Maclaurin Series

Kutay

Made with LaTeX

February 21, 2024

Outline

What is it?

2 Why?

What is it?

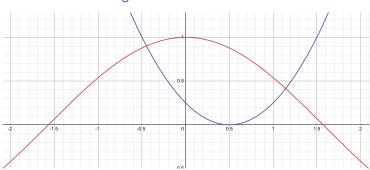
- Approximation of a function with an infinite series
- Approximates near 0

Why?

- To compute $\sin x$, $\cos x$, and e^x fast
- Calculators (your TI) use this technique
- To simplify equations/functions
- \bullet In simple pendulum, we approximated $\sin x$ with x

- Calculators can multiply, add, subtract, divide, and take powers of whole numbers quickly
- Let us use polynomials
- Polynomials are just multiplications, additions, and exponentiations

Figure: The Function $\cos x$

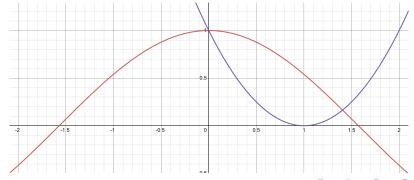


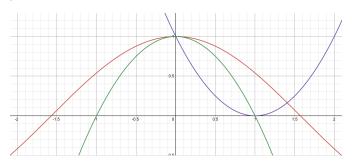
- Approximate to two degrees
- \bullet Find real numbers for a,b, and c that approximate $\cos x$ the best

$$\cos x \approx a + bx + cx^2$$

- We want to approximate near x = 0

$$\cos 0 = a + b \cdot 0 + c \cdot 0^2$$
$$1 = a$$





- The green function is better, but why?
- \bullet The rate of change is the same as $\cos x$ at x=0
- ullet Our approximation must have the same derivative at x=0
- $\cos' x = -\sin x$ and $(a + bx + cx^2)' = b + 2cx$

$$-\sin 0 = 0 = b + 2c \cdot 0$$
$$b = 0$$