

Problem: Implement a binary search tree with an insert method.

Constraints

- Can we insert None values?
 - No
- Can we assume we are working with valid integers?
 - Yes
- Can we assume all left descendents $\leq n <$ all right descendents?
 - Yes
- Do we have to keep track of the parent nodes?
 - This is optional
- Can we assume this fits in memory?
 - Yes

Test Cases

Insert

Insert will be tested through the following traversal:

In-Order Traversal

- 5, 2, 8, 1, 3 -> 1, 2, 3, 5, 8
- 1, 2, 3, 4, 5 -> 1, 2, 3, 4, 5

If the root input is None, return a tree with the only element being the new root node.

You do not have to code the in-order traversal, it is part of the unit test.

Algorithm

Insert

- If the root is None, return Node(data)
- If the data is \leq the current node's data
 - If the current node's left child is None, set it to Node(data)
 - Else, recursively call insert on the left child
- Else

- If the current node's right child is None, set it to Node(data)
- Else, recursively call insert on the right child

Complexity:

- Time: $O(h)$, where h is the height of the tree
 - In a balanced tree, the height is $O(\log(n))$
 - In the worst case we have a linked list structure with $O(n)$
- Space: $O(m)$, where m is the recursion depth, or $O(1)$ if using an iterative approach