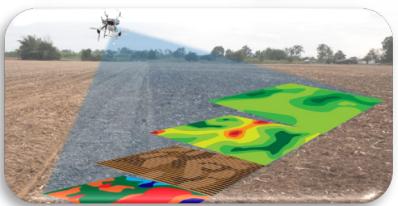
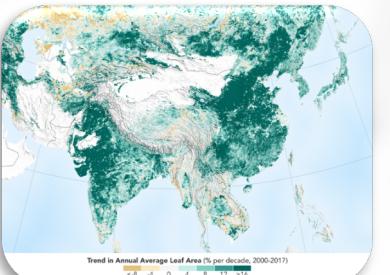


Latent Meshed Gaussian Processes for Scalable Bayesian Regression

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with
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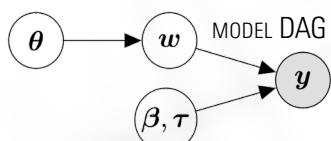
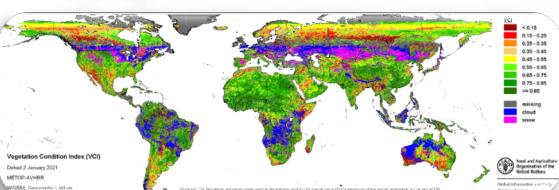
References
Meshed GPs (2020). JASA in press
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Better MGPs via GriPS (2021). Technometrics (in review)
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Spamtrees (2021). JMLR (in review)
arxiv.org/abs/2012.00943



Crowd-sourced
Satellites
Remote sensing

SPATIAL BIG DATA

Multivariate
Misaligned
Multi-type
Huge dimension



MODEL DAG

$$j\text{th outcome} \quad y_j(\ell) = \mathbf{x}_j(\ell)^\top \boldsymbol{\beta}_j + w_j(\ell) + \varepsilon_j(\ell)$$

Gaussian measurement error $\varepsilon(\ell) \sim N(0, \tau_j^2)$

modeling Gaussian outcomes

characterize spatial associations across outcomes across locations

multivariate GP with cross-covariance \mathbf{C}_θ

$$\mathbf{w}(\cdot) \sim GP(\mathbf{0}, \mathbf{C}_\theta)$$

dimension (nq, nq)

modeling multi-type outcomes

jth outcome $y_j(\ell) | \eta_j(\ell), \tau_j \sim P_j(\eta_j(\ell), \tau_j)$

linear predictor $\eta_j(\ell) = \mathbf{x}_j(\ell)^\top \boldsymbol{\beta}_j + w_j(\ell)$

outcome index $j = 1, \dots, q$ spatial coordinate $\ell \in \mathcal{D} \subset \mathbb{R}^d$

does not scale

REPLACE WITH

MESHED GP

$$\mathbf{w}(\cdot) \sim MGP_{\mathcal{S}, \mathcal{G}}(\mathbf{0}, \mathbf{C}_\theta)$$

DIY MESHED SPATIAL PROCESS

- reference set \mathcal{S} of knots
- fix a DAG with patterns
- partition of \mathcal{S} linked to DAG nodes
- a rule to determine what happens at other locations

```

meshout <- meshed::spmeshed(
  y = Y,
  x = X,
  coords = coords,
  family = c("poisson",
            "gaussian",
            "binomial"),
  k = 2,
  grid_size = c(30, 30),
  block_size = 20,
  n_samples = 5000,
  n_burn = 2000,
  n_thin = 5,
  n_threads = 4,
  prior = list(phi=c(2, 20))
)
  
```

(optional. spmeshed will try to figure out what's best for speed)

parallel computing with **OpenMP**

...if meshed was compiled with OpenMP support

works best with R linked to **OpenBLAS/Intel MKL**

R PACKAGE meshed

Y matrix of outcomes
q columns
OK with NA (will predict)

X covariates

coords spatial coordinates
OK with spacetime

family list outcome types
OK with multi-type

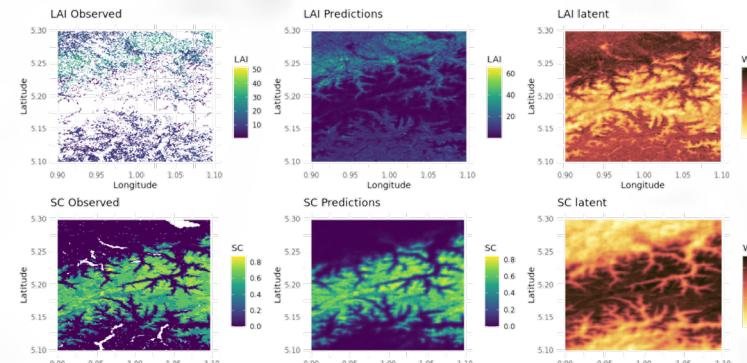
k number of spatial factors
linear coregionalization: OK $k < q$

grid_size to build \mathcal{S} .

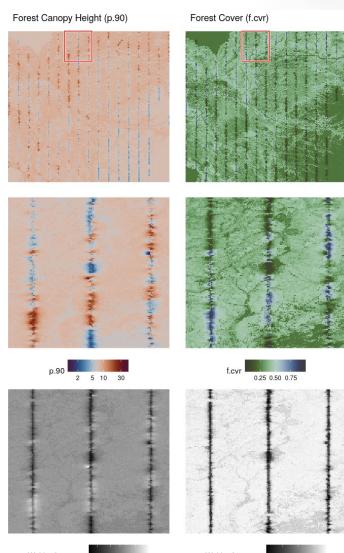
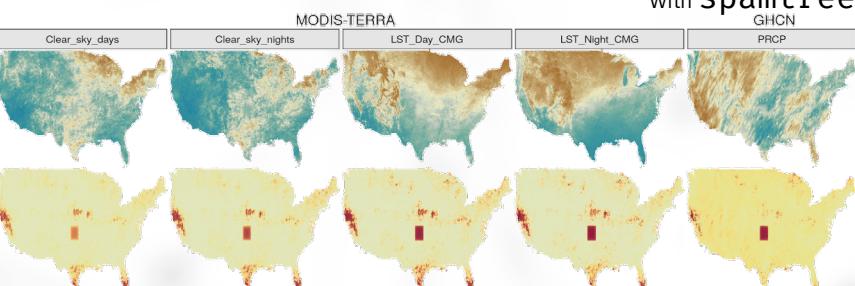
count and discrete outcomes

multivariate big data with **meshed**

continuous outcomes modeled as Gaussians

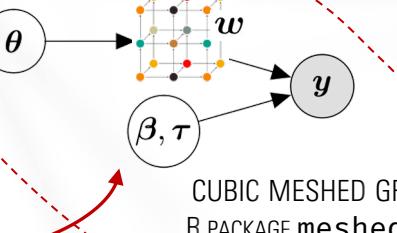


with spamtree



SCALABLE MCMC FOR MGPs

- Gridded \mathcal{S}
- Parameter expansion & parametrization (GriPS)
- Gibbs sampler for Gaussian outcomes
- Meshed Langevin on Riemann Manif. otherwise (MELANGE)



SPATIAL MULTIVARIATE TREES
R PACKAGE **spamtree**

