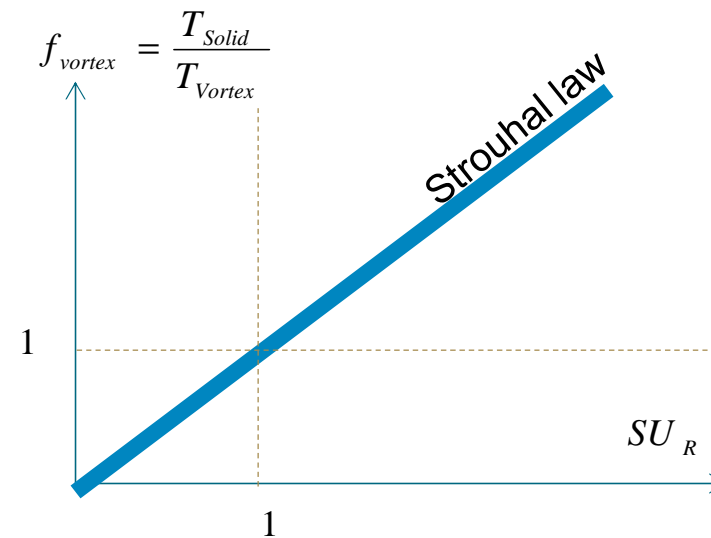


## FREQUENCY OF VORTEX SHEDDING



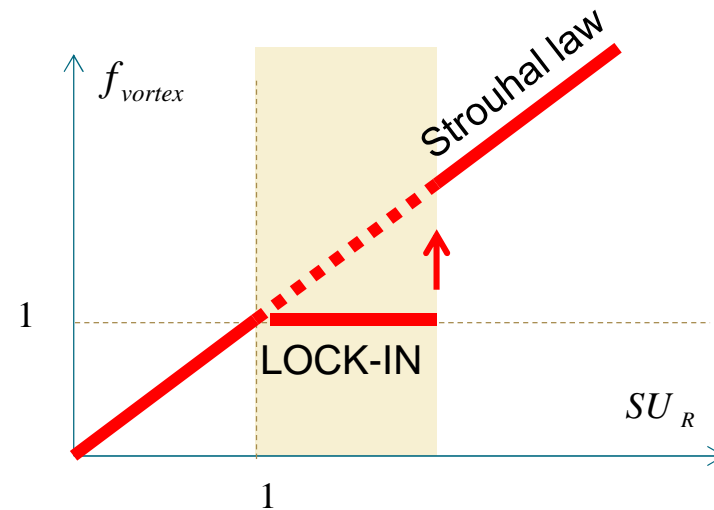
Fixed cylinder



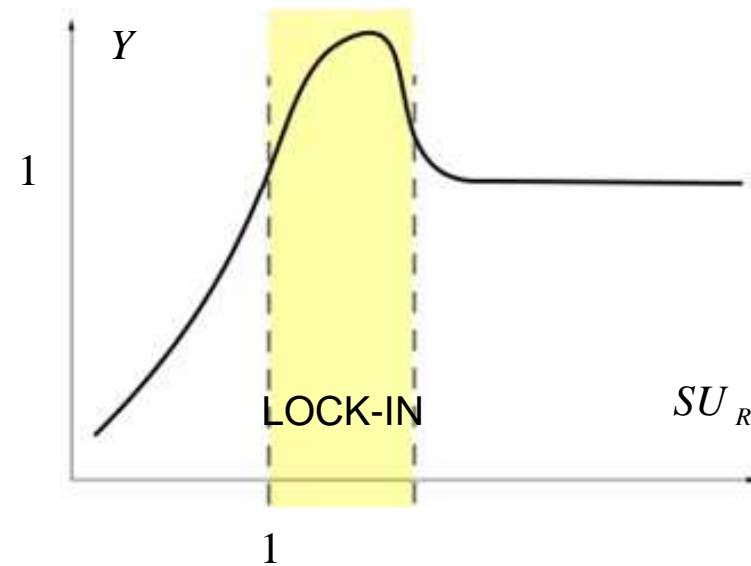
$$\text{Strouhal law } f_{Vortex} = \frac{T_{Solid}}{T_{Vortex}} = SU_R$$

# LOCK-IN OF THE FREQUENCY OF VORTEX SHEDDING

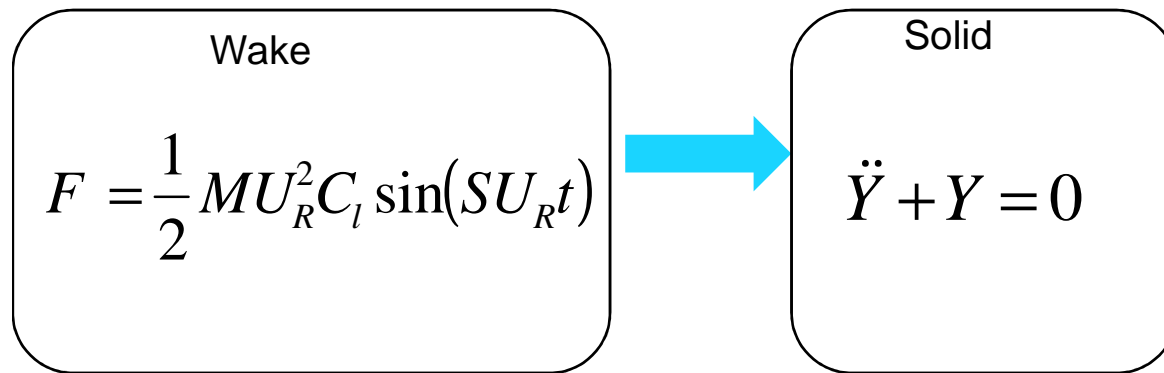
Cylinder free to move



# LOCK-IN OF THE FREQUENCY OF VORTEX SHEDDING



## BASIC MODEL OF VIV



$$\ddot{Y} + Y = \frac{1}{2} M U_R^2 C_l \sin(S U_R t)$$



Resonance curve

## BASIC MODEL OF VIV




Wake

$$\ddot{F} + (SU_R)^2 F = 0$$



Solid

$$\ddot{Y} + Y = 0$$

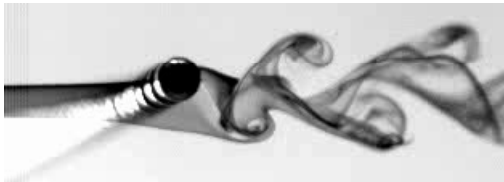
$$\ddot{Y} + Y = \frac{1}{2} MU_R^2 C_l F(t)$$


Resonance curve

## IMPROVED MODEL OF VIV

Wake

$$\ddot{F} + (SU_R)^2 F = A\ddot{Y}$$



Solid

$$\ddot{Y} + Y = \frac{1}{2} MU_R^2 C_l F$$



# VORTEX-INDUCED VIBRATION

Wake

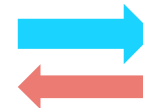


Cylinder



$$\ddot{Y} + Y = \frac{1}{2} MU_R^2 C_l \sin(SU_R t)$$

Wake

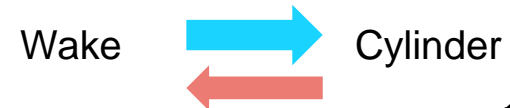


Cylinder

$$\ddot{F} + (SU_R)^2 F = A\ddot{Y}$$

$$\ddot{Y} + Y = \frac{1}{2} MU_R^2 C_l F$$

## COUPLED MODEL OF VIV



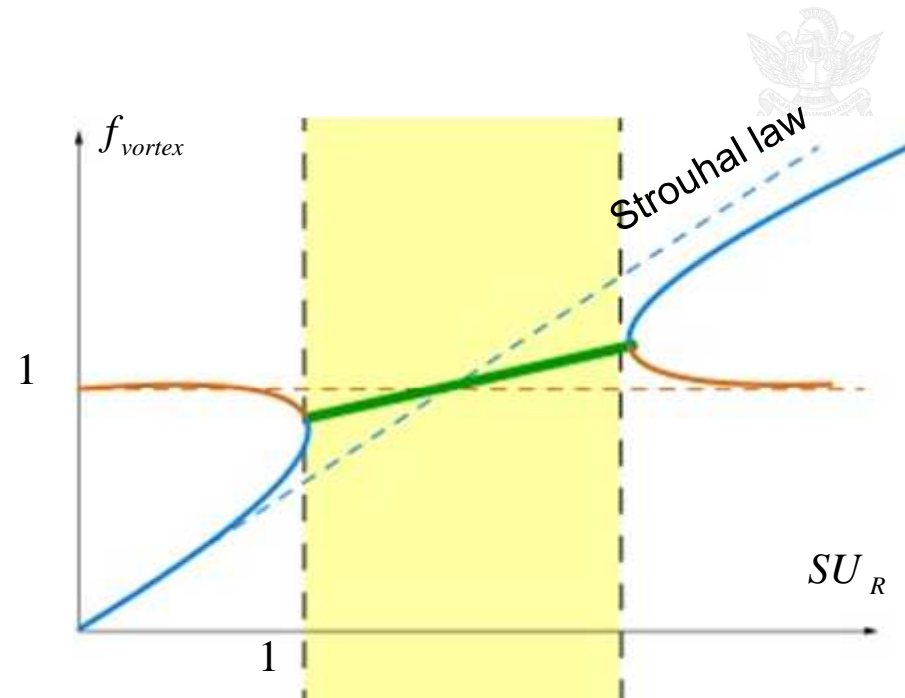
$$\ddot{F} + (SU_R)^2 F = A\ddot{Y} \qquad \ddot{Y} + Y = \frac{1}{2} MU_R^2 C_l F$$

$$\begin{bmatrix} Y \\ F \end{bmatrix} = \begin{bmatrix} Y_0 \\ F_0 \end{bmatrix} e^{i\alpha t}$$

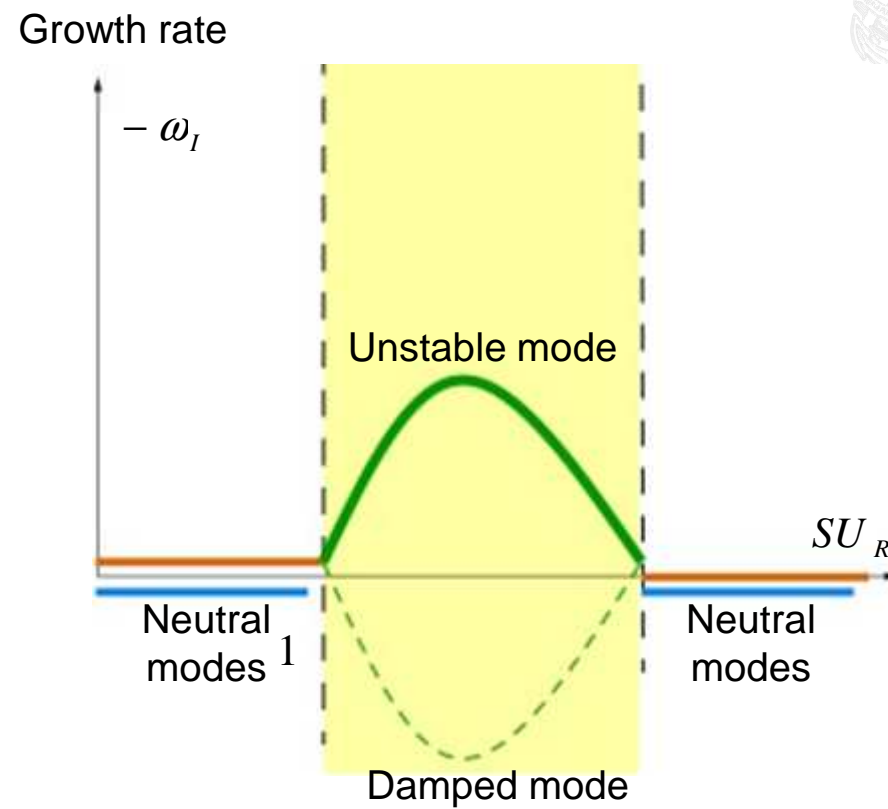
$$\omega_1(U_R) \quad \omega_2(U_R)$$



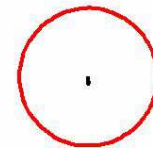
## COUPLED MODEL OF VORTEX-INDUCED VIBRATION



# COUPLED MODEL OF VORTEX-INDUCED VIBRATION



## TIME SCALES



# COUPLED-MODE INSTABILITIES

Solid mode 1

FLOW  
COUPLING

Solid mode 2

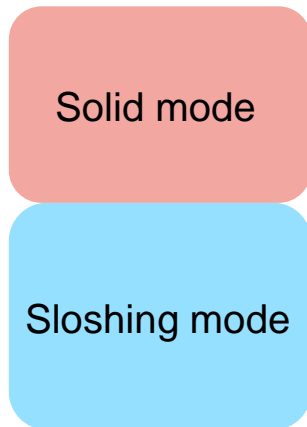
Solid mode

Fluid mode



# MODE COUPLING BETWEEN FLUID AND SOLID

Stable coupled mode



Unstable coupled mode  
with lock-in

