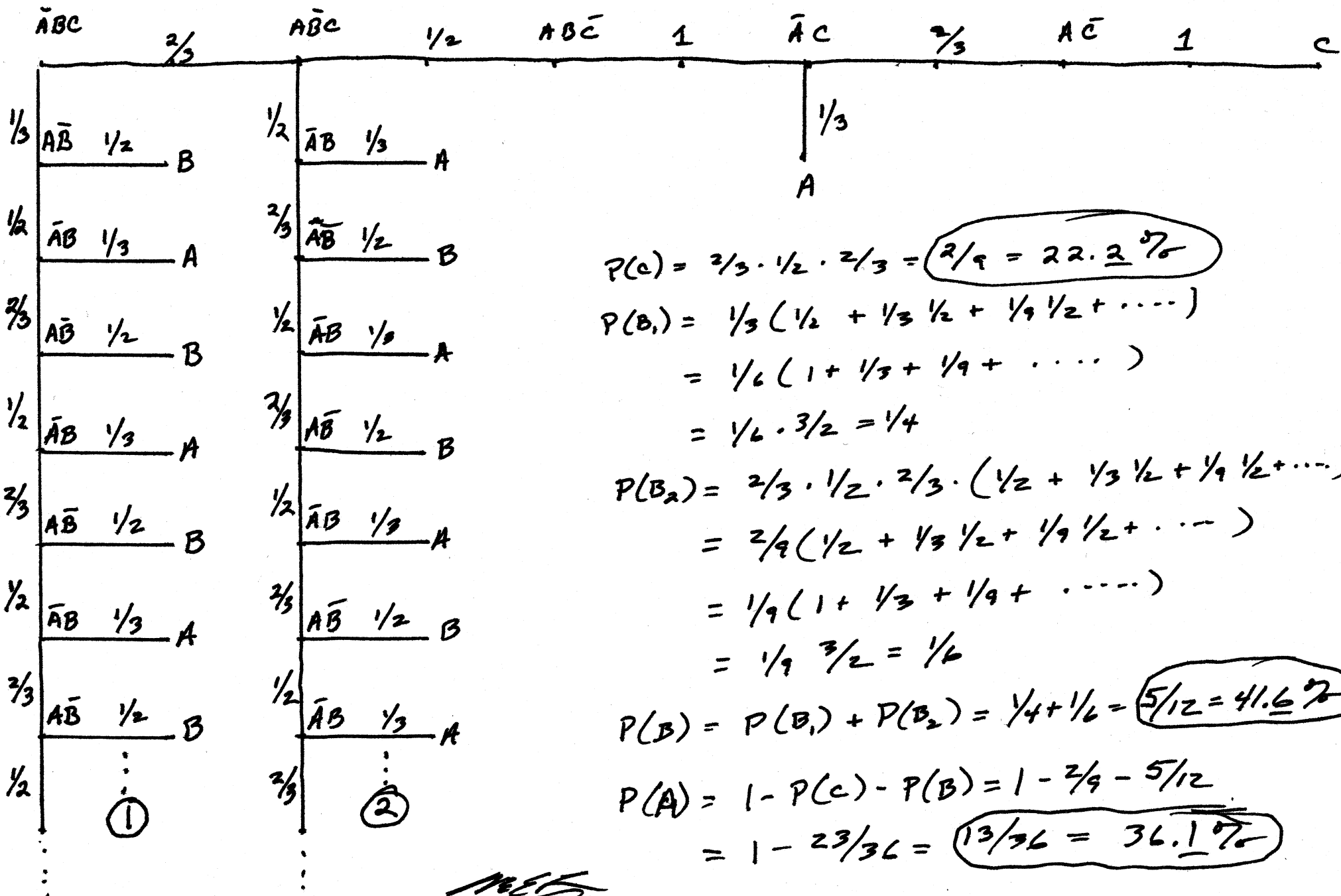


Shoot - Out Problem

Compare Calculations to Simulation



$$P(C) = \frac{2}{3} \cdot \frac{1}{2} \cdot \frac{2}{3} = \frac{2}{9} = 22.\underline{2}\%$$

$$\begin{aligned} P(B_1) &= \frac{1}{3} \left(\frac{1}{2} + \frac{1}{3} \frac{1}{2} + \frac{1}{9} \frac{1}{2} + \dots \right) \\ &= \frac{1}{6} \left(1 + \frac{1}{3} + \frac{1}{9} + \dots \right) \\ &= \frac{1}{6} \cdot \frac{3}{2} = \frac{1}{4} \end{aligned}$$

$$\begin{aligned} P(B_2) &= \frac{2}{3} \cdot \frac{1}{2} \cdot \frac{2}{3} \cdot \left(\frac{1}{2} + \frac{1}{3} \frac{1}{2} + \frac{1}{9} \frac{1}{2} + \dots \right) \\ &= \frac{2}{9} \left(\frac{1}{2} + \frac{1}{3} \frac{1}{2} + \frac{1}{9} \frac{1}{2} + \dots \right) \\ &= \frac{1}{9} \left(1 + \frac{1}{3} + \frac{1}{9} + \dots \right) \\ &= \frac{1}{9} \cdot \frac{3}{2} = \frac{1}{6} \end{aligned}$$

$$P(B) = P(B_1) + P(B_2) = 1/4 + 1/6 = \underline{5/12 = 41.6\%}$$

$$P(A) = 1 - P(C) - P(B) = 1 - \frac{2}{9} - \frac{5}{12}$$
$$= 1 - \frac{23}{36} = \frac{13}{36} = 36.1\%$$