Shape
                                                                       Connected to
input_2 (InputLayer)
                              [(None, 2)]
                                                                       []
dense_6 (Dense)
                                                                       ['input_2[0][0]']
                              (None, 20)
                                                            60
                                                                       concatenate_1 (Concatenate (None, 22)
 dense_7 (Dense)
                              (None, 2)
                                                                       ['concatenate_1[0][0]']
Total params: 106 (424.00 Byte)
Trainable params: 106 (424.00 Byte)
Non-trainable params: 0 (0.00 Byte)
Epoch 1/100
```

The results of execution



2 inner layers of 10 neurons each:

```
In [1]: import numpy as np
             import tensorflow as tf
             import matplotlib.pyplot as plt
              # Function of Two Variables
              def func(x):
                  y = np.cos(x[0]) / x[1] - np.sin(x[0]) / x[1]**2
z = np.sin(x[0] / 2) + y * np.sin(x[0])
                    return y, z
              # Collecting Dataset
             # cottecting bataset
x = np.linspace(12, 19, 7)
x0, x1 = np.meshgrid(x, x)
x0, x1 = x0.ravel(), x1.ravel()
X = [[x0[i], x1[i]] for i in range(len(x0))]
y, z = zip(*[func(x) for x in X])
              split = int(len(X) * 0.8)
              x_train, y_train, z_train = X[:split], y[:split], z[:split]
x_test, y_test, z_test = X[split:], y[split:], z[split:]
              # Function to display
              def visual(his):
                    loss = his.history['loss']
val_loss = his.history['val_loss']
epochs = range(len(loss))
                    plt.figure(figsize=(10, 6))
plt.plot(epochs, loss, label='Training')
plt.plot(epochs, val_loss, label='Validation')
                     plt.title('Training and Testing')
                     plt.legend()
```

```
plt.plot(epochs, val_loss, label='Validation')
plt.title('Training and Testing')
plt.legend()
plt.grid()
plt.spid()
plt.show()

# Model with 2 inner layers of 10 neurons each
inputs = tf.keras.layers.Dense(10, activation='relu')(inputs)
x1 = tf.keras.layers.Dense(10, activation='relu')(tf.keras.layers.concatenate([inputs, x0]))
utputs = tf.keras.layers.Dense(2)(tf.keras.layers.concatenate([inputs, x0, x1])) # Two outputs for y and z
model_cf2 = tf.keras.Model(inputs, outputs)

model_cf2.compile(
    optimizer=tf.keras.optimizers.SGD(
        learning_rate=tf.keras.optimizers.schedules.ExponentialDecay(0.005, decay_steps=75, decay_rate=0.96)
),
    loss='mae',
    metrics=['mae']
)

# Train the model
history_cf2 = model_cf2.fit(
    np.aray(x_train), np.array([y_train, z_train]).T, # Two outputs
epochs=100,
    validation_data=(np.array(x_test), np.array([y_test, z_test]).T),
)

# Display learning curves
visual(history_cf2)
```

The results of execution

x_cross_entropy is deprecat	ed. Please use tf.comp	at.v1.losses.spar	<pre>\keras\src\losses.py:2976: The name tf.losses.sp se_softmax_cross_entropy instead. \keras\src\backend.py:1398: The name tf.executing</pre>	_
			eagerly_outside_functions instead.	.вв
Model: "model"				
louel: model				
Layer (type)	Output Shape	Param #	Connected to	
input_1 (InputLayer)	[(None, 2)]	0	[]	
dense (Dense)	(None, 10)	30	['input_1[0][0]']	
concatenate (Concatenate)	(None, 12)	0	['input_1[0][0]', 'dense[0][0]']	
dense 1 (Dense)	(None, 10)	130	['concatenate[0][0]']	
delise_i (belise)				



Network type:elman backprop::

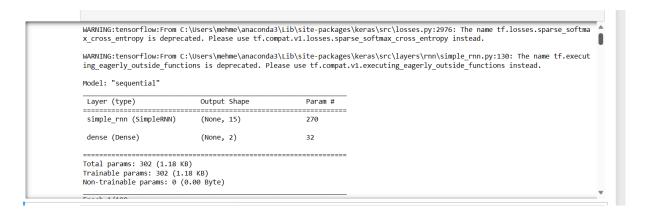
1 inner layer with 15 neurons;

Display learning curves

```
In [1]: import numpy as np
import tensorflow as tf
            import matplotlib.pyplot as plt
             # Function of Two Variables
            def func(x):
                y = np.cos(x[0]) / x[1] - np.sin(x[0]) / x[1]**2

z = np.sin(x[0] / 2) + y * np.sin(x[0])
                 return y, z
            # Collecting Dataset
           x = np.linspace(12, 19, 7)
x0, x1 = np.meshgrid(x, x)
x0, x1 = x0.ravel(), x1.ravel()
X = [[x0[i], x1[i]] for i in range(len(x0))]
y, z = zip(*[func(x) for x in X])
            split = int(len(X) * 0.8)
x_train, y_train, z_train = X[:split], y[:split], z[:split]
x_test, y_test, z_test = X[split:], y[split:], z[split:]
             # Function to display
            def visual(his):
                 loss = his.history['loss']
val_loss = his.history['val_loss']
epochs = range(len(loss))
                 plt.figure(figsize=(10, 6))
                 plt.plot(epochs, loss, label='Training')
plt.plot(epochs, val_loss, label='Validation')
plt.title('Training and Testing')
                 plt.legend()
     plt.plot(epochs, val_loss, label='Validation')
     plt.title('Training and Testing')
     plt.legend()
     plt.grid()
     plt.show()
# Model with 1 inner layer and 15 neurons for Elman backprop
model_elman1 = tf.keras.models.Sequential([
    tf.keras.layers.SimpleRNN(15, activation='relu', input_shape=(1, 2)),
     tf.keras.layers.Dense(2) # Two outputs for y and z
model_elman1.summary()
x_{train} = np.reshape(x_{train}, (np.shape(x_{train})[0], 1, np.shape(x_{train})[1]))
x_test = np.reshape(x_test, (np.shape(x_test)[0], 1, np.shape(x_test)[1]))
model elman1.compile(
    optimizer=tf.keras.optimizers.SGD(
          learning_rate=tf.keras.optimizers.schedules.ExponentialDecay(0.005, decay_steps=75, decay_rate=0.96)
     loss='mae',
     metrics=['mae']
# Train the model
history elman1 = model elman1.fit(
    x_train, np.array([y_train, z_train]).T, # Two outputs
     validation_data=(x_test, np.array([y_test, z_test]).T),
```

Creating a model:

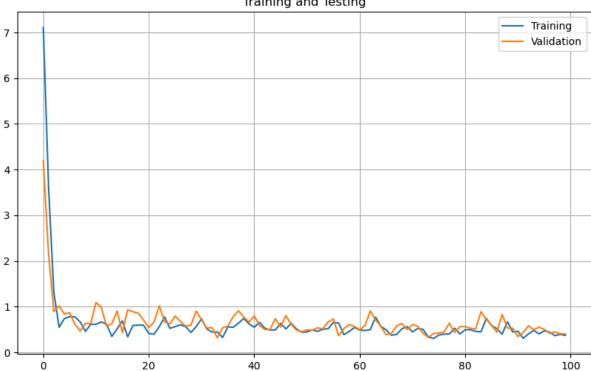


The results of execution

```
Epoch 1/100
WARNING:tensorflow:From C:\Users\mehme\anaconda3\Lib\site-packages\keras\src\utils\tf_utils.py:492: The name tf.ragged.Ragged TensorValue is deprecated. Please use tf.compat.v1.ragged.RaggedTensorValue instead.
WARNING:tensorflow:From C:\Users\mehme\anaconda3\Lib\site-packages\keras\src\engine\base_layer_utils.py:384: The name tf.exec uting_eagerly_outside_functions is deprecated. Please use tf.compat.v1.executing_eagerly_outside_functions instead.
2/2 [========] - 1s 243ms/step - loss: 7.1083 - mae: 7.1083 - val_loss: 4.1945 - val_mae: 4.1945 Epoch 2/100
2/2 [======
Epoch 3/100
2/2 [======
Epoch 4/100
                              ===] - 0s 30ms/step - loss: 1.3091 - mae: 1.3091 - val_loss: 0.8961 - val_mae: 0.8961
2/2 [=======
Epoch 5/100
2/2 [=======
Epoch 6/100
                           ========] - 0s 31ms/step - loss: 0.5506 - mae: 0.5506 - val_loss: 1.0157 - val_mae: 1.0157
                                            - 0s 30ms/step - loss: 0.7419 - mae: 0.7419 - val_loss: 0.8406 - val_mae: 0.8406
                                ======] - 0s 31ms/step - loss: 0.7827 - mae: 0.7827 - val_loss: 0.8672 - val_mae: 0.8672
2/2 [=====
```

In []:

Training and Testing



3 inner layers with 5 neurons each;

```
In [1]: import numpy as np
import tensorflow as tf
import matplotlib.pyplot as plt

# Function of Two Variables
def func(X):
    y = np.cos(x[0]) / x[1] - np.sin(x[0]) / x[1]**2
    z = np.sin(x[0] / 2) + y * np.sin(x[0])
    return y, z

# Collecting Dataset
    x = np.linspace(12, 19, 7)
    x0, x1 = np.meshgrid(x, x)
    x0, x1 = x0-ravel(), x1.ravel()
    X = [[x0[i]], x1[i]] for in range(len(x0))]
    y, z = zip(*[func(x) for x in x])

split = int(len(x) * 0.8)
    x_train, y_train, z_train = x[:split], y[:split], z[:split]
    x_test, y_test, z_test = x[split:], y[split:], z[split:]

# Function to display
def visual(his):
    loss = his.history['loss']
    val loss = his.history['val_loss']
    epochs = range(len(loss))

plt.figure(figsize=(10, 6))
    plt.figure(figsize=(10, 6))
    plt.plot(epochs, loss, label='training')
    plt.plot(epochs, val_loss, label='rainian')
    plt.plot(epochs, val_loss, label='validation')
```

```
pit.grid()
    plt.show()
# Model with 3 inner layers and 5 neurons each for Elman backprop
model_elman2 = tf.keras.models.Sequential([
    tf.keras.layers.SimpleRNN(5, activation='relu', input_shape=(1, 2)),
    tf.keras.layers.Dense(5, activation='relu'),
tf.keras.layers.Dense(5, activation='relu'),
tf.keras.layers.Dense(2) # Two outputs for y and z
1)
model elman2.summary()
x_train = np.reshape(x_train, (np.shape(x_train)[0], 1, np.shape(x_train)[1]))
x_test = np.reshape(x_test, (np.shape(x_test)[0], 1, np.shape(x_test)[1]))
model_elman2.compile(
    optimizer=tf.keras.optimizers.SGD(
        learning_rate=tf.keras.optimizers.schedules.ExponentialDecay(0.001, decay_steps=75, decay_rate=0.96)
    loss='mae',
metrics=['mae']
# Train the model
history_elman2 = model_elman2.fit(
    x_train, np.array([y_train, z_train]).T, # Two outputs
    epochs=100,
    validation_data=(x_test, np.array([y_test, z_test]).T),
# Display learning curves
visual(history_elman2)
```

The results of execution

```
2/2 [======
Epoch 2/100
                                            1s 284ms/step - loss: 0.2806 - mae: 0.2806 - val_loss: 0.3443 - val_mae: 0.3443
                                                                                                                                                2/2 [======
Epoch 3/100
                                            0s 34ms/step - loss: 0.2651 - mae: 0.2651 - val_loss: 0.3247 - val_mae: 0.3247
2/2 [======
Epoch 4/100
2/2 [======
Epoch 5/100
                                             0s 32ms/step - loss: 0.2551 - mae: 0.2551 - val_loss: 0.3086 - val_mae: 0.3086
                                            0s 33ms/step - loss: 0.2484 - mae: 0.2484 - val_loss: 0.2974 - val_mae: 0.2974
2/2 [=====
Epoch 6/100
                                            0s 33ms/step - loss: 0.2464 - mae: 0.2464 - val_loss: 0.3051 - val_mae: 0.3051
2/2 [=====
Epoch 7/100
                                            Os 32ms/step - loss: 0.2453 - mae: 0.2453 - val_loss: 0.3026 - val_mae: 0.3026
                                            Os 32ms/step - loss: 0.2429 - mae: 0.2429 - val_loss: 0.2983 - val_mae: 0.2983
2/2 [=====
Epoch 8/100
                                            0s 31ms/step - loss: 0.2404 - mae: 0.2404 - val_loss: 0.2838 - val_mae: 0.2838
2/2 [=====
Epoch 9/100
                                            0s 30ms/step - loss: 0.2383 - mae: 0.2383 - val loss: 0.2950 - val mae: 0.2950
```

