

Outlier Detection of Generalized Deduplication Compressed IoT Data

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June 5, 2022

Abstract—The emerging growth of Internet of Things leads to an immense volume of data being generated. Leading to numerous network and storage challenges that are to be solved with compression. Decompressing the large amount of data to apply analytical methods is costly. Generalized Deduplication is a compression technique that has low distortion and enables analytical capabilities of compressed data. Anomaly detection techniques are applied and evaluated on the compressed and decompressed data. The techniques used are Isolation Forest and an extended version tailored to data compressed by Generalized Deduplication. It showed that the capability of identifying anomalies is not lost after compression. The extended version succeeding in classifying fewer inliers as outliers, but at the cost of processing time and memory usage.

Index Terms—Internet of Things, Anomaly Detection, data compression, data mining

I. INTRODUCTION

The expansive growth of Internet of Things (IoT) enables many revolutionary and futuristic applications. However, the large quantity of sensors leads to an immense volume of data needing to be processed at the edge and potentially forwarded to the cloud. Hence, the topology meets severe challenges regarding data transmission and storage. Compression is the apparent mechanism to address these challenges by reducing the volume being transmitted and stored. Compressing the data does not come without disadvantages. Processing time is required during compression and decompression. Additionally, it might not be possible to perform various analytics on the compressed data, as it might have lost its intrinsic meaning. This leads to a trade-off between compression and distortion[1]. The possibility of performing analytics varies on the compression algorithm and whether it is lossy or lossless. Being able to perform analytics on the compressed data enables edge nodes to act more intelligently without the drawbacks of decompression. Analytics of interest are techniques such as clustering, classification, basic queries (e.g. mean and variance) and outlier detection. Depending on the results of an analytic the node could make intermediate decisions and improve the performance and overall functionality of the system.

Performing analytics on compressed data is not an untouched subject. There are researchers looking at different

aspects, analytics and compression algorithms. Work has been done in performing classification and anomaly detection within network communication on compressed data [2]. It is done by developing a novel collection of algorithms and models that uses compression techniques to identify classes and anomalies. The core idea of the method is to utilize their new slice compression (SC) as a pre-processing step to identify parts of data as either application or protocol data. This is used for classification and extended to slice compression for anomaly detection (SCADe). SCADe utilizes the slice compression in combination with a threshold for identifying anomalous data. Slice compression is lossy and used to tell what features are need to be examined. Therefore, there is no need to analyze all decompressed data, but instead only analyze the features depicted by slice compression.

Lossy compression can by definition obtain better compression than lossless compression, and still maintain key information regarding the performance of analytics. However, the data distortion is not feasible for all applications. Being able to easily decide between lossy and lossless compression at different parts of the system is therefore a desired quality. We will use Generalized Deduplication[3] (GD) which is a lossless compression technique, however it does not require much change to become lossy. GD has desired features such as easy explainability, suits IoT data and good random access. The efficient random access is key and enables the analytical capabilities. Previous work has been done regarding analytics of GD compressed data[4]. It researches how clustering can be performed on an artificial, an artificial with noise and a power consumption data set. The research showed that even with high compression rate it was still performing close to the uncompressed data sets.

This paper will look at performing anomaly detection on GD compressed data. There are many anomaly detection methods suited for IoT data[5]. Each have their own advantages and disadvantages. Some are supervised, distributed, online while others are unsupervised, centralized and offline. We will utilize the ensemble tree method Isolation Forest (iForest). The reasoning is that it is simple, well-suited for IoT data and normalization of features is not required. Isolation Forest works by performing horizontal and vertical splits in the

feature space, and thereby identifying the anomalies by seeing how easy they are to isolate. The horizontal and vertical splits is a potential flaw and can result in certain anomalies not being detected. This is handled in an extended version, that performs diagonal splits [6]. We will not utilize the diagonal splits, however we propose our own extension that is tailored for GD compressed data. GD natively creates a large amount of duplicates. Therefore, we look into utilizing the amount of duplicates to avoid wrongly classifying inliers as outliers.

The rest of this paper covers the background of used methods in Section II, the proposed methods in Section III, the conducted experiments in Section IV and an evaluation of the results in Section V. The paper is concluded in Section VI.

II. BACKGROUND

A. Generalized Deduplication

Deduplication is a technique to perform compression in storage systems. The technique works by utilizing the similarity of file chunks. Each unique file chunk is stored once. Subsequent copies of the chunks are then replaced with a reference to the stored chunk. The method is established and shown to have good compression gain on various practical scenarios[7]. However, if there are minor discrepancies in the file chunks, the technique will not leverage any of the similarities. Resulting in the near-identical chunks being stored in full. Sensor data from IoT devices is one example of the data potentially being near-identical.

To utilize the similarities in the almost identical data, a generalization of deduplication has been studied. This method considers the chunks at the bit level and splits them into two parts, the *base* and *deviation*. The *base* is the identical part that is to be stored once and hereafter referenced with pointers. The *deviation* is the disparity between the chunks. Looking at a simple example with four 6-bit numbers, 100000, 100001, 100010 and 100011. It can be identified that the four most significant bits of the numbers are identical. Hence, leading to all having a shared *base* of 1000. The two least significant bits are then the *deviation*[3].

B. Isolation Forest

Anomaly detection is a combination of outlier- and novelty detection. Including both identifying outliers in the training data and determining if unseen observations are outliers. Isolation Forest (iForest) is an anomaly detection method. It differs from other popular techniques in the way that it identifies anomalies explicitly instead of profiling ordinary data points[8]. IForest utilizes decision trees similar to other tree ensemble methods. The main principle is to recursively split each data point, and then evaluate the amount of splits necessary to split each data point. The logic is that anomalies will require fewer splits to be isolated than an ordinary point. Trees are built by selecting a random feature and then selecting a random value between the minimum and maximum value of that feature. The process is then repeated until all data points

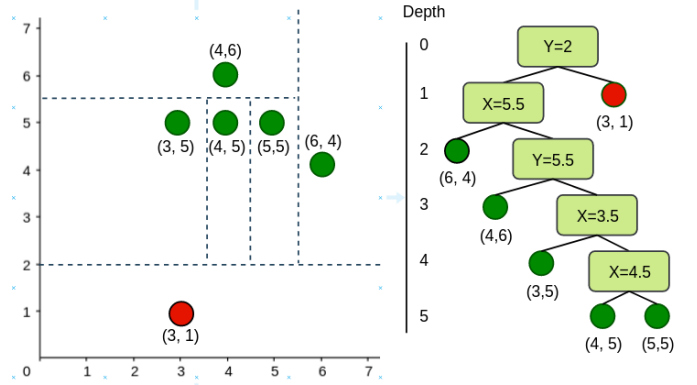


Fig. 1: *left*: Green data points forming a cluster while the red is an outlier. The dotted lines are the splits performed by iForest. *right*: The decision tree build by the splits.

are isolated or a maximum height of the tree is reached. An illustration can be seen on Figure 1.

The graphic shows an example of a decision tree and how an anomaly is at a lower depth of the tree. When determining if an observation is an outlier iForest calculates a score, it is defined as:

$$s(x, n) = 2^{-\frac{E(h(x))}{c(n)}} \quad (1)$$

$E(h(x))$ is the average length from the root node to the specific data point. This is the average over a group of trees. $c(n)$ is the average length from the root node to an external node. The anomaly score s is between 0 and 1. Scores close to 1 is seen as anomalies while values close to 0 is seen as normal data points.

III. METHODS

A. Isolation Forest on GD compressed Data

Data compressed with Generalized Deduplication results in having a set of bases, deviation and references linking a data point to its base and deviation. In the following example the deviation will be omitted. Say we have the data set S where $S \in \mathbb{R}^2$. Performing GD on S will result in each feature of the points being mapped to their bases. Having a point $x = [x_1, x_2]$ where $x \in S$ and some computed bases ids b_0, b_1, \dots, b_n , then the transformed version $x^* = [x_1^*, x_2^*]$ will hold the computed bases. This is depicted on Figure 2. The bases are computed on the raw data and referenced in the features x_1^* and x_2^* .

Isolation forest is then to be performed on the transformed version of the data set. The isolation forest splits before compression could be seen on Figure 1. Figure 3 is similar but is instead performing the splits on the bases. It is seen that certain data points will map to identical bases on both features.

B. DupRes Isolation Forest

The bases of GD compressed data will inherently be grouped. Stripping the deviation of each data point will result

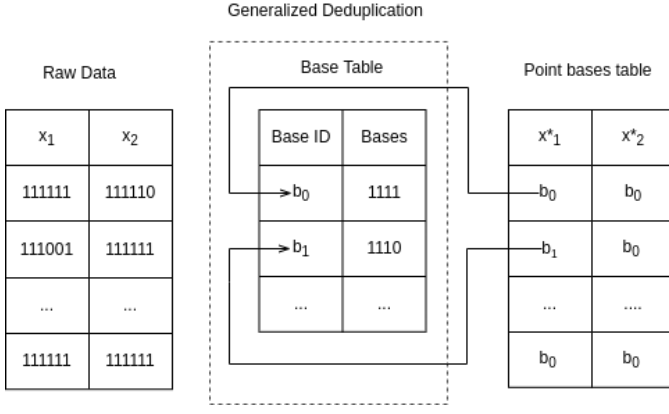


Fig. 2: Illustration showing how Generalized Deduplication compresses the raw data into points referencing the bases.

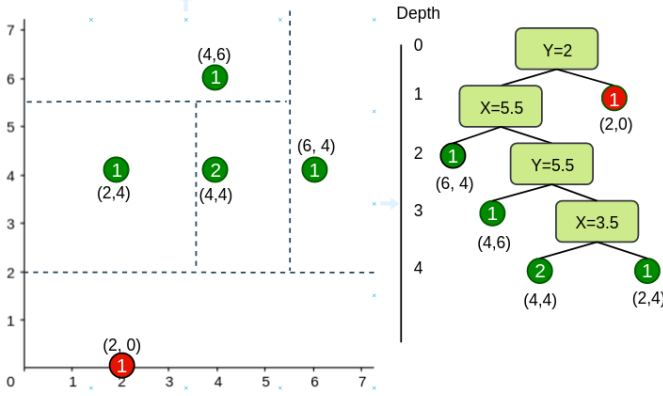


Fig. 3: Similar to Figure 1 but instead illustrates iForest on the compressed data. The number in the circles illustrates amount of grouped data points.

in data points being placed in bins. This binning is illustrated on Figure 4 and 5. The graphics shows the bins created with different amount of deviation bits. The circles are samples. The dotted lines are enclosing areas where data points in an area will be mapped to the closest base in the negative direction. The arrows illustrate the base each data point will be mapped to. Having a larger amount of deviation bits is leading to larger bins.

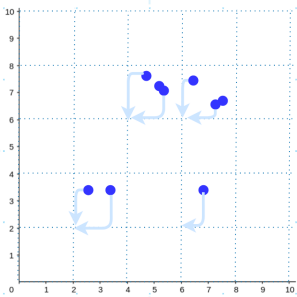


Fig. 4: Binning with 1 deviation bit

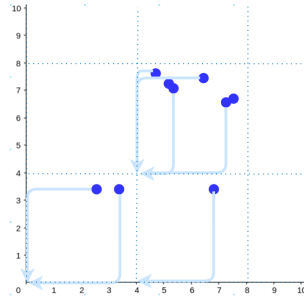


Fig. 5: Binning with 2 deviation bits

Larger bins might lead to a better compression rate however it could lead to undesired behavior when trying to detect anomalies with iForest. An outlier could be mapped to the same base as an inlier on all or some of its features. Having the same base on some features will make it harder to isolate the outlier meanwhile having identical bases on all features makes it impossible. The binning as well leads to inliers being grouped on fewer points. This causes them to be isolated more easily, and thus labeled as outliers.

Isolation Forest is not fit for the large amount of duplicates that is potentially created by compressing with Generalized Deduplication. Therefore, a more duplicate resistant (DupRes) version is proposed. The core idea of the new version is to utilize the amount of duplicates when building the tree. The amount is then used to adjust the score of an observation. A revised version of the score function is:

$$s(x, n) = 2^{-\frac{E(h(x)) + \log_2(x_{count})}{c(n)}} \quad (2)$$

The new function differs from Equation 1 by the introduction of the $\log_2(x_{count})$ term. x_{count} is the amount of occurrences of the given sample. The reason behind using the binary logarithm is firstly that having one occurrence will not modify the score, $\log_2(1) = 0$. Secondly, it is a strictly increasing function. Resulting in the higher the x_{count} , the larger adjustments will be made to the score. The modification makes no changes in the range of s and in how it should be interpreted. For further details, see the original paper [8].

The change implies that the count of each sample is known. This requires extending what is done in the training phase of the model. Beside building the decision trees, the model must store each unique sample with the amount of occurrences. Worst case the training set contains no duplicates and will store all training samples with the count of one. Hereby, the model is not optimal if the data is expected to have a low amount of duplicates. The flow during the evaluation of unseen observations, is to identify the ones that were seen in the training phase and retrieve their counts. The adjusted score is then computed and can be used to identify anomalies.

IV. EXPERIMENTS

The experimental setup will be described in this section. Three models will be evaluated, Isolation Forest on the original data before compression, Isolation Forest on the compressed data and the proposed DupRes Isolation Forest on the compressed data. We will refer to the different models in the same order as, **original**, **bases** and **DupRes**. The models are evaluated on various datasets containing anomalies. The datasets are described in the following subsections.

Synthetic

The synthetic dataset is self-generated. It is two-dimensional where each feature is an integer. The dataset contains three clusters where the samples are normally distributed with a standard deviation of 2, $N(\mu, 2^2)$ where μ varies on the cluster center. The data set is represented before and after compression on Figure 6. Each cluster consists of 150 samples

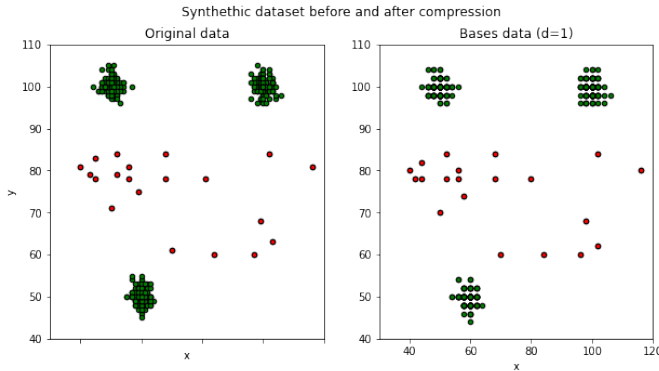


Fig. 6: Synthetic data set before(left) and after(right) compression with 1 deviation bit. Green points are inliers, while the red are outliers.

and 20 outliers are generated between the clusters. There is then a total of 470 samples.

Pendigits

Pendigits is a database for handwritten digits. Originally it contains 16 integer features with 10 classes (one for each digit). The dataset's 6870 samples is mapped to inliers and outliers to be utilized for anomaly detection [9].

Shuttle

The shuttle dataset contains 49097 samples collected from a shuttle. It has 9 dimensions all being integers [9].

Waveform

Waveform contains 3443 samples with 100 outliers. It has 21 features that are all numeric [10].

WBC

The WBC dataset contains data of measurements from breast cancer cases. The inliers are the benign class, while the outliers are the malignant class. It contains 278 samples with 30 dimensions [9].

A. Preprocessing

All the features of the synthetic, pendigits and shuttle datasets can be represented as a one byte integer. However, the WBC and waveform datasets contains floating numbers. Therefore, the features are scaled with a factor of 10.

B. Procedure

The experiments are realized in Python and can be found for replication on GitHub¹. DupRes is implemented by extending *sklearn*'s existing Isolation Forest functionality. Thus, a fork is as well to be found on GitHub². Each dataset is split in a training set and test set with a 80%/20% proportionality. The split is done in a stratified manner, meaning it is ensured to be inliers and outliers in both sets. We had the three

models; **original**, **bases** and **DupRes**. The original requires no additional transformation of the data. However, the other two requires the GD compressed version of the data. Hence, we store both the original and the compressed data. The models are then trained on the training data and evaluated on the test data in sequence.

C. Performance evaluation

As Isolation Forest by nature introduces randomness in building its decision trees, we train and evaluate each model 50 times. At each iteration various performance metrics are stored. When all iterations are complete we remove the lowest and highest scoring of each metric and take the mean of the remaining values. The mean value is then the resulting value for that metric on a given model. The different metrics that is looked at is training time, testing time, accuracy, f1, recall and precision. The training and testing time tells, how much processing time is used to fit the model on the training data and to predict unseen samples in form of the test data. Accuracy show in percentage how many observations are predicted correctly. Recall relate to the ability of finding all positive samples. In the experiments conducted we have set the inliers to be the positives while the outliers to be the negatives. Precision includes the false positives in its calculation. This means in our case that precision can intuitively be used to see if the outliers are correctly detected. The f1-score is the harmonic mean of the precision and recall [11].

V. RESULTS

This section will present and interpret the results from the conducted experiments. There are many experimental setups. Three different models evaluated on five datasets with varying amount of compression. Then in addition to that, there is many metrics to be looked at. To illustrate this comprehensive amount of results, Table I has been constructed. The table contains the results of three of the five datasets. The table will be referred to repeatedly in the following examination of the results. The values that are referred to is marked with bold.

A. Execution time

Starting off with looking at the execution time. The training and test time on the synthetic dataset can visually be seen on Figure 7. It shows no apparent difference between neither the training nor testing time of the original and bases model. However, there is a clear difference between those two and DupRes. Both the training in which the uniques are found and in the testing in which the duplicates are looked up adds additional execution time. This performance cost can also be seen in the table for the pendigits dataset. Here we have 93.7/55.3 ms train/test time for the original model, while DupRes with 1 deviation bit has 135/282 ms train/test time. Additionally, it can be seen that DupRes with 6 deviation bits has 145/131 train/test time. This implies that, as the amount of deviation bits rise, the testing time decreases. This makes sense as less uniques are found during the training phase, and thus fewer entries in the table need to be looked through during

¹<https://github.com/mIRosenquist/au-mlr-research-and-development-dedup>

²<https://github.com/mIRosenquist/scikit-learn>

Model	Dataset	Dev. bits	Metric				Time		Lossy Compression Rate	
			acc.	f1	rec.	prec.	T(ms)	E(ms)	Rate	Memory Overhead (bytes)
Original	Synthetic		0.75	0.85	0.73	1	78.8	51.4	1	0
	Pendigits		0.54	0.70	0.54	1	93.7	55.3	1	0
	WBC		0.94	0.97	0.94	1	75.2	22.0	1	0
Bases	Synthetic	1	0.72	0.83	0.71	1	80.2	51.2	0.35	0
		3	0.90	0.95	0.90	1	74.6	46.4	0.08	0
		6	0.04	0	0	0	74.3	45.0	0.01	0
	Pendigits	1	0.53	0.70	0.53	1	95.1	55.7	0.875	0
		3	0.51	0.67	0.51	1	94.3	55.9	0.625	0
		6	0.42	0.59	0.41	1	95.3	56.0	0.06	0
	WBC	1	0.94	0.97	0.94	1	75.3	21.6	0.58	0
		3	0.94	0.97	0.94	1	75.6	21.6	0.41	0
		6	0.95	0.97	0.94	1	74.8	21.4	0.02	0
DupRes	Synthetic	1	0.87	0.93	0.87	1	90.4	59.7	0.35	195
		3	0.92	0.95	0.91	1	85.8	55.4	0.08	56
		6	0.98	0.99	1.00	0.98	86.5	53.4	0.01	6
	Pendigits	1	0.54	0.70	0.53	1	135	282	0.875	118410
		3	0.50	0.67	0.50	1	135	286	0.625	86680
		6	0.80	0.89	0.80	1	145	131	0.06	4245
	WBC	1	0.94	0.97	0.94	1	86.9	23.4	0.58	5123
		3	0.94	0.97	0.94	1	87.7	23.7	0.41	3713
		6	0.95	0.97	0.94	1	85.6	23.5	0.02	153

TABLE I: Table containing results of the conducted experiments. The original model performing iForest on uncompressed data. Bases performing iForest on the compressed Data. DupRes which performs extended iForest on the compressed data. Shows the performance metrics(accuracy, f1, recall and precision) and execution time of the various datasets with different amount of compression.

testing. This incentivizes to not use the model if a low amount of duplicates is expected in the data or a low amount of deviation bits is utilized. Originally an implementation utilizing pandas[12] dataframes was used. However, this performed notably worse than the current implementation which uses numpy[13] arrays. To optimize this further an implementation could be made in c or c++ and utilize the interoperability to Python.

B. Metrics and Scoring

Then we look at the performance of the models in terms of metrics and scoring. Figure 8 illustrates the performance metrics of the models on the datasets. In general, it can be seen on the figure that the models are performing quite similar. Investigating the metrics for the synthetic dataset a clear pattern can be seen. The bases model performs better than the original, meanwhile DupRes performs better than the bases. The cause of this can be derived from the recall. Since the positives are the inliers the original is simply classifying more inliers as outliers than the others. It is using too few splits in isolating them. As we compress the data the inliers

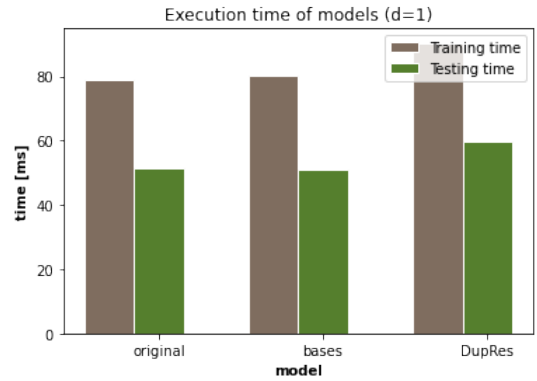


Fig. 7: Training and testing time of the models on the synthetic dataset.

are harder to isolate due to clustering. Utilizing the many duplicates in DupRes we are then classifying fewer inliers as outliers. Similar trends are not be seen on the other datasets. On the recall of the Pendigits dataset it is seen that the original

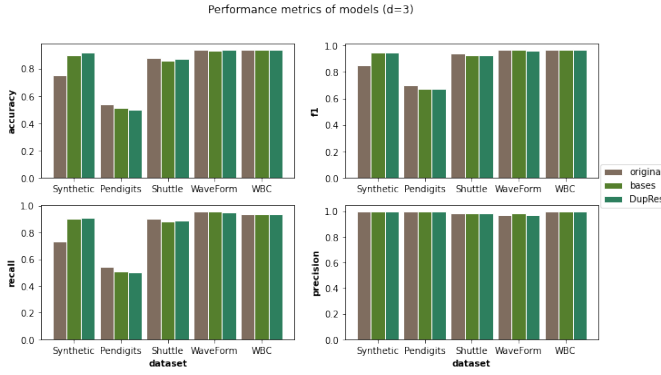


Fig. 8: Performance metrics of the models with 3 deviation bits.

model predicts less false positives than the others.

Looking at the table there is several interesting observations. All models except two detect every outlier. The two instances are the bases model and DupRes on the synthetic dataset with 6 deviation bits. The bases model predicts every observation as an outlier resulting in 0 scores. Since a lot of data points is grouped with this amount of deviation bits, DupRes will not do the same action as the other model, and therefore have a precision score of 0.98. This implies that one outlier observation might have grouped with the inliers. DupRes will wrongfully push this to be an inlier. Investigating the performance regarding the WBC set it is seen that the performance is almost identical. There are minor discrepancies in the accuracy however the rest is identical. This implies that even though compression is performed, the analytical capabilities are still intact. This is a general trend across all datasets, as was also depicted on Figure 8.

The amount of deviation bits shows a pattern. Looking at the Pendigits dataset the higher the amount of deviation bits the more inliers will be classified as an outlier. This is natural as the compression will place the observations in larger bins that are easier to separate. DupRes does not wrongfully classify these inliers as the large binning has resulted in more duplicates and therefore pushing their score towards being inliers.

C. Compression and Memory

The two right-most column in the table describes the compression rate and memory overhead for each model. The compression rate is calculated by dividing the number of compressed bits with the original number of bits. As each feature in every dataset can be represented as a byte, the uncompressed size is: $size_{org} = N \cdot 8 \cdot f$, where N is the amount of samples and f is the amount of features. The lossy compression, without deviation, will then be: $size_{lossy} = N_{unique} \cdot (8-d) \cdot f$, where N_{unique} is the amount of unique samples and d is the amount of deviation bits. The calculation for $size_{lossy}$ is simplified in the sense, that it is neglected that features across samples can be the same. In the simplified version we only look at the uniqueness across an entire sample. Therefore,

the actual compression rate will be better than depicted in the table. The memory overhead covers the amount of bytes necessary to contain the table of uniques used in DupRes. The calculation is $overhead = (f \cdot (8-d) \cdot N_{unique} + 8 \cdot N_{unique}) / 8$. This calculation covers storing each unique sample and an eight bits number to store the count. This calculation is simplified similarly to the lossy compression, but as well under the assumption that the count does not exceed eight bits.

Looking at the table the original model naturally has no compression. The two others compression varies on their amount of deviation bits. $d = 6$ for both of the models catches all outliers except on the synthetic data set as described previously. This is a quite significant compression rate of 0.06 on Pendigits and 0.02 on WBC. A compression rate of 0.875 at 1 deviation bit and 0.625 at 3 deviation bits is seen on the Pendigits dataset. This indicates that no duplicates are found, and therefore only being compressed by the selected amount of deviation bits.

The memory overhead shows the trade-off with DupRes and performing original Isolation Forest on the bases. They have the same compression rate. However, DupRes needs additional memory to store the table. The trend between amount of deviation bits and memory overhead is clearly seen in the table. This emphasizes the fact that DupRes is penalized when there is a low amount of duplicates. The overhead combined with the time spent creating the table and the testing time looking up in the table is not to be neglected.

VI. CONCLUSION

This paper looked into performing anomaly detection on compressed data. Generalized Deduplication was the compression algorithm of choice, that enables direct analysis of the bases derived from the transformed data. The amount of compression controlled the clustering and performance of the anomaly detection models. The duplicates created by the algorithm is taken advantage of in an extended version of Isolation Forest. Comparing the proposed model with original Isolation Forest it showed that utilizing the duplicates improves classification performance. However, the improved scoring is a trade-off with memory usage and execution time. A general observation is that performing Isolation Forest on the uncompressed data versus compressed had no large discrepancies in performance.

VII. FUTURE WORK

DupRes currently uses the $\log_2(x_{count})$ term to tune the score towards being an inlier based on the count. This is potentially a hyperparameter that can be tuned. Maybe a completely different term fits better. This could be something that also includes the dimensionality of the data or other factors. This report looked at a limited amount of datasets. It would therefore be interesting to see how the different models perform on others. In regards to generalized deduplication we only investigated 8 bit integers. Thus, a task is to research the anomaly detection behaviour on floating numbers.

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