NOD Codes

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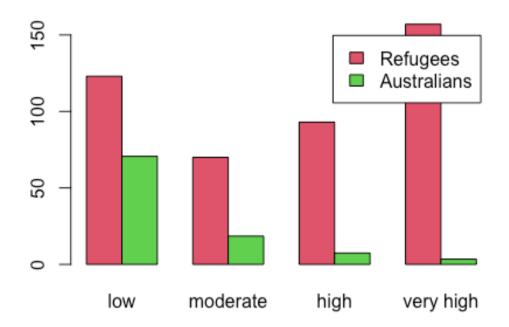
27/10/2021

Iraqi Refugees

Loading the data

Visualisation

```
barplot(m, beside = TRUE, col = 2:3,
    legend.text = c('Refugees', 'Australians'))
```



Hypothesis Testing

 ${
m H0:}$ There is no difference in distribution of distress between iraqi and aihw ${
m H1:}$ There is a difference CV: 0.05

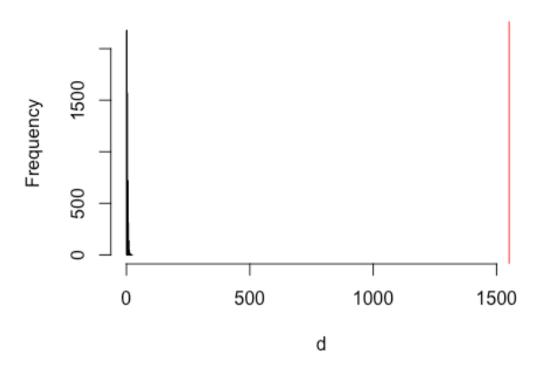
```
expected = aihw * 443 / 100
cs <- sum((iraqi - expected) ^ 2 / expected)
cs

## [1] 1550.75

d <- replicate(5000, {
  obs <- rmultinom(1, 443, expected)
  sum((obs - expected) ^2 / expected)
})</pre>
```

```
hist(d, col="lightblue", xlim = c(0,1580))
abline(v = cs, col = "red")
```

Histogram of d



```
pVal <- mean(d > cs)
pVal
## [1] 0
```

And another method for hypothesis testing

```
chisq.test(iraqi, p = aihw, rescale.p = TRUE, simulate.p.value = TRUE,
B = 5000)

##

## Chi-squared test for given probabilities with simulated p-value
(based
## on 5000 replicates)
```

```
##
## data: iraqi
## X-squared = 1550.6, df = NA, p-value = 2e-04
```

Eye Color:

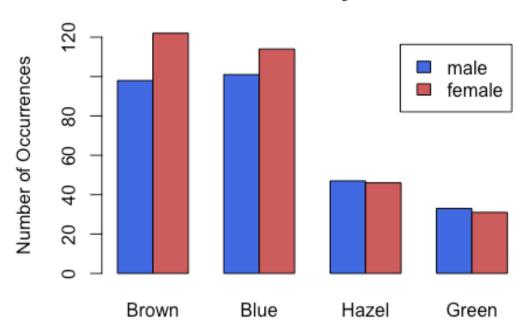
Loading the data:

```
male = c(98, 101, 47, 33)
female = c(122, 114, 46, 31)
levs = c("Brown", "Blue", "Hazel", "Green")
names(male) = levs
names(female) = levs
m <- rbind(male, female)</pre>
m
##
          Brown Blue Hazel Green
## male
             98 101
                         47
                               33
## female
            122 114
                         46
                               31
```

Visualisation

```
barplot(m, beside = TRUE,col = c("Royalblue", "indianred"),
    main = "Distribution of Eye Colours",
    ylab = "Number of Occurrences",
    legend = TRUE)
```

Distribution of Eye Colours



simulation

```
chisq.test(m, rescale.p = TRUE, simulate.p.value = TRUE, B = 5000)

##

## Pearson's Chi-squared test with simulated p-value (based on 5000
## replicates)

##

## data: m

## X-squared = 1.5298, df = NA, p-value = 0.6801
```

FFIS

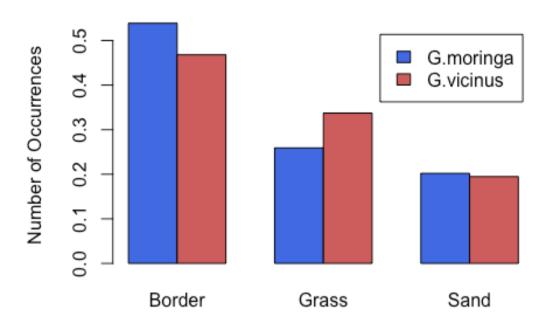
Loading the data:

```
eels \leftarrow matrix(c(264, 161, 127, 116, 99, 67), ncol = 3)
speciesLabels <- c('G.moringa', 'G.vicinus')</pre>
locationLabels <- c('Border', 'Grass', 'Sand')</pre>
dimnames(eels) <- list(species = speciesLabels,</pre>
                        location = locationLabels)
eels
##
               location
              Border Grass Sand
## species
##
     G.moringa
                   264
                         127
                                99
##
     G.vicinus
                          116
                   161
                                67
sampleSize = sum(eels)
```

Visualisation:

```
eels1 = eels ## Proportions
eels1[1,] = eels[1,] / sum(eels[1,])
eels1[2,] = eels[2,] / sum(eels[2,])
eels1
##
              location
## species
                  Border
                             Grass
    G.moringa 0.5387755 0.2591837 0.2020408
##
     G.vicinus 0.4680233 0.3372093 0.1947674
barplot(eels1, beside = TRUE, col = c("Royalblue", "indianred"),
        main = "Distribution of Eels",
        ylab = "Number of Occurrences",
        legend = TRUE)
```

Distribution of Eels



Simulation

```
speciesCount = rowSums(eels)
locationProps = colSums(eels) / sampleSize

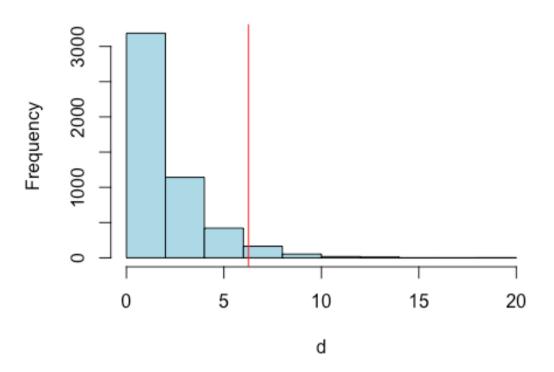
# our expected distribution
exp <- outer(speciesCount, locationProps)

cs <- sum((eels - exp)^2 / exp)
# Simulate / the distribution of differences
#
# simulate the data, assuming that the species
# does not effect the location
speciesProps <- speciesCount / sampleSize

d <- replicate(5000, {</pre>
```

```
# sample of species
  sp <- sample(speciesLabels,</pre>
                size = sampleSize,
                replace = TRUE,
                prob = speciesProps)
 # sample of locations
  lc <- sample(locationLabels,</pre>
                size = sampleSize,
                replace = TRUE,
                prob = locationProps)
  # tabulate the results
 res <- table(sp, lc)</pre>
 # re-compute the expected
 r <- rowSums(res)</pre>
 c <- colSums(res) / sum(res)</pre>
 ex <- outer(r, c)
 # compute diff between sample and expected
 sum((res - ex)^2 / ex)
})
hist(d, col="lightblue")
abline(v = cs, col = "red")
```

Histogram of d



```
pVal <- mean(d > cs)
pVal

## [1] 0.0444

chisq.test(eels, simulate.p.value = TRUE, B = 5000)

##

## Pearson's Chi-squared test with simulated p-value (based on 5000

## replicates)

##

## data: eels

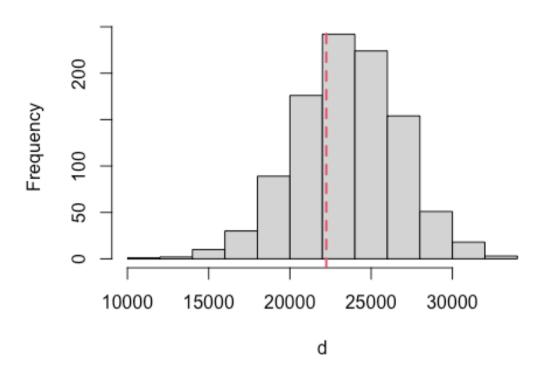
## X-squared = 6.2621, df = NA, p-value = 0.04899
```

Card Piles

Simulation

```
x1 <- sample(1:52)
x2 <- sample(1:52)
# x1 <- x2 with this commented out, x1 and x2 are different, otherwise
identical
cs <- sum((x1 - x2)^2)
# Simulate what is supposedly random
d <- replicate(1000,</pre>
                 a <- sample(1:52)
                 b <- sample(1:52)
                 sum((a - b)^2)
               })
hist(d)
abline(v = cs, col = 2, lwd = 2, lty = 2)
```

Histogram of d



Birth Weight

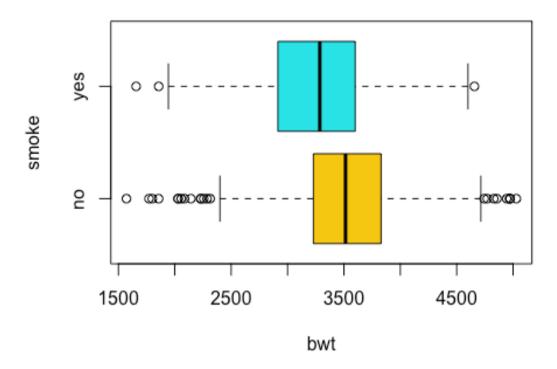
Loading the data

```
birthWeight <- read.csv("../datasets/birthwt.csv")</pre>
head(birthWeight)
##
      bwt smoke
## 1 3429
              no
## 2 3229
              no
## 3 3657
             yes
## 4 3514
              no
## 5 3086
             yes
## 6 3886
              no
table(birthWeight$smoke)
```

```
##
## no yes
## 742 484
summary(birthWeight)
##
        bwt.
                    smoke
## Min. :1571 Length:1226
## 1st Ou.:3114 Class :character
## Median :3429 Mode :character
## Mean :3415
## 3rd Qu.:3743
## Max. :5029
aggregate(bwt~smoke, birthWeight, mean)
##
    smoke
              bwt
## 1
      no 3515.639
## 2
      yes 3260.285
```

Visualisation

```
boxplot(bwt~smoke, birthWeight, col = c(7,5), horizontal = TRUE)
```



Hypothesis Testing

```
# H0: mu1 == mu2, There is no difference
# H1: mu1 < mu2, There is a difference

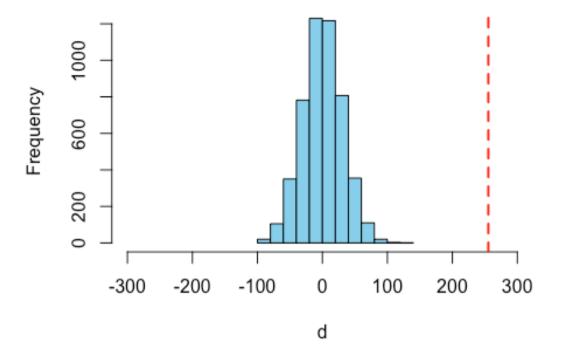
delta <- aggregate(bwt ~ smoke, birthWeight, mean)$bwt
delta

## [1] 3515.639 3260.285

cs <- -diff(delta)

d <- replicate(5000, {
    smoke.shuffle <- sample(birthWeight$smoke)
    del <- aggregate(bwt~smoke.shuffle, birthWeight, mean)$bwt
    -diff(del)
})</pre>
```

```
hist(d, main = '', col = 'skyblue', xlim = c(-1, 1) * 300)
abline(v = cs, col = "red", lwd = 2, lty = 2)
```



```
# One sided test, so p-value calculation uses one side of the
distribution
# The +ve side is used since mu2 - mu1 > 0
pVal <- mean(d > cs)
```

Drugs Data

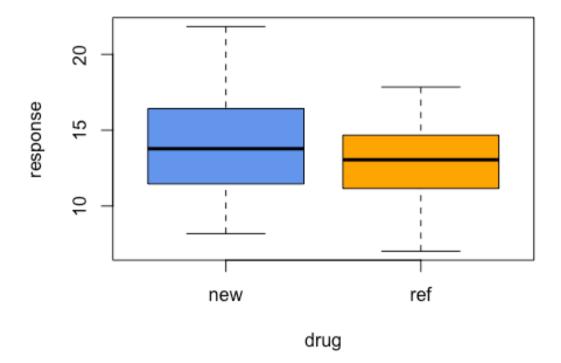
Loading the data

```
# Loading the drug data from file "assignmentB_drugData.csv".
drug_data <- read.csv("../datasets/drugs.csv")
head(drug_data) # viewing the first 6 rows of the data</pre>
```

```
## response drug
## 1 8.661020 new
## 2 11.431452 new
## 3 13.904322 ref
## 4 8.300664 new
## 5 14.662067 new
## 6 9.971347 ref
```

Visualisation

Visualisation

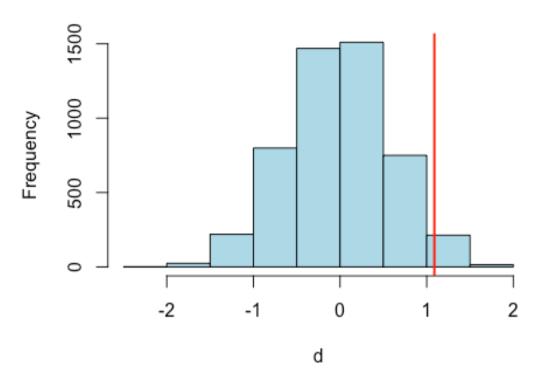


Hypothesis Testing

```
# For the Hypothesis, we are using null and alternate hypothesis as
follows:
# HO: mu1 == mu2, There is no statistically significant improvement
exist for new drug over ref drug.
# H1: mu1 > mu2. There exists a statistically significant improvement
for new drug over ref drug.
\# CV = 0.05 (5\%)
cv <- 0.05 # critical value
replications <- 5000 # number of replications for simulation
# calculating mean data for new drug and ref drug
delta <- aggregate(response ~ drug, drug data, mean)$response</pre>
# Calculating difference in means
cs <- -diff(delta)
cat("Difference in means of new drugs and ref drugs is: ", cs, "\n")
## Difference in means of new drugs and ref drugs is: 1.088462
# setting the seed value.
set.seed(2)
# Simulating the difference in means by 5000 times for the shuffled
drug categories within same data.
d <- replicate(replications, {</pre>
  shuffled drug <- sample(drug data$drug) ## Shuffling the drug
categories
  delta <- aggregate(response ~ shuffled drug, drug data, mean)</pre>
$response
 c <- -diff(delta)</pre>
})
cat("Average difference in means for simulated results", mean(d),
"\n\n")
## Average difference in means for simulated results -0.009275686
# Visualising the simulated outcome
hist(d, col = "lightblue", main = "Distribution of difference in
```

```
means")
abline(v = cs, col = "red", lwd = 2)
```

Distribution of difference in means



```
# counting the number of replications which have bigger difference
than original difference.
count <- sum(d > cs)

# calculating p-value
pvalue <- count/replications
cat("Calculated p-value from the simulation:", pvalue, "\n\n")

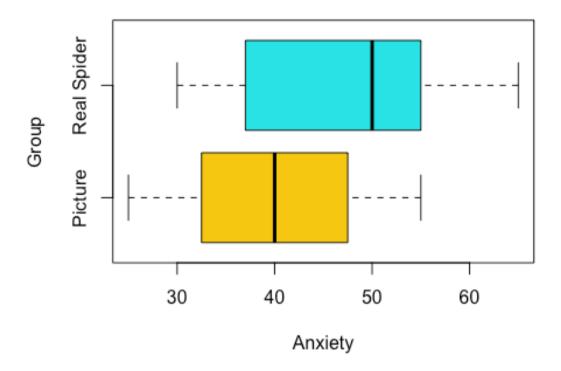
## Calculated p-value from the simulation: 0.0348
cat("Is critical value greater than p-value?", cv > pvalue, "\n")

## Is critical value greater than p-value? TRUE
```

Spider Data set

Hypothesis testing

```
spider <- read.csv("../datasets/Spider.csv")</pre>
head(spider)
##
       Group Anxiety
## 1 Picture
                  30
## 2 Picture
                  35
## 3 Picture
                  45
## 4 Picture
                  40
## 5 Picture
                  50
## 6 Picture
                  35
table(spider$Group)
##
##
       Picture Real Spider
##
            12
                        12
summary(spider)
##
       Group
                          Anxiety
## Length:24
                       Min.
                               :25.0
##
   Class:character 1st Ou.:35.0
##
   Mode :character
                       Median :42.5
##
                       Mean
                              :43.5
##
                       3rd Ou.:50.0
##
                       Max. :65.0
aggregate(Anxiety~Group, spider, mean)
##
           Group Anxiety
## 1
         Picture
                      40
## 2 Real Spider
                      47
boxplot(Anxiety~Group, spider, col = c(7,5), horizontal = TRUE)
```



```
# H0: mu1 == mu2, There is no difference
# H1: mu1 < mu2, There is a difference

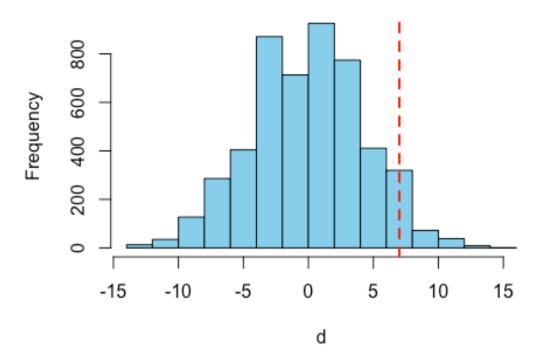
delta <- aggregate(Anxiety~Group, spider, mean)$Anxiety
delta

## [1] 40 47

cs <- diff(delta)

d <- replicate(5000, {
   Group.shuffle <- sample(spider$Group)
   del <- aggregate(Anxiety~Group.shuffle, spider, mean)$Anxiety
   diff(del)
})</pre>
```

```
hist(d, main = '', col = 'skyblue')
abline(v = cs, col = "red", lwd = 2, lty = 2)
```



```
# One sided test, so p-value calculation uses one side of the
distribution
# The +ve side is used since mu2 - mu1 > 0
pVal <- mean(d > cs)
```

Wilcoxon and Confidence Interval example

```
# Confidence intervals
# The luxury of a known populations; use normal distribution
x <- rnorm(50, 15) # actual pop mean = 15
y <- rnorm(50, 10) # actual pop mean = 10
# difference in means is actually 5
# but we pretend we don't know that!</pre>
```

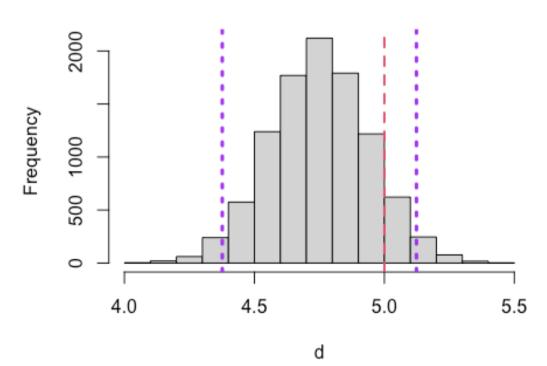
```
wilcox.test(x, v)
                                       # Are they different: absolutely
##
##
   Wilcoxon rank sum test with continuity correction
##
## data: x and v
## W = 2500, p-value < 2.2e-16
## alternative hypothesis: true location shift is not equal to 0
wilcox.test(x, y, alternative = 'l') # Is x < y, no way
##
## Wilcoxon rank sum test with continuity correction
##
## data: x and y
## W = 2500, p-value = 1
## alternative hypothesis: true location shift is less than 0
wilcox.test(x, y, alternative = 'q') \# Is x > y, absolutely
##
## Wilcoxon rank sum test with continuity correction
##
## data: x and y
## W = 2500, p-value < 2.2e-16
## alternative hypothesis: true location shift is greater than 0
# Generate estimate of population difference in means
p \leftarrow mean(x) - mean(y)
р
## [1] 4.752681
# Determine a confidence interval for the difference between x and y
# Generate confidence interval for true difference in population means
d <- replicate(10000,
                 ix <- sample(1:length(x), replace = TRUE)</pre>
                 iy <- sample(1:length(y), replace = TRUE)</pre>
                 mean(x[ix]) - mean(y[iy])
               })
```

```
hist(d)
abline(v = 5, col = 2, lwd = 2, lty = 2)

# calculate 95% confidence interval
q <- quantile(d, c(0.025, 0.975))
q

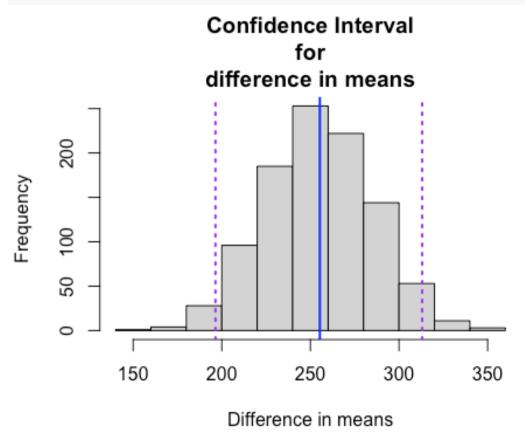
## 2.5% 97.5%
## 4.376405 5.123247
abline(v = q, col = 'purple', lwd = 3, lty = 3)
```

Histogram of d



Confidence interval - Birth Weight

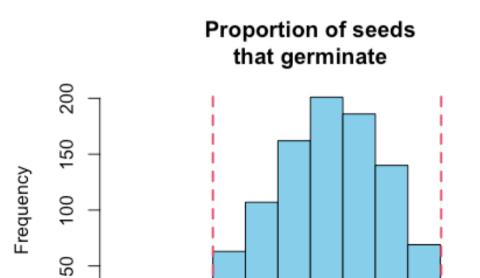
```
# Confidence interval for maternal smoking dataset
df <- read.csv('../datasets/birthwt.csv')</pre>
# Extract entire data set into the two groups
no <- subset(df$bwt, df$smoke == 'no')
ves <- subset(df$bwt, df$smoke == 'ves')</pre>
# Difference means for the sample:
# estimate of difference in population
res <- mean(no) - mean(yes)
## Alternal approach: delta <- aggregate(bwt~smoke, df, mean)
# resample using "boostrapping"
d <- replicate(1000,
                 # bootstrapping means doing the following:
                 # - create new sample of same size as original
                 # - must use replacement;
                       otherwise we generate a shuffled original!
                 # - must preserve group sizes; 472 no smoke, 484
smoke
                       so doing the two samples! Don't want to induce
differences
                 ns <- sample(no, replace = TRUE)</pre>
                 s <- sample(yes, replace = TRUE)</pre>
                 # difference in means
                 mean(ns) - mean(s)
               })
# find boundaries for central 95% of the data
q \leftarrow quantile(d, c(0.025, 0.975))
      # conf interval, range within which true pop. difference is
expected to reside
       2.5%
               97.5%
## 196.4152 313.0799
```



Binomial Confidence Interval - Method 1

```
# Bootstrap binomial confidence intervals for true rate in pop.
# Method 1
germinate <- 1
notGerminate <- 0</pre>
```

```
seeds <- c(rep(germinate, 15),</pre>
           rep(notGerminate, 5))
d <- replicate(1000,</pre>
                  res <- sample(seeds, replace = TRUE)</pre>
                  mean(res)
                })
mean(d)
## [1] 0.74995
q \leftarrow quantile(d, c(0.025, 0.975))
q
##
      2.5%
              97.5%
## 0.55000 0.90125
# use of expression allows showing Greek letter
hist(d, col = 'skyblue', xlab = expression(rho),
     main = 'Proportion of seeds\nthat germinate')
abline(v = q, col = 2, lwd = 2, lty = 2)
```



0.6

Binomial Confidence Interval - Method 2

0.5

0.4

```
# Method 2
d <- rbinom(1000, size = 20, prob = 15/20)
d <- d / 20

mean(d)
## [1] 0.7536

q <- quantile(d, c(0.025, 0.975))
q

## 2.5% 97.5%
## 0.55 0.95</pre>
```

0.7

ρ

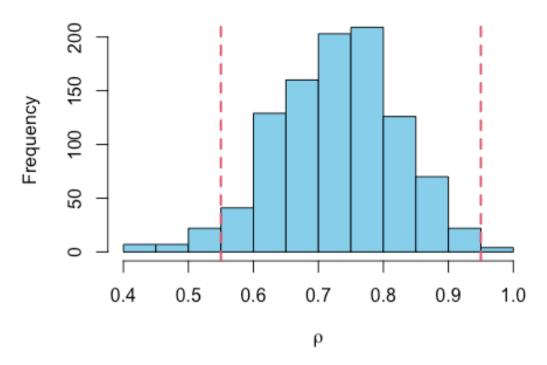
8.0

0.9

1.0

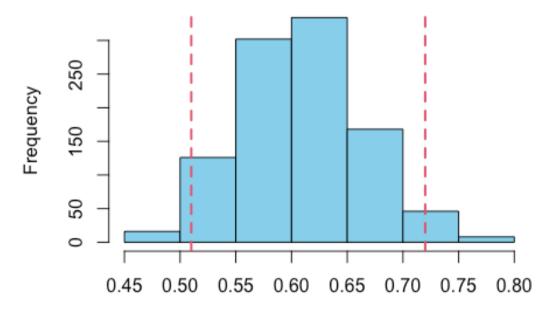
```
hist(d, col = 'skyblue', xlab = expression(rho),
    main = 'Proportion of seeds\nthat germinate')
abline(v = q, col = 2, lwd = 2, lty = 2)
```

Proportion of seeds that germinate

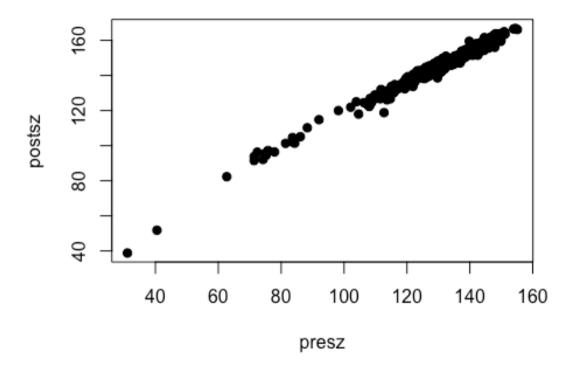


Poison distribution confidence interval

Proportion of deaths by horse kick



Crabs data - Correlation hypothesis



```
cor(df$presz, df$postsz)

## [1] 0.9903699

obs.cor = cor(df$presz, df$postsz)

x= replicate(1000, {
   post.perm = sample(df$postsz)
   cor(df$presz, post.perm)
})
```

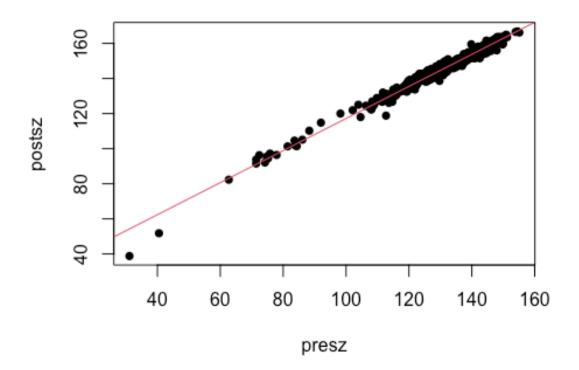
```
sum(abs(x) > abs(obs.cor))/1000
## [1] 0
cor.test(df$presz, df$postsz, method = "pearson")
##
## Pearson's product-moment correlation
##
## data: df$presz and df$postsz
## t = 155.08, df = 470, p-value < 2.2e-16
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.9884701 0.9919580
## sample estimates:
## cor
## 0.9903699</pre>
```

Linear Models - Hypothesis testing - slope = 0

```
# Slide 4
df <- read.csv('../datasets/crabsmolt.csv')</pre>
fit = lm(postsz~presz, data = df)
summary(fit)
##
## Call:
## lm(formula = postsz ~ presz, data = df)
##
## Residuals:
##
       Min
                 10
                     Median
                                   30
                                           Max
## -15.4269 -1.1611 -0.0669
                                        5.9251
                              1.2169
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 25.802580
                          0.767201
                                     33.63
                                             <2e-16 ***
                          0.005893 155.08
## presz
               0.913965
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 2.029 on 470 degrees of freedom
## Multiple R-squared: 0.9808, Adjusted R-squared: 0.9808
## F-statistic: 2.405e+04 on 1 and 470 DF, p-value: < 2.2e-16

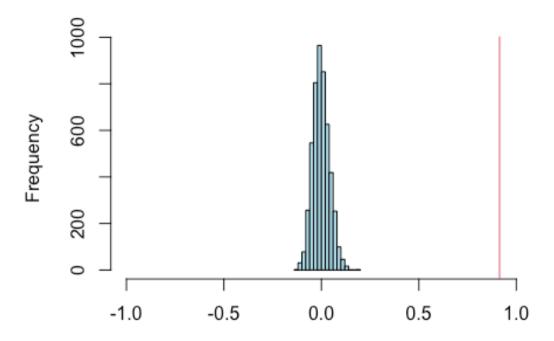
plot(postsz ~ presz, data=df, pch=16)
abline(fit, col = 2)</pre>
```



```
## Hypothesis for slope = 0

## compute the slope of the data
cs <- coef(fit)[2]
## compute the slope if the population b = 0
x= replicate(5000, {
   presz.perm = sample(df$presz) # shuffle one variable to force
population b = 0</pre>
```

```
fit = lm(postsz ~ presz.perm, data=df) # fit the straight line model
  coef(fit)[2] # return the fitted b
})
## examine the distribution of b, when the population b = 0
hist(x, col="lightblue", main="", xlab="", xlim = c(-1,1))
abline(v = cs, col = 2)
```



```
## compute the chance of getting the data b, if the population b = 0
(pValue = mean(x > abs(cs)) + mean(x < -abs(cs)))
## [1] 0</pre>
```

Linear Models - Hypothesis testing - Slope = 1

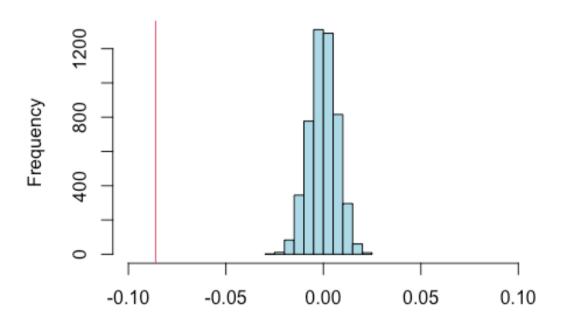
```
# Slide 4
df <- read.csv('../datasets/crabsmolt.csv')</pre>
```

```
## Hypothesis for slope = 1

## compute the estimate of b - 1 from the data
fit = lm((postsz - presz) ~ presz, data = df)
cs = coef(fit)[2]

## compute many sample gradients, when the population gradient is 1
x= replicate(5000, {
   presz.perm = sample(df$presz) # shuffle one variable
   fit = lm((postsz - presz) ~ presz.perm, data = df) # fit the model
   coef(fit)[2] # return the estimate of b
})

## examine the distribution of b - 1, when the population b = 1
hist(x, col="lightblue", main="", xlab="", xlim = c(-0.1,0.1))
abline(v = cs, col = 2)
```



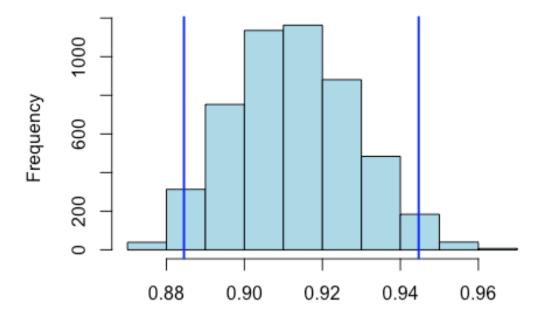
```
## compute the chance of getting the data b, if the population b = 1
(pValue = mean(x > abs(cs)) + mean(x < -abs(cs)))

## [1] 0

## Conclusion - Assuming the slope is 1, the probability of seeing
## a slope at least this extreme by mere chance is practically 0.
## It is concluded that the slope is not equal to 1.</pre>
```

Linear Models - Confidence interval

```
# Slide 4
df <- read.csv('../datasets/crabsmolt.csv')</pre>
n = nrow(df) # store the number of observations n
## compute a set of bootstrap samples of b
x= replicate(5000, {
  samp = sample(1:n, replace = TRUE, size = n) # sample the row
numbers (with replacement)
 # fit the regression model to the selected rows (samp) of the data
 fit = lm(postsz ~ presz, data = df[samp,])
 coef(fit)[2] # extract the estimate of b
})
## examine the bootstrap distribution of b
hist(x, col = "lightblue", main = "", xlab = "")
## add the interval lines
abline(v = quantile(x,c(0.025, 0.975)), col = "blue", lwd = 2)
```



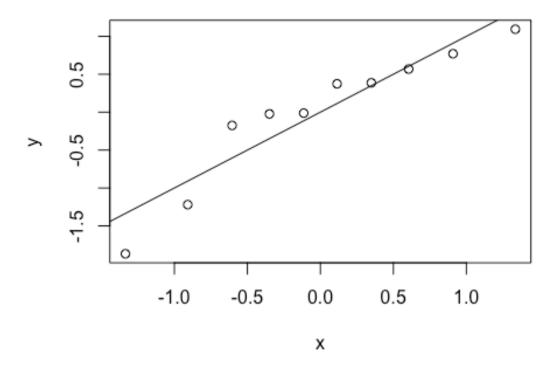
```
## print out the interval boundaries (95% interval)
quantile(x, c(0.025, 0.975))

## 2.5% 97.5%
## 0.8845042 0.9446943
```

QQ - Plot

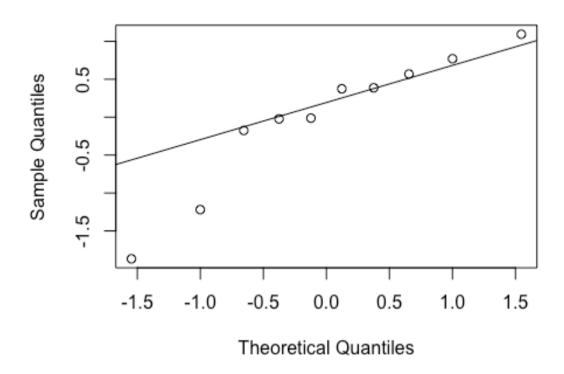
```
# Slide 12
# QQ plot
#
# y is the data being considered evaluated
# x is the normally distributed data being used as a reference
n <- 10 # Try different sample sizes</pre>
```

```
y <- rnorm(n)
# y <- rexp(n) # could try other distributions</pre>
# Order / sort the values
y <- sort(y)
\# P(Z < zi) = i / (n + 1)
# x represents probabilities (0, 1)
# BUT zero and one are not included
x \leftarrow 1: length(y) / (length(y) + 1)
# Convert the x values (probabilities) to x axis locations
x \leftarrow qnorm(x)
# Our crude version of a QQ plot
plot(y \sim x)
# intercept of zero, slope of one
# crude, probability not the best fit
abline(coef = 0:1)
```

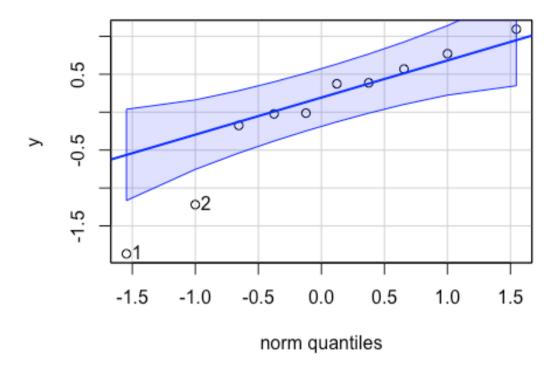


```
# built in functions to do this
# compare with above
qqnorm(y) # plot the QQ-plot
qqline(y) # add the line to the plot showing Normality
```

Normal Q-Q Plot



```
# better version
# An alternative is to use the car add-on library:
library(car)
## Loading required package: carData
qqPlot(y) # plot a QQ-plot with a line
```

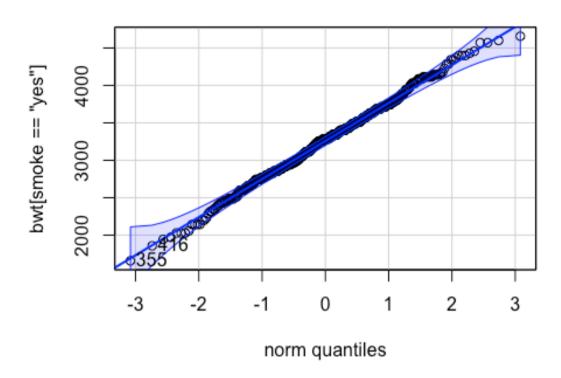


[1] 1 2

Birth weight QQ - Normal plot

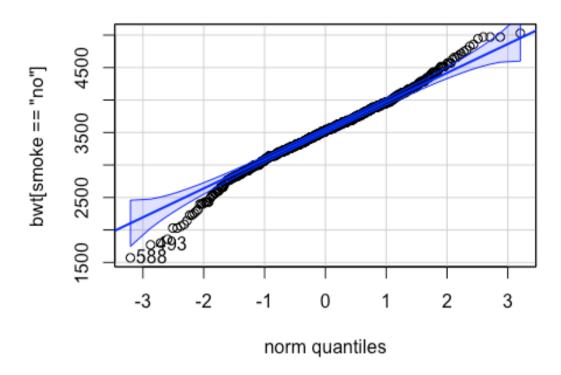
```
birthwt = read.csv("../datasets/birthwt.csv")
with(birthwt, qqPlot(bwt[smoke=="yes"], main="Smokers"))
```

Smokers



```
## [1] 355 416
with(birthwt, qqPlot(bwt[smoke=="no"], main="Non Smokers"))
```

Non Smokers



```
## [1] 588 493
```

T-test Birth weight

```
df <- read.csv('../datasets/birthwt.csv')
aggregate(df$bwt, list(df$smoke), length)
## Group.1 x
## 1 no 742
## 2 yes 484
aggregate(df$bwt, list(df$smoke), mean)</pre>
```

```
##
     Group.1
## 1
          no 3515,639
## 2
         yes 3260.285
aggregate(df$bwt, list(df$smoke), sd)
##
     Group.1
## 1
          no 497,0966
## 2
         ves 517.1097
# or
aggregate(bwt ~ smoke, df, sd)
##
     smoke
                hw+
## 1
       no 497.0966
## 2
      ves 517.1097
# Assuming equal variances in the populations
t.test(df$bwt ~ df$smoke, var.equal = TRUE,
       alternative = 't') # H1: mu1 <> mu2
##
##
   Two Sample t-test
##
## data: df$bwt by df$smoke
## t = 8.6527, df = 1224, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group no
and group yes is not equal to 0
## 95 percent confidence interval:
## 197.4554 313.2520
## sample estimates:
## mean in group no mean in group yes
##
            3515.639
                              3260.285
t.test(df$bwt ~ df$smoke, var.equal = TRUE,
       alternative = 'l') # H1: mu1 < mu2</pre>
##
    Two Sample t-test
##
## data: df$bwt by df$smoke
## t = 8.6527, df = 1224, p-value = 1
## alternative hypothesis: true difference in means between group no
```

```
and group yes is less than 0
## 95 percent confidence interval:
##
        -Tnf 303.9322
## sample estimates:
## mean in group no mean in group yes
            3515.639
##
                              3260.285
t.test(df$bwt ~ df$smoke, var.equal = TRUE,
       alternative = 'g') # H1: mu1 > mu2
##
## Two Sample t-test
##
## data: df$bwt by df$smoke
## t = 8.6527, df = 1224, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group no
and group yes is greater than 0
## 95 percent confidence interval:
## 206.7752
                  Tnf
## sample estimates:
## mean in group no mean in group yes
            3515.639
##
                              3260.285
```