

# Documentation for `maxwell.py`

This Python script simulates electromagnetic wave propagation using finite difference time domain (FDTD) methods. It utilizes the NumPy library for numerical operations and Matplotlib for visualizing the results through animations.

## Overview of the Code

The script initializes physical constants and simulation parameters, sets up the fields for electromagnetic waves, and iteratively computes the evolution of these fields over a specified number of timesteps. The results are displayed using an animated heatmap representation of the electric field.

## Code Structure

### Variables

- `num_timesteps` : Number of timesteps for the simulation, set to 1200.
- `n` : Size of the grid (1000 x 1000) for the simulation.
- `epsilon` : Permittivity of free space, a physical constant.
- `mu` : Permeability of free space, another physical constant.
- `Ez` : 2D NumPy array to hold the electric field (E) values along the z-axis.
- `Hy` : 2D NumPy array to hold the magnetic field (H) values along the y-axis.
- `Hx` : 2D NumPy array to hold the magnetic field (H) values along the x-axis.
- `c` : Calculated speed of light in the medium.
- `S` : Stability factor, set to  $1/\sqrt{2}$ .
- `dx` : Spatial step size, set to 1 micron.
- `dt` : Time step size calculated based on stability criteria.
- `lambda` : Wavelength of the wave, defined as 20 times the spatial step size.
- `omega` : Angular frequency calculated using the speed of light and wavelength.
- `Ca` , `Da` : Constants used in the update equations for the electric field.
- `Cb` , `Db` : Constants used in the update equations for the magnetic fields.

### Main Logic

The core of the simulation is encapsulated in a loop that iterates over the specified number of timesteps. Here's a breakdown of the operations performed in each iteration:

- If it is the first timestep, the central point of the electric field array `Ez` is initialized to 1, simulating an impulse.
- The magnetic field along the y-axis (`Hy`) is updated based on the differences in the electric field.
- The magnetic field along the x-axis (`Hx`) is updated similarly.
- The electric field (`Ez`) is updated based on the current values of the magnetic fields.
- The central point of the electric field is reset to 1.
- Every fifth timestep, an image of the current state of the electric field is captured for animation.

## Visualization

After the loop, an animation of the electric field is created using Matplotlib's `ArtistAnimation` feature. This animation displays the evolution of the electric field over time, providing a visual representation of the wave propagation.

## Example Usage

To run the script, simply execute it in a Python environment where NumPy and Matplotlib are installed. You can observe the animated output showing the propagation of electromagnetic waves.

## Conclusion

This script is a great example of how to implement FDTD methods for electromagnetic simulations. It's a useful starting point for anyone interested in computational physics and can be easily modified to explore different parameters and configurations.