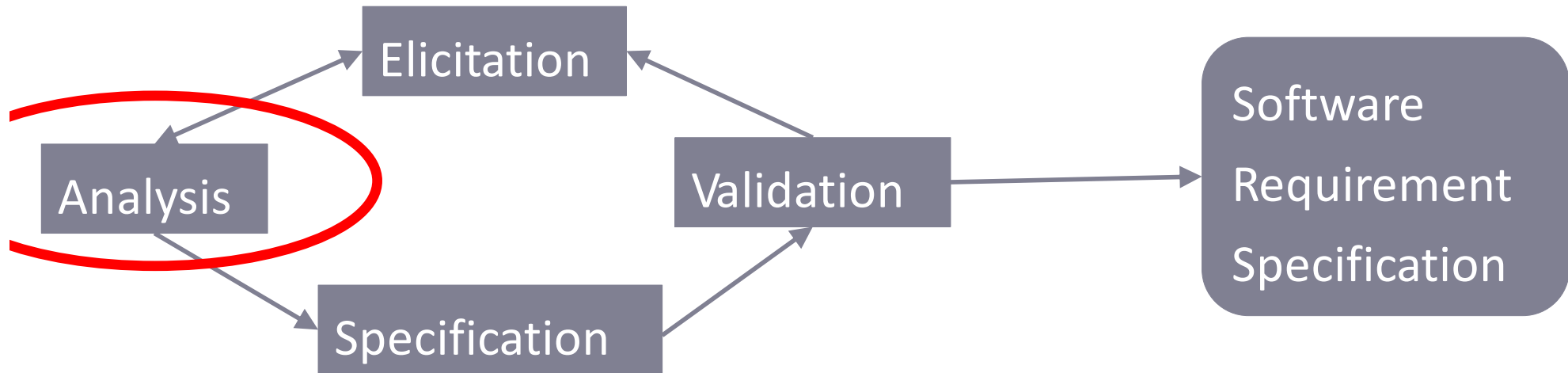


SOFTWARE ENGINEERING PRINCIPLES REQUIREMENTS ANALYSIS

STEFAN HALLESTEDE
PETER GORM LARSEN
CARL SCHULTZ

UNIVERSITET

PROCESS FOR CAPTURING REQUIREMENTS

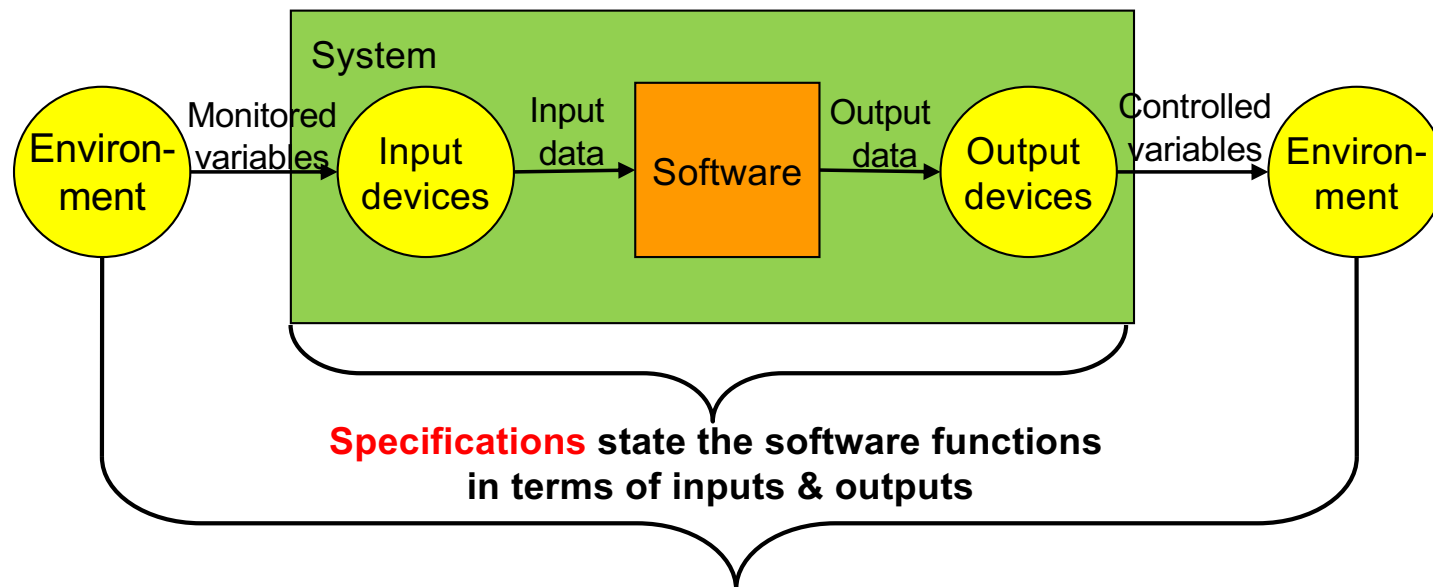


- › **Elicitation:** Collecting the user's requirements
- › **Analysis:** Understanding and modelling of desired behaviour
- › **Specification:** Documenting the behaviour of the proposed software system
- › **Validation:** Checking that the specification matches the user's requirements

AGENDA

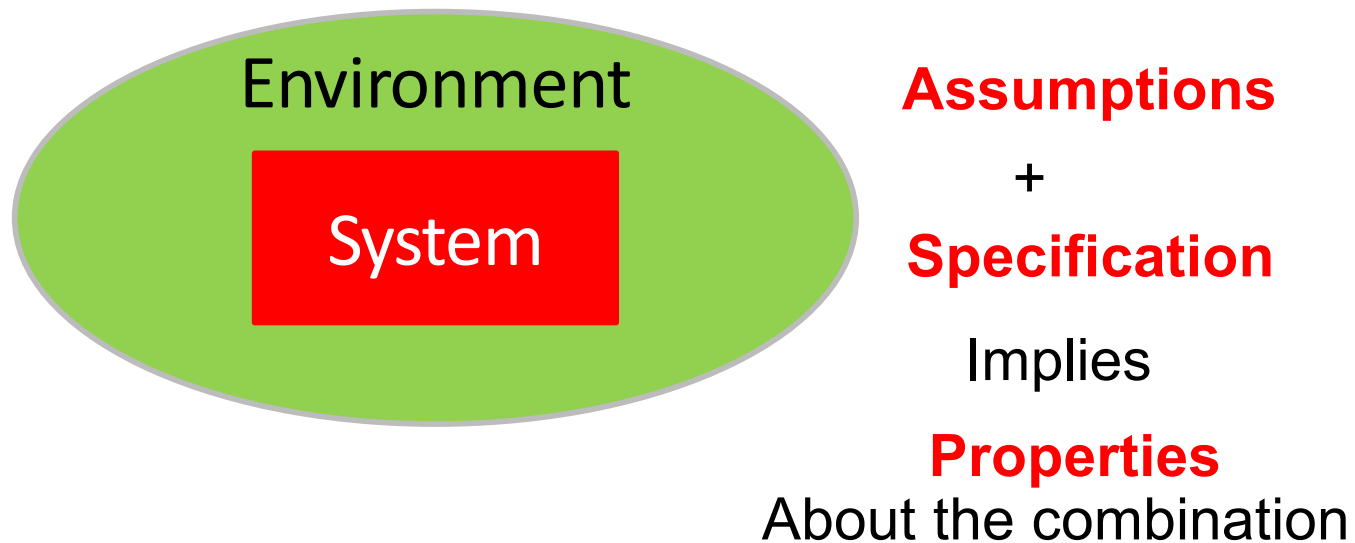
- › **Logical reasoning (A+S |- P)**
- › Elevator example
- › Logic
- › Brief VDM introduction
- › Executable models

HOW SOFTWARE ENGINEERS SEE THE WORLD



Assumptions about expectations of the environment behaviour are important
Properties about the desired behaviour of the new system in the environment express a desired relationship between monitored and controlled variables

ASSUMPTIONS, SPECIFICATIONS AND SYSTEM PROPERTIES



ENGINEERING ARGUMENTS

- › The ability to predict the properties of a product before it is built
 - › Feed-forward loop from specification to product properties
 - › Assumptions and Specification entail Properties
 - › Properties are those desired for the System under Development:
 - › System Requirements
 - › System Constraints
 - › See Software for Dependable Systems: Sufficient Evidence? Daniel Jackson et al.
-

EXAMPLE ENGINEERING ARGUMENTS

Engineering knowledge

- › Products with this kind of decomposition usually have properties P
- › Since this product will have this kind of decomposition
- › It will probably have properties P

Throw-away prototyping

- › Since the prototype has properties P,
- › And the prototype is similar to the final product
- › The final product probably has properties P

EXAMPLE ENGINEERING ARGUMENTS

Model execution

- › Since the model execution has properties P
- › If the system implements this model exactly
- › Then the system will have properties P

Model checking

- › Since the state transition graph has properties P,
- › If the system implements this graph correctly
- › Then the system will have properties P

EXAMPLE ENGINEERING ARGUMENTS

Theorem proving

- › Since the decomposition has been proved to have properties P,
- › If the system correctly implements this decomposition
- › Then the system will have properties P

EXAMPLE ENGINEERING ARGUMENTS

Exercise - give the following arguments:

Model execution argument

Throw-away prototyping

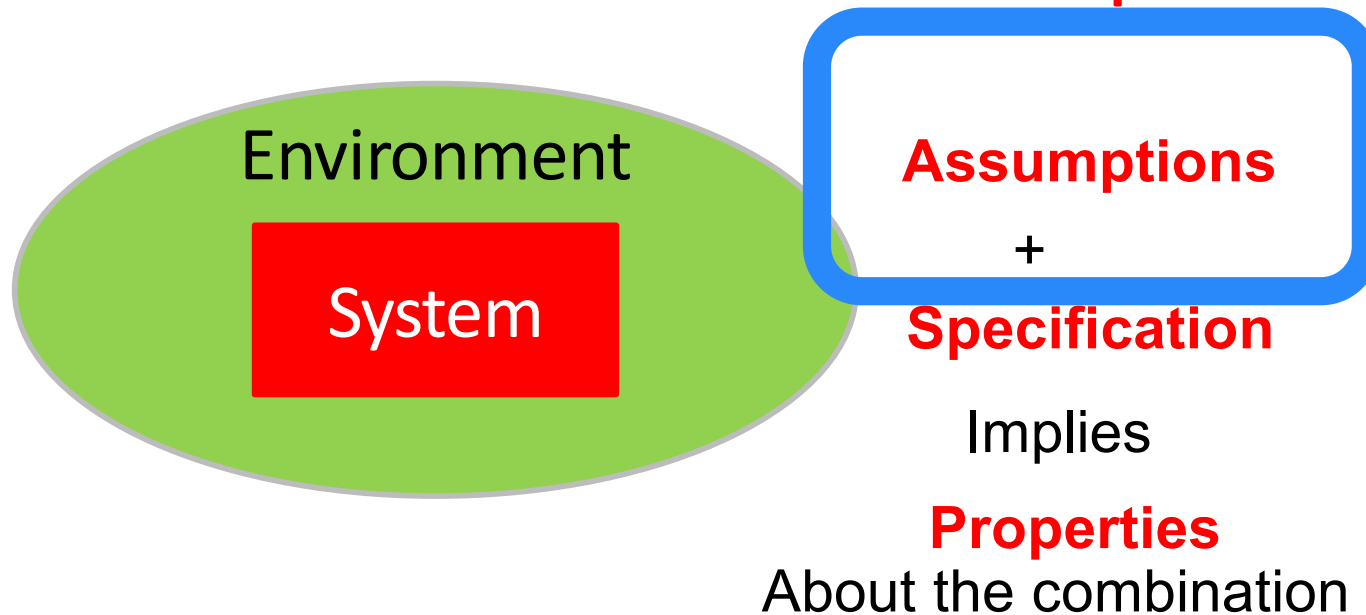
Model checking

Theorem proving

Engineering knowledge

ASSUMPTIONS ABOUT THE ENVIRONMENT

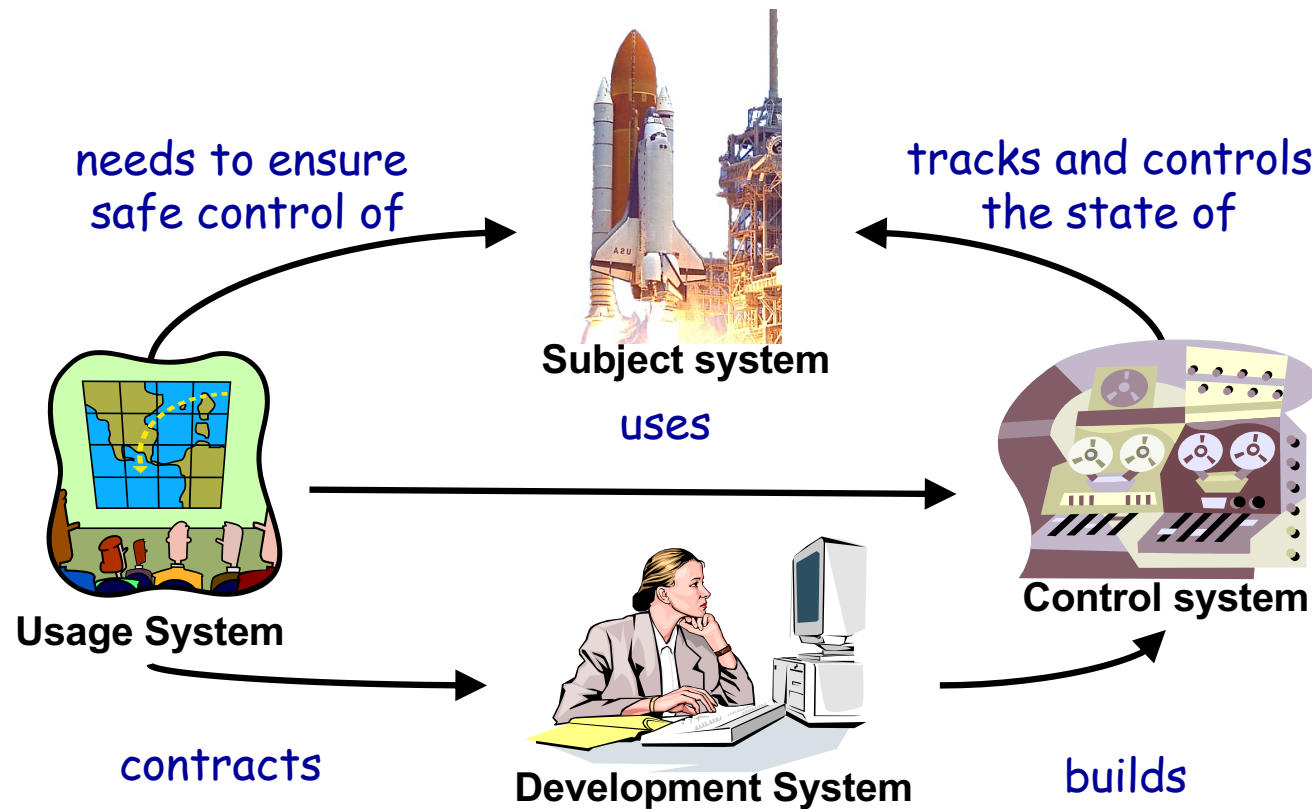
What are assumptions?



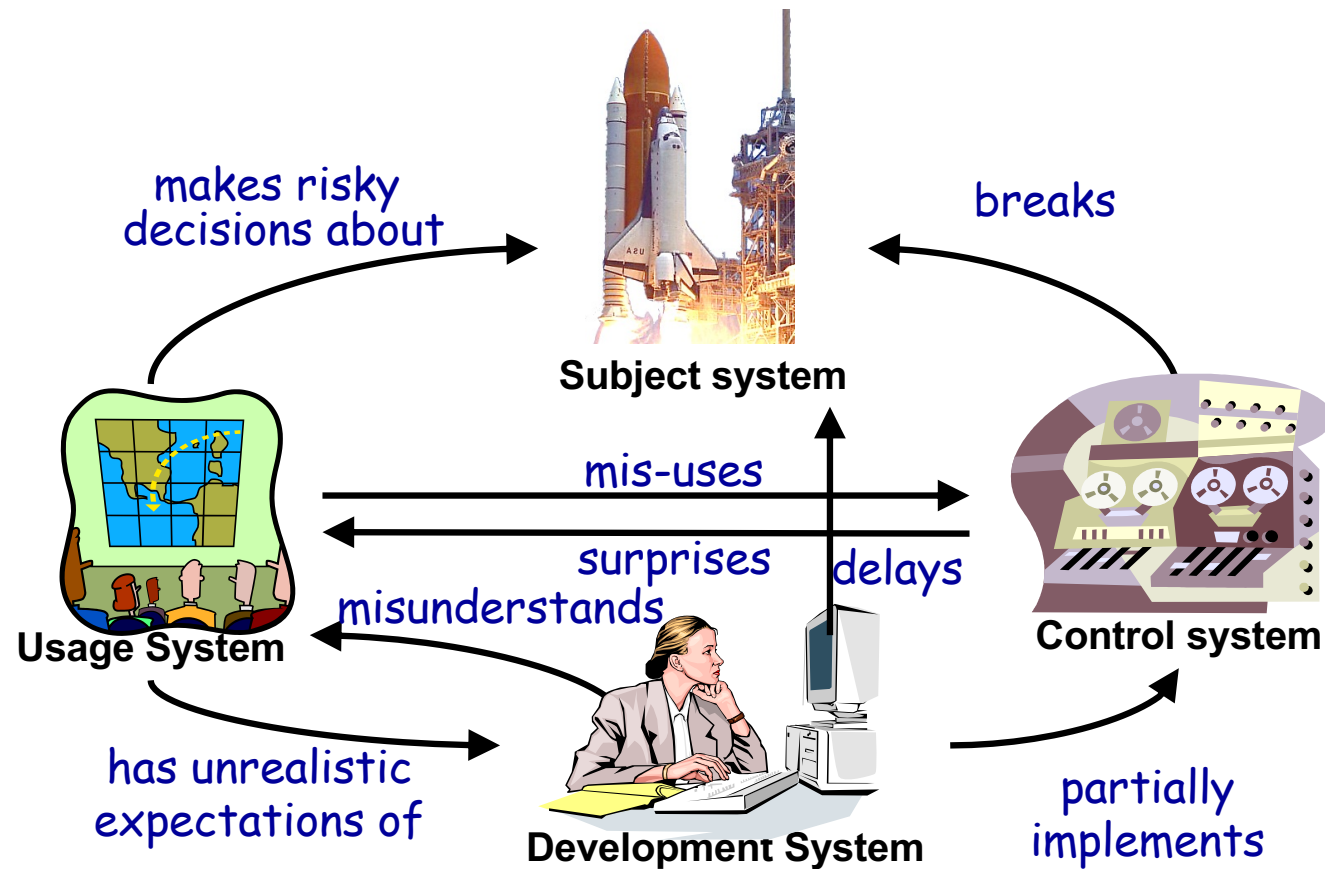
ASSUMPTIONS ABOUT THE ENVIRONMENT

- › Assumptions are statements about the environment
- › Must be true for the (stimulus, response) pair to be desirable
- › Beyond control of System under Development
- › Examples of categories of assumptions
 - › Laws of nature
 - › Properties of devices
 - › Properties of people (users, operators, ...)
 - › Some are explicit – and some are implicit

HOW SYSTEMS ENGINEERS SEE THE WORLD



HOW THE WORLD REALLY IS...



WHO USES REQUIREMENTS?

- › What are the uses of a software requirement specification?
- › For it is a specification of the product that will be delivered, ***a contract***
- › For it can be used as a basis ***for scheduling and measuring progress***
- › For the it provides a specification of ***what to design***
- › For it defines the range of ***acceptable implementations*** and the ***outputs that must be produced***
- › For personnel it is used for ***validation, test planning, and verification***

WHO USES REQUIREMENTS?

- › What are the uses of a software requirement specification?
 - › For customers it is a specification of the product that will be delivered, ***a contract***
 - › For managers it can be used as a basis ***for scheduling and measuring progress***
 - › For the software designers it provides a specification of ***what to design***
 - › For coders it defines the range of ***acceptable implementations*** and the ***outputs that must be produced***
 - › For quality assurance personnel it is used for ***validation, test planning, and verification***
-

AGENDA

- › Logical reasoning (A+S | - P)
- › **Elevator example**
- › Logic
- › Brief VDM introduction
- › Executable models

Please refer to
ElevatorExample.PDF

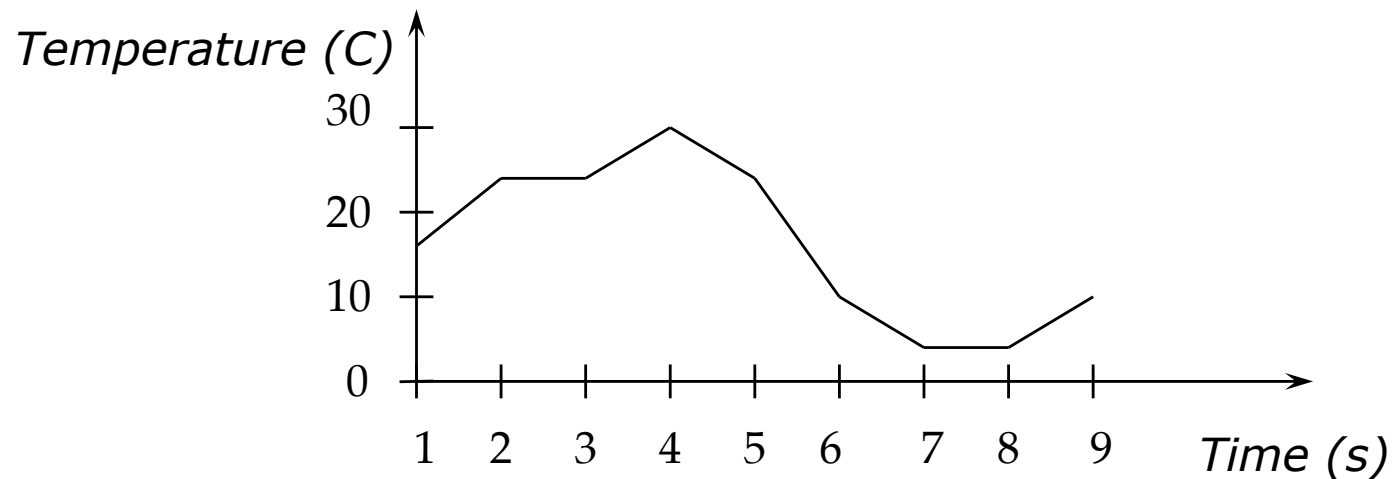
AGENDA

- › Logical reasoning (A+S | - P)
- › Elevator example
- › **Logic**
- › Brief VDM introduction
- › Executable models

LOGIC

- › Our ability to state invariants, record pre-conditions and post-conditions, and the ability to reason about a formal model depend on the logic on which the modelling language is based.
- › Classical logical propositions and predicates
- › Connectives
- › Quantifiers

A TEMPERATURE MONITOR EXAMPLE



The monitor records the last five temperature readings

25	10	5	5	10
----	----	---	---	----

A TEMPERATURE MONITOR EXAMPLE

› The following conditions are to be detected by the monitor:

1. Rising: the last reading in the sample is greater than the first
2. Over limit: there is a reading in the sample in excess of 400 C
3. Continually over limit: all the readings in the sample exceed 400 C
4. Safe: If readings do not exceed 400 C by the middle of the sample, the reactor is safe. If readings exceed 400 C by the middle of the sample, the reactor is still safe provided that the reading at the end of the sample is less than 400 C.
5. Alarm: The alarm is to be raised if and only if the reactor is not safe

PREDICATES AND PROPOSITIONS

› *Predicates* are simply logical expressions. The simplest kind of logical predicate is a *proposition*.

› A *proposition* is a logical assertion about a particular value or values, usually involving a Boolean operator to compare the values, e.g.

› $3 < 27$ $5 = 9$

PREDICATES

- › A predicate is a logical expression that is not specific to particular values but contains variables which can stand for one of a range of possible values, e.g.

$$x < 27$$

$$(x^{**2}) + x - 6 = 0$$

- › The truth or falsehood of a predicate depends on the value taken by the variables.

PREDICATES IN THE MONITOR EXAMPLE

```
Monitor :: temps : seq of int  
        alarm : bool
```

```
inv m == len m.temps = 5
```

› Consider a monitor m . m is a sequence so we can index into it:

› First reading in m : $m.temps(1)$

› Last reading in m : $m.temps(5)$

› Predicate stating that the first reading in m is strictly less than the last reading:

$$m.temps(1) < m.temps(5)$$

› The truth of the predicate depends on the value of m .

THE RISING CONDITION

- › The last reading in the sample is greater than the first

```
Monitor :: temps : seq of int  
        alarm : bool
```

```
inv m == len m.temps = 5
```

- › We can express the rising condition as a Boolean function:

```
Rising: Monitor -> bool
```

```
Rising(m) == m.temps(1) < m.temps(5)
```

- › For any monitor m, the expression Rising(m) evaluates to true iff the last reading in the sample in m is higher than the first, e.g.

```
Rising( mk_Monitor([233,45,677,650,900], false) )
```

```
Rising( mk_Monitor([23,45,67,50,20], false) )
```

LOGICAL OPERATORS (CONNECTIVES)

We will examine the following logical operators:

- › Negation (NOT)
- › Conjunction (AND)
- › Disjunction (OR)
- › Implication (if – then)
- › Biconditional (if and only if)
- › Truth tables can be used to show how these operators can combine propositions to compound propositions.

NEGATION (NOT)

- › Negation allows us to state that the opposite of some logical expression is true, e.g.
- › *The temperature in the monitor mon is not rising:*
- › **not** Rising(mon)

Truth table for negation:

P	$\neg P$
true	false
false	true

DISJUNCTION (OR)

- › Disjunction allows us to express alternatives that are not necessarily exclusive:
- › Over limit: There is a reading in the sample in excess of 400 C

OverLimit: Monitor \rightarrow bool

OverLimit(m) ==

```
m.temps(1) > 400 or  
m.temps(2) > 400 or  
m.temps(3) > 400 or  
m.temps(4) > 400 or  
m.temps(5) > 400
```

P	Q	$P \vee Q$
true	true	true
true	false	true
false	true	true
false	false	false

CONJUNCTION (AND)

- › Conjunction allows us to express the fact that all of a collection of facts are true.
- › Continually over limit: all the readings in the sample exceed 400 C

```
COverLimit: Monitor -> bool
```

```
COverLimit(m) ==
```

```
  m.temps(1) > 400 and
```

```
  m.temps(2) > 400 and
```

```
  m.temps(3) > 400 and
```

```
  m.temps(4) > 400 and
```

```
  m.temps(5) > 400
```

P	Q	$P \wedge Q$
true	true	true
true	false	false
false	true	false
false	false	false

IMPLICATION

- › Implication allows us to express facts which are only true under certain conditions (“if ... then ...”):
- › Safe: If readings do not exceed 400 C by the middle of the sample, the reactor is safe. If readings exceed 400 C by the middle of the sample, the reactor is still safe provided that the reading at the end of the sample is less than 400 C.

Safe: Monitor \rightarrow **bool**

Safe(m) ==

(m.temps(3) > 400) \Rightarrow

(m.temps(5) < 400)

P	Q	$P \Rightarrow Q$
true	true	true
true	false	false
false	true	true
false	false	true

BIIMPLICATION

- › Biimplication allows us to express equivalence (“if and only if”).
- › Alarm: The alarm is to be raised if and only if the reactor is not safe
- › This can be recorded as an invariant property:

```
Monitor :: temps : seq of int
         alarm : bool
```

```
inv m ==
```

```
len m.temps = 5 and
```

```
not Safe(m) <=> m.alarm
```

P	Q	$P \Leftrightarrow Q$
true	true	true
true	false	false
false	true	false
false	false	true

QUANTIFIERS

- › For large collections of values, using a variable makes more sense than dealing with each case separately.
- › `inds m.temps` represents indices (1-5) of the sample
- › The “over limit” condition can then be expressed more economically as:
 - › **`exists i in set inds m.temps & m.temps(i) > 400`**
- › The “continually over limit” condition can then be expressed using “forall”:

```
CoverLimit: Monitor -> bool  
CoverLimit(m) ==  
  forall i in set inds m.temps & m.temps(i) > 400
```


QUANTIFIERS

Syntax:

```
› forall binding & predicate  
› exists binding & predicate
```

There are two types of binding:

Type Binding, e.g.

```
x : nat  
n : seq of char
```

*A type binding lets the bound variable range over a **type** (a possibly infinite collection of values).*

Set Binding, e.g.

```
i in set inds m  
x in set {1,...,20}
```

*A set binding lets the bound variable range over a **finite set of values**.*

UNIVERSAL QUANTIFICATION

- › Universal quantification is a generalised form of conjunction
 - › For example, the statement “every natural number is greater than or equal to zero” is denoted by
 - › $\forall n: \mathbf{nat} \bullet n \geq 0$ (\forall is a turned-round “A”, “for All” and written as “**forall**” in ASCII)
 - › “for all n drawn from the natural numbers,
 - › n is greater than or equal to zero”
 - › This statement is equivalent to (and a lot more succinct than):
 - › $0 \geq 0 \wedge 1 \geq 0 \wedge 2 \geq 0 \wedge 3 \geq 0 \wedge \dots$
-

QUESTIONS

Formulate the following statements using predicate logic:

1. Everybody likes Danish pastry
2. Everybody either likes Danish pastry or is a vegetarian
3. Either everybody likes Danish pastry or everybody is a vegetarian
4. Are the last two statements equivalent?

EXISTENTIAL QUANTIFICATION

- › Existential quantification allows us to assert that a predicate holds for at least one value — but not necessarily all values — of a given set
- › For example, the statement “there is a natural number that is greater than or equal to zero” is denoted by:
 - › $\exists n: \mathbf{nat} \bullet n \geq 0$ (\exists is a turned-round “E”, “there Exists” and written as “**exists**” in ASCII)
 - › “there exists an n drawn from the natural numbers such that n is greater than or equal to zero”
 $0 \geq 0 \vee 1 \geq 0 \vee 2 \geq 0 \vee 3 \geq 0 \vee \dots$

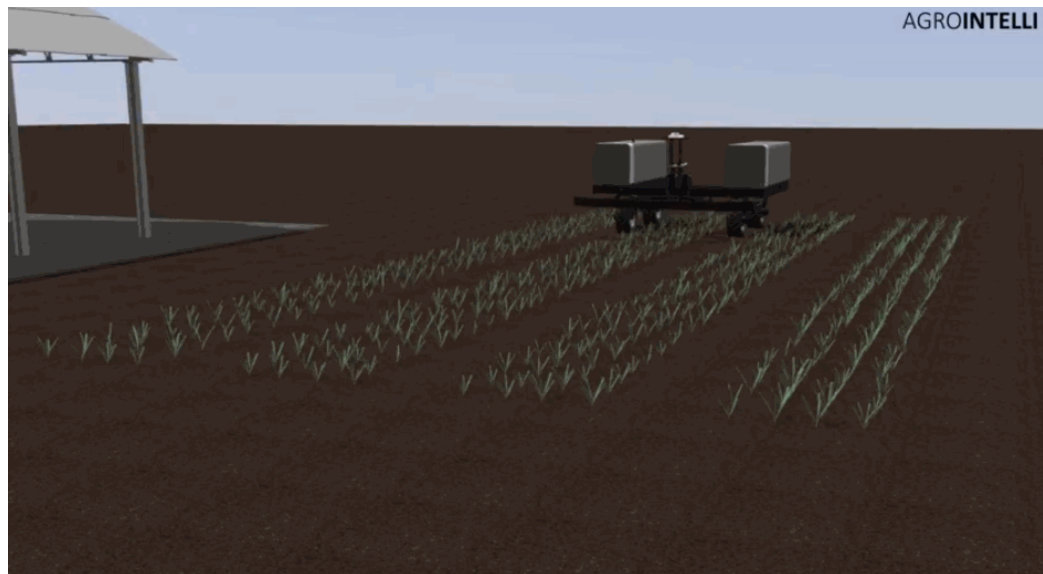
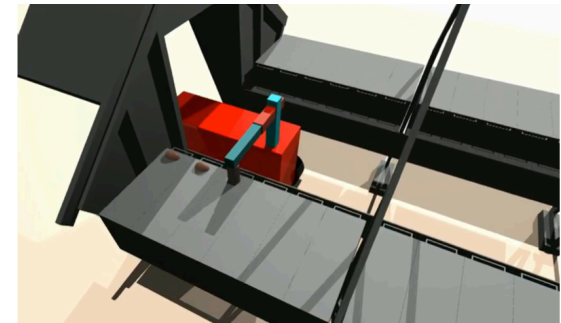
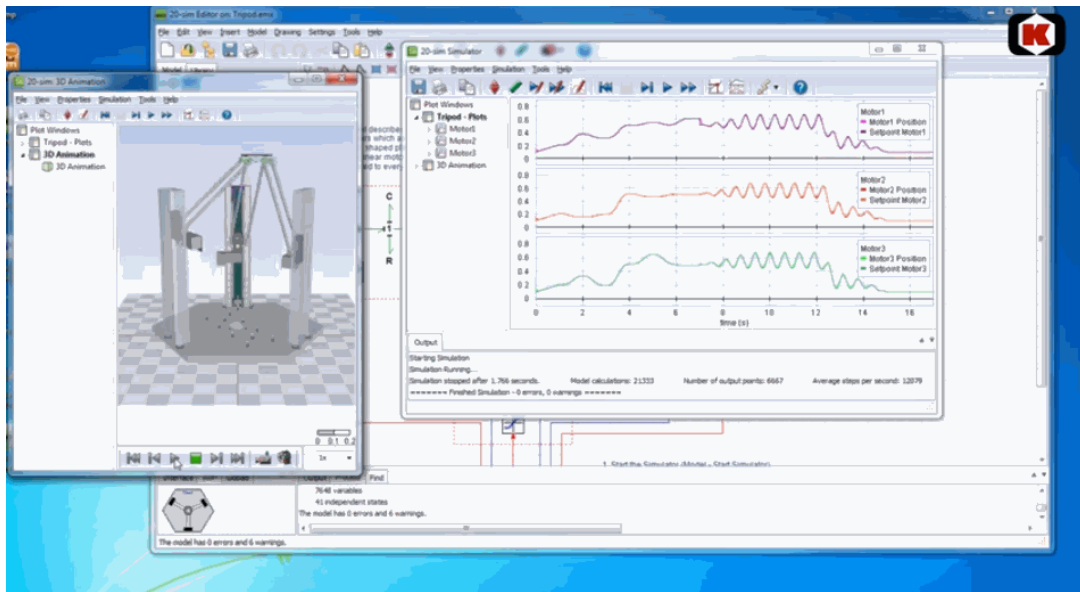
QUESTIONS

Formulate the following statements using predicate logic:

1. Somebody likes Danish pastry
2. There is somebody who either likes Danish pastry or is a vegetarian
3. Either somebody likes Danish pastry or somebody is a vegetarian
4. Are the last two statements equivalent?

AGENDA

- › Logical reasoning (A+S | - P)
- › Elevator example
- › Logic
- › **Brief VDM introduction**
- › Executable models



VDM BACKGROUND

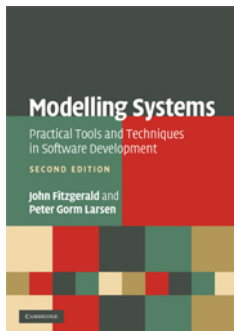
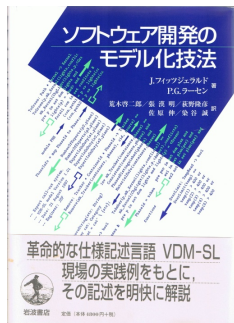
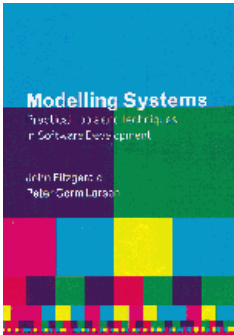
- › Our goal: well-founded but accessible modelling & analysis technology
- › VDMTools → Overture → Crescendo → Symphony
- › Pragmatic development methodologies
- › Industry applications
- › VDM: Model-oriented specification language
- › Extended with objects and real time.
- › Basic tools for static analysis
- › Strong simulation support
- › Model-based test



VDM (VIENNA DEVELOPMENT METHOD)

- › A formal method for specification of software
- › Three flavours
 - › VDM-SL (Specification Language)
 - › VDM++ adds object-orientation
 - › VDM-RT adds real-time features (clock and deployment)
- › Model-oriented specification language
 - › Simple, abstract data types
 - › Invariants to restrict membership
 - › Specification of functionality:
 - › Implicit specification (pre/post)
 - › Explicit specification (functional or imperative)

VDM-SL MODULE OUTLINE



module *<module-name>*

imports

exports

...

Interface

definitions

state

types

values

functions

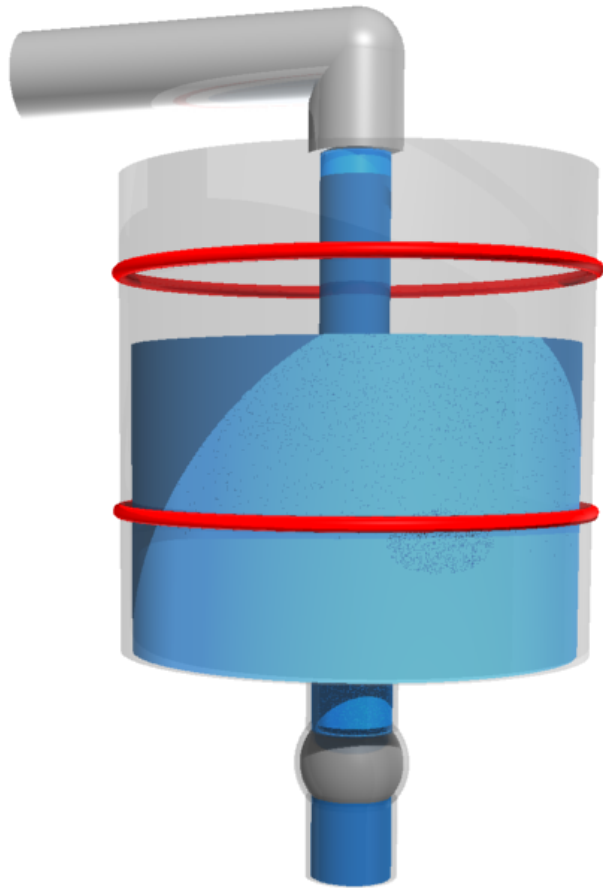
operations

...

Definitions

end *<module-name>*

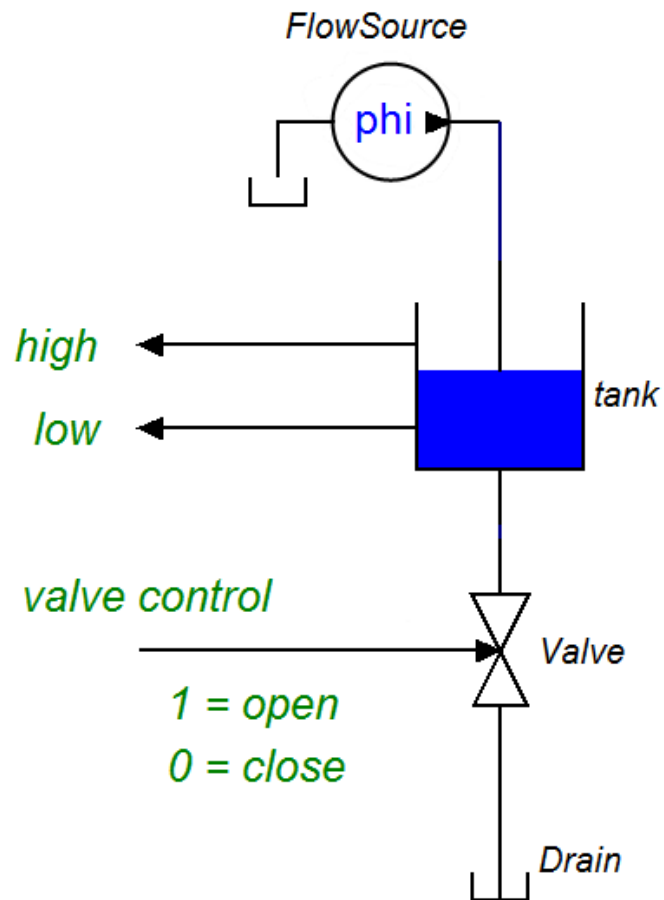
EXAMPLE: WATER TANK



$$\frac{dV}{dt} = \varphi_{in} - \varphi_{out}$$

$$\varphi_{out} = \begin{cases} \frac{\rho \cdot g}{A \cdot R} \cdot V & \text{if valve open} \\ 0 & \text{if valve closed} \end{cases}$$

EXAMPLE: WATER TANK



CT-side

```

class Controller
instance variables
  private i : Interface
operations
  async public Open:() ==> ()
  Open() == duration(50)
  i.SetValve(true);
  async public Close:() ==> ()
  Close() == cycles(1000)
  i.SetValve(false);
sync
  mutex(Open, Close);
  mutex(Open); mutex(Close)
end Controller
  
```

DE-side

OVERTURE TOOLS

Debugging

Changing perspective

Editing

Script Explorer

- Alarm
 - alarm.vdmpp
 - expert.vdmpp
 - plant.vdmpp
 - test1.vdmpp
- Interpreter Libraries [VDMJ Interpreter for VDM++]

Project explorer with VDM model files

```

class Plant

instance variables

alarms : set of Alarm;
schedule : map Period to
inv PlantInv(alarms,sched

functions

PlantInv: set of Alarm *
bool
PlantInv(as,sch) ==
(forall p in set dom sch
(forall a in set as &
forall p in set dom
exists expert in s
a.GetReqQuali()

types

```

Debug - AlarmPP/plant.vdmpp - Overture Platform

File Edit Navigate Search Project Run Window Help

Debug Variables Breakpoints

Name Value

- alarms set[1] (id=22)
- Element1 Alarm
- schedule map[2] (id=1)
- Maplet1 {mk_token("Monday day") |-> {Expert{#3, quali={<Bio>...
- Maplet2 {mk_token("Monday night") |-> {Expert{#4, quali={<Ele...

Call traces in debug

Inspector variables

Editor

```

\begin(vdm_al)
public ExpertIsOnDuty: Expert ==> set of Period
ExpertIsOnDuty(ex) ==
return {p | p in set dom schedule &
ex in set schedule(p)};
\end(vdm_al)

```

Outline

- Plant
 - alarms : set of Alarm
 - ExpertIsOnDuty(Expert) : set of Period
 - ExpertToPage(Alarm, Period) : Expert
 - NumberOfExperts(Period) : nat
 - Period : token
 - Plant(set of Alarm, map Period to set of Expert)

Interactive console

AlarmPP Run [VDM PP Model] VDM debugger

Combinatorial Testing

/test1.vdmpp - Overture Tools

Project Run Window Help

test1.vdmpp plant.vdmpp expert.vdmpp tracker.vdmpp

```

operations
public Run: () ==> set of Plant*Period * Expert
Run() ==
let periods = plant.ExpertIsOnDuty(ex1),
expert = plant.ExpertToPage(al,p1)
in
return mk_(periods,expert);
traces
AddingAndDeleting: let myex in set exs
in
let myex2 in set exs \ {myex}
in
let p in set ps
in
(plant.AddExpertToSchedule(p,myex);
plant.AddExpertToSchedule(p,myex2);
plant.RemoveExpertFromSchedule(p,myex);
plant.RemoveExpertFromSchedule(p,myex2));

```

Regular expression

Overview of results

- Test 000001
- Test 000002
- Test 000003
- Test 000004
- Test 000005
- Test 000006
- Test 000007
- Test 000008
- Test 000009
- Test 000010
- Test 000011
- Test 000012
- Test 000013
- Test 000014
- Test 000015
- Test 000016
- Test 000017

Detailed test case and results

Trace Test case	Result
plant.AddExpertToSchedule(mk_token("Tuesday day"), myex)	0
plant.AddExpertToSchedule(mk_token("Tuesday day"), myex2)	0
plant.RemoveExpertFromSchedule(mk_token("Tuesday day"), myex)	Error 4130: Instance invariant violated: inv_Plant in 'Plant'

Proof

alarm.vdmpp expert.vdmpp plant.vdmpp test1.vdmpp

```

p in set dom schedule
post let expert = RESULT
in
expert in set schedule(p) and
a.GetReqQuali() in set expert.GetQuali();

```

(let expert:Expert = RESULT in p in set dom schedule)

Proof Obligation Explorer

No.	PO Name	Type	Status
1	Plant: PlantInv(set of (Alarm), map (...	map apply	✓
2	Plant: PlantInv(set of (Alarm), map (...	map apply	✓
3	Plant: ExpertToPage(Alarm, Period)	map apply	✗
4	Plant: ExpertToPage(Alarm, Period)	operation post condition	✗
	Plant: ExpertToPage(Alarm, Period)	let be st existence	✗
	Plant: ExpertToPage(Alarm, Period)	map apply	✗
	NumberOfExperts(Period)	map apply	✗
	ExpertIsOnDuty(Expert)	map apply	✗
	Plant(set of (Alarm), map (Per...	state invariant	✗
	Plant	map sequence compatible	✗

SPECIFYING BEHAVIOUR

- › Specifications in terms of post-conditions define a contract

```
sqrt(x: nat) r: real
```

```
post x = r * r
```

← Implicit definition, not executable

- › Explicit version

```
sqrt: nat -> real
```

← Explicit definition can be executed

```
sqrt(x) == Math.sqrt(x)
```

- › Pre-condition and post-conditions

```
sqrt: int -> real
```

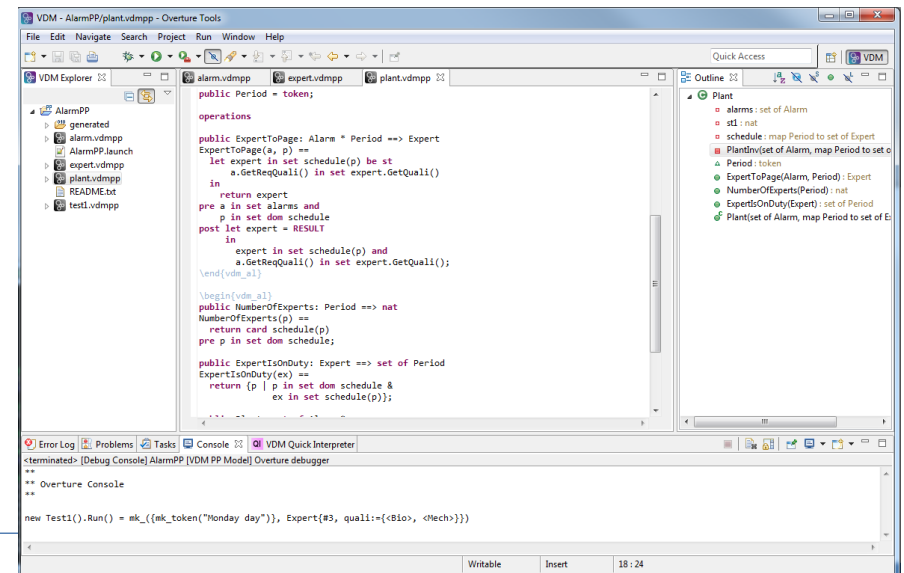
```
sqrt(x) == Math.sqrt(x)
```

```
pre x > 0
```

```
post x = RESULT * RESULT
```

THE OVERTURE TOOL

- › Open-source tool for analysing VDM models
- › Eclipse/Java based
- › Currently in version 2.5.2 (September 11th 2017)
- › Visit us at <http://overturetool.org/>
- › Useful references
- › Examples can be imported
- › Language manual
- › Tool users manual



AGENDA

- › Logical reasoning (A+S | - P)
- › Elevator example
- › Logic
- › Brief VDM introduction
- › **Executable models**

VALIDATION TECHNIQUES

Exercise: match techniques with definitions

- › **Inspection**
- › **Static Analysis**
- › **Testing**
- › **Model Checking**
- › **Proof**

› automatic checks of syntax & type correctness, detect unusual features

› search the state space to find states that violate the properties we are checking.

› run the model and check outcomes against expectations

› use a logic to reason symbolically about whole classes of states at once.

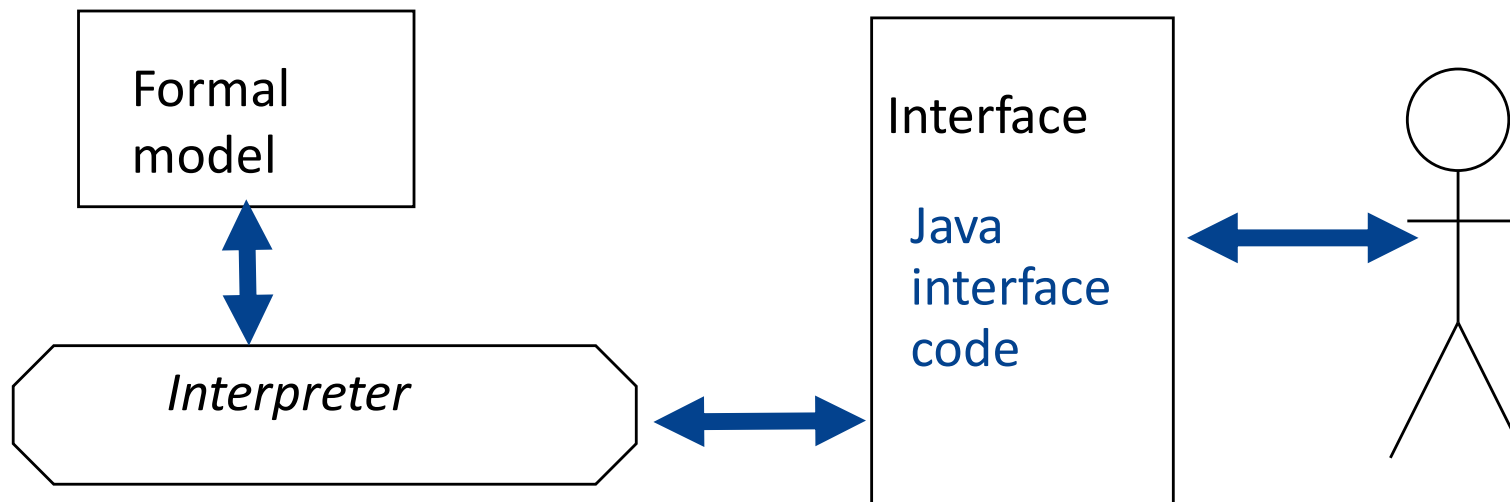
› organized process of examining the model alongside domain experts

VALIDATION TECHNIQUES

- › **Inspection:** organized process of examining the model alongside domain experts.
- › **Static Analysis:** automatic checks of syntax & type correctness, detect unusual features.
- › **Testing:** run the model and check outcomes against expectations.
- › **Model Checking:** search the state space to find states that violate the properties we are checking.
- › **Proof:** use a logic to reason symbolically about whole classes of states at once.

VALIDATION VIA ANIMATION

Execution of the model through an interface. The interface can be coded in the Java programming language



Testing can increase confidence, but is only as good as the test set. Exhaustive techniques could give greater confidence.

FUNCTION DEFINITIONS (1/2)

› Explicit functions:

```
f: A * B * ... * Z -> R1 * R2 * ... * Rn  
f(a,b,...,z) ==  
  expr  
pre preexpr(a,b,...,z)  
post postexpr(a,b,...,z, RESULT)
```

› Implicit functions:

```
f(a:A, b:B, ..., z:Z) r1:R1, ..., rn:Rn  
pre preexpr(a,b,...,z)  
post postexpr(a,b,...,z, r1,...,rn)
```

Implicit functions cannot be executed by the VDM interpreter.

FUNCTION DEFINITIONS (2/2)

› Extended explicit functions:

```
f (a:A, b:B, ..., z:Z) r1:R1, ..., rn:Rn ==  
  expr  
pre preexpr (a,b,...,z)  
post postexpr (a,b,...,z, r1,..., rn)
```

Extended explicit functions are a non-standard combination of the implicit colon style with an explicit body.

› Preliminary explicit functions:

```
f: A * B * ... * Z -> R1 * R2 * ... * Rn  
f (a,b,...,z) ==  
  is not yet specified  
pre preexpr (a,b,...,z)  
post postexpr (a,b,...,z, RESULT)
```

EXPLICIT FUNCTION DEFINITIONS

› A recursive function definition could look like:

```
fac: nat -> nat1
fac (n) ==
    if n > 1
    then n * fac(n-1)
    else 1
measure Id;
Id: nat -> nat
Id(a) == a
```

› Pre-conditions can also be used:

```
Division: real * real -> real
Division(p,q) ==
    p/q
pre q <> 0
```

AGENDA

- › Logical reasoning (A+S | - P)
- › Elevator example
- › Logic
- › Brief VDM introduction
- › Executable models