



# APEX

# Autonomous Vehicle Plan Verification & Execution

## A Driver's License for Autonomous Vehicles

Matthew O'Kelly, Houssam Abbas, and Rahul Mangharam, University of Pennsylvania

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### Overview

The possibility that an auto manufacturer might ultimately be deemed *legally responsible for an autonomous vehicle's actions* highlights the urgent need for a technology that *can automatically and exhaustively certify the impossibility of accidents* in various driving scenarios, and under well-defined conditions.

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### Towards Verified Decisions for Autonomous Systems

We focus on three main *challenge problems* which will lead to expressive, tractable, and validated models for *formal verification of autonomy*

#### Problem #1

Verification of non-linear hybrid vehicle dynamics under environmental non-determinism.

#### Problem #2

Composition of a verified sequence of scenarios from verified scenarios.

#### Problem #3

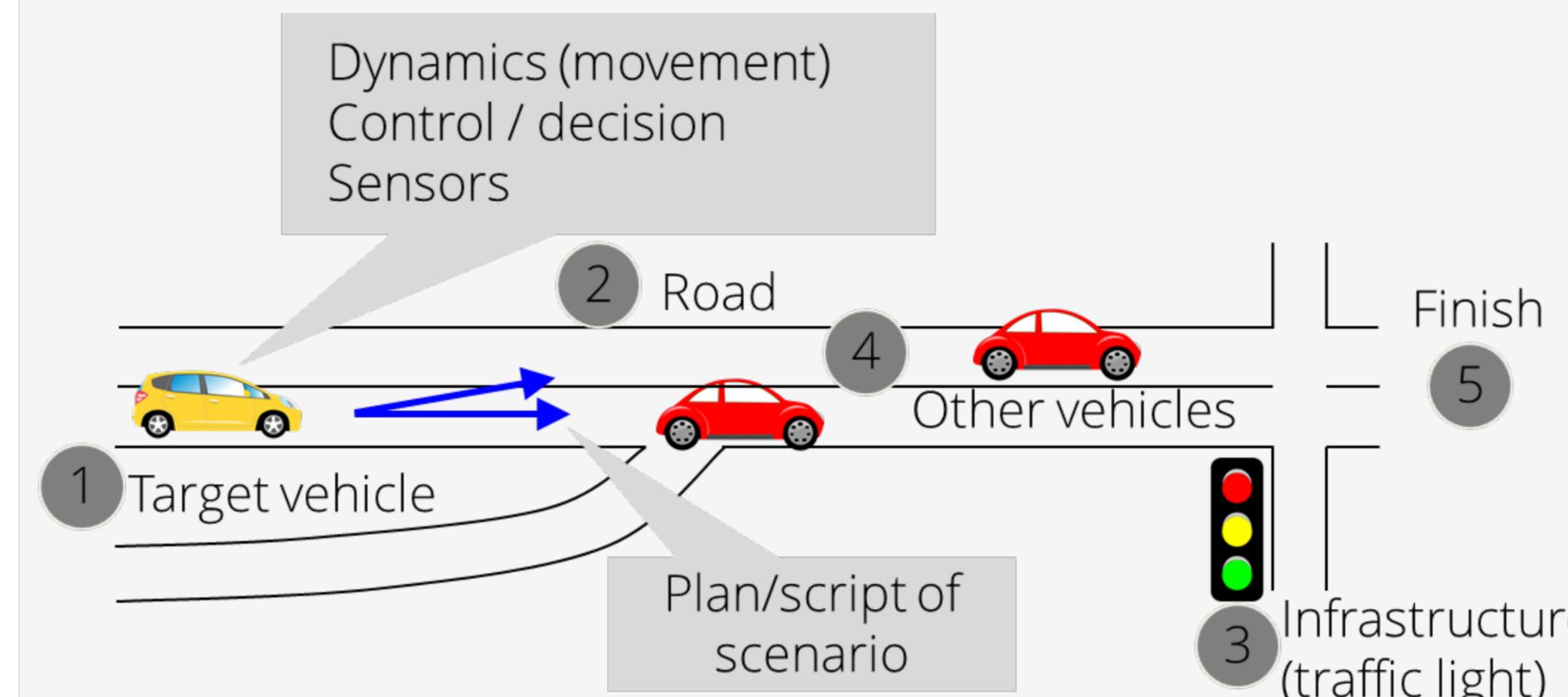
Online evaluation of behavioral controller goal sequences with respect to hierarchically ordered properties: safety, comfort, performance...

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### Intuition for Driving Scenarios

An *agent* is an entity that functions continuously and autonomously in an environment in which other processes take place and other agents exist

A *scenario* can be thought of as a *disembodied agent* that adjusts or *creates the environment* in which an autonomous system operates



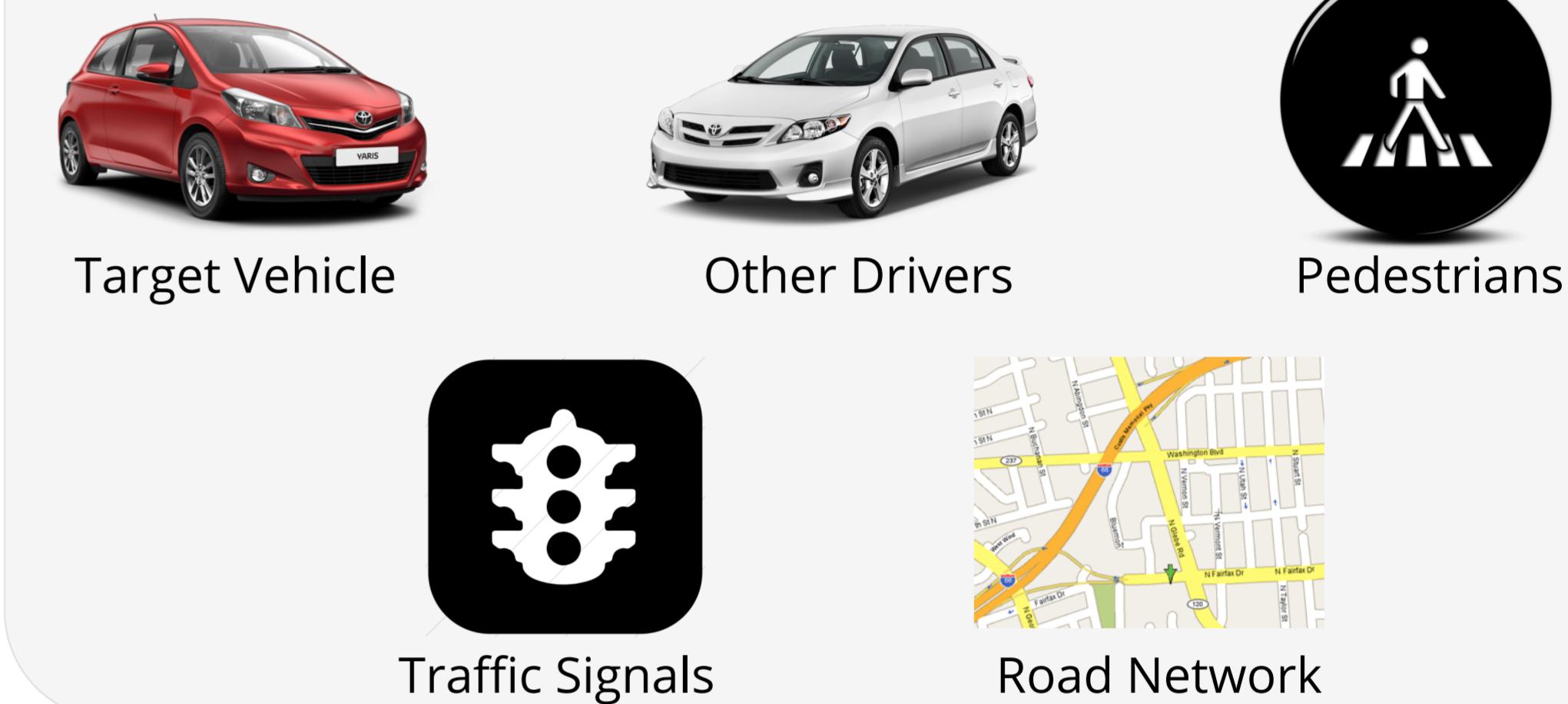
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### Common Agents

From representative driving scenarios...



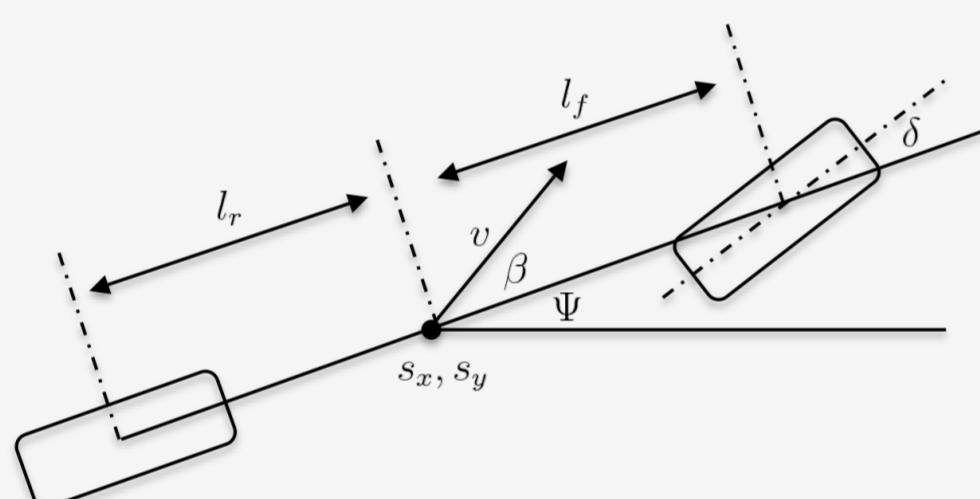
Understand *common agents* for more intuitive modeling:



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### Vehicle Dynamics: Intermediate Representation

The *bicycle model* is used as the intermediate representation (IR) because it supports verification of *low level trajectory trackers* and analysis with respect to first order logic necessary for *formal verification*.

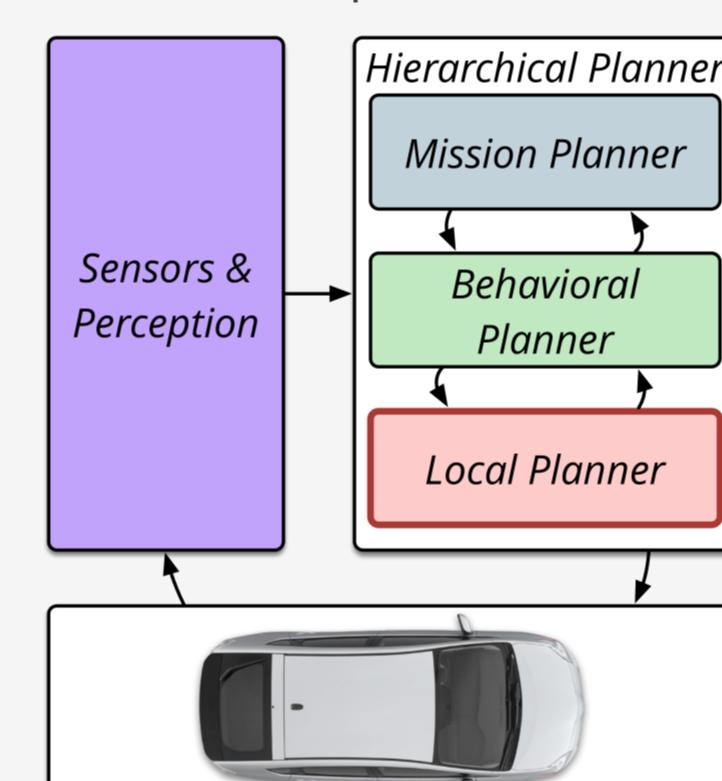


$$\begin{aligned}\dot{\beta} &= \left( \frac{C_r l_r - C_f l_f}{mv^2} \right) \psi + \left( \frac{C_f}{mv} \right) \delta - \left( \frac{C_f + C_r}{mv} \right) \beta + y_\beta \\ \ddot{\psi} &= \left( \frac{C_r l_r - C_f l_f}{I_z} \right) \beta - \left( \frac{C_f l_f^2 - C_r l_r^2}{I_z} \right) \left( \frac{\dot{\psi}}{v} \right) + \left( \frac{C_f l_f}{I_z} \right) \delta + y_\psi \\ \dot{v} &= a_x + y_v \\ \dot{s}_x &= v \cos(\beta + \psi) + y_{s_x} \\ \dot{s}_y &= v \sin(\beta + \psi) + y_{s_y} \\ \dot{\delta} &= v_w + y_d\end{aligned}$$

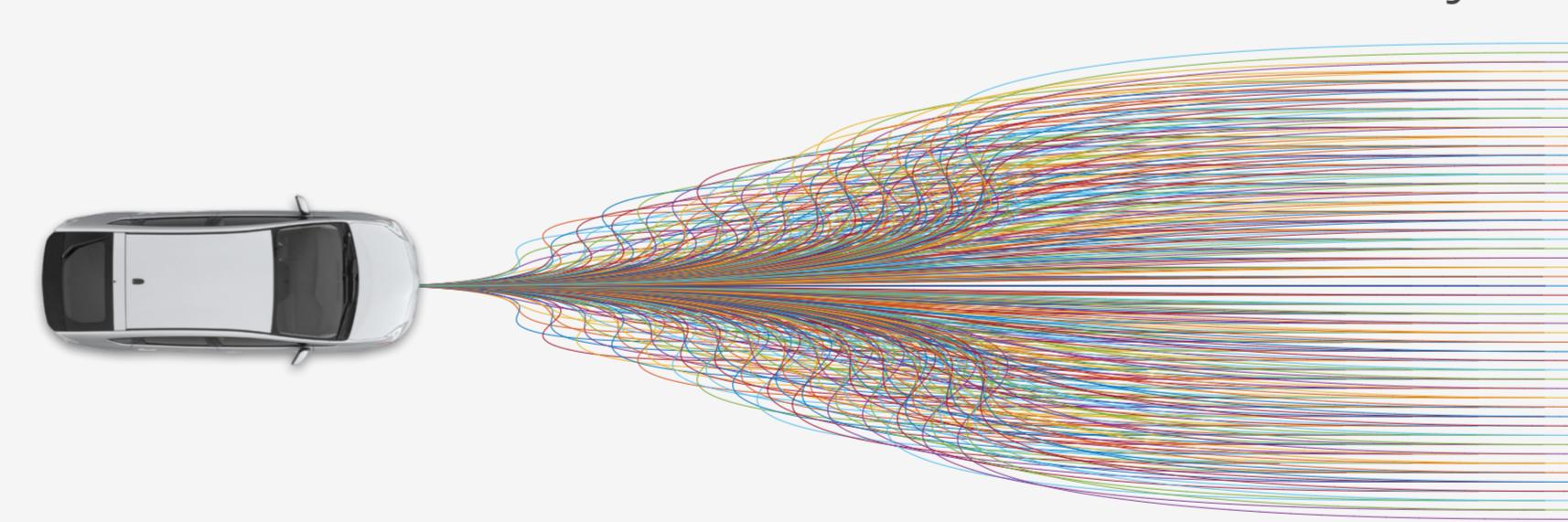
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### Vehicle Control: Planning Stack

APEX includes a *planning stack* for AVs which has been *validated* on multiple real vehicles.



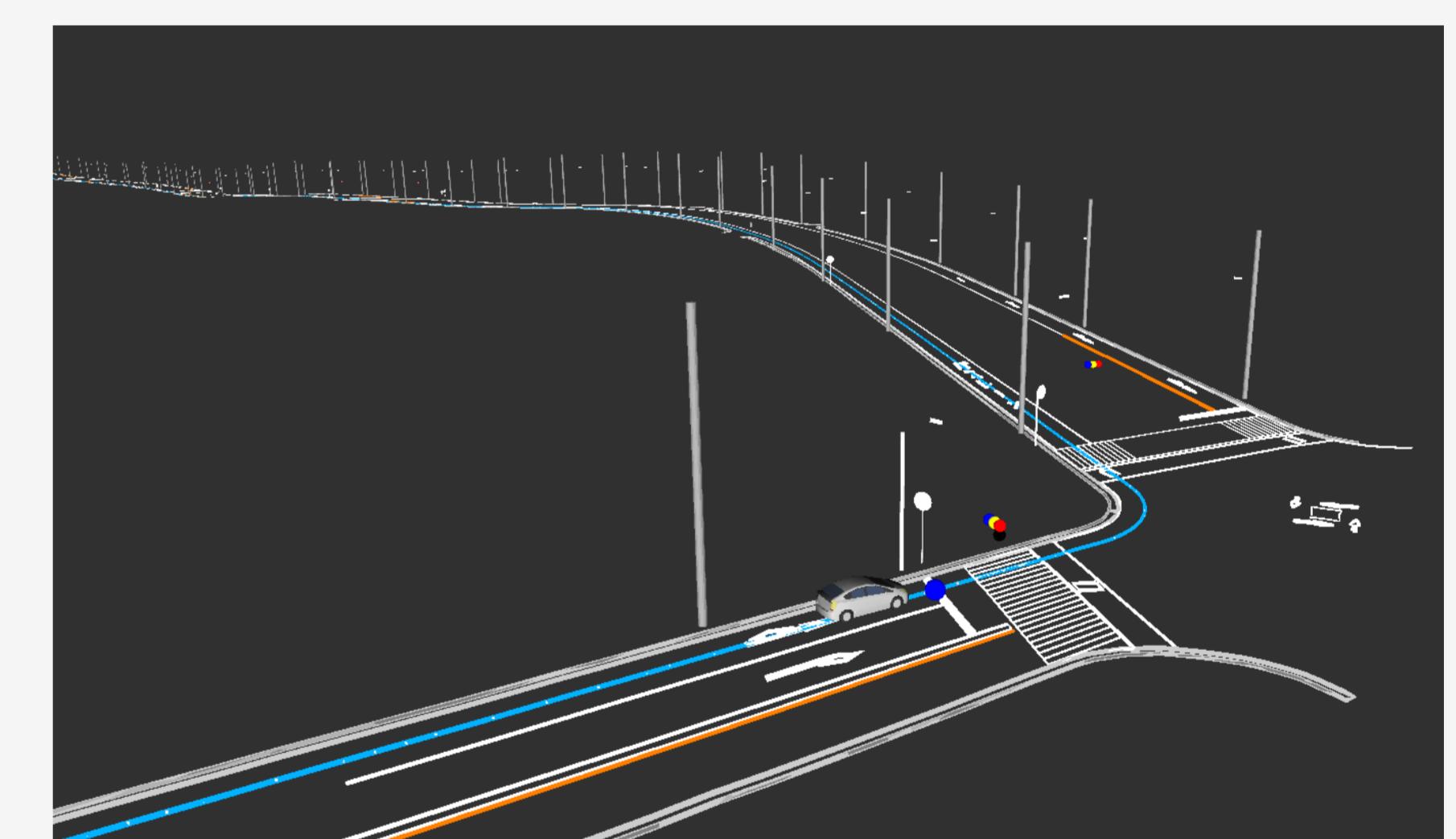
The planning stack generates a *set of trajectories*, from which *one is chosen* to be followed by the AV



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### Simulation Environment

Simulation helps the user: (1) *gain confidence* in the *modeling* effort and (2) *visualize* and understand *counterexamples* returned in the verification process.

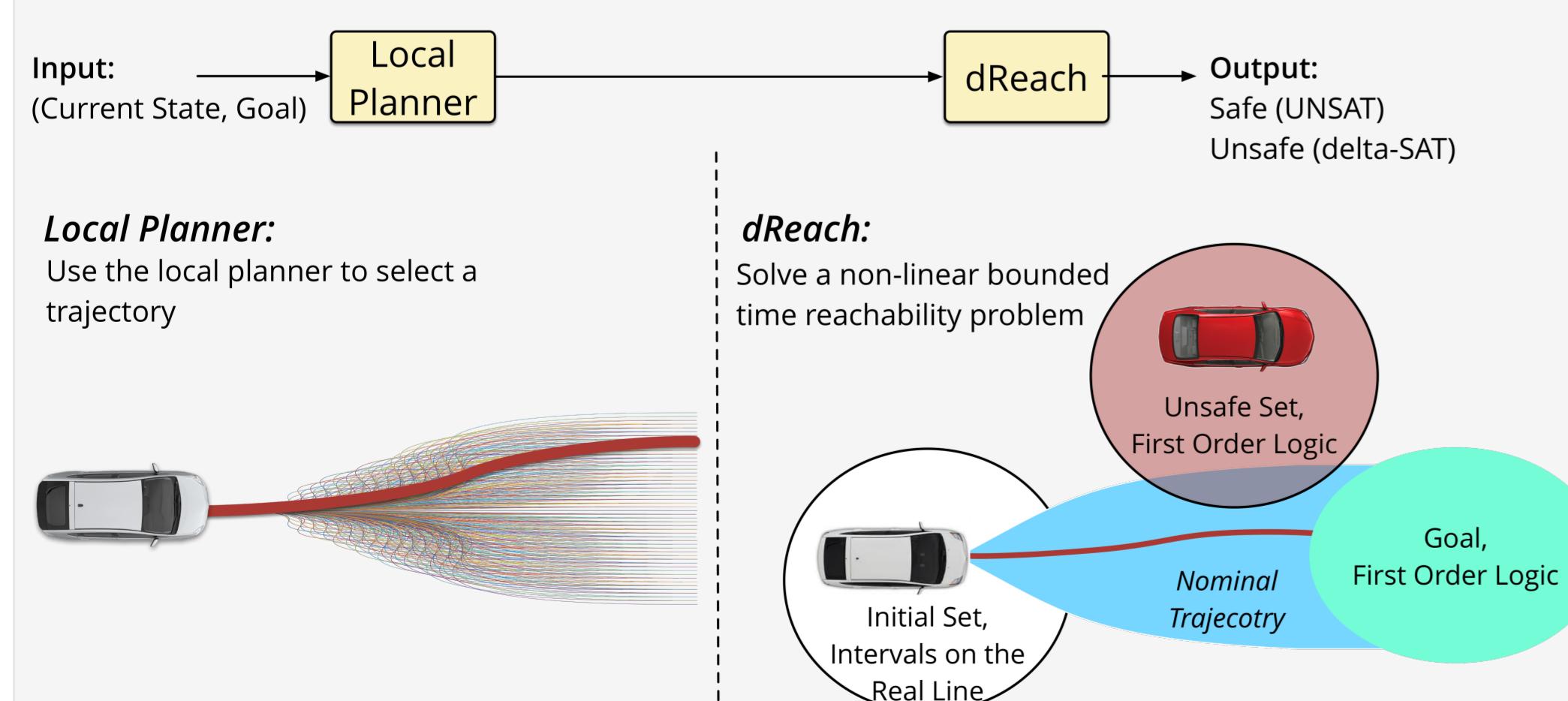


APEX includes an rViz based *simulation* environment capable of *interfacing with ROS*.

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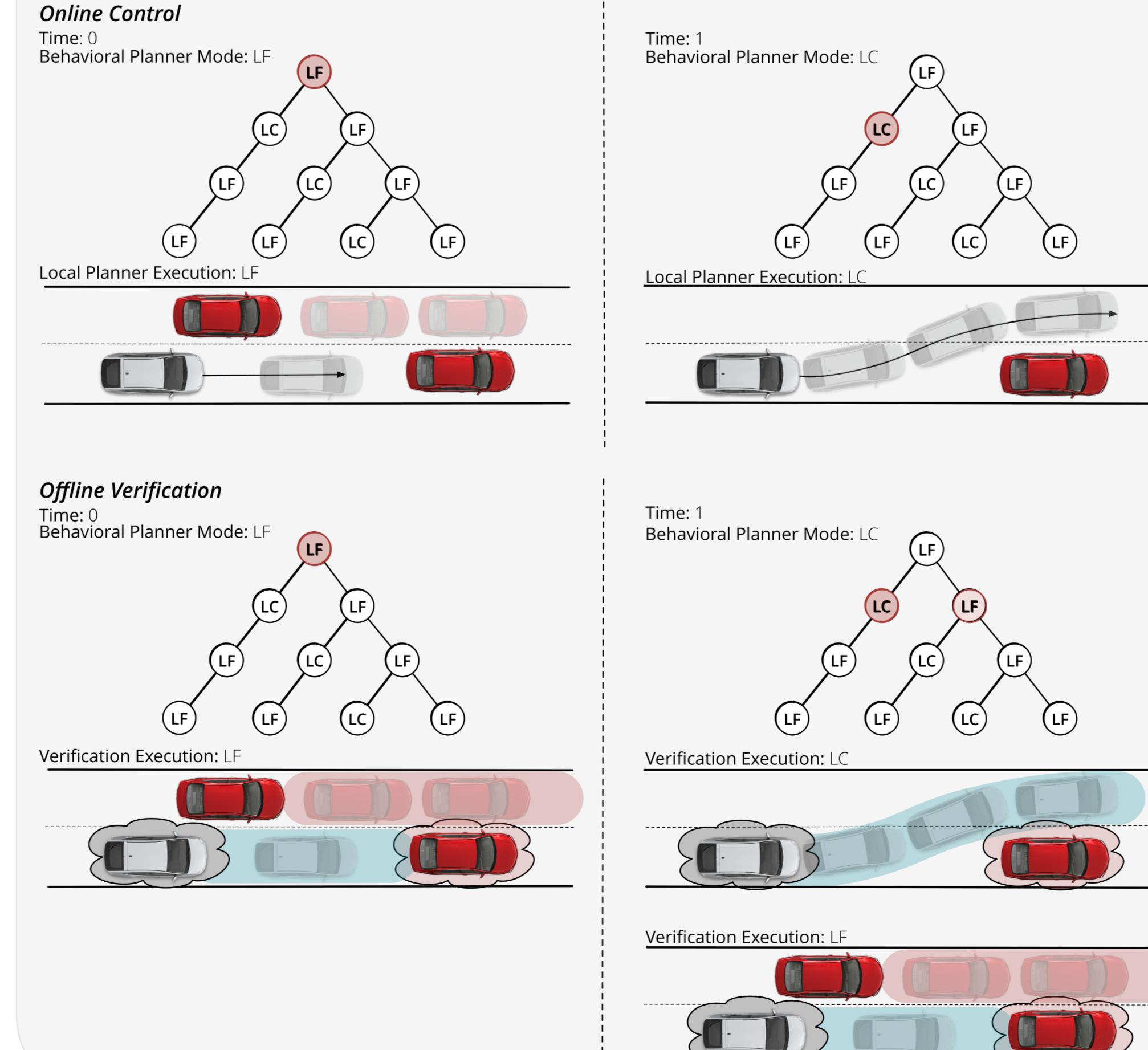
### Formalizing Driving Scenarios

In sharp contrast to a simulation based approach, the result of formal verification is that we have converted a hopeless *brute force search over real intervals* into a finite series of tractable bounded *reachability problems* automatically generated by executing the local planner...



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### Verification Engine



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### Test Bed

We have verified the effectiveness of the planning stack on a *Toyota Prius* capable of *full autonomy* with only a camera and LIDAR. Our planner is part of *Autoware*, an open source operating system for autonomous vehicles.

