

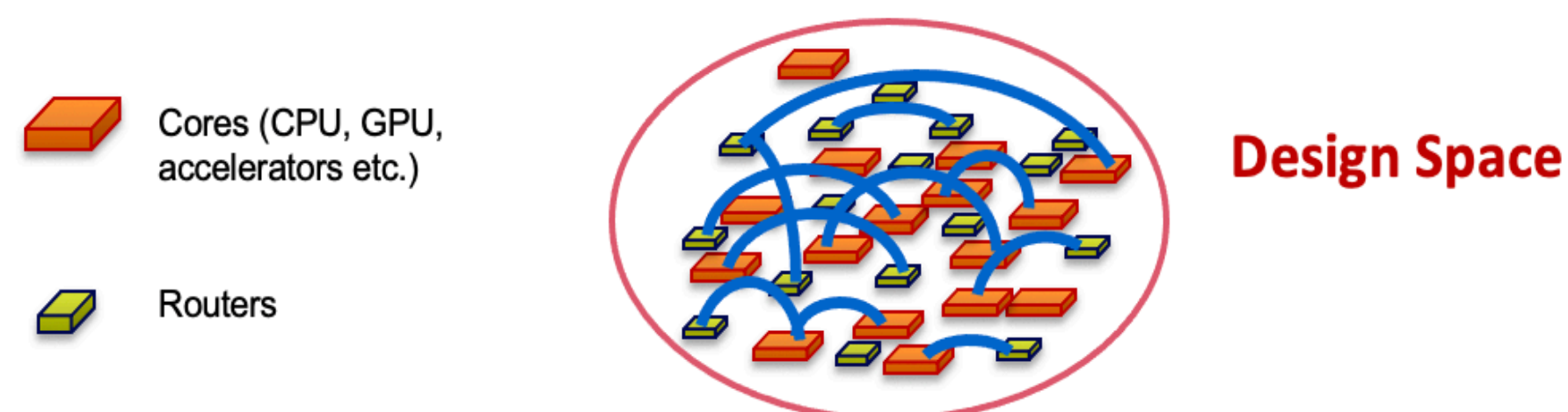
# Scalable Combinatorial Bayesian Optimization with Tractable Models

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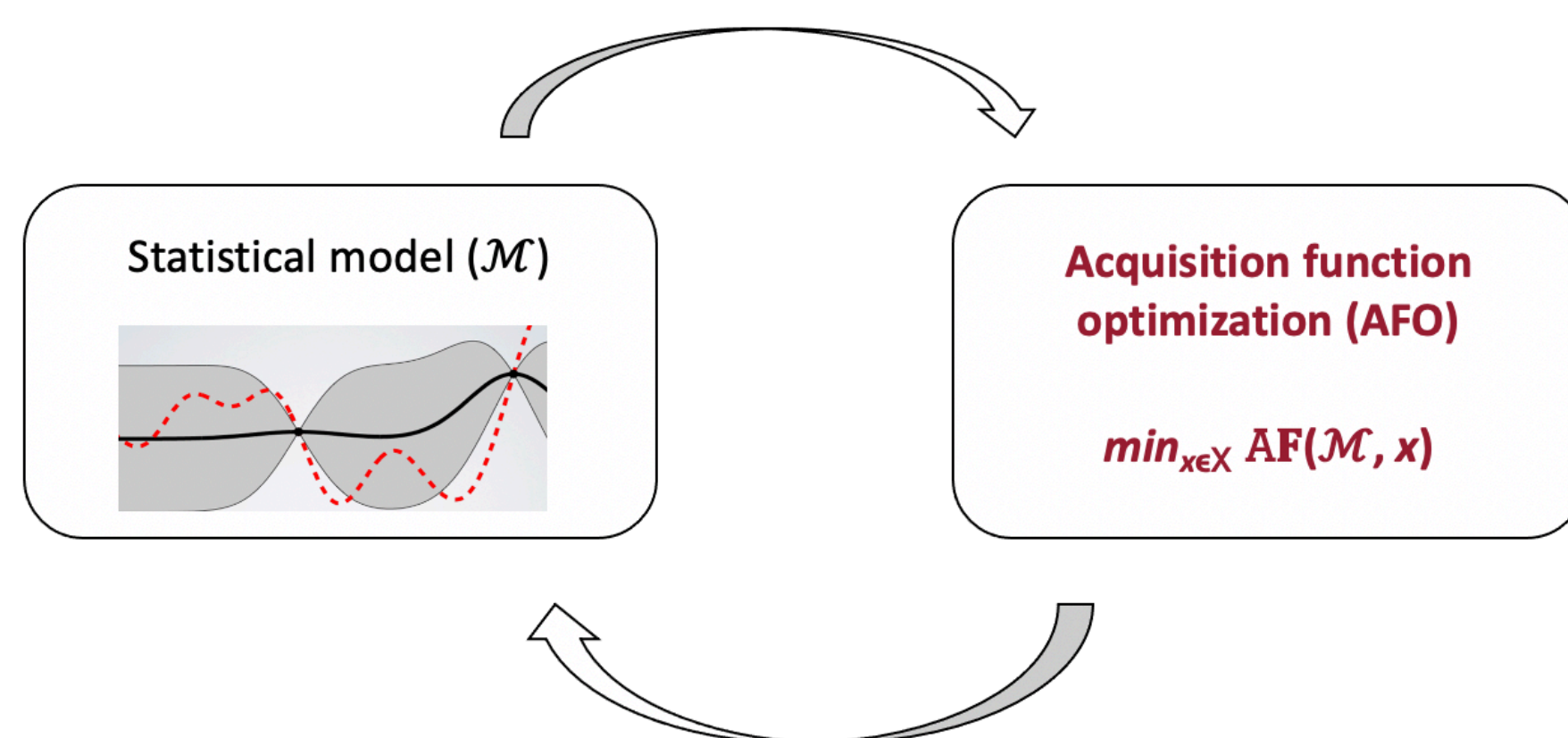
## Introduction

- **Problem:** Optimize *expensive black-box* functions over *combinatorial* spaces (e.g. sets, sequences, graphs)
- Many applications in science and engineering. For example, multi-core chip design, materials design etc.



- **Goal:** find a structure that optimizes a black-box function by *minimizing the number of function evaluations*

## Bayesian Optimization Framework



- **Key challenge:** Balancing tradeoff between Statistical model and Acquisition function optimization

## Parametrized Submodular Relaxation

- **Statistical model** (Baptista R. And Poloczek M.)   
 -  $f_{\alpha}(x) = \alpha_0 + \sum_j \alpha_j x_j + \sum_{i,j > i} \alpha_{ij} x_i x_j; x \in \{0,1\}^n$
- **Acquisition function** : Thompson Sampling
- **Acquisition function optimization (AFO)**   

$$\min_{x \in \{0,1\}^n} f_{\alpha_t}(x)$$

$$\min_{x \in \{0,1\}^n} x^T A x + b^T x$$
 Binary quadratic programming (BQP) problem

- Construct a  $\Lambda$ -parametrized submodular of the BQP objective

$$h_{\Lambda}(x) + x^T A^- x \leq x^T A x + b^T x$$

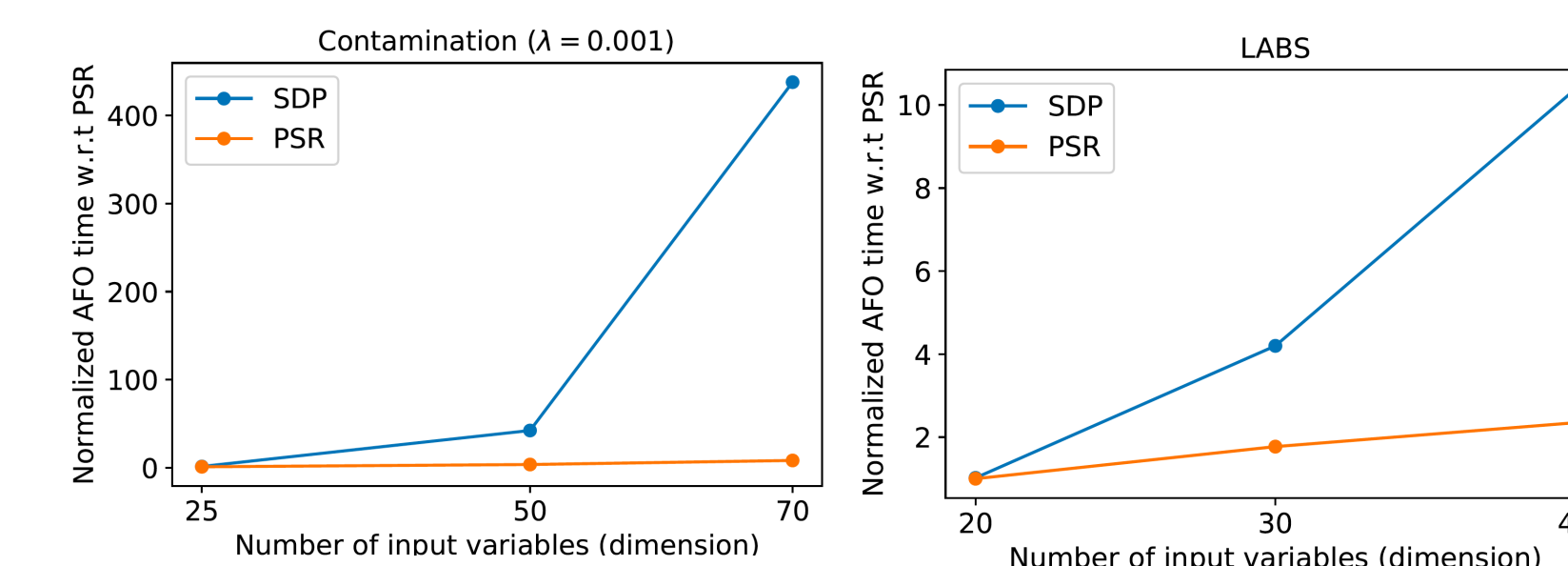
- Relaxation solvable via scalable & efficient minimum graph cut algorithms
- Optimize the relaxation over  $\Lambda$

$$h_{\Lambda_1}(x) + x^T A^- x \leq h_{\Lambda_2}(x) + x^T A^- x \leq \dots \leq x^T A x + b^T x$$

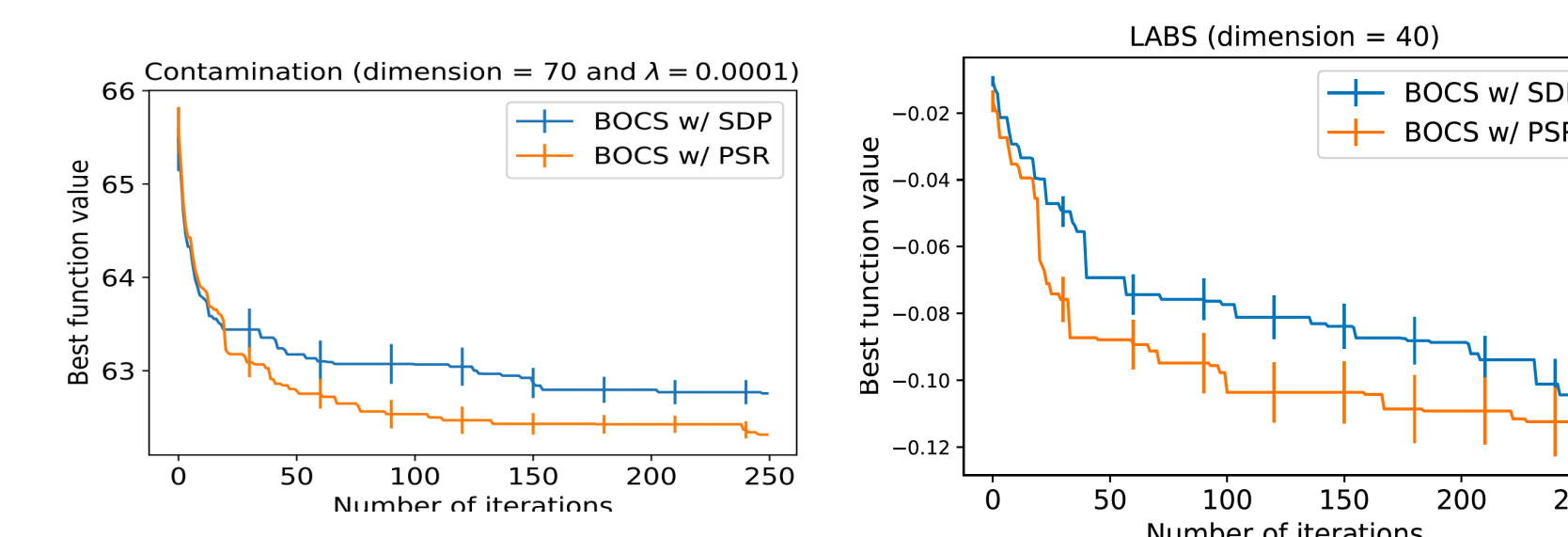
- Inspired by work on prescriptive price optimization (Ito S. and Fujimaki R.)

## Experimental Results

- **Scalability**   
 - PSR scales better than SDP



- **Overall BO performance**   
 - PSR finds better AFO solutions



## References

- Baptista, R. & Poloczek, M..** (2018). Bayesian optimization of combinatorial structures. *Proceedings of the 35th International Conference on Machine Learning*, in PMLR 80:462-471
- Ito, S., & Fujimaki, R.** (2016). Large-scale price optimization via network flow. In *Advances in Neural Information Processing Systems* (pp. 3855-3863).

